

RESONANCE CORRECTION IN THE SNS

G. PARZEN

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Assumptions

1. Assume one wants to correct non-linear resonances driven by magnet errors.
2. Initial correction will be done for low intensity, no space charge effects, case. (~~This may be sufficient.~~)
3. Assume one can use BPM and Fourier analysis to measure tunes as ~~function~~ function of betatron oscillation amplitude. HERA, FNAL (1990) to correct linear coupling resonance. (see Bourianoff and Pilat (SSC, 1991))
4. Tune versus amplitude can be used to correct non-linear resonances.

Hayes, Schmidt, Tomas (2002, SPS)

Bai, Blaskewitz, Lehrach, Rosen, Schmidt, Van Assett (2001, BNL)

Bartolini, Schmidt (1996, Simulation)

Schmidt, Tomás, Faus-Golfe (2001, SPS)

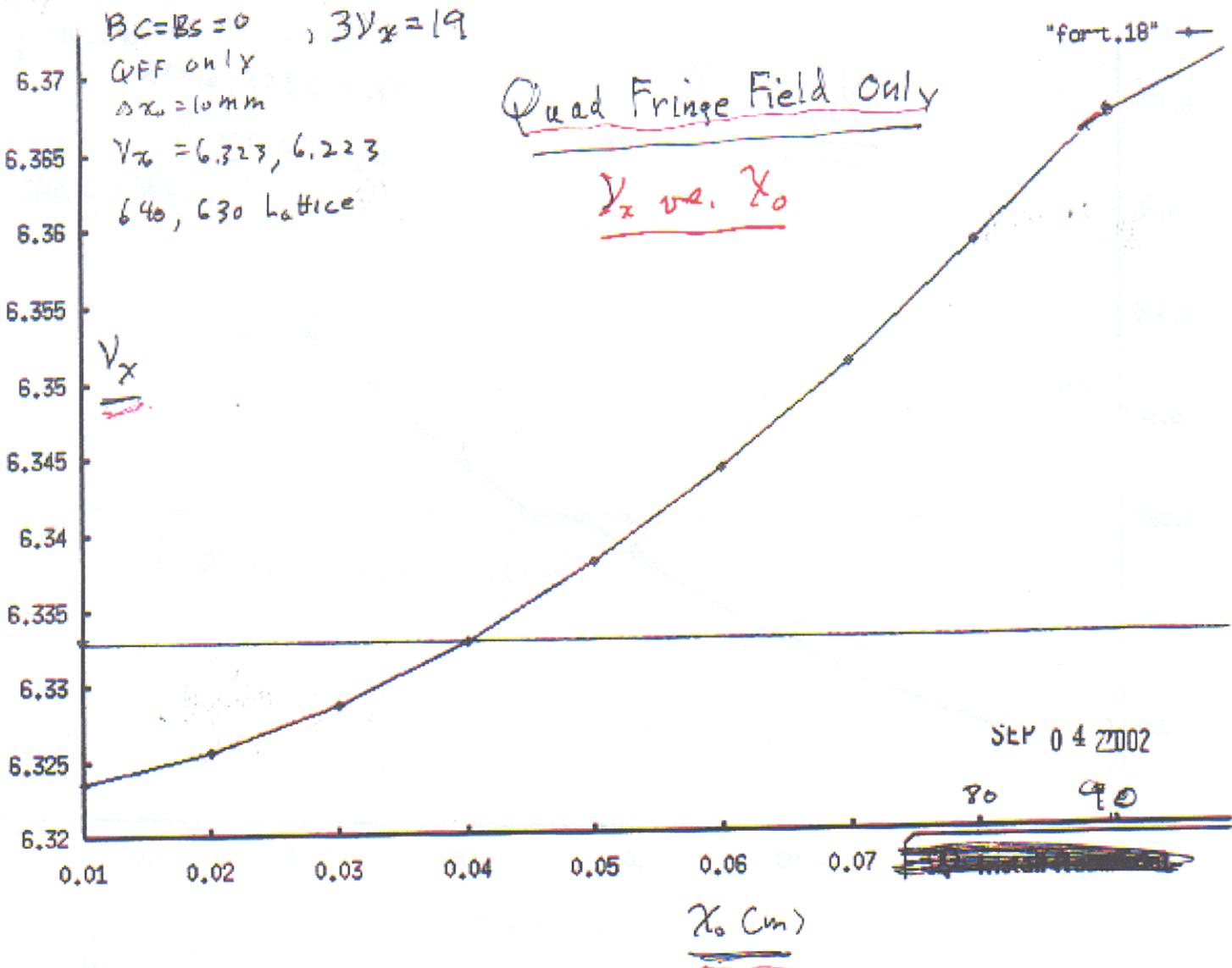
Pruett, Wallenmeyer (1960, MURIA)

Resonance Meter Choice

Resonance Meter - a measurable effect due to presence of non-linear resonance which can be used to measure "strength" of the resonance - depends on which resonance is to be corrected, and what other non-linear fields are present.

For SNS, tune versus amplitude due to quad fringe fields is strong enough to affect the effects of non-linear resonances due to magnet ~~effects~~ errors. One sees islands and distortions in phase space plots, but no direct instability.

Simulation studies will indicate the choice of resonance meter.



6.40, 6.30 Lattice

Move tune to 6.323, 6.223 for $3\gamma_x = 19$ resonance

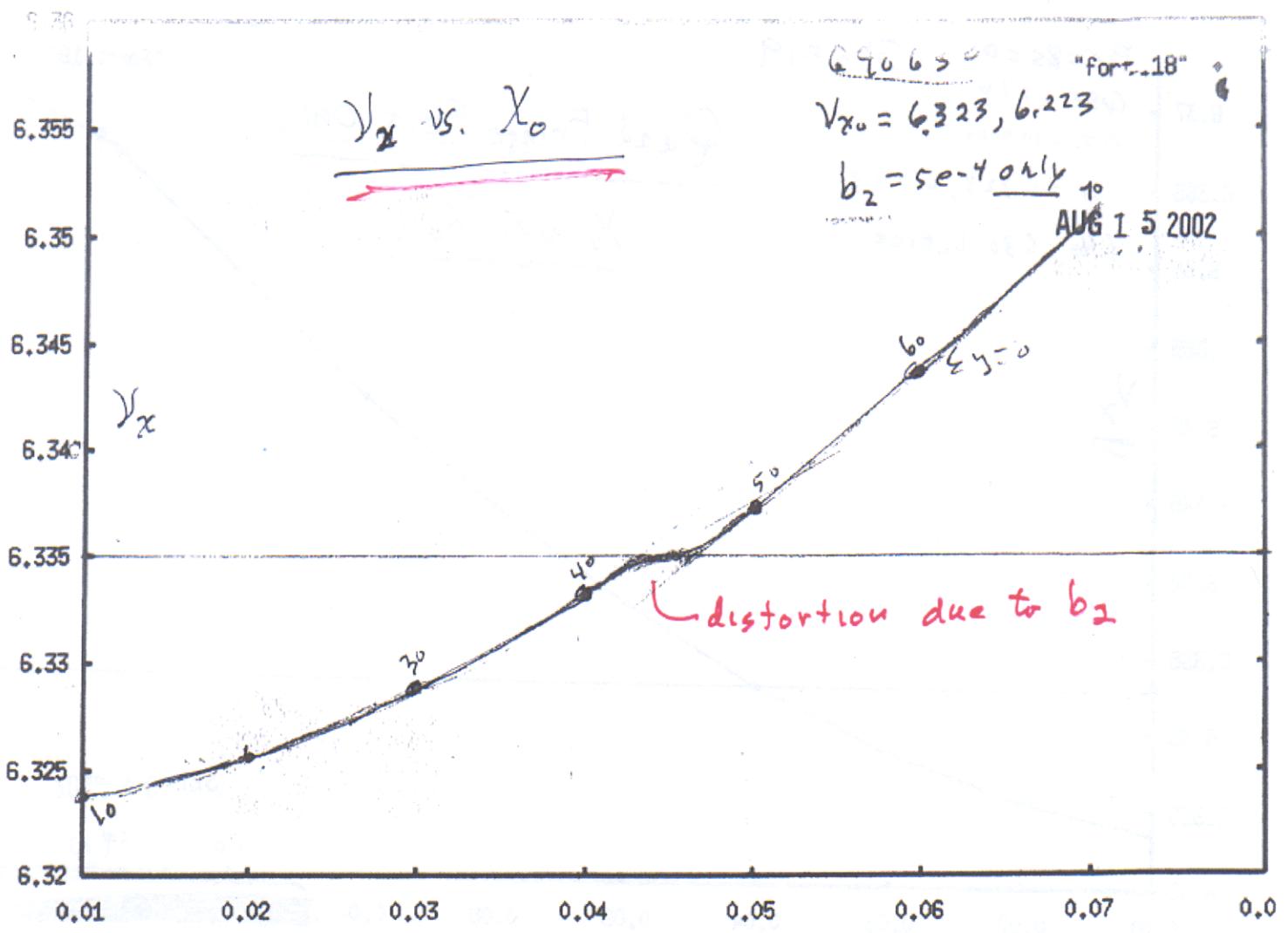
Measure γ_x vs. χ_0 ; $\gamma_0 \text{ s.m.u.}$, $E_{\chi_0} = 1 \times 10^{-4} E_{x_0}$

