

Neutron Physics

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5 lectures:

1. Physics/Technology of Cold and Ultracold Neutrons
2. Electroweak Standard Model Tests [neutron beta decay]
3. Nuclear physics/QCD [weak interaction between nucleons]
4. Physics Beyond the Standard Model [EDM/T violation, B]
5. Other interesting stuff that neutrons can do [NNN interaction, searches for extra dimensions,...]

Physics Beyond SM with Neutrons: T/B Violation

1. Some facts about T violation
2. Connection with Big Bang Theory: Baryon Asymmetry
3. Neutron electric dipole moment searches
4. Neutron-antineutron oscillations

Thanks for slides to: Jen-chieh Peng (Illinois), Philip Harris (Sussex), Yuri Kamshkov (Tennessee), Albert Young (NC State), Tony Mann (Tufts)

T/CPT Invariance: Some Facts

Classical Mechanics: $T = \text{motion reversal}$: $x \rightarrow x$, $p \rightarrow -p$, $s \rightarrow -s$

Quantum Mechanics: demand same behavior for operators \rightarrow
 $[p, x] = -ih$, $[p', x'] = T [p, x] T^{-1} = [-p, x] \rightarrow T i T^{-1} = -i$, T is an antiunitary operator, no conserved quantum number. $T = UK$, U unitary

$T^2 = \pm 1$ for even/odd # of spin 1/2 particles

T reverses initial and final states: $|\psi'\rangle = T |\psi\rangle$, $|\phi'\rangle = T |\phi\rangle \rightarrow$
 $\langle \psi' | \phi' \rangle = \langle T\psi | T | \phi \rangle = \langle U\psi^* | U | \phi^* \rangle = \langle \psi^* | U^\dagger U | \phi^* \rangle = \langle \psi | \phi \rangle^* = \langle \phi | \psi \rangle$
 \rightarrow for an odd system $|\psi\rangle$ and $T |\psi\rangle$ are orthogonal (Kramers theorem)

Relativistic QFT: CPT theorem says CPT is conserved for systems (1) described by local field operators, (2) invariant under Lorentz transformations, and (3) with a Hermitian Hamiltonian

T Invariance: Some Consequences

A system with spherical symmetry cannot possess a static EDM (in the absence of an accidental degeneracy) if the dynamics are T invariant

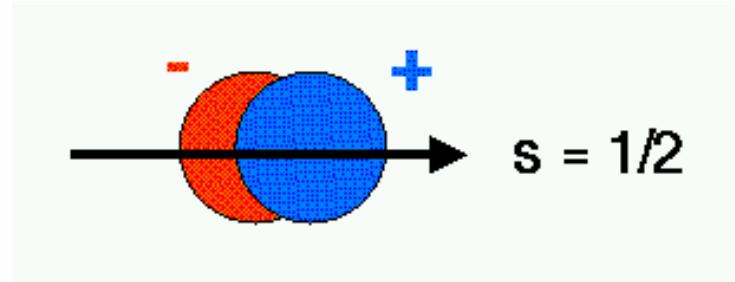
$T ET^{-1} = E$, $T DT^{-1} = D$, $T JT^{-1} = -J$, rotational invariance: $D \sim J$,
 $T HT^{-1} = H$, $H = D \bullet E \rightarrow D = 0$ (D also violates P)

T invariant dynamics implies detailed balance, but not the other way around! (ex: thermal equilibrium can give detailed balance even if forces violate T)

$$S_{ba} = \langle \psi_b^- | \psi_a^+ \rangle = \langle T\psi_a^+ | T\psi_b^- \rangle = e^{i(\phi_b - \phi_a)} \langle \psi_a^- | \psi_b^+ \rangle \\ = e^{i(\phi_b - \phi_a)} S_{a'b}$$

Neutron Electric Dipole Moment

$$q_n = \int \rho(x) d^3x = (-0.4 \pm 1.1) \times 10^{-21} e$$



$$\vec{d}_n = \int \vec{x} \rho(x) d^3x = d_n \hat{s}$$

Non-zero d_n violates both P and T

Under a parity operation: Under a time-reversal operation:

$$\hat{s} \rightarrow \hat{s}, \quad \vec{E} \rightarrow -\vec{E} \quad \hat{s} \rightarrow -\hat{s}, \quad \vec{E} \rightarrow \vec{E}$$

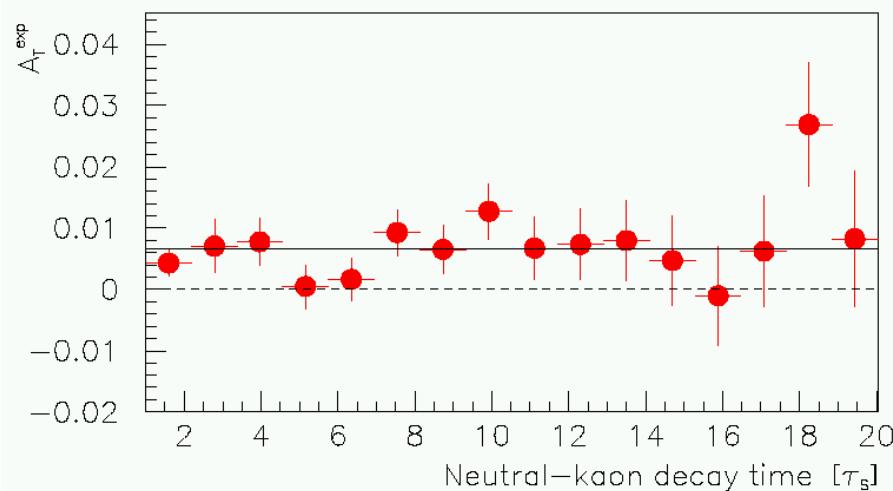
$$\vec{d}_n \cdot \vec{E} \rightarrow -\vec{d}_n \cdot \vec{E} \quad \vec{d}_n \cdot \vec{E} \rightarrow -\vec{d}_n \cdot \vec{E}$$

CP-Violation Experiments

Neutral Kaon System

Observation of T-violation at CPLEAR

$$A_T = \frac{P(\bar{K}^0 \rightarrow K^0) - P(K^0 \rightarrow \bar{K}^0)}{P(\bar{K}^0 \rightarrow K^0) + P(K^0 \rightarrow \bar{K}^0)}$$

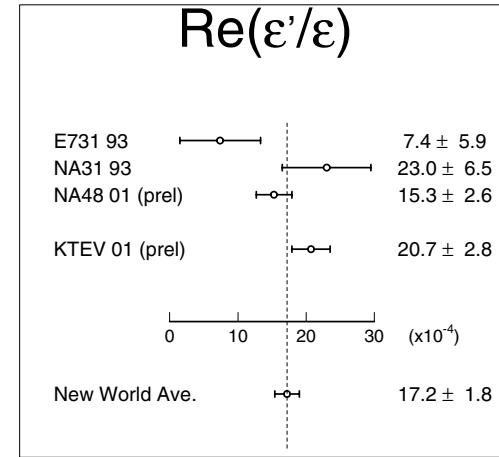


$$\langle A_T^{\text{exp}} \rangle = (6.6 \pm 1.3) \times 10^{-3}$$

(PLB 444(1998)43)

Observation of Direct CP-violation

$$R = \frac{\Gamma(K_L \rightarrow \pi^+ \pi^-)/\Gamma(K_S \rightarrow \pi^+ \pi^-)}{\Gamma(K_L \rightarrow \pi^0 \pi^0)/\Gamma(K_S \rightarrow \pi^0 \pi^0)}$$



$$\text{Re}(\epsilon'/\epsilon) = (17.2 \pm 1.8) \times 10^{-4}$$

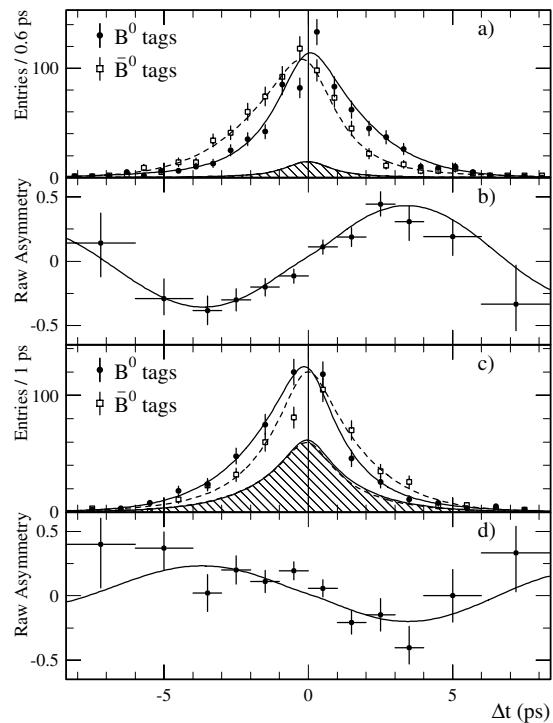
(hep-ex/0110020)

CP-Violation Experiments

Neutral B-Meson System

Observation of CP-violation at BaBar and Belle

$$A_{CP}(\Delta t) = \frac{f_+(\Delta t) - f_-(\Delta t)}{f_+(\Delta t) + f_-(\Delta t)} = -\eta_f \sin 2\beta \sin(\Delta m_d \Delta t)$$



BaBar: $\sin 2\beta = 0.741 \pm 0.067 \pm 0.034$

(hep-ex/0207042)

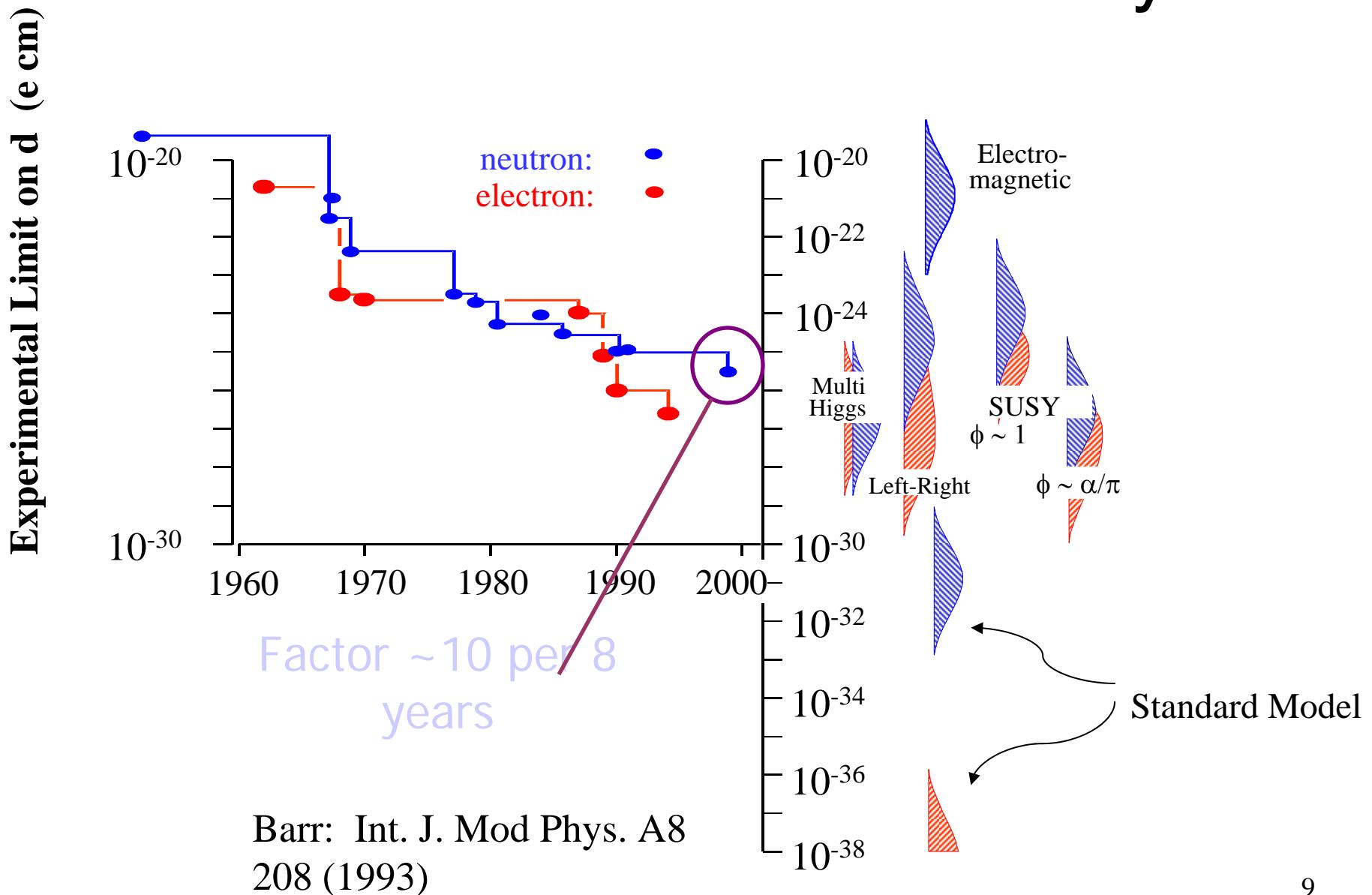
Belle: $\sin 2\beta = 0.719 \pm 0.074 \pm 0.035$