4

~~Graphs~~

20 20

3 - |



χ_o (m)

$$K_m \gamma = 3.2$$

$$\text{energy} = 4.2$$

$$f_m \chi_o = 1000$$

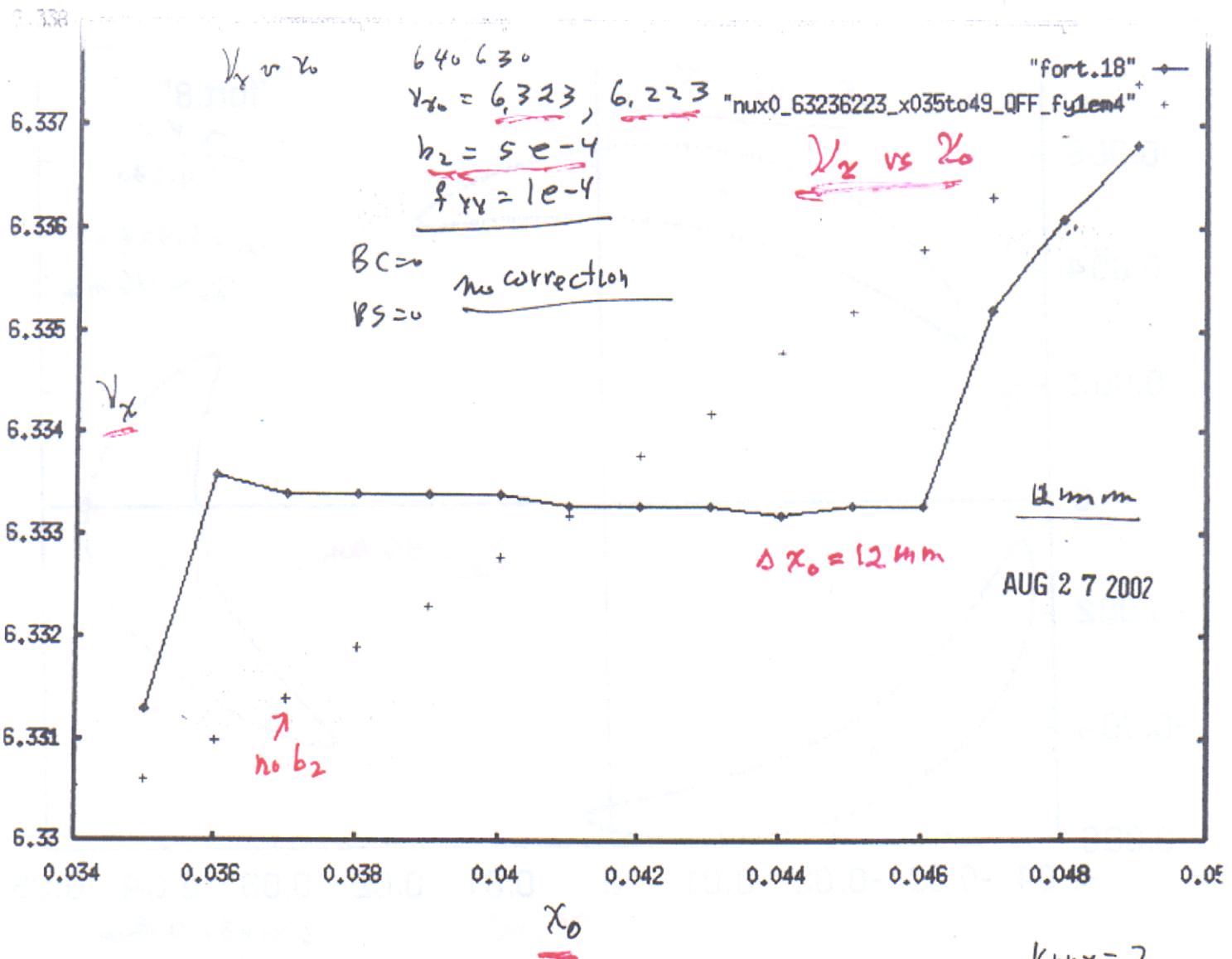
$$f_{\gamma} \gamma = 1, \gamma = 1e-4$$

$$\gamma_0 \text{ small}, \cancel{\Sigma \gamma_0} = 10^{-4} \Sigma \chi_0$$

$$b_2 = 5 \times 10^{-4} \text{ or } R \text{ of Iron.}$$

$$\approx 3 \times 10^{-4} \text{ or } R = 2/3 (\text{R}_{\text{Iron}})$$

3 - 2

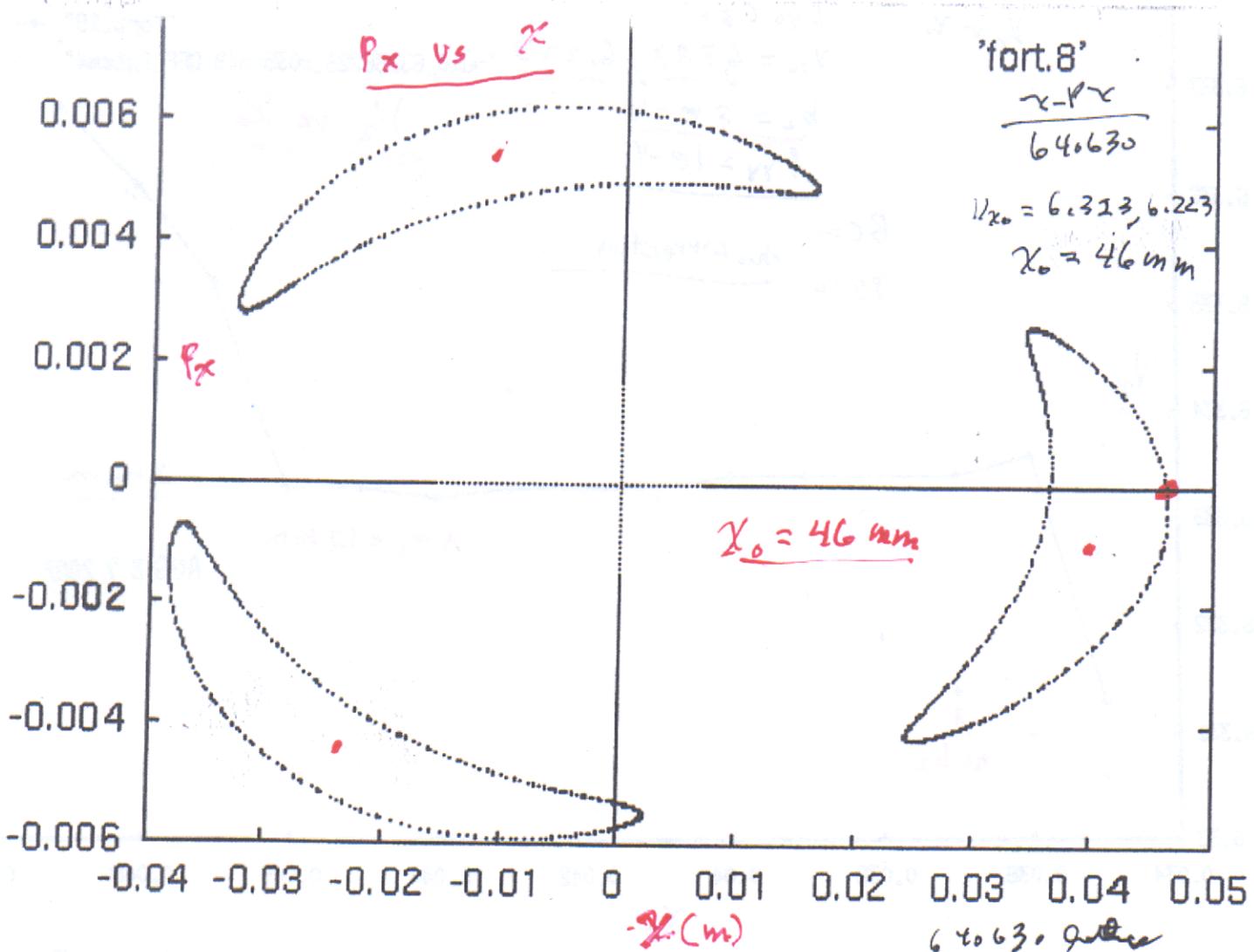


$$b_2 = 5e-4 \text{ at } R_{\text{iron}}$$

$$b_2 = 3.3e-4 + \frac{2}{3} R_{\text{iron}}$$

$$\begin{aligned}
k_{\gamma\chi} &= 2 \\
\gamma + \text{iron} &= 50^\circ \\
f_{\gamma\chi} &= 1 \\
f_{\gamma\chi} &= 1e-4
\end{aligned}$$

3-3



$$64630 \text{ gather}$$

$$\lambda_{x_0} = 6.323, 6.223$$

no conver

$$BC, BS = 0$$

$$k r_n x = 3$$

~~area~~ in m^2

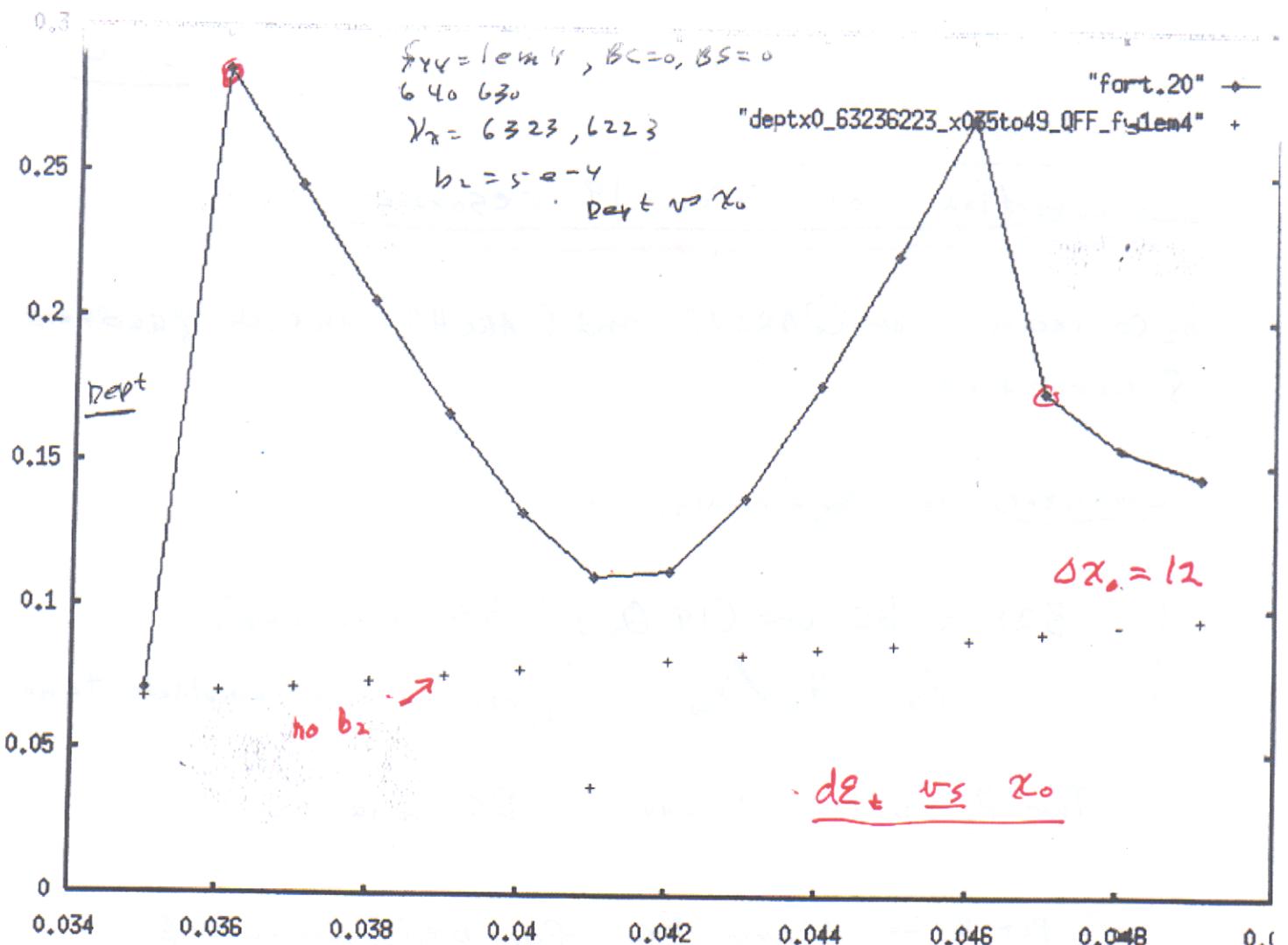
lower + upper

$$\lambda_0 = 46$$

$$f_{xy} = 1 \text{ Hz}$$

3 + 4

λ_x appears constant across island.
 λ_x in ν_x vs x_0 plot, is not true,
but is the main harmonic found
by the Fourier Analysis which is
 $\lambda_x = \frac{6.3333}{46}$ inside the island.