(hep-ex/0207098)

EDM candidates

- Neutron: Intrinsic EDM
- Electron/muon: Intrinsic EDM
- Atoms: P, T violating nucleon-nucleon or nucleon-electron interaction
- Ions?
 - all sensitive to different physics beyond SM
 - each gives new window on T
 - must measure all to distinguish between T violation models

EDM limits: the first 50 years

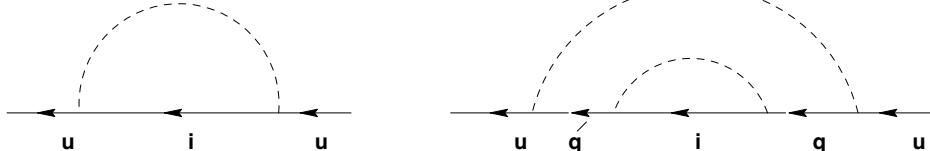


Neutron EDM in Standard Model

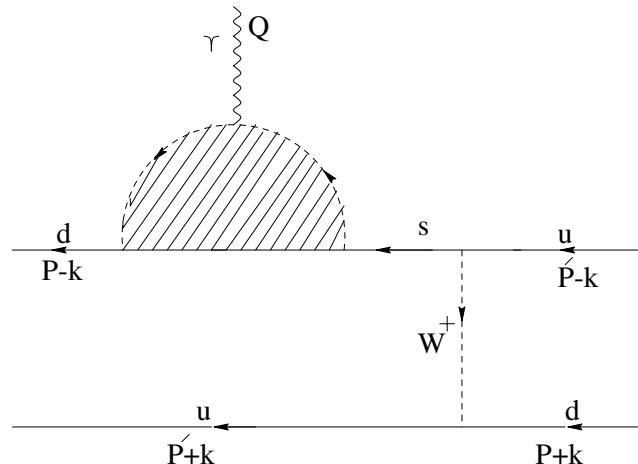
1) Electroweak Process

a) Contributions from single quark's EDM:

$$d_n \approx \frac{1}{3} d_u - \frac{4}{3} d_d$$



b) Contributions from diquark interactions:



$$d_n = \frac{38}{9\pi^3} (G_F m_N^2)^2 \frac{m_t^2}{m_s^2} \frac{m_N^2}{m_W^2} \frac{\Lambda}{m_N^4} \frac{e}{m_N} (\text{Im } V)$$

$$\text{Im } V = c_1 s_1^2 c_2 s_2 c_3 s_3 \sin(\delta)$$

$$d_n \sim 10^{-32} \text{ e}\cdot\text{cm}$$

One and two-loop contributions are zero.
Three-loop contribution is $\sim 10^{-34} \text{ e}\cdot\text{cm}$

(hep-ph/0008248)

Neutron EDM in Standard Model

2) Strong Interaction

θ term in the QCD Lagrangian :

$$L_\theta = \frac{\theta}{32\pi^2} \frac{g_s^2}{G_{\mu\nu}} \tilde{G}^{\mu\nu}$$

θ term's contribution to the neutron EDM :

$$d_n = \frac{e}{m_p} \frac{g_{\pi NN} \bar{g}_{\pi NN}}{4\pi^2} \ln \frac{m_\rho}{m_\pi}$$

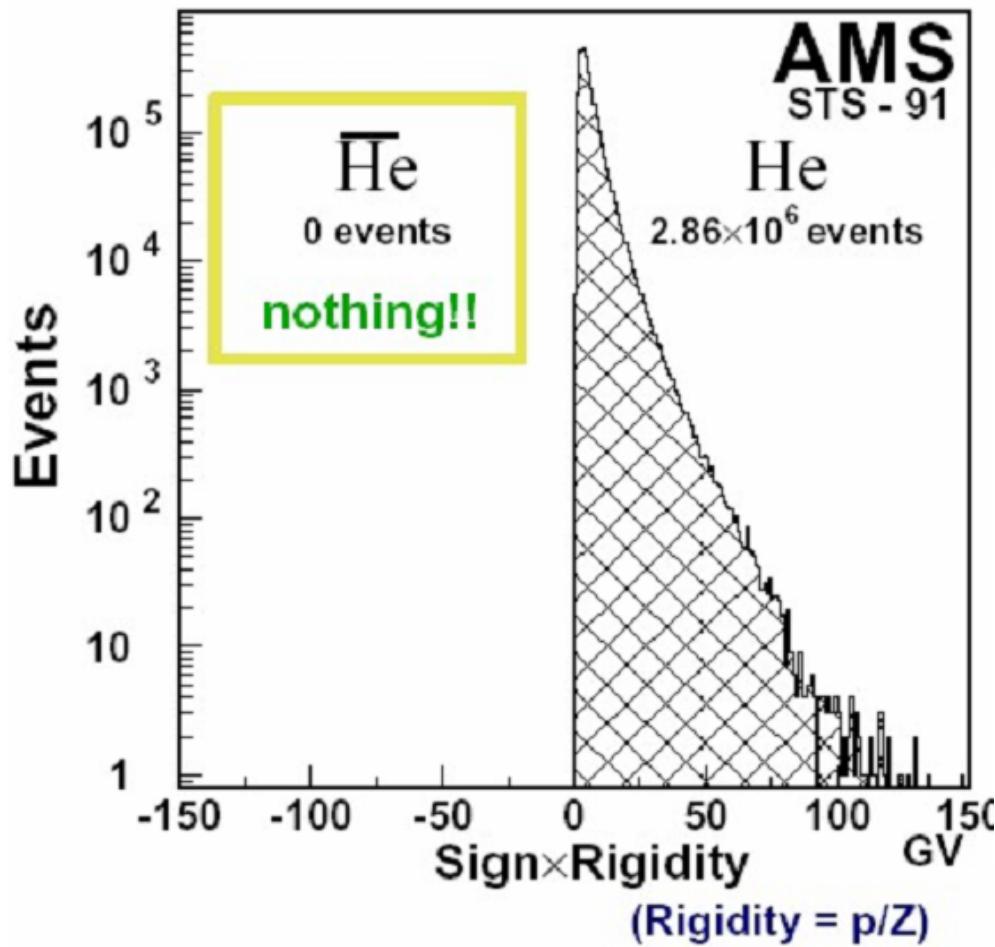
$$\bar{g}_{\pi NN} = -\theta \frac{m_u m_d}{m_u + m_d} \frac{\sqrt{2}}{f_\pi} \frac{M_\Xi - M_\Sigma}{m_s}$$

$$d_n < 10^{-25} \text{ e}\cdot\text{cm} \rightarrow |\theta| < 3 \times 10^{-10}$$

Spontaneously broken Pecci-Quinn symmetry?

No evidence of a pseudoscalar axion!

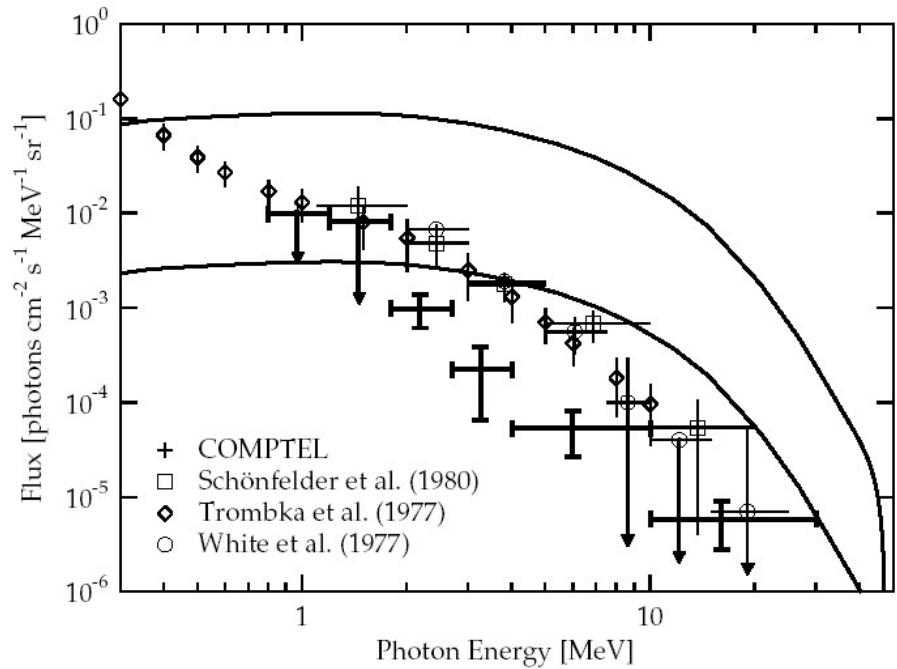
Where's the antimatter?



"Search for antihelium in cosmic rays"

Phys. Lett. B461 (1999) 387.

Diffuse γ -ray flux
expected from annihilation



Cohen, De Rujula, Glashow;
[astro-ph/9707087](https://arxiv.org/abs/astro-ph/9707087)

Sakharov conditions for Baryon Asymmetry in Big Bang

A.D. Sakharov, JETP Lett. 5, 24-27, 1967

1. Baryon number violation
 - Not allowed at tree level, but permitted in higher-order processes in SM
2. Departure from thermal equilibrium
 - Expansion of Universe
 - Phase transitions
3. T violation
 - Note SM CPv is *orders of magnitude* too small to explain observed asymmetry – *we need new physics.*
 - Whatever model you choose, the larger-than-SM CPv brings with it a larger-than-SM EDM

Physics Motivation for Neutron EDM Measurement

- Time Reversal Violation
- Physics Beyond the Standard Model
 - Standard Model predicts $d_n \sim 10^{-31} \text{ e}\cdot\text{cm}$
 - Super Symmetric Models predict $d_n \leq 10^{-25} \text{ e}\cdot\text{cm}$
- Baryon Asymmetry of universe
 - Require CP violation beyond the SM

	SM Prediction	Experiment
e	$10^{-40} \text{ e}\cdot\text{cm}$	$10^{-27} \text{ e}\cdot\text{cm}$
p	$10^{-38} \text{ e}\cdot\text{cm}$	$10^{-19} \text{ e}\cdot\text{cm}$
n	$10^{-31} \text{ e}\cdot\text{cm}$	$10^{-25} \text{ e}\cdot\text{cm}$

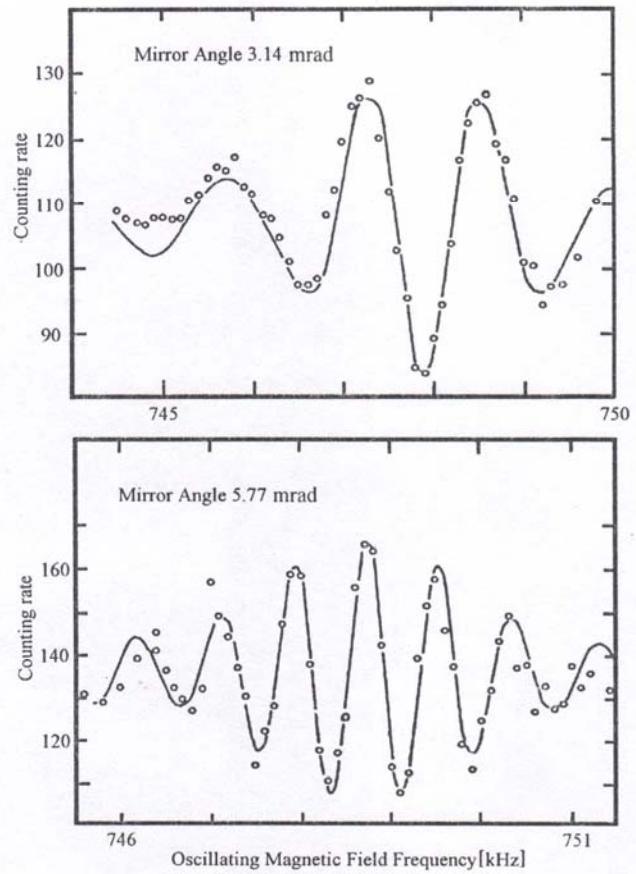
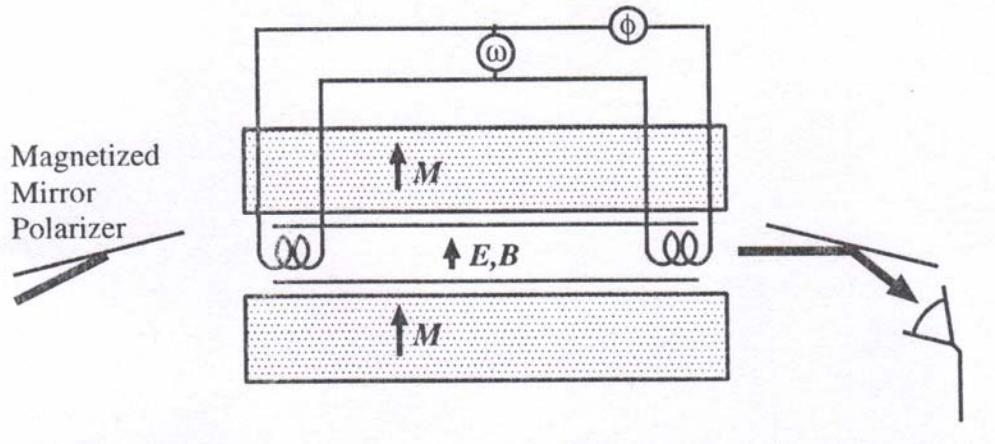
List of Neutron EDM Experiments