$\underline{\chi_0}$

$$\Delta \epsilon_t = \frac{\epsilon_{t\max} - \epsilon_{t\min}}{\epsilon_{t\max} + \epsilon_{t\min}} = \text{emittance spread}$$

Does $\Delta \chi_0$ from distortion in γ_x vs χ_0
give the width of the resonance?

Correction of $3\gamma_x = 19$ resonance

b₂ correctors or QARCV1 and QARCH1 in each quadrant.
3 correctors.

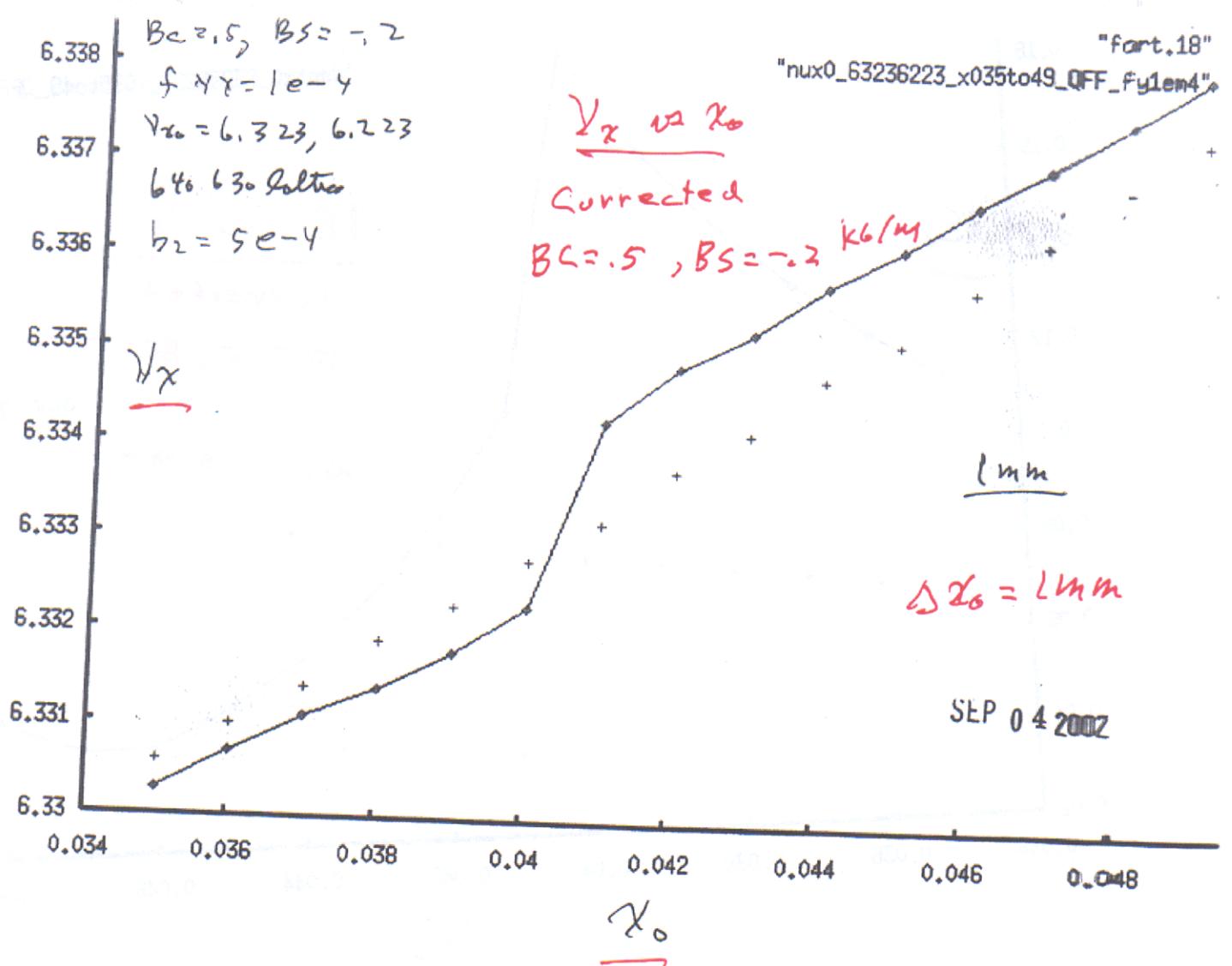
Correctors Set according to

$$B_{2L} = BC \cos(19\theta_x) + BS \sin(19\theta_x)$$

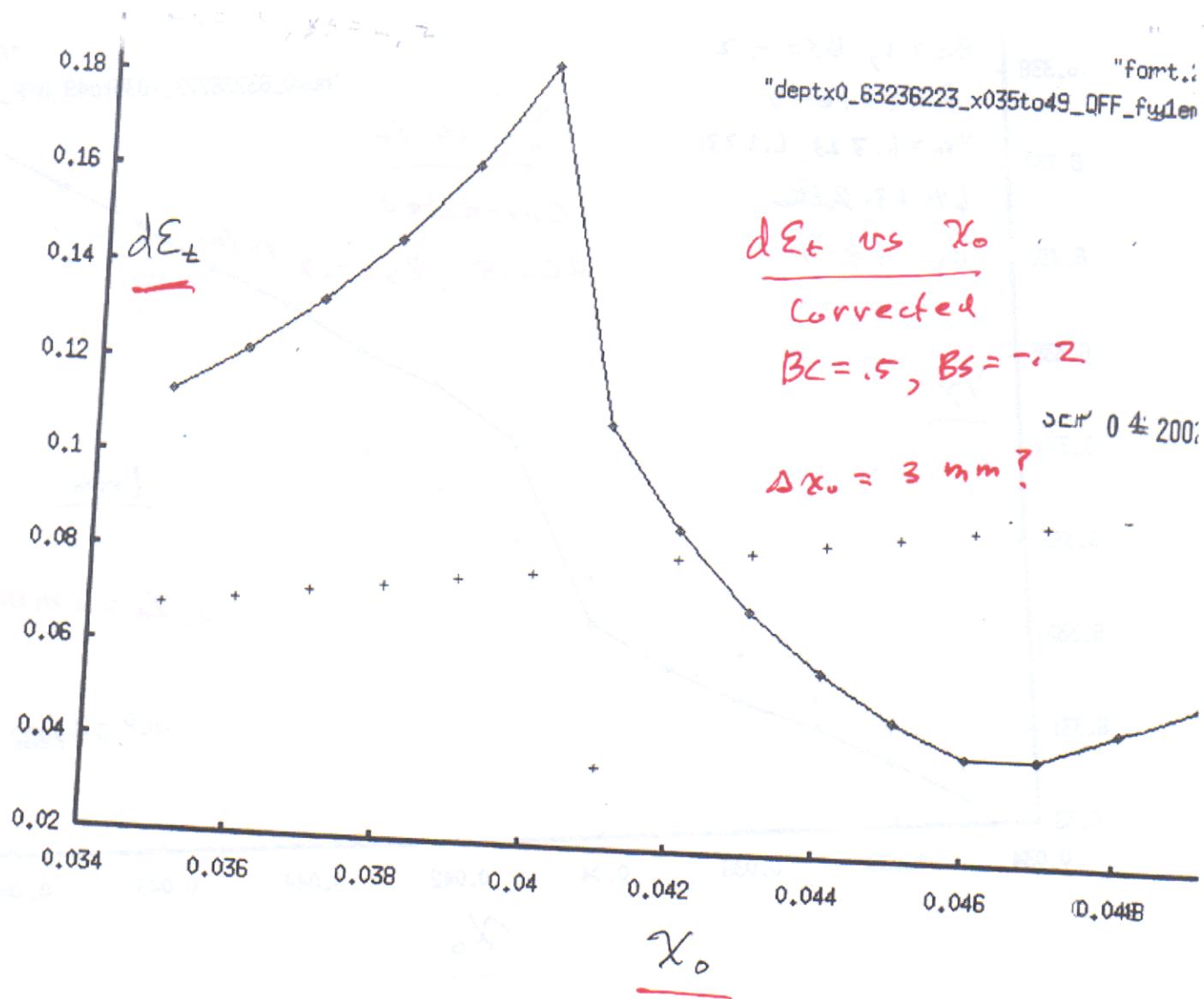
$$\theta_x = \psi_x / \gamma_{x0}, \quad \gamma_{x0} \text{ is small amplitude tune.}$$

Two Parameters to vary, BC and BS

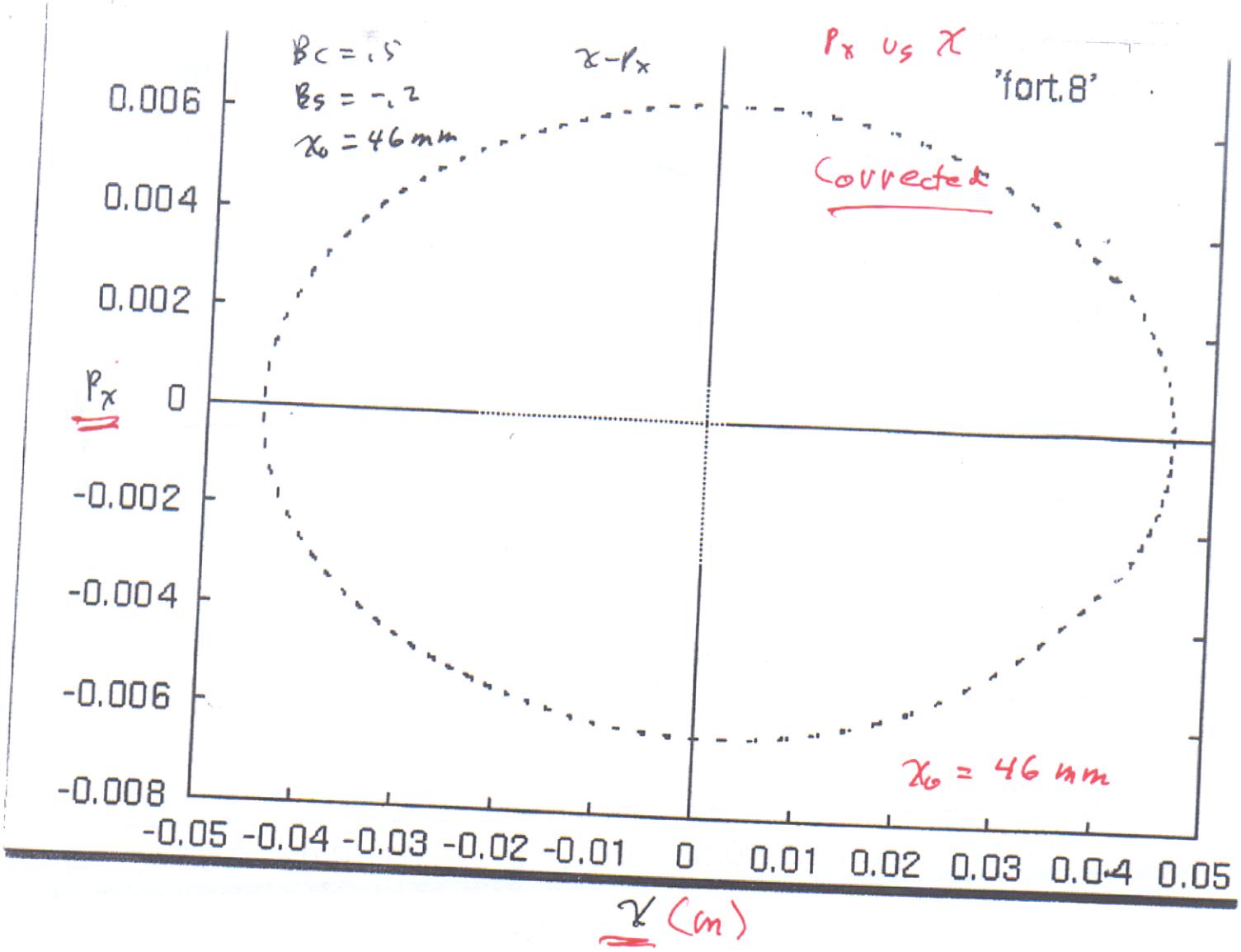
- 1) Put BS = 0, Vary BE for best correction
- 2) Fix BC at result from ①, Vary BS
- ③ repeat



3-7

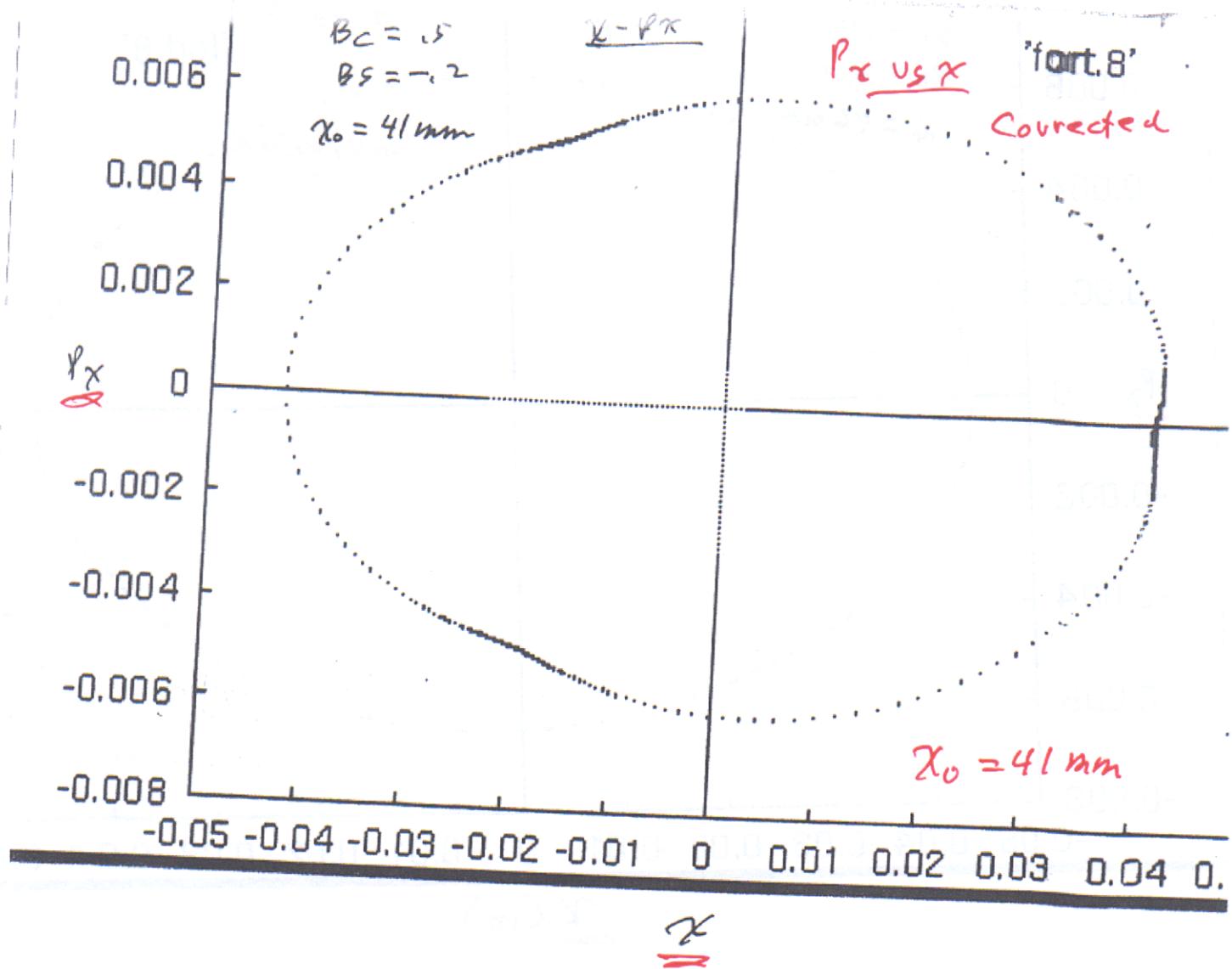


3-8



$x_0 = 46 \text{ mm}$ gave the islands uncorrected

3-9

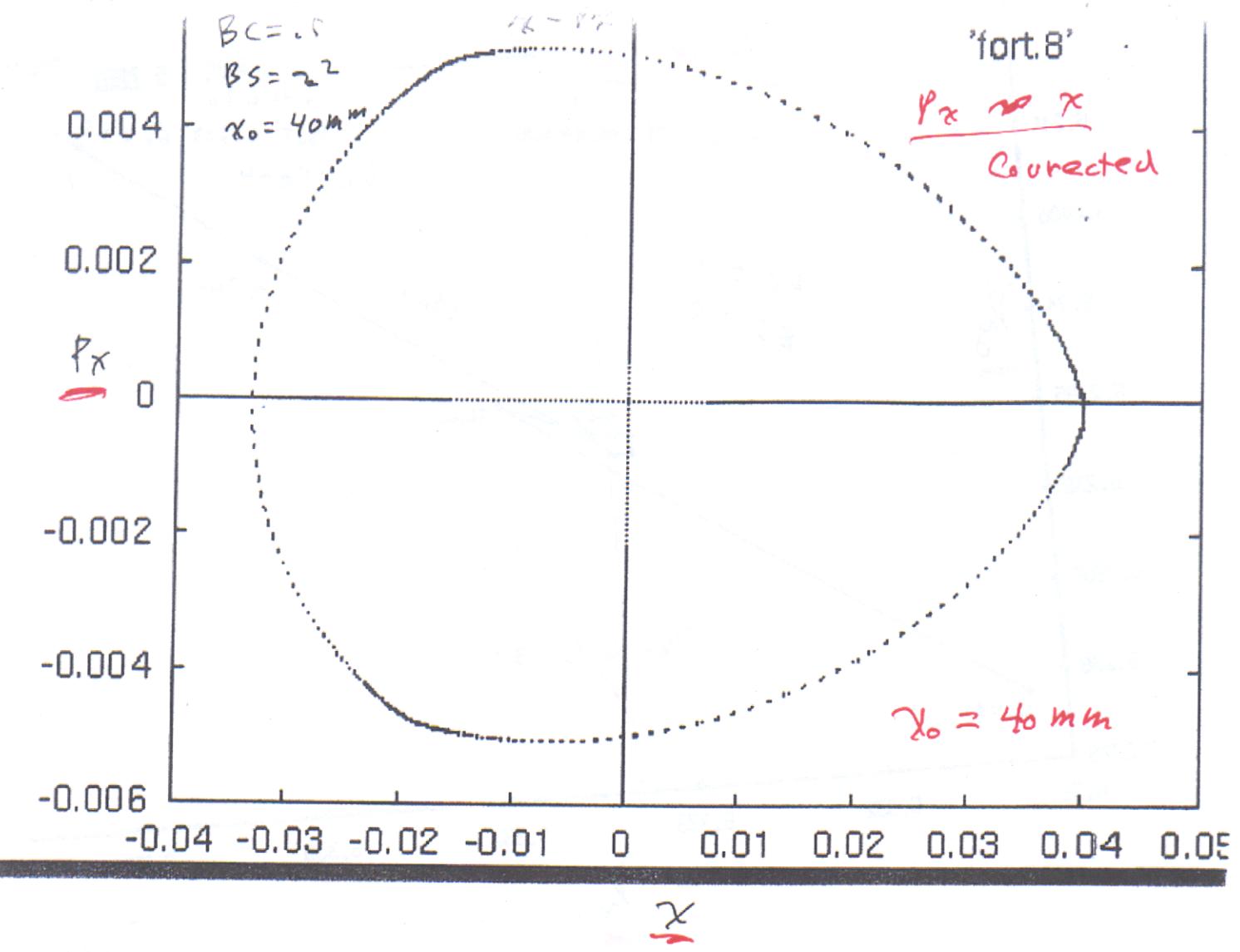


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ν_x vs x_0 distortion indicates resonance