Ex. Type	$\langle v \rangle$ (m/cm)	E (kV/cm)	B (Gauss)	Coh. Time (s)	EDM (e.cm)	year
Scattering	2200	10^{25}	--	10^{-20}	$< 3 \times 10^{-18}$	1950
Beam Mag. Res.	2050	71.6	150	0.00077	$< 4 \times 10^{-20}$	1957
Beam Mag. Res.	60	140	9	0.014	$< 7 \times 10^{-22}$	1967
Bragg Reflection	2200	10^9	--	10^{-7}	$< 8 \times 10^{-22}$	1967
Beam Mag. Res.	130	140	9	0.00625	$< 3 \times 10^{-22}$	1968
Beam Mag. Res.	2200	50	1.5	0.0009	$< 1 \times 10^{-21}$	1969
Beam Mag. Res.	115	120	17	0.015	$< 5 \times 10^{-23}$	1969
Beam Mag. Res.	154	120	14	0.012	$< 1 \times 10^{-23}$	1973
Beam Mag. Res.	154	100	17	0.0125	$< 3 \times 10^{-24}$	1977
UCN Mag. Res.	<6.9	25	0.028	5	$< 1.6 \times 10^{-24}$	1980
UCN Mag. Res.	<6.9	20	0.025	5	$< 6 \times 10^{-25}$	1981
UCN Mag. Res.	<6.9	10	0.01	60-80	$< 8 \times 10^{-25}$	1984
UCN Mag. Res.	<6.9	12-15	0.025	50-55	$< 2.6 \times 10^{-25}$	1986
UCN Mag. Res.	<6.9	16	0.01	70	$< 12 \times 10^{-26}$	1990
UCN Mag. Res.	<6.9	12-15	0.018	70-100	$< 9.7 \times 10^{-26}$	1992
UCN Mag. Res.	<6.9	4.5	0.01	120-150	$< 6.3 \times 10^{-26}$	1999

$$H = -\vec{\mu} \cdot \vec{B} \pm \vec{d} \cdot \vec{E} \quad B = 1 \text{ mG} \Rightarrow 3 \text{ Hz neutron precession freq.}$$

$$d = 10^{-26} \text{ e}\cdot\text{cm}, E = 10 \text{ KV/cm} \Rightarrow 10^{-7} \text{ Hz shift in precession freq.}$$

Neutron Beam EDM Experiments

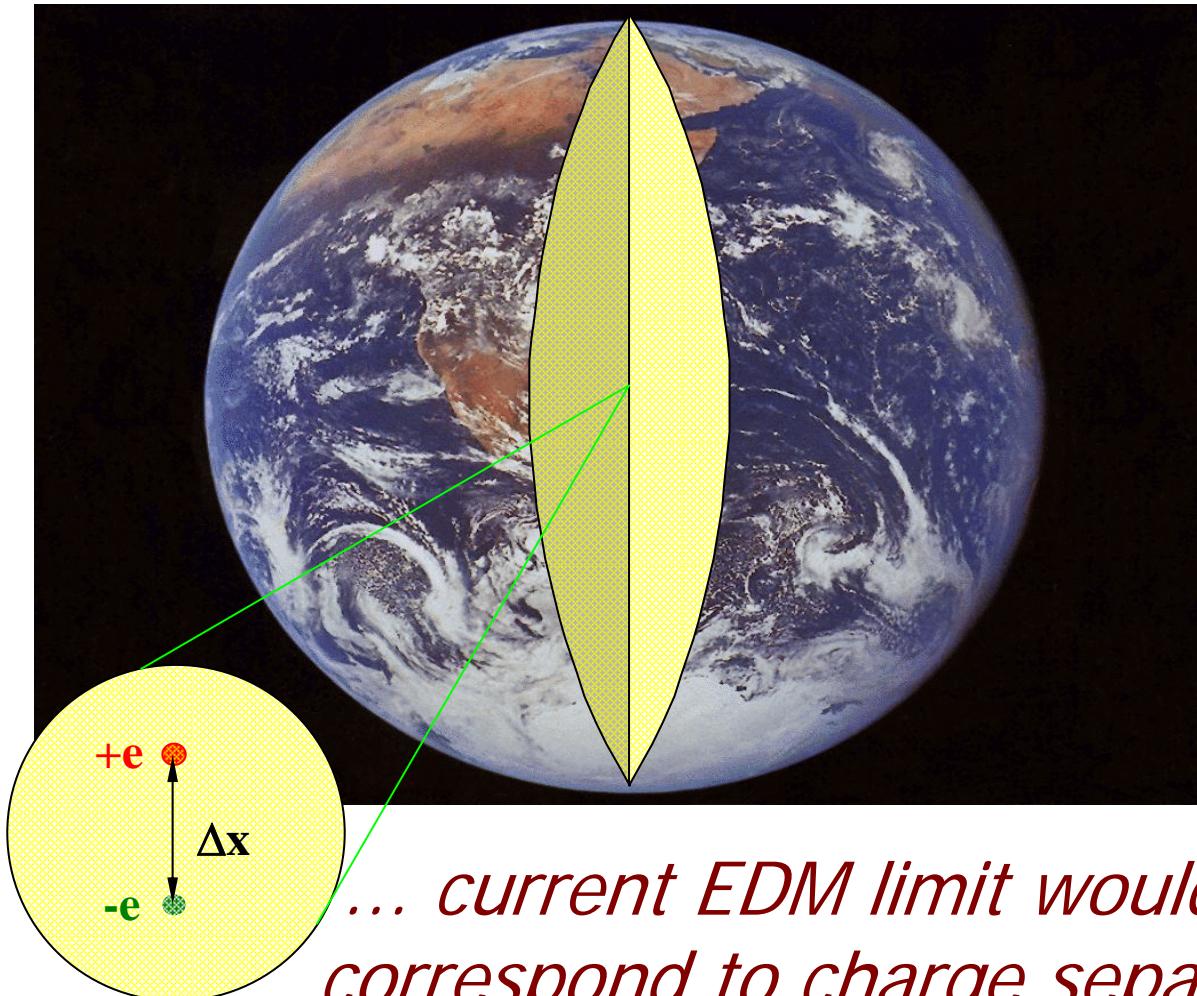


Limitations:

- Short duration between the two RF pulses
- Systematic error due to motional magnetic field ($v \times E$)

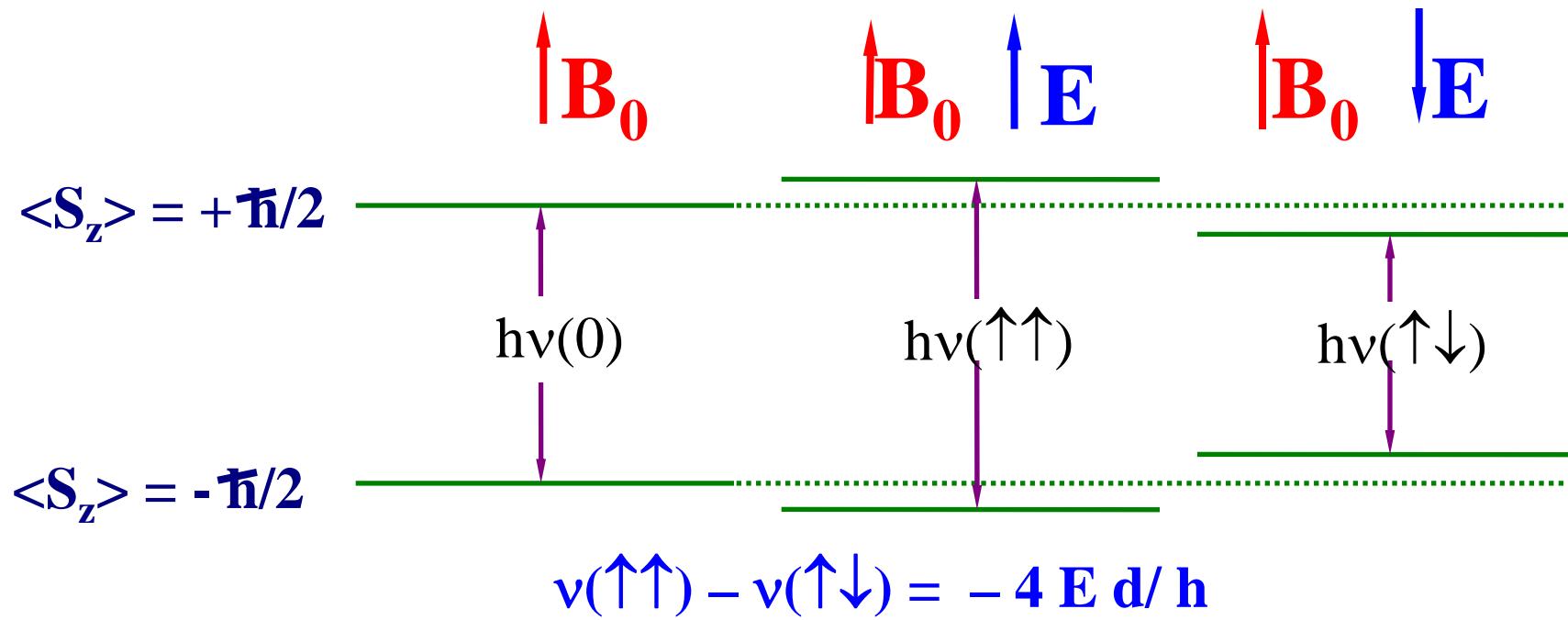
Both can be improved using lower-energy neutrons

Reality check



*... current EDM limit would
correspond to charge separation of
 $\Delta x \approx 10\mu$*

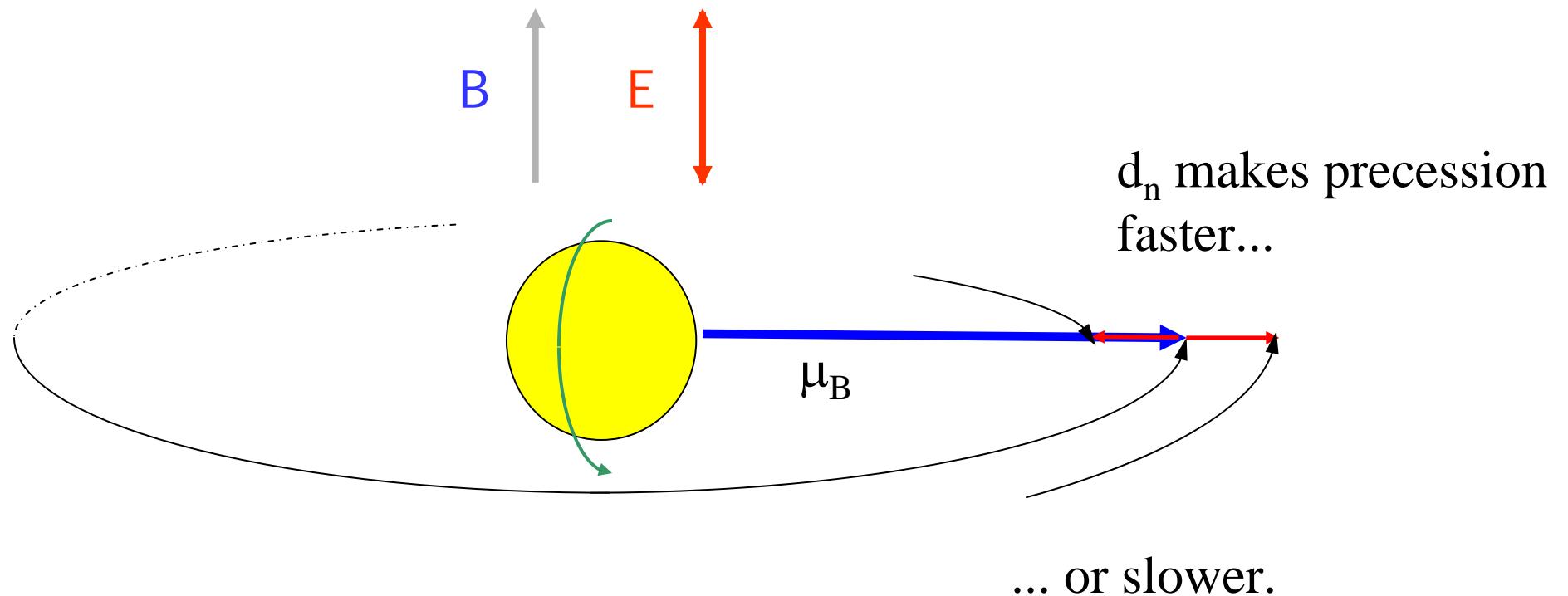
EDM Measurement principle



assuming B unchanged when E is reversed.

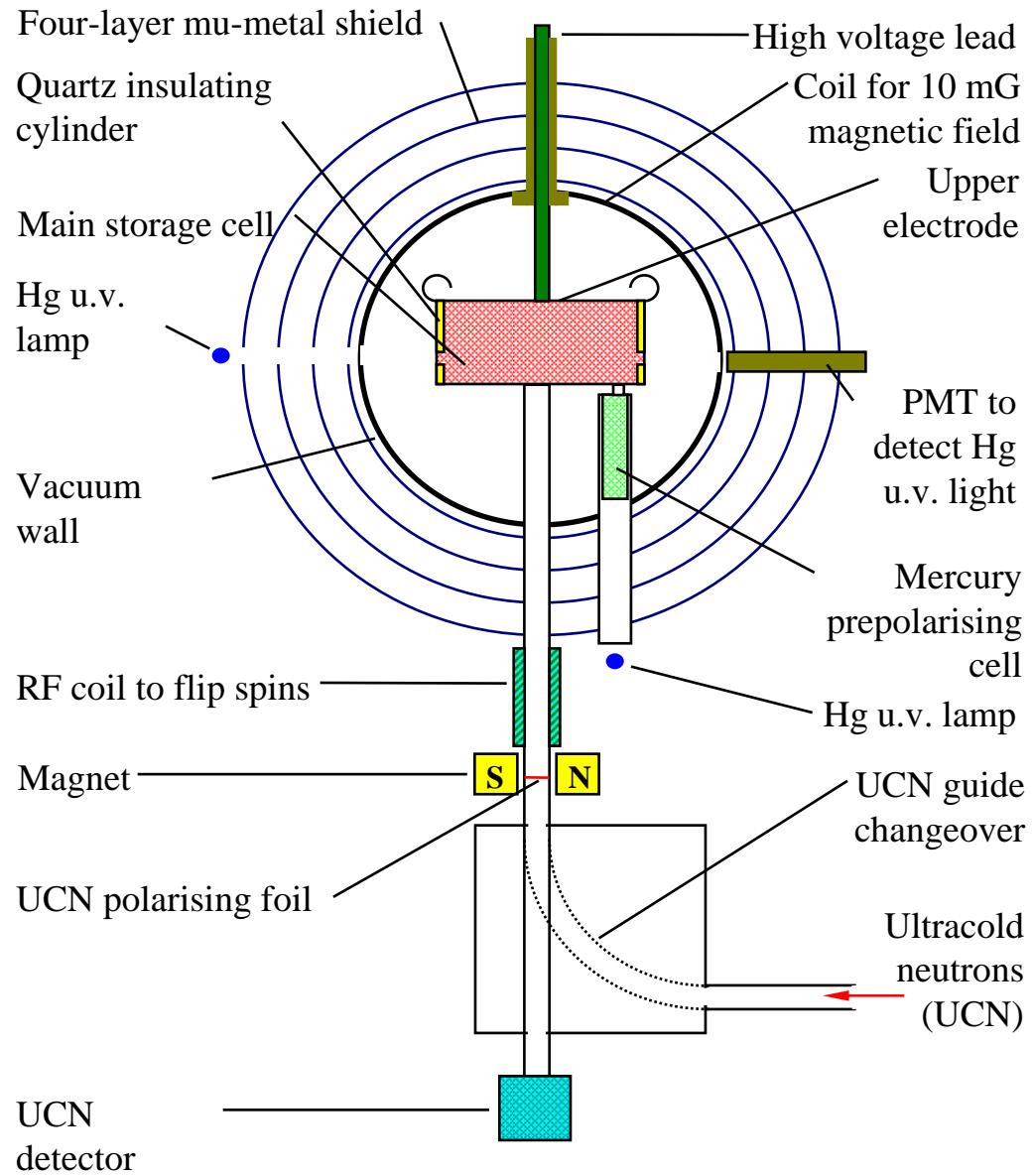
Measurement principle

- Measure Larmor spin precession freq in parallel & antiparallel **B** and **E** fields

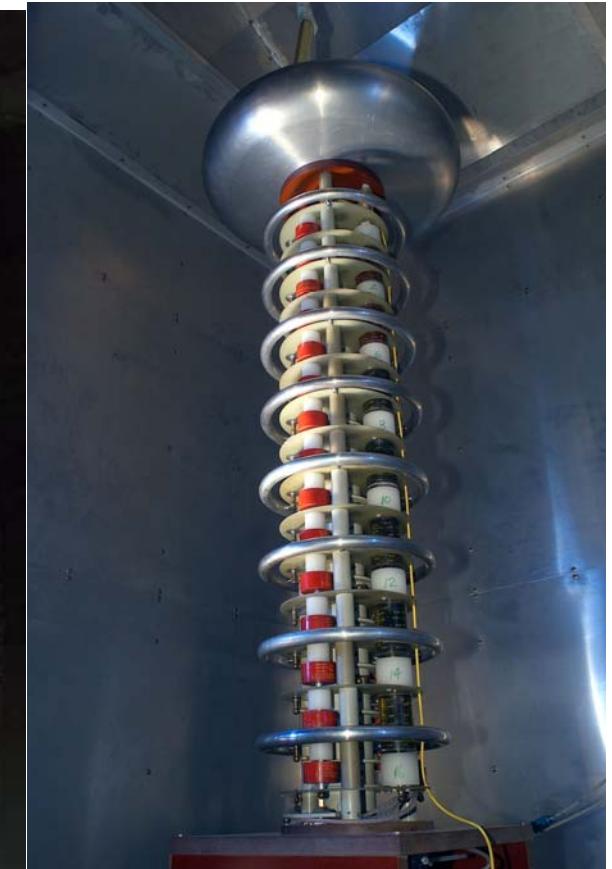
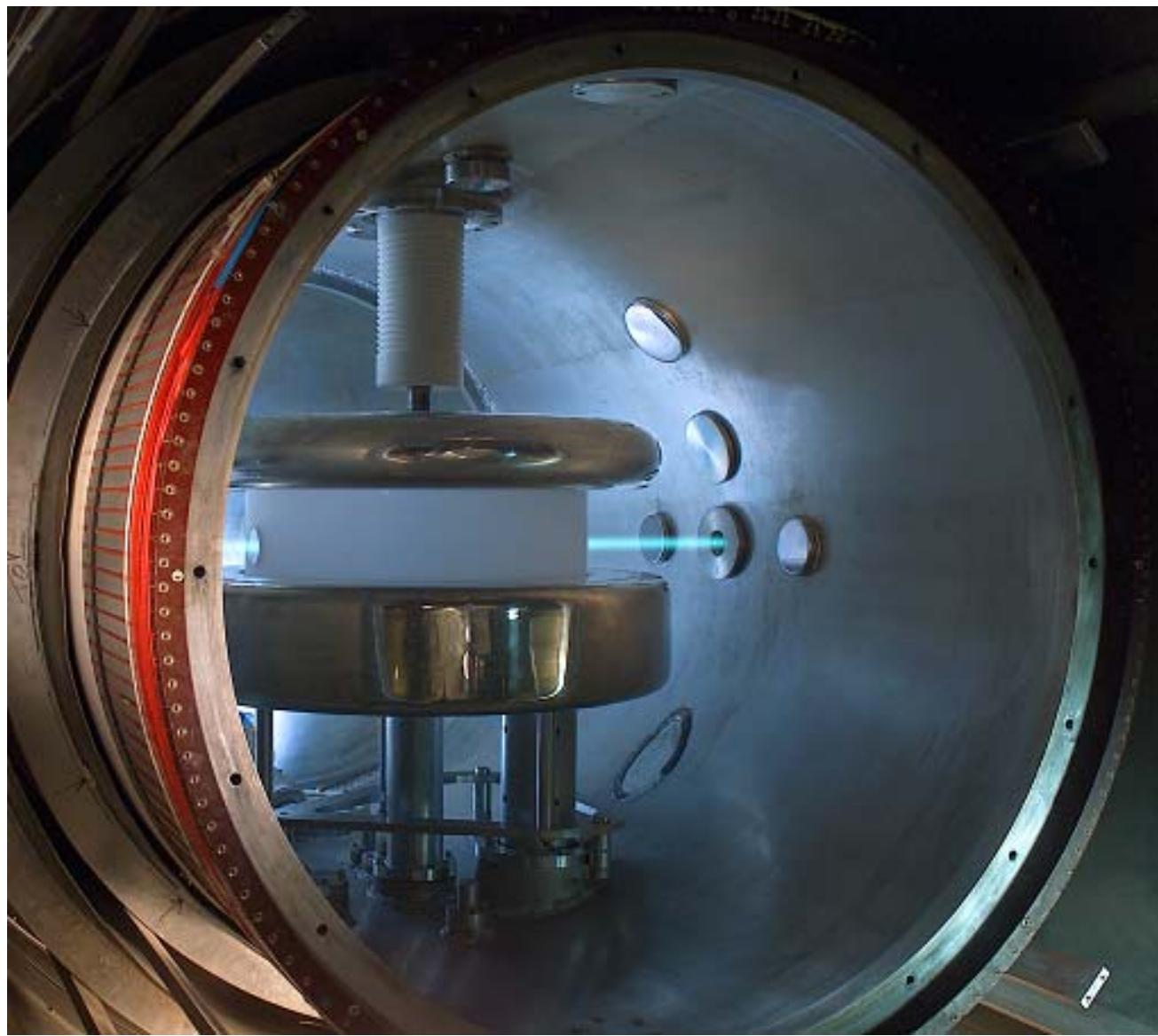


So, reverse E relative to B and look for freq shift.

nEDM apparatus at ILL



Neutron storage bottle



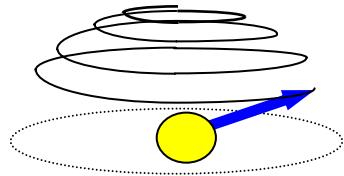
Ramsey method of Separated Oscillating Fields

1.



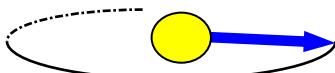
*“Spin up”
neutron...*

2.



*Apply $\pi/2$
spin
flip pulse...*

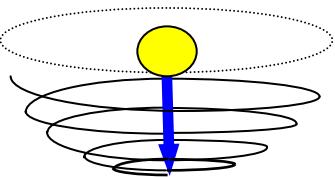
3.



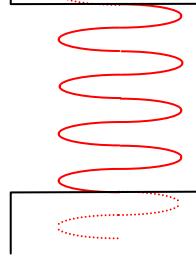
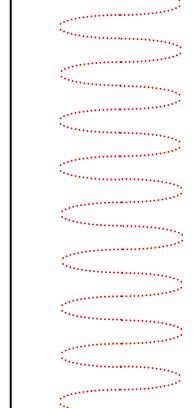
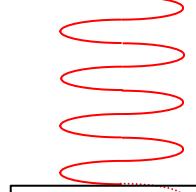
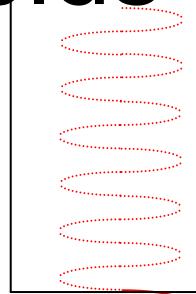
*Free
precession.*

..

4.