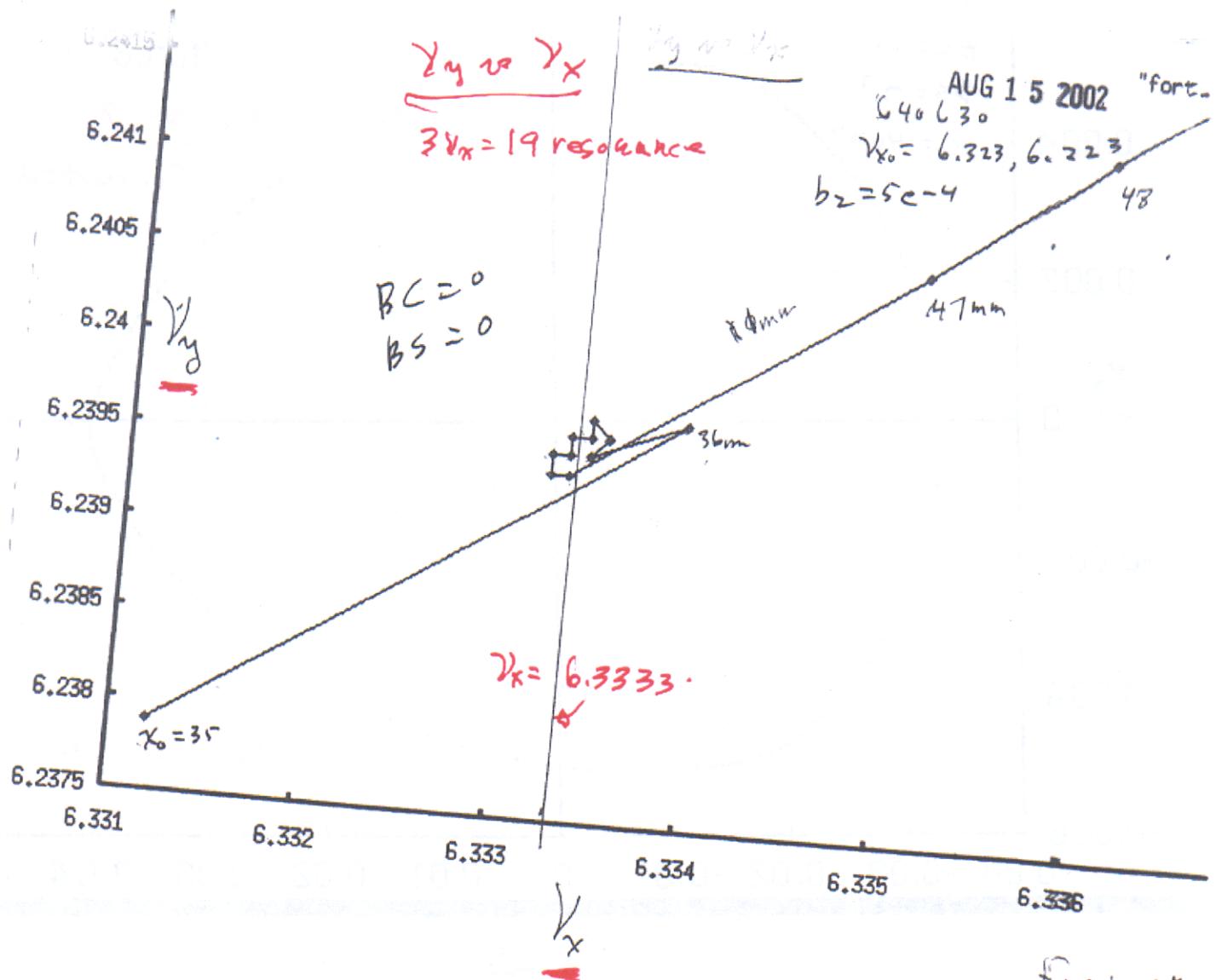
extends from $x_0 = 40$ to $x_0 = 41 \text{ mm}$

3 - 10

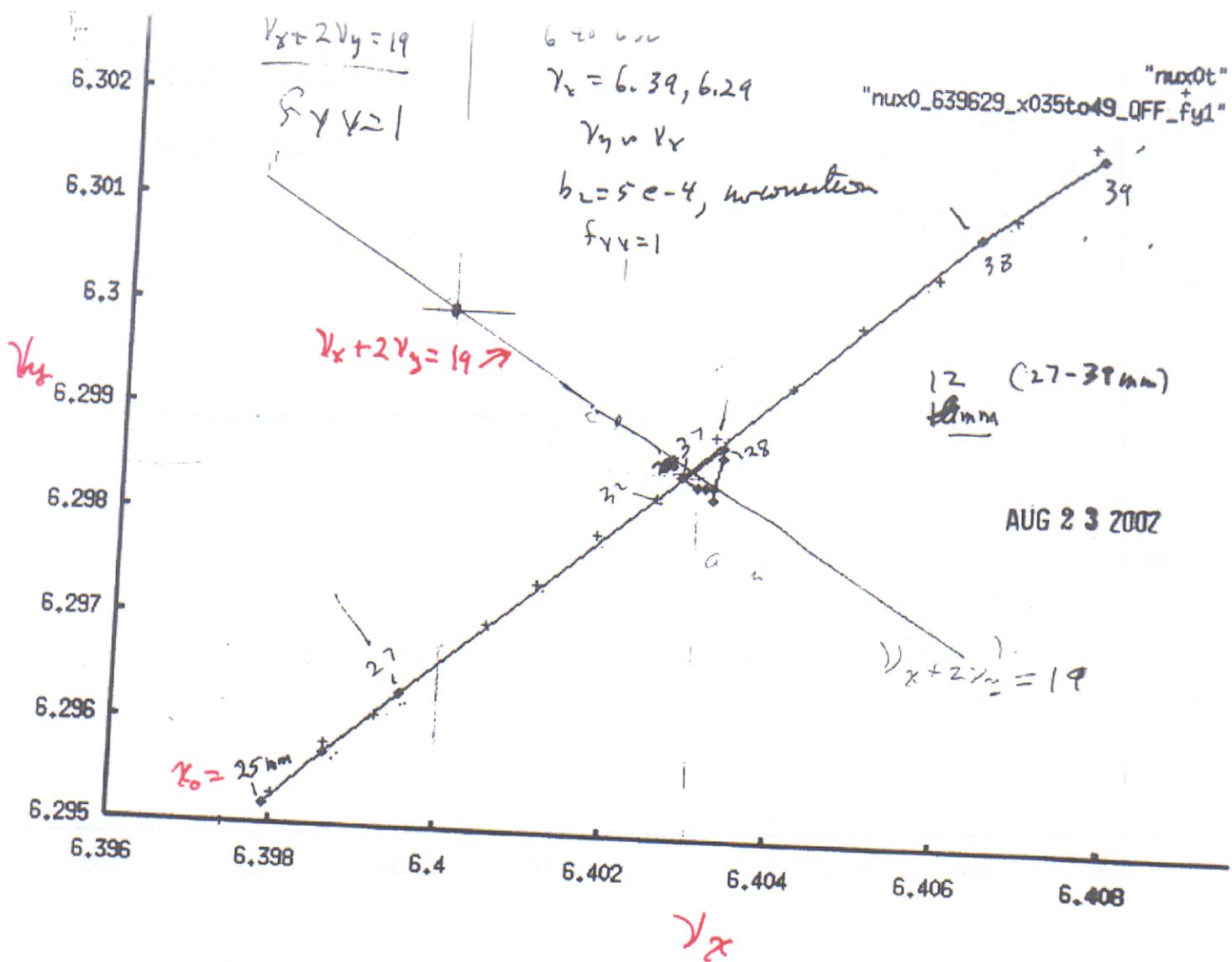


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3-4



$\gamma_y \approx \gamma_x$ could be used to correct
 γ_y, γ_x distortion due to b_2
 but more difficult to interpret.