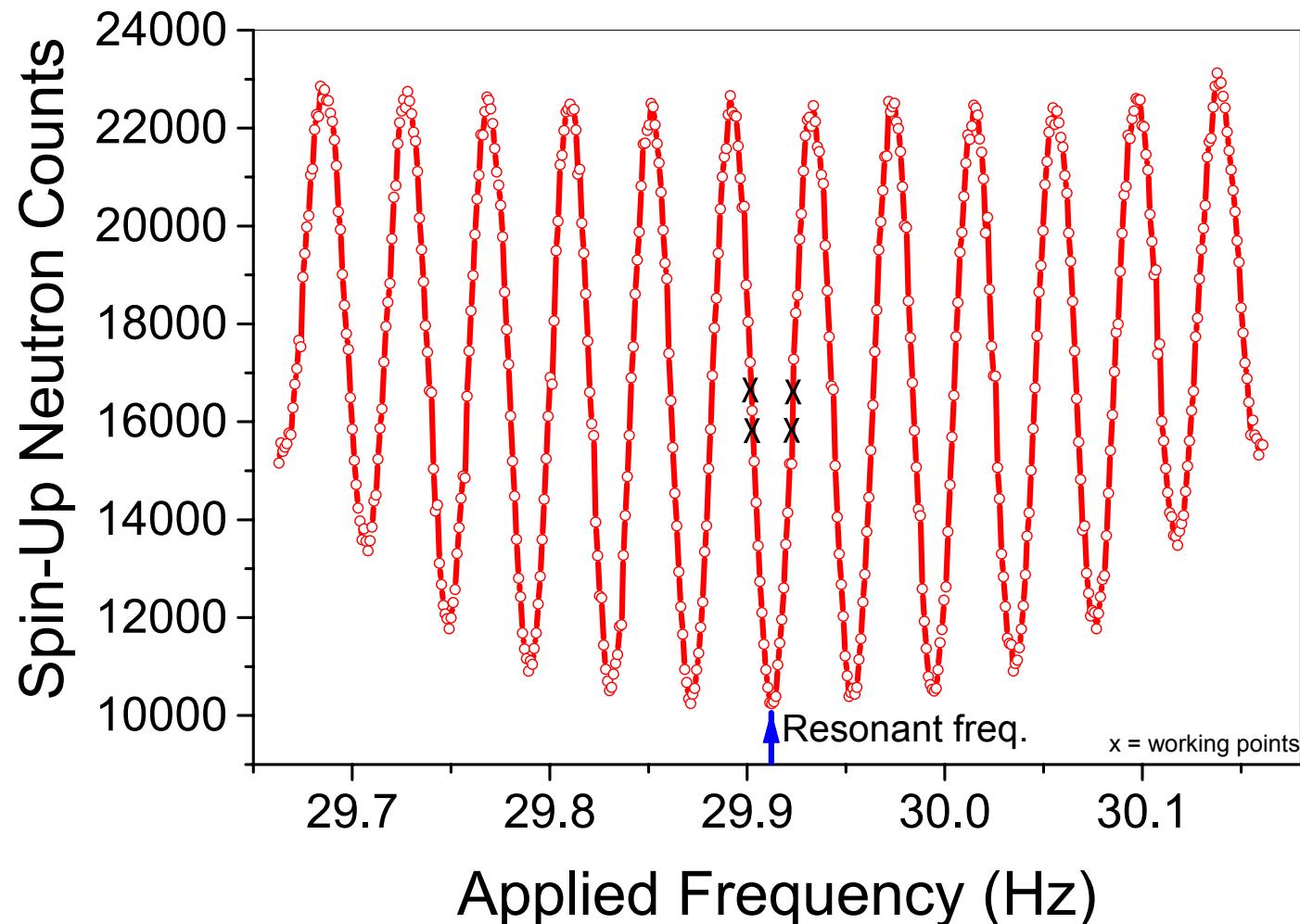


*Second $\pi/2$
spin
flip pulse.*



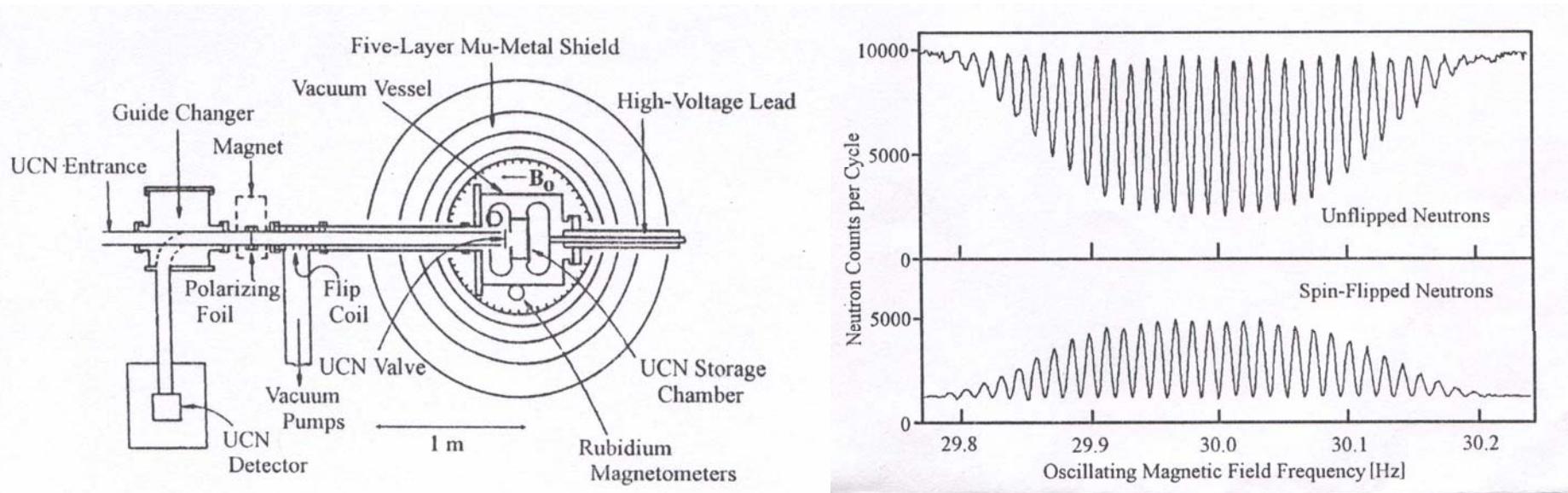
Ramsey resonance

- “2-slit” interference pattern
- Phase gives freq offset from resonance



Neutron EDM Experiment with Ultra Cold Neutrons

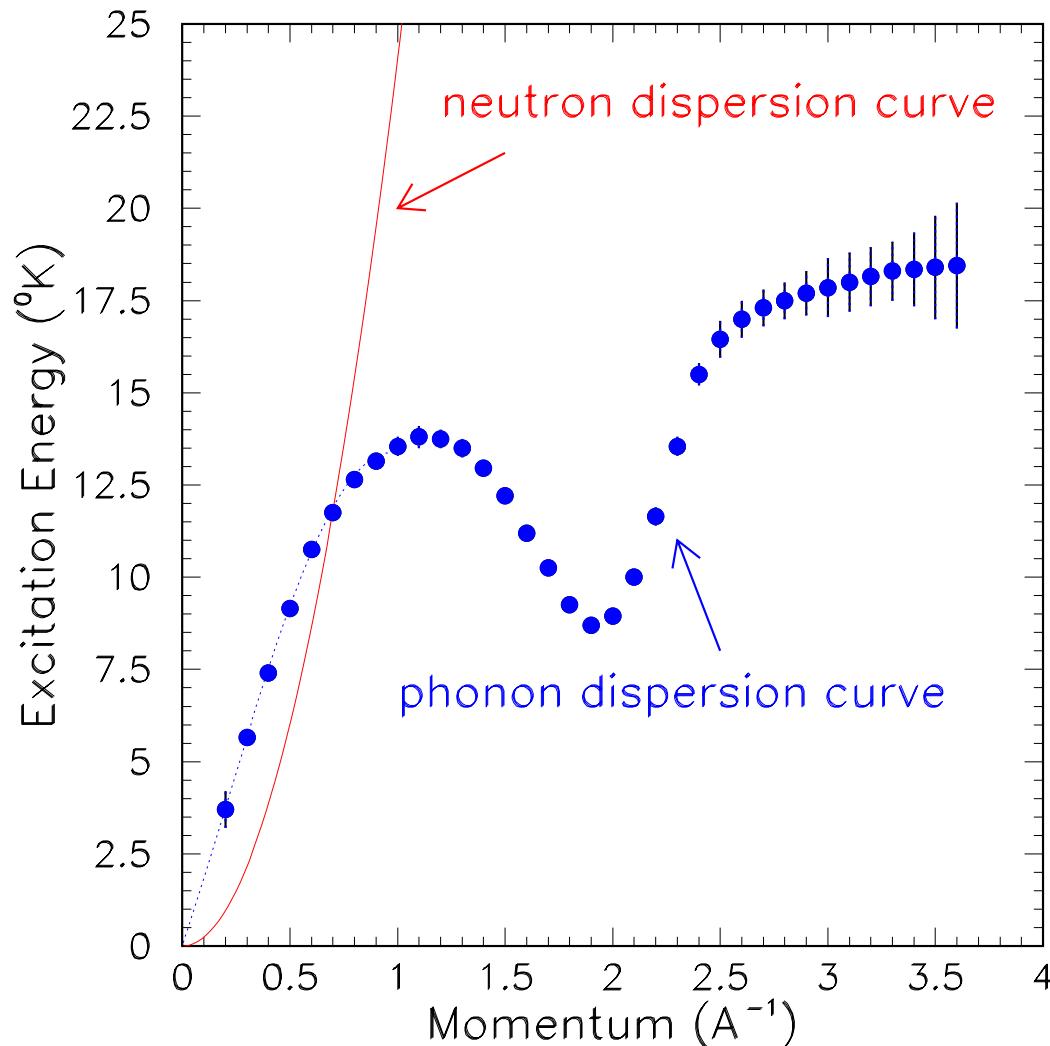
Most Recent ILL Measurement



- Use ^{199}Hg co-magnetometer to sample the variation of B-field in the UCN storage cell
- Limited by low UCN flux of $\sim 5 \text{ UCN/cm}^3$
- Figure-of-merit $\sim E(NT)^{1/2}$

A new approach aims at $N \rightarrow 100 \text{ N}$, $T \rightarrow 5 \text{ T}$, $E \rightarrow 5 \text{ E}$

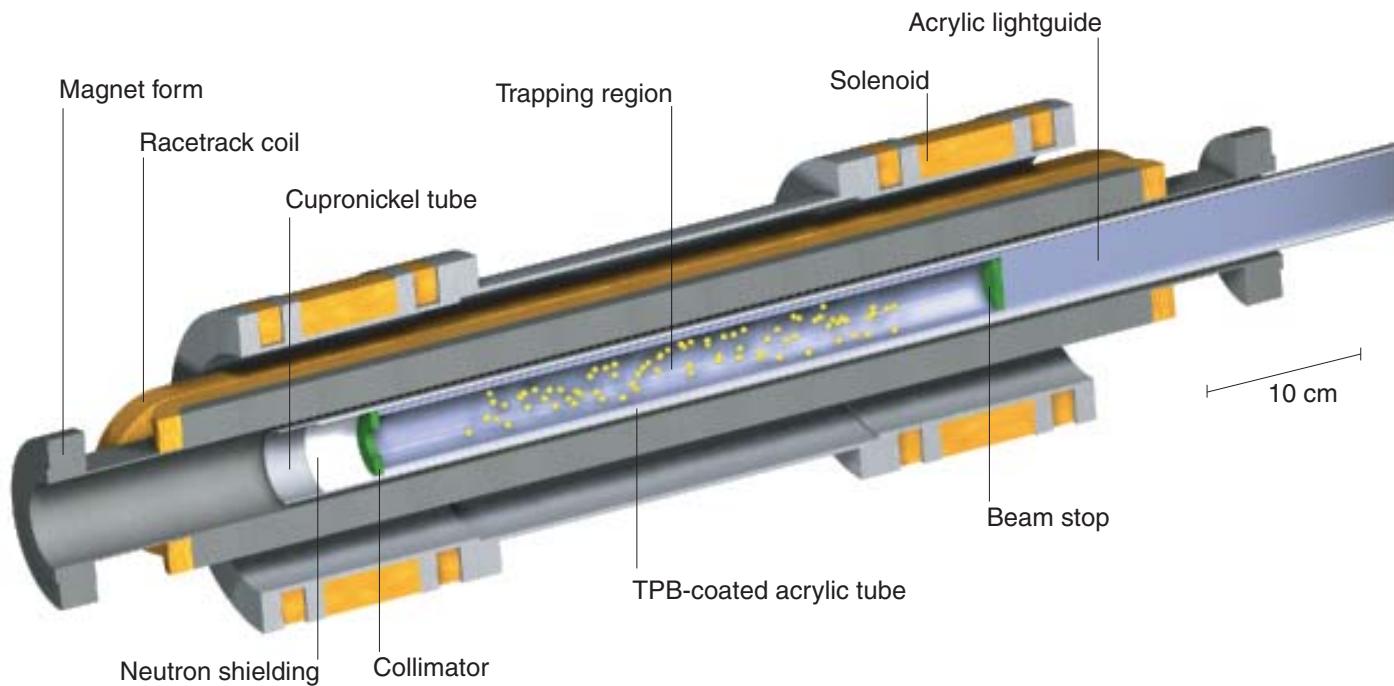
UCN Production in Superfluid ^4He



Incident cold neutron with momentum of 0.7 \AA^{-1} (1 mev)
can excite a phonon in ^4He and become an UCN

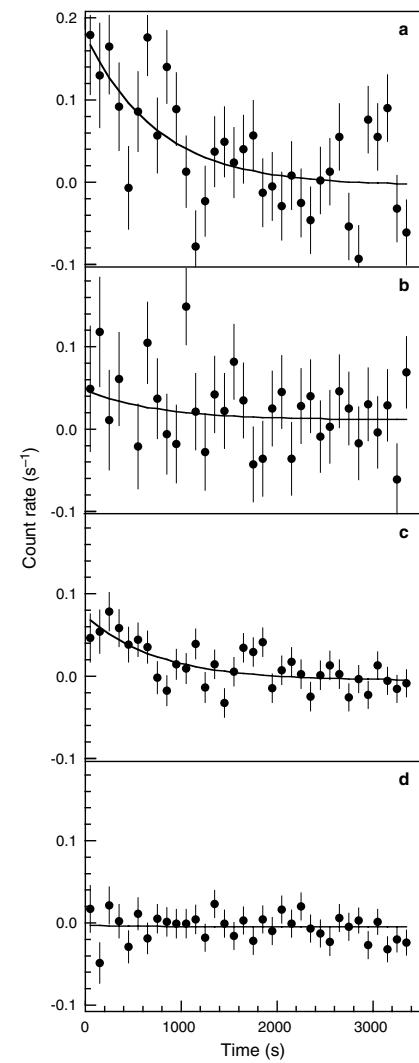
UCN Production in Superfluid ^4He

Magnetic Trapping of UCN (Nature 403 (2000) 62)



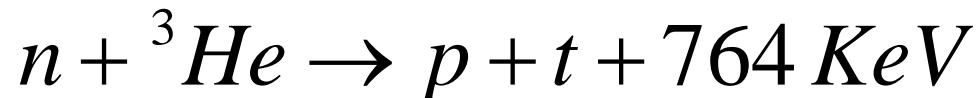
560 ± 160 UCNs trapped per cycle (observed)

480 ± 100 UCNs trapped per cycle (predicted)



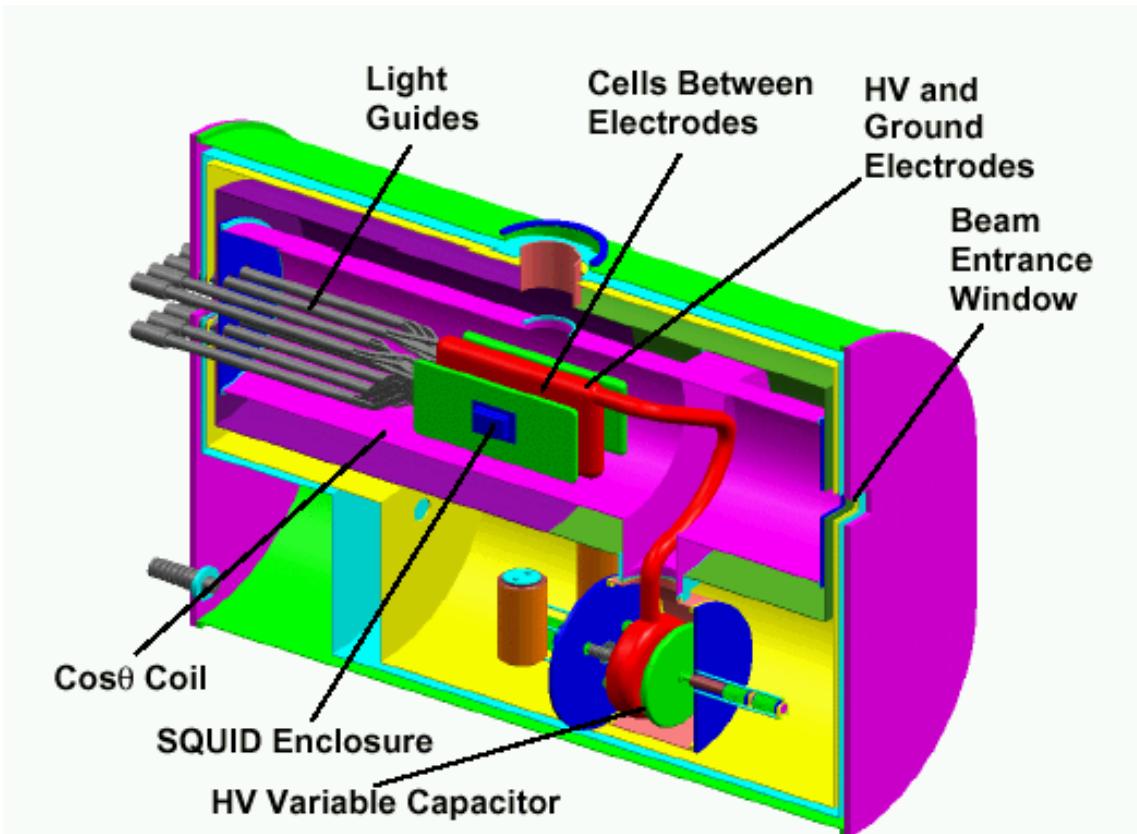
UCN Losses in Superfluid ^4He Bottle

- Neutron beta decay
- Wall absorption
- Upscattering in superfluid ^4He
 - Single-phonon upscattering rate $\sim e^{-1/KT}$
 - Multi-phonon upscattering rate $\sim T^7$
- $n - ^3\text{He}$ absorption
 - Require purified ^4He with $^3\text{He}/^4\text{He} < 10^{-11}$



Total spin	σ_{abs} at $v = 5\text{ m/sec}$
$J = 0$	$\sim 4.8 \times 10^6 \text{ barns}$
$J = 1$	~ 0

A Preproposal by the UCN Collaboration



(Based on the idea originated by R. Golub and S. Lamoreaux in 1994)

Collaborating institutes:

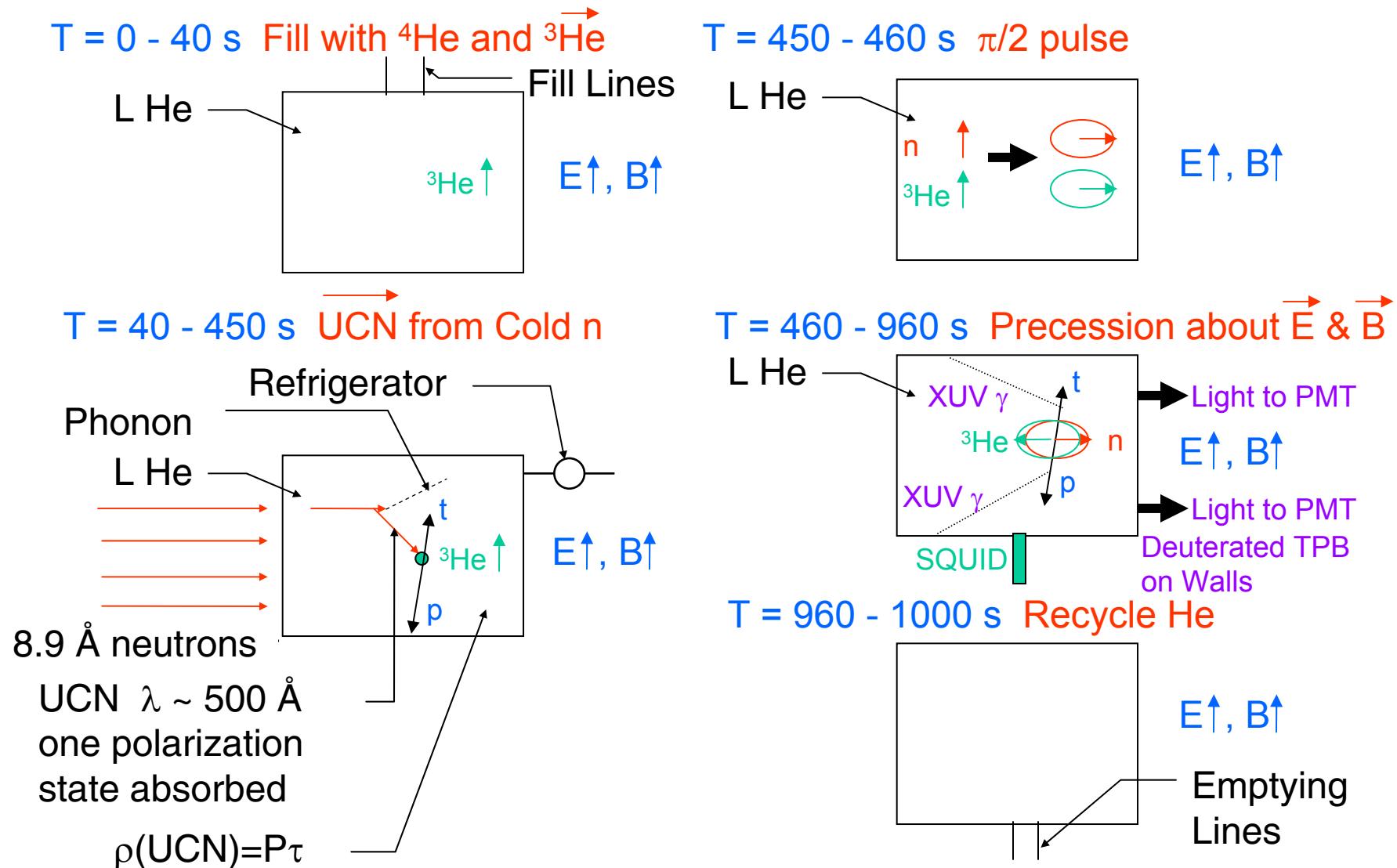
UC Berkeley, Caltech, Duke, Hahn-Meitner, Harvard,
Hungarian Academy of Sciences, UIUC, ILL, Leiden, LANL,
NIST, UNM, ORNL, Simon-Fraser

Neutron EDM Measurement Cycle

- Fill cells with superfluid ^4He containing polarized ^3He
- Produce polarized UCNs with polarized cold neutron beam
- Flip n and ^3He spin by 90° using a $\pi/2$ RF coil
- Precess UCN and ^3He in a uniform B field ($\sim 1\text{mG}$) and a strong E field ($\sim 50\text{KV/cm}$). ($v(^3\text{He}) \sim 3.3\text{ Hz}$, $v(n) \sim 3\text{ Hz}$)
- Detect scintillation light from the reaction $n + ^3\text{He} \rightarrow p + t$ (and from other sources, including neutron beta decays)
- Empty the cells and change E field direction and repeat the measurement