$$v_x + 2v_y = 19 \text{ resonance}$$

Move v_{x0}, v_{y0} to 6.39, 6.29

just below $v_x + 2v_y = 19$ resonance

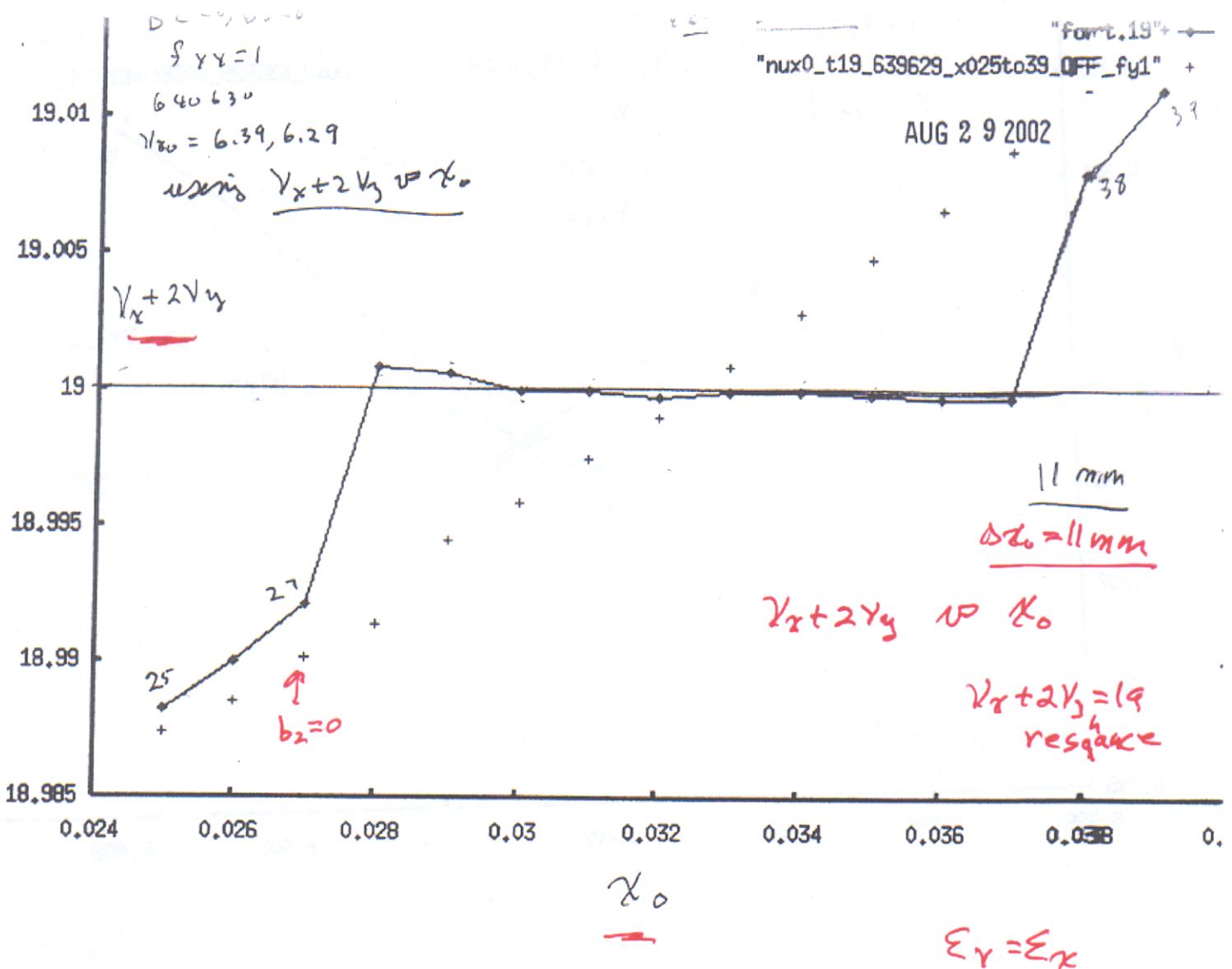
$\epsilon_y = \epsilon_x$, y motion large.

$S_{yy} = 1$

$K_{yy} =$

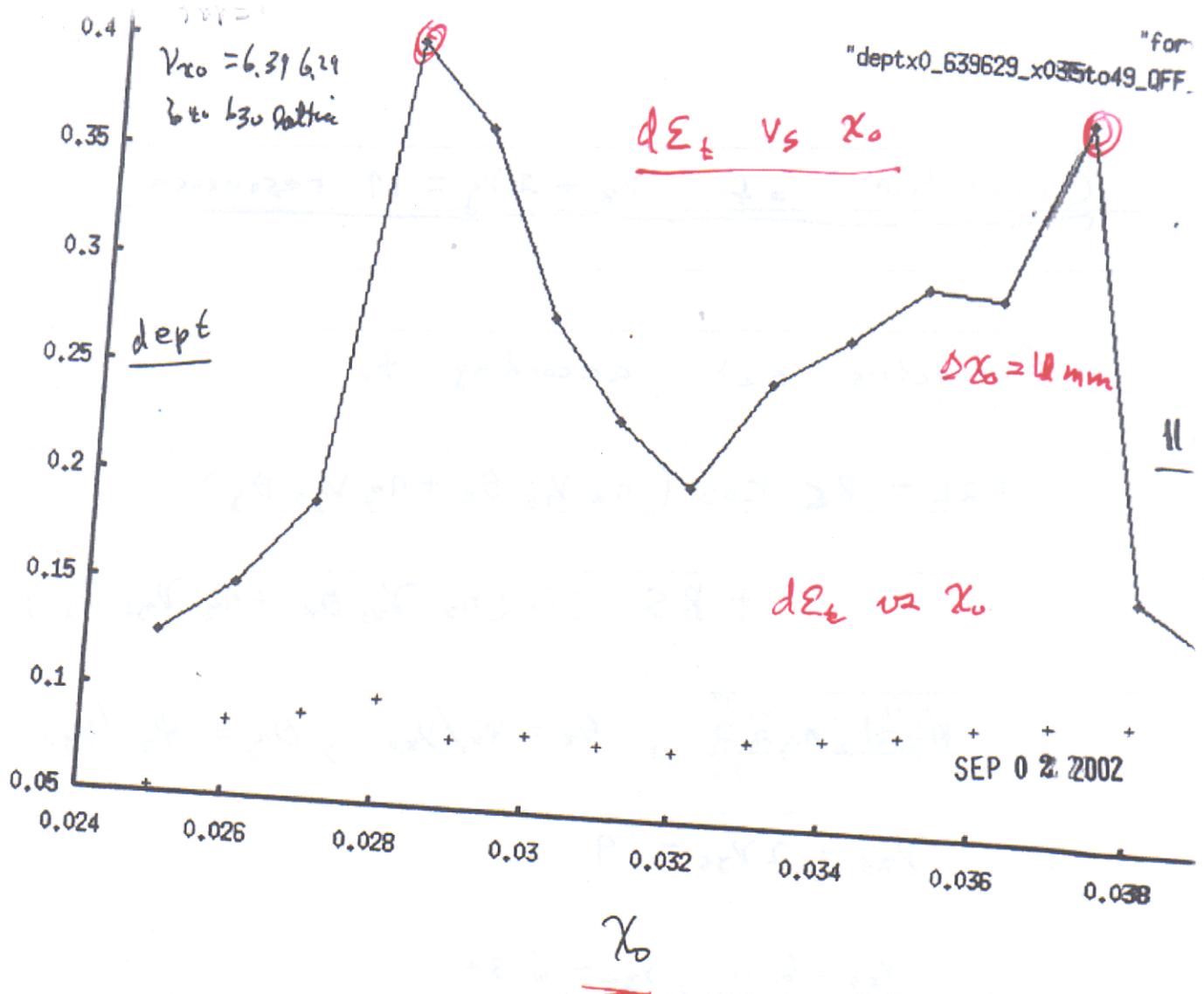
Ln 2

4-1



"Islands" in 4D phase space -
 main harmonics in x motion and y motion
 obey $\gamma_x + 2\gamma_y = 19$.

4-2



Correction of $\gamma_x + 2\gamma_y = 19$ resonance

Correctors set according to.

$$B_{2L} = BC \cos(\gamma_x \gamma_{xs} \theta_x + \gamma_y \gamma_{ys} \theta_y)$$

$$+ BS \sin(\gamma_x \gamma_{xs} \theta_x + \gamma_y \gamma_{ys} \theta_y)$$

$$\gamma_x = 1, \gamma_y = 2 \rightarrow \theta_x = \psi_x / \gamma_{x0}, \theta_y = \psi_y / \gamma_{y0}$$

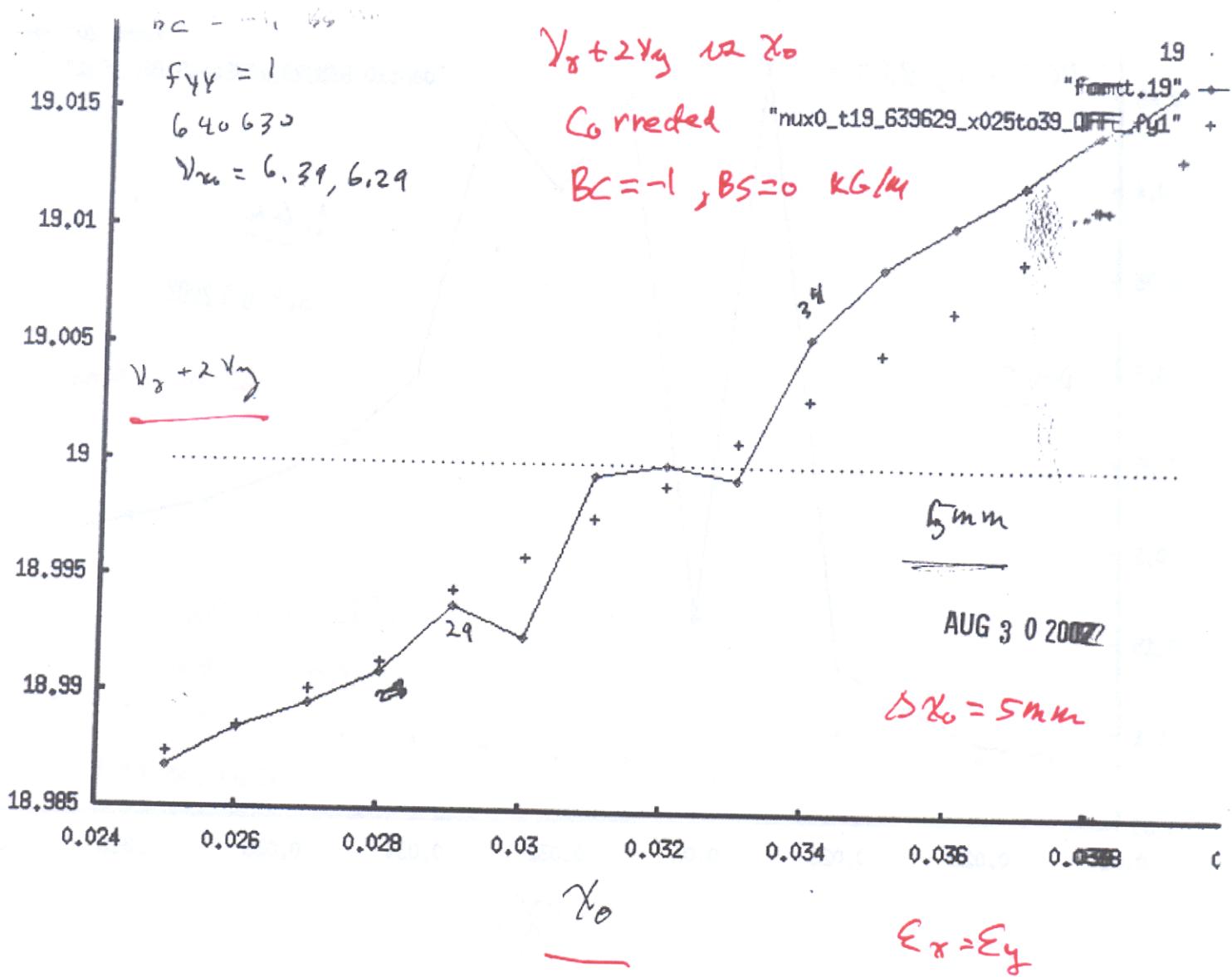
$$\gamma_{xs} + 2\gamma_{ys} = 19$$

$$\gamma_{xs} = 6.40, \gamma_{ys} = 6.30$$

$$\gamma_{xs} = 6.4030, \gamma_{ys} = 6.2985$$

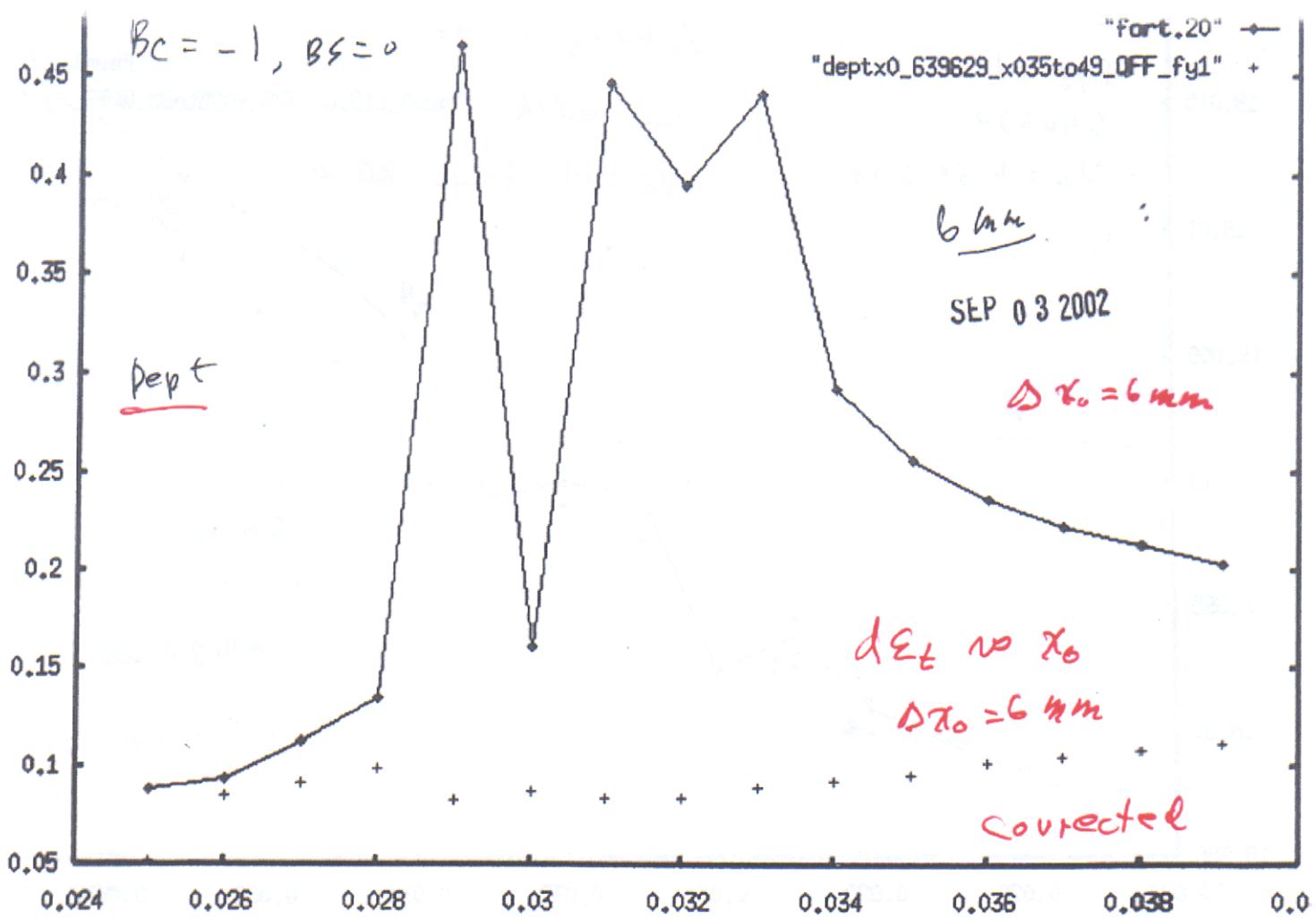
Vary 2 parameters, BC, BS

4-3 b



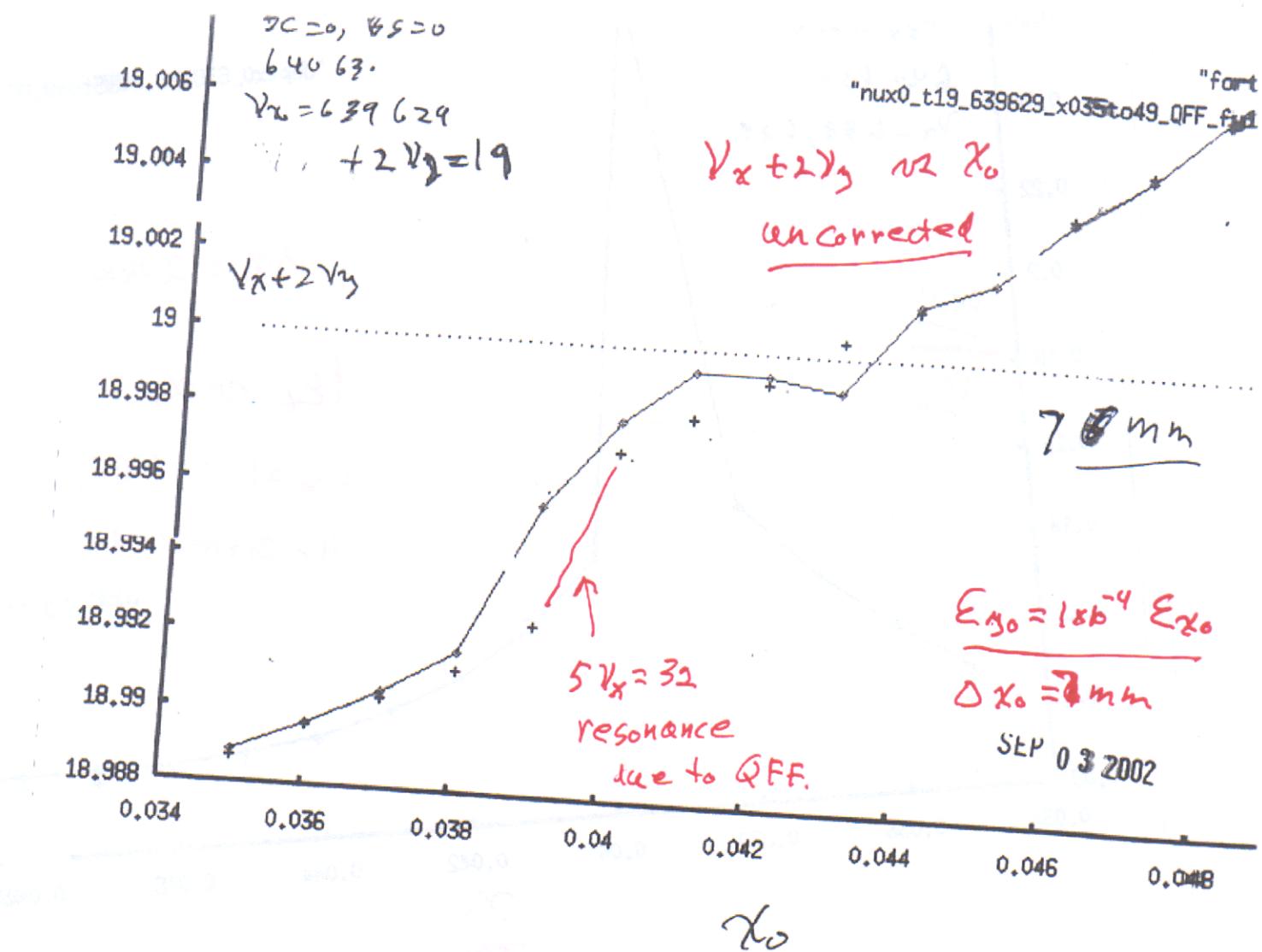
$\Delta \chi_0$ reduced from 11mm to 5mm.

How to improve Correction?