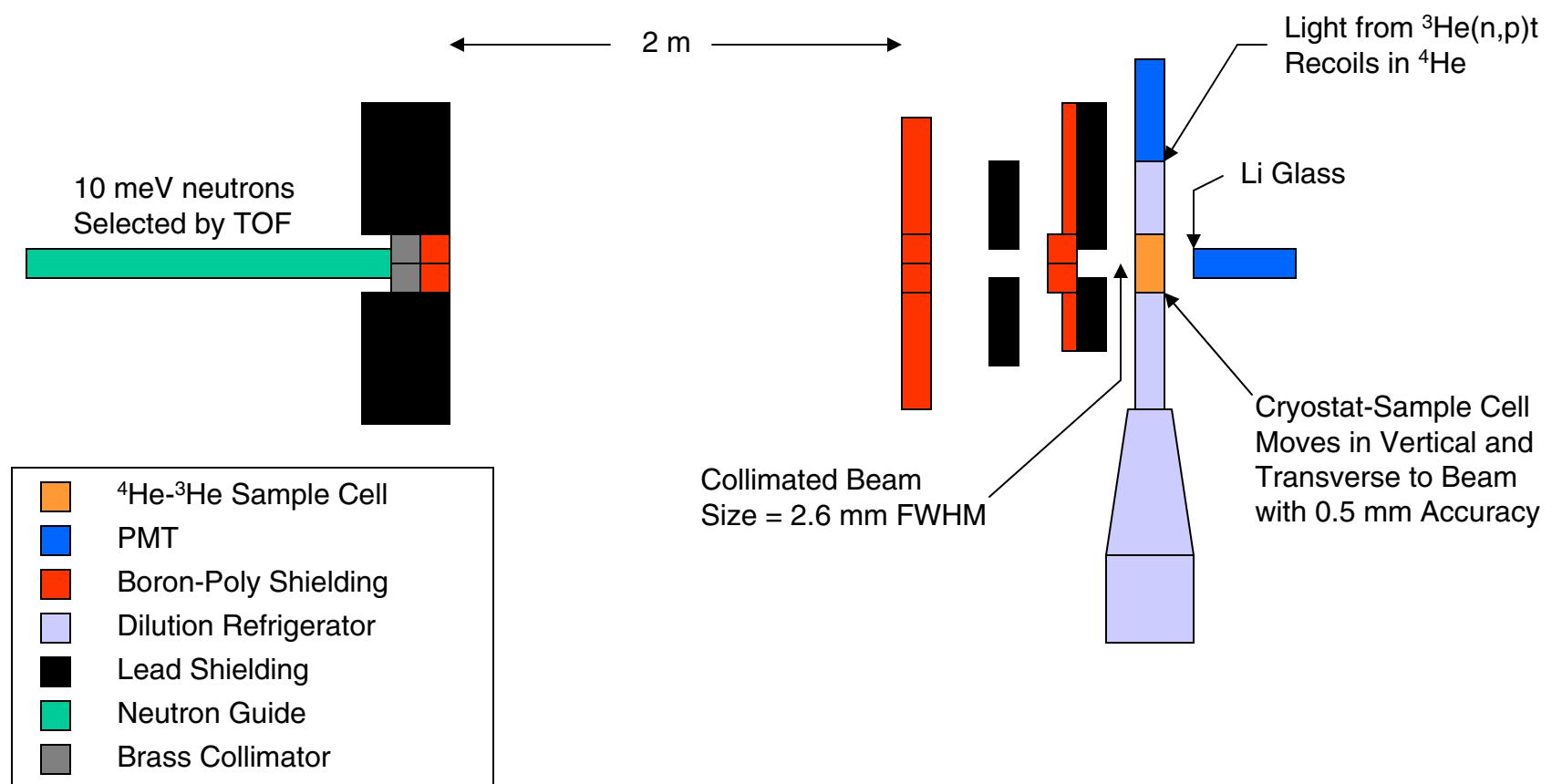
$$\phi(t) = Ne^{-\Gamma_{tot}t} \left\{ \frac{1}{\tau_\beta} + \frac{1}{\tau_3} [1 - P_3 P_n \cos(\omega_r t + \phi)] \right\}$$

EXPERIMENT CYCLE



EXPERIMENTAL LAYOUT

LANSCE FP 11a



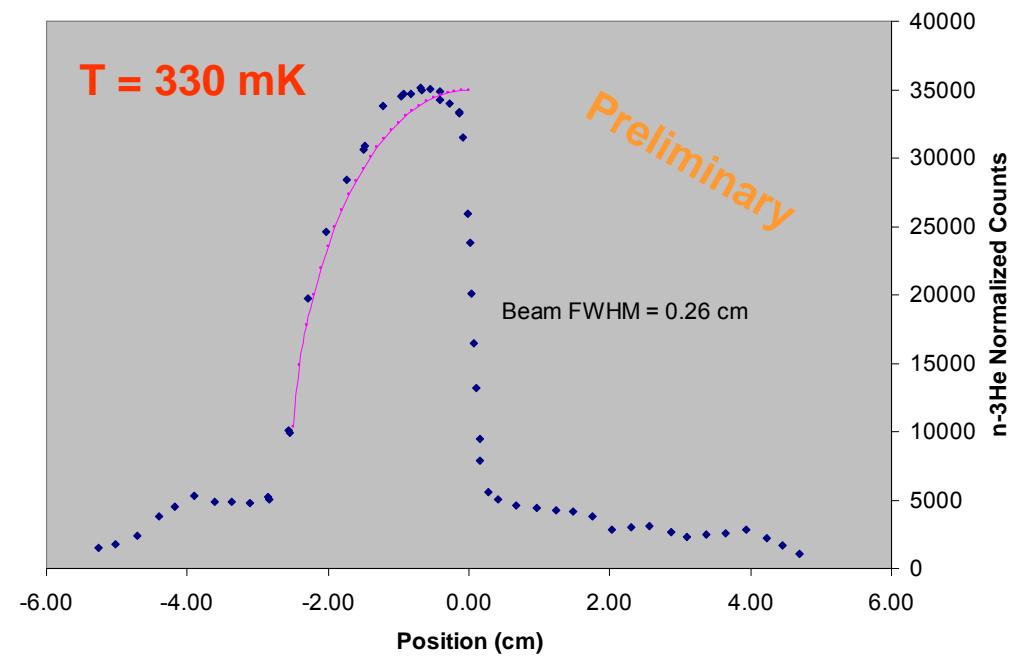
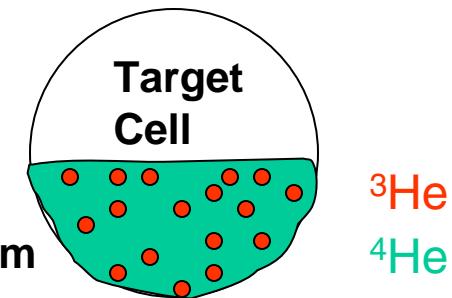
^3He Distributions in Superfluid ^4He