x_0

4-5



For $E_{y0} = 10^{-4} \cdot E_{x0}$,

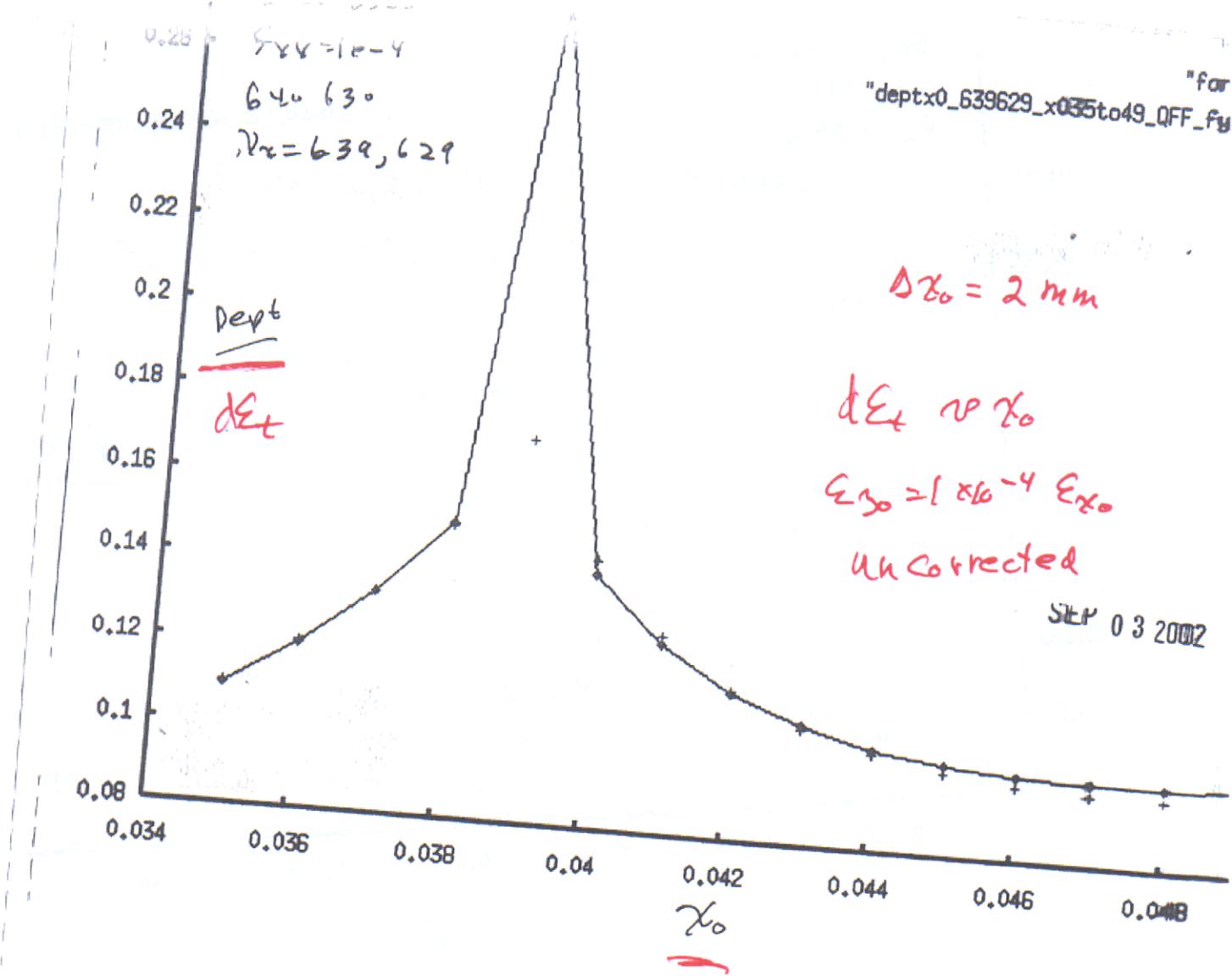
Resonance width is smaller

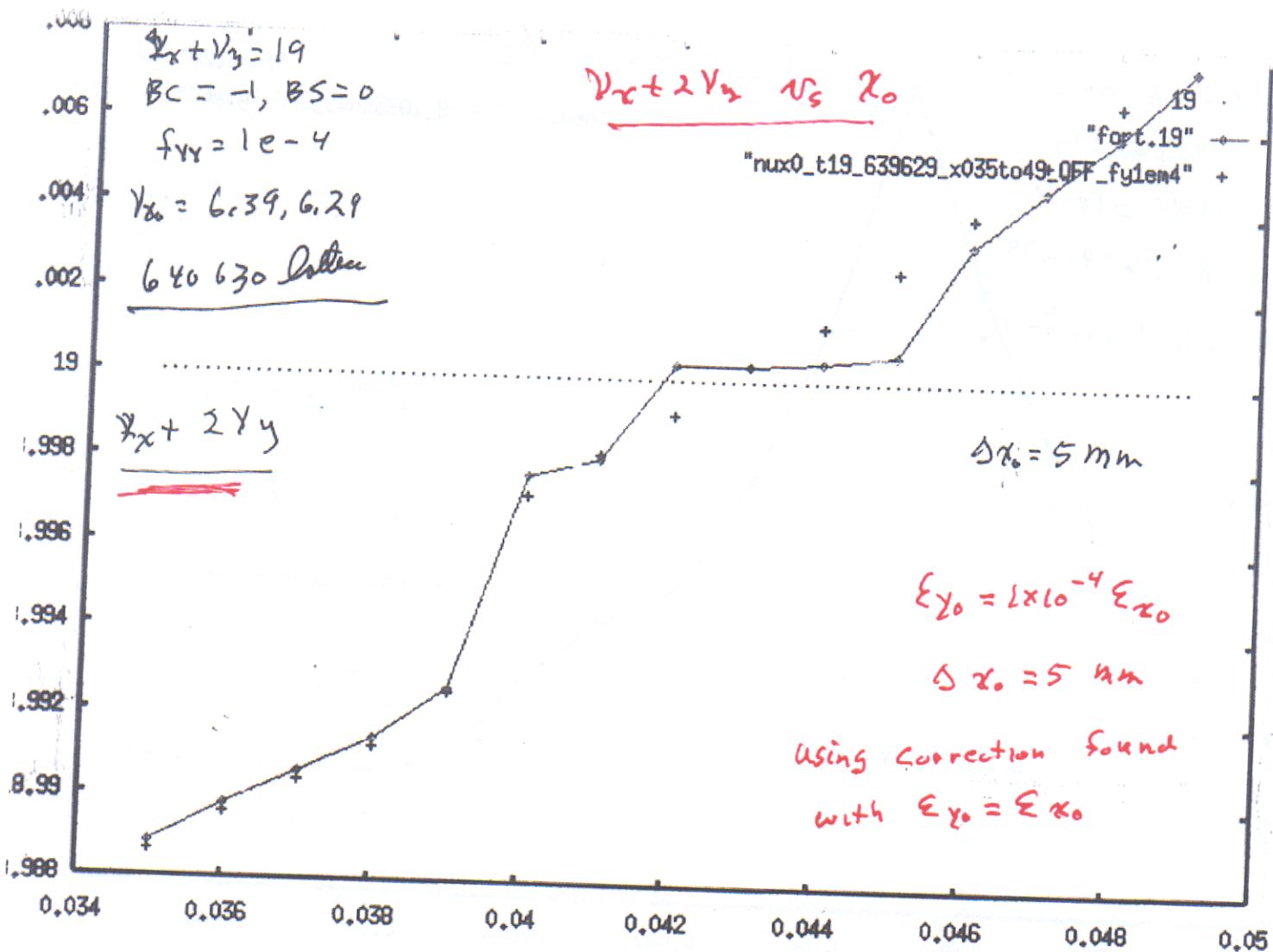
Complicated by $5\gamma_x = 32$ resonance.

Two reasons not to use

$$E_{y0} = 1 \times 10^{-4} E_{x0}$$

using $f_{YY} > 1 \text{ e-4}$ duration
 resonance with small
 can have to use the $f_{YY} = 1$ duration

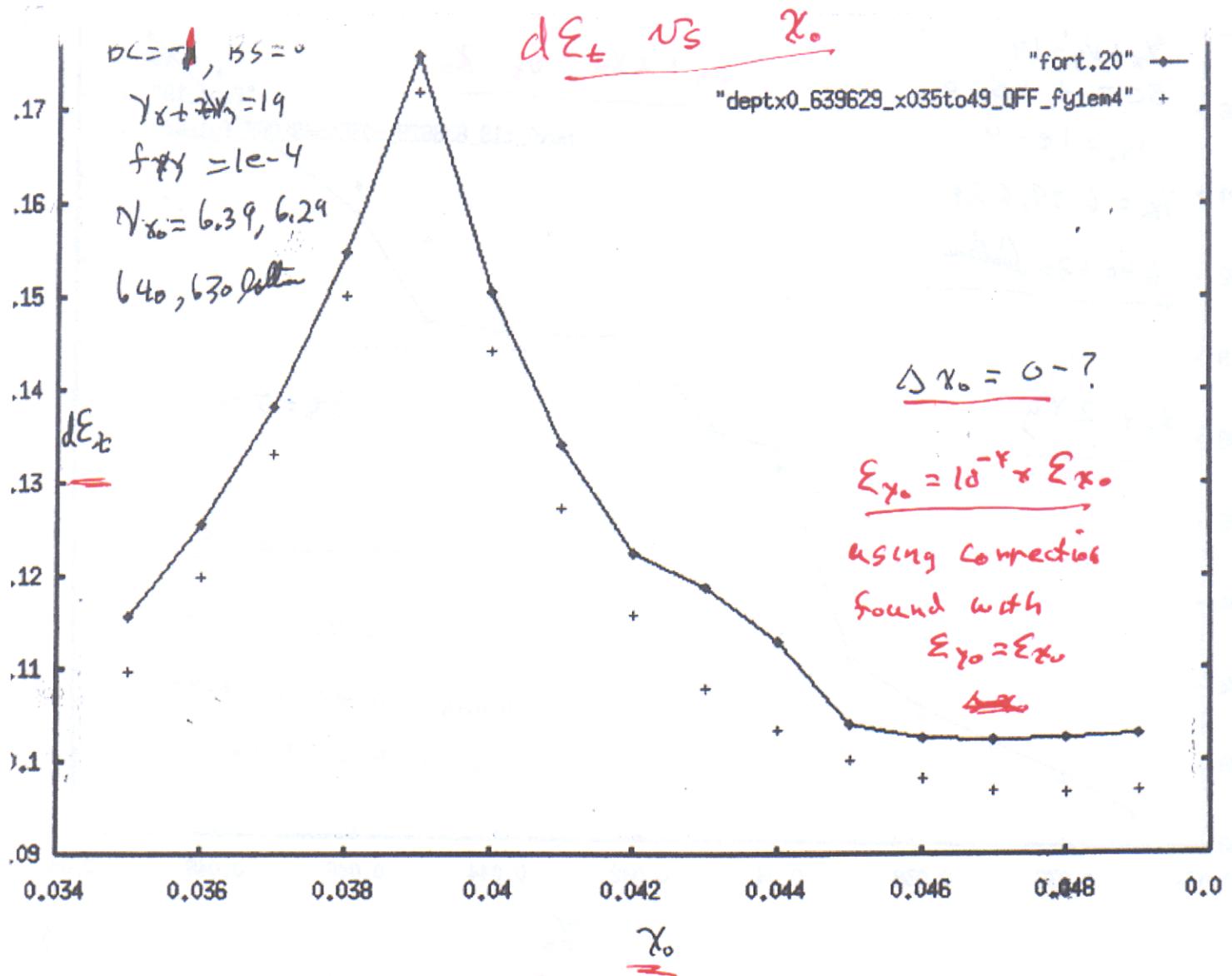




$\underline{x_0}$

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4-8



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~~4x~~

4-9

Questions - To Do List

1. Octupole correctors - There are b_3 correctors
but no skew, a_3 , correctors

2. Correction of a_2 driven resonances.

$$\Rightarrow 2\nu_x + \nu_y = 19, \quad 3\nu_y = 19$$

3. Correction of b_3 driven resonances

$$4\nu_x = 25, \quad 2\nu_x + 2\nu_y = 25 \quad 4\nu_y = 25$$

4. Hardware and Software for tune
versus amplitude correction using BPM.