Dilution Refrigerator at
LANSCE Flight Path 11a

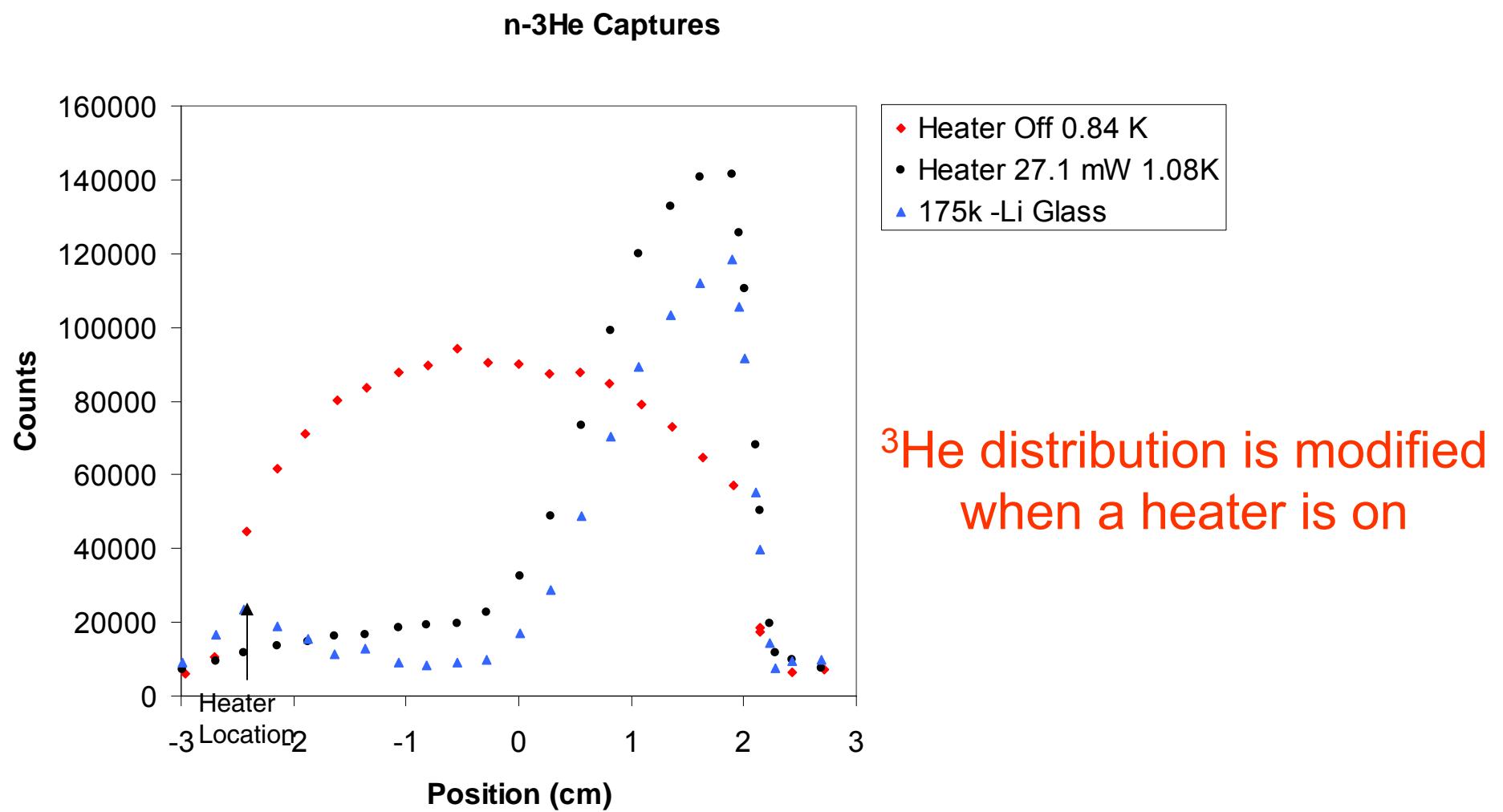


Position

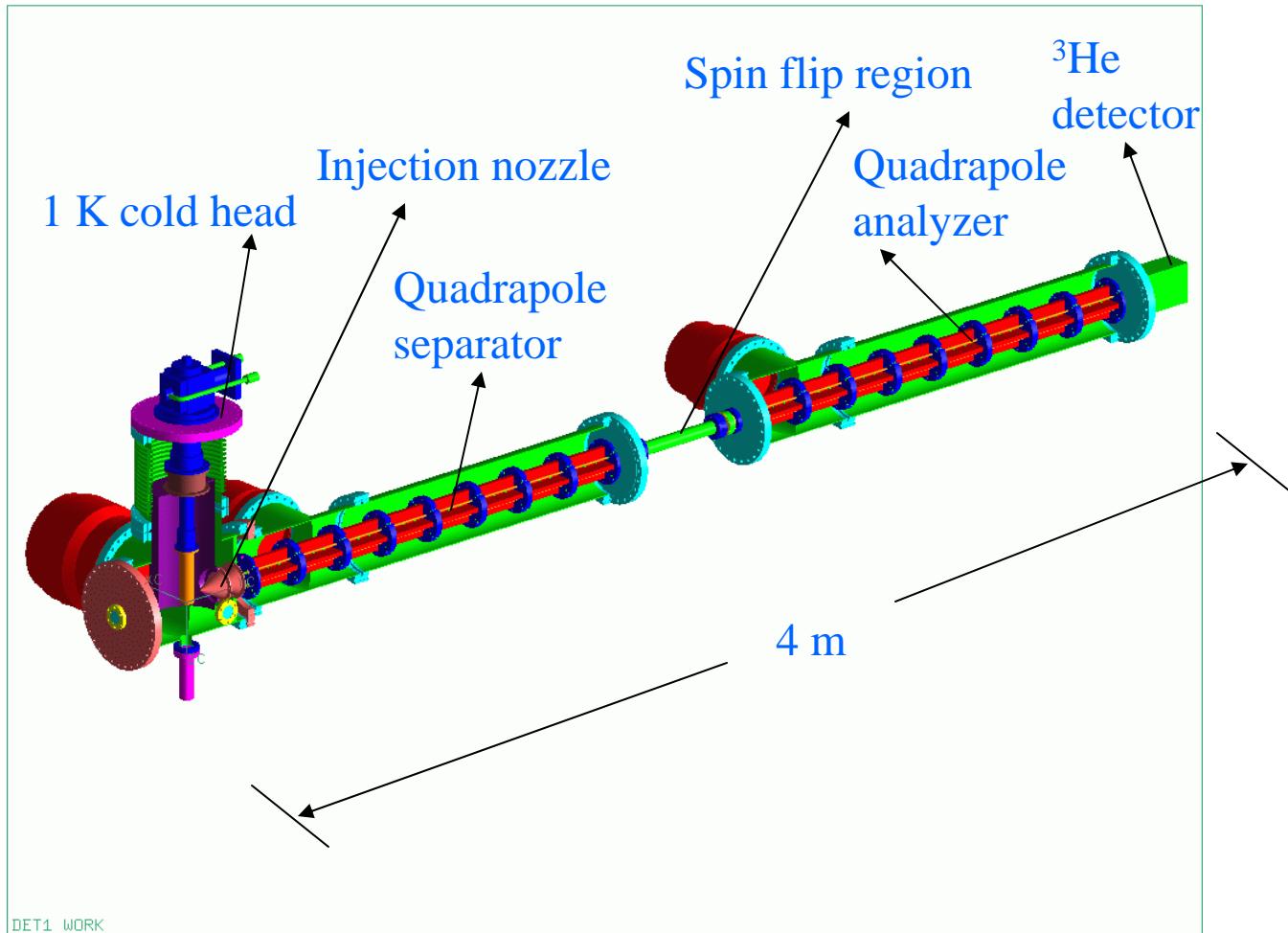
Neutron Beam



HEAT EFFECTS

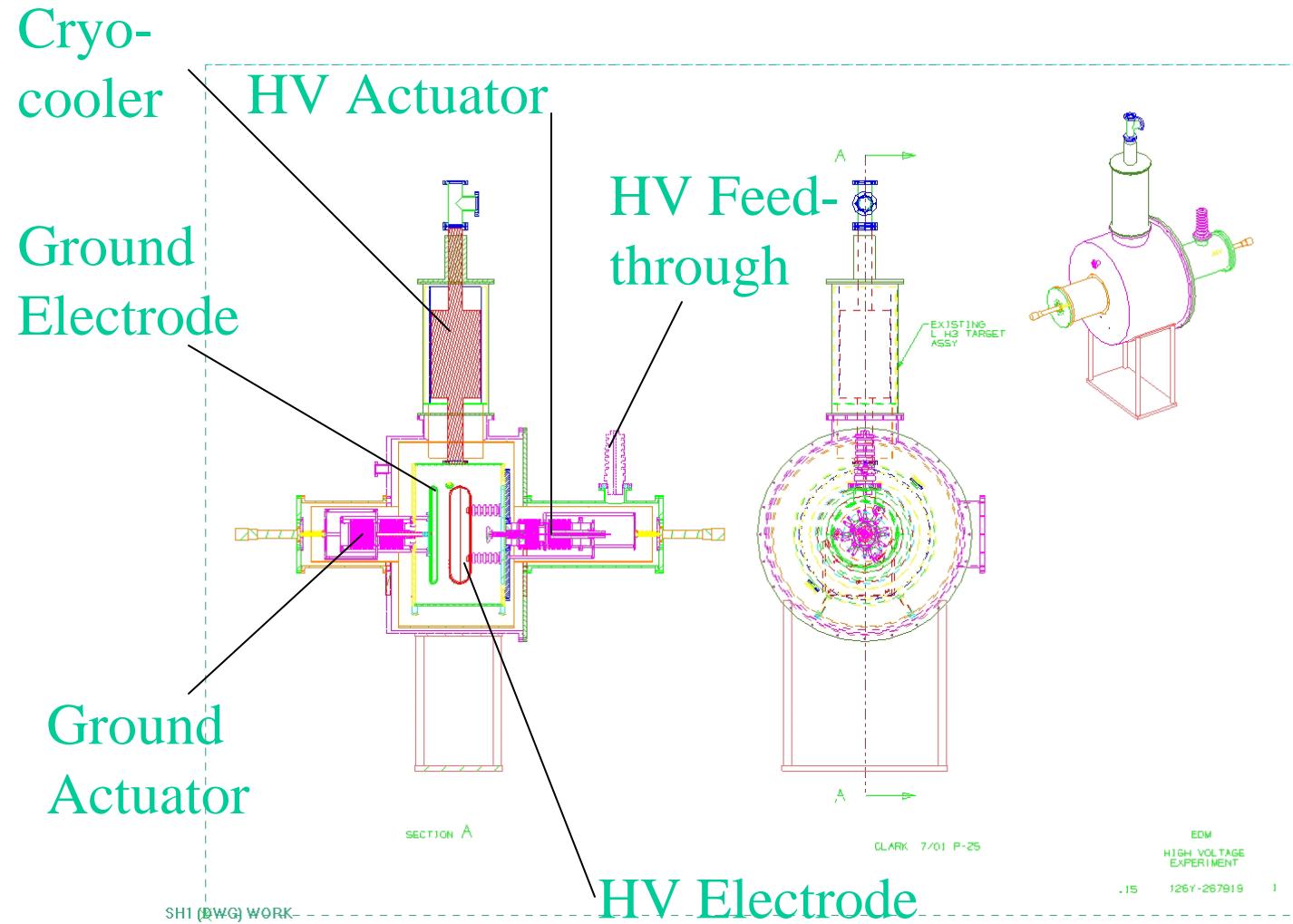


POLARIZED ^3He SOURCE



Being constructed and tested at Los Alamos

Electric Field Test



Voltage amplification / Variable capacitor / Moveable HV contact

What motivates searches for B Violation?

- Baryon asymmetry of the universe (BAU) requires B violation if it is not present in the initial conditions
 - *Sakharov (1967), Kuzmin (1970)*
- In Standard Model baryon number is not conserved
 - (at the non-perturbative level) *'t Hooft (1976) ...*
- Idea of Unification of particles and their interactions predict various mechanisms for B violation
 - *Pati & Salam (1973): quark–lepton unification, Left - Right symmetry, Georgi & Glashow (1974): SU(5) - unification of forces ...*
 - New low quantum gravity scale models: *N. Arkani-Hamed, S. Dimopoulos, G. Dvali (1998) ...*

Conservation or violation of (B-L) is an essential issue

Conservation of angular momentum in N disappearance

$$\rightarrow \Delta B = \pm \Delta L \quad \text{or} \quad |\Delta(B-L)| = 0, 2$$

In Standard Model and in GUTS which lead to proton decay, $\Delta(B-L) = 0$

What about $|\Delta(B-L)| = 2$?

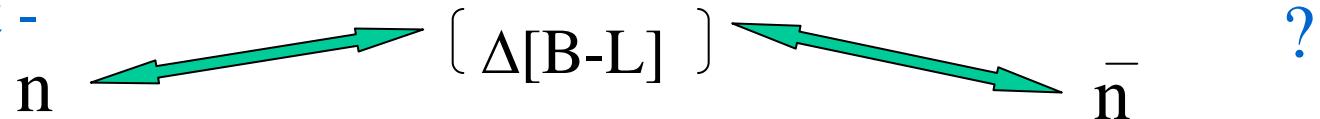
$n \otimes \bar{n}$ transitions — “too crazy”? But neutral meson $|q\bar{q}\rangle$ states oscillate -



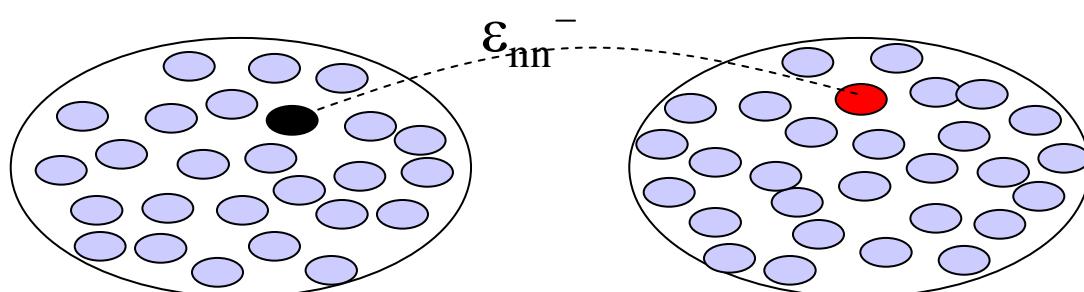
And neutral fermions can oscillate too -



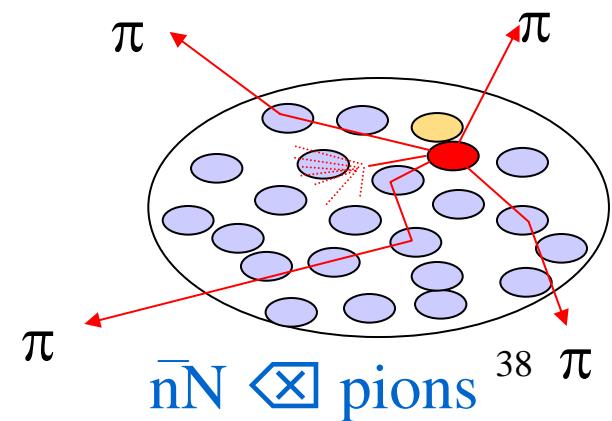
So why not -



$n\bar{n}$ signature is nN annihilation:



$$\text{Nucleus A} \otimes \text{A}^* + n$$



What Mass Scale is probed?

in the lowest order the n-nbar transition should involve a 6-quark operator with the amplitude suppressed by $\sim m^{-5}$:

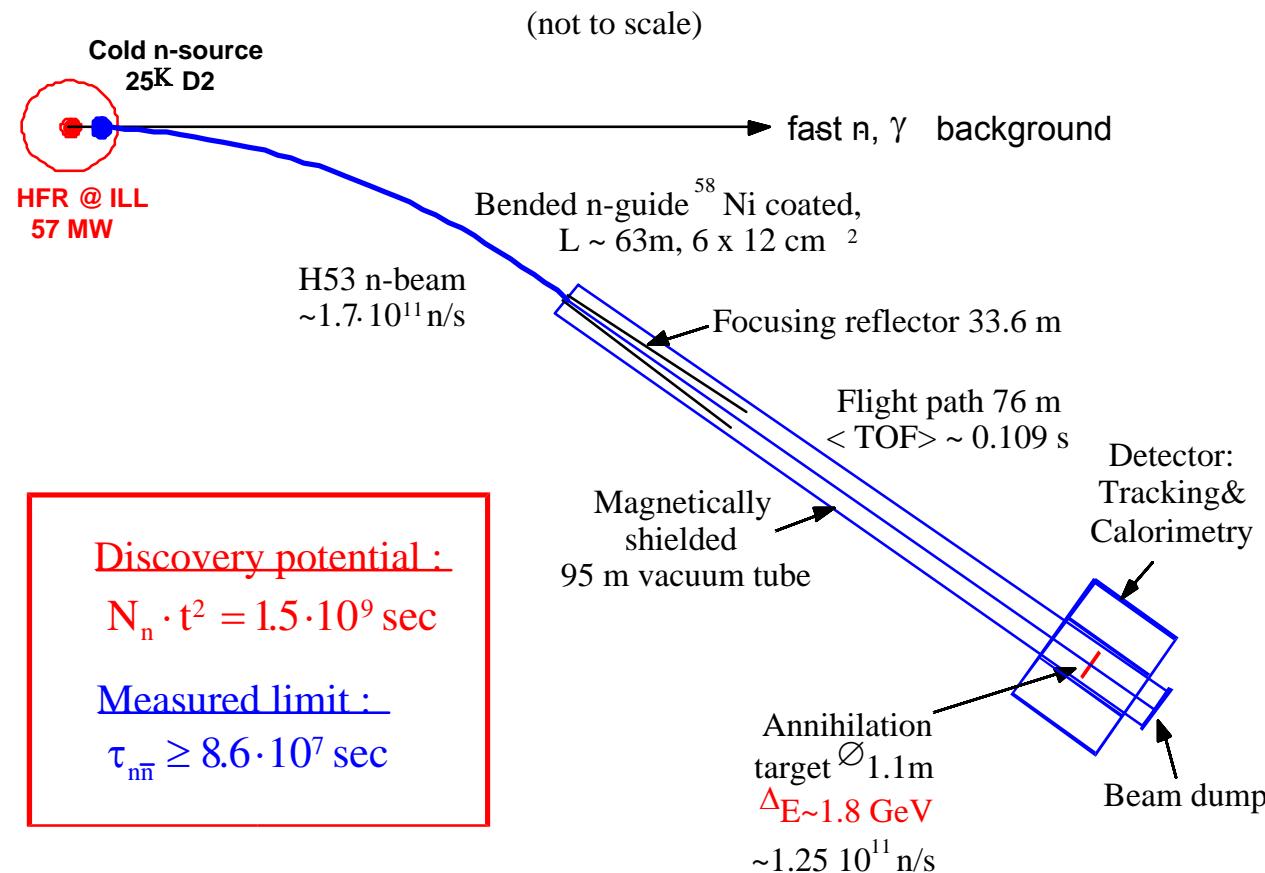
- Observable transition rates would correspond to the mass scale $m \sim 100$ TeV
- Anything happening at this scale?

New Ideas for n-nbar Oscillations

- G. Dvali and G. Gabadadze, “Non-conservation of global charges in the brane universe and baryogenesis”, Physics Letters B 460 (1999) 47-57
- K. S. Babu and R. N. Mohapatra. “Observable neutron-antineutron oscillations in seesaw models of neutrino mass, Physics Letters B 518, (2001) 269-275
- S. Nussinov and R. Shrock, “N-nbar Oscillations in models with large extra dimensions” Phys. Rev. Lett. 88, (2002) 171601

Last Experiment at ILL

Schematic layout of
Heidelberg - ILL - Padova - Pavia $n\bar{n}$ search experiment
at Grenoble 89-91



Typical detector for the “neutrons in the bottle experiment”

