

4/22/03  
W. Marciano

## Very Long Baseline Neutrino Oscillations (CP Violation & Much More)

e.g. BNL - Homestake 2540 km

or BNL - WIPP 2900 km

BNL - Henderson, Colorado

BNL Study Commissioned by Tom Kirk → White Papers  
Led by M. Diwan, W. Marciano & W. Wenz + Many Participants

### Outcome

Conventional Horn Focused  $\nu_\mu$  ( $\bar{\nu}_\mu$ ) Beam (Wide Band)

+

AGS Upgrade 0.14 MW → 1 MW

+

500 kton Water Cerenkov Detector (2000 ~ 3000 km.)



Precision Measurements:  $\sin^2 \theta_{23}$ ,  $\sin^2 \theta_{12}$ ,  $\Delta m_{32}^2$ ,  $\Delta m_{21}^2$

(very powerful)

sign of  $m_3^2 - m_2^2$  Hierarchy (Matter effect)

Measure:  $\sin^2 \theta_{13}$  or bound → 0.003!

Determine: CP Violating Phase  $\delta$

$J_{CP} = \sin \theta_{12} \sin \theta_{23} \sin \theta_{13} \cos \theta_{12} \cos \theta_{23} \cos^2 \theta_{13} \sin \delta$  to  $\approx \pm 25\%$ !

Also probe: Sterile Neutrino Mixing  
Effects of Extra Dimensions  
New Interactions with Matter } Deviations  
From  
3Gcr. Expectations

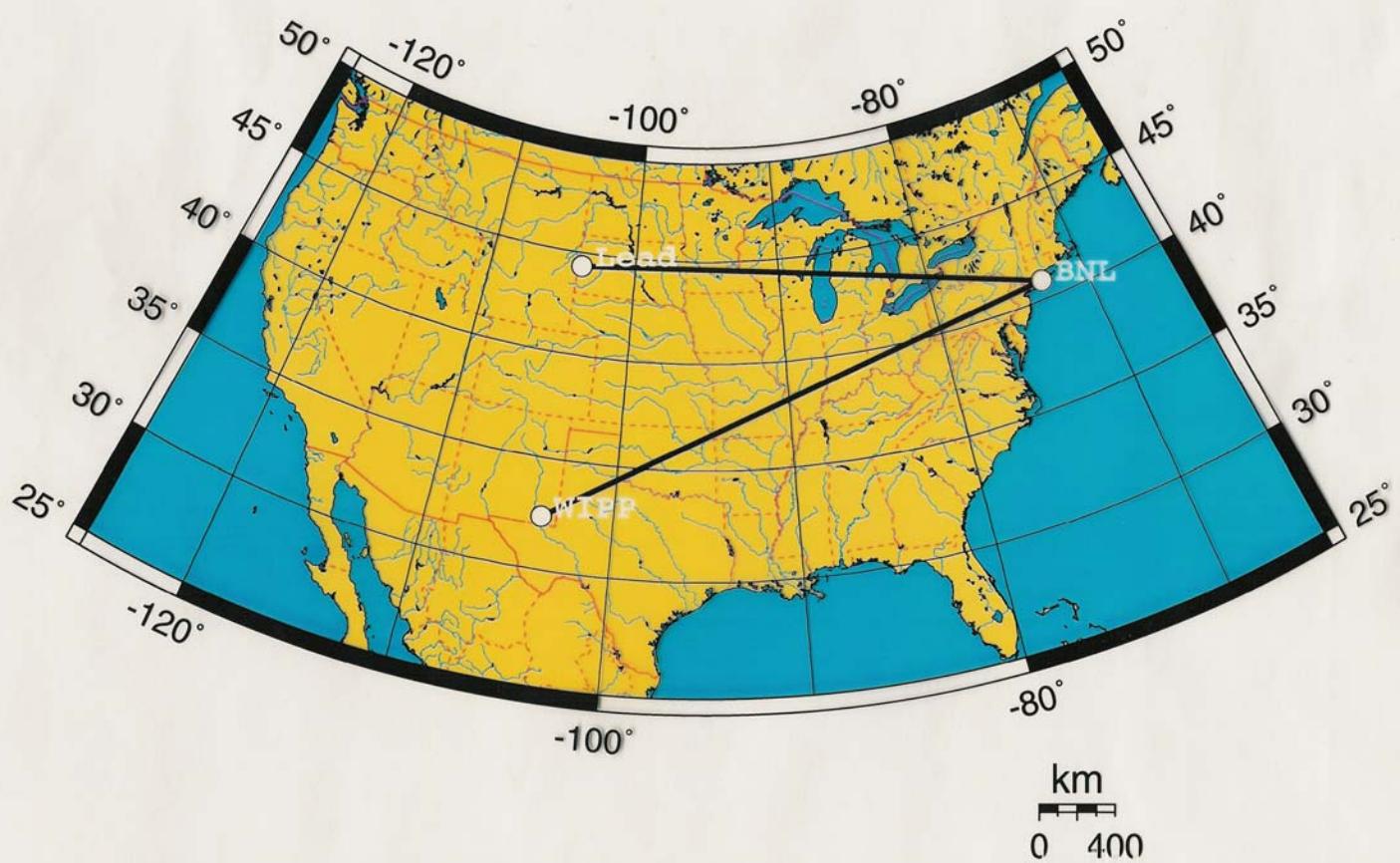
A Bold & Ambitious Neutrino Program for 21st Century  
determines Lepton Mixing  $\simeq$  Quark Mixing

Large Water Cerenkov Detector (500 kton)  
 $\sim 20 \times$  SuperK (eg UNO)

Proton Decay  $\Gamma(p \rightarrow e^+ \pi^0) \sim 10^{36} \text{ yr}$   
Supernova Neutrino Studies ( $> 100,000$  events!)  
Precision Atmospheric Neutrinos (multiple peaks)  
Solar Neutrinos  
 $\nu - \bar{\nu}$  osc., magnetic monopoles ... Neutrino Sources  
etc.

A complete physics facility with potential for  
Revolutionary Discoveries & Solid Measurements

Anchor for National Underground Lab!



### Current Status of Neutrino Mixing

$$\begin{pmatrix} |\nu_e\rangle \\ |\nu_\mu\rangle \\ |\nu_\tau\rangle \end{pmatrix} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23}-c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23}-s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23}-c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23}-s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix} \begin{pmatrix} |\nu_1\rangle \\ |\nu_2\rangle \\ |\nu_3\rangle \end{pmatrix}$$

$$c_{ij} = \cos \theta_{ij}, \quad s_{ij} = \sin \theta_{ij} \quad 0 \leq \delta < 2\pi$$

Atmospheric  $\nu_\mu \rightarrow \nu_\mu$   
+ K2K

$$\Delta m_{32}^2 = m_3^2 - m_2^2 = \pm 2.5^{+1.5}_{-1.2} \times 10^{-3} \text{ eV}^2$$

(Rumored Lower Value!)

$$\sin^2 2\theta_{23} \simeq 0.85 - 1.0 \text{ (Maximal) } 45^\circ$$

Solar  $\nu_e \rightarrow \nu_e, \nu_x$

$$\Delta m_{21}^2 = m_2^2 - m_1^2 = 7.3 \pm 2 \times 10^{-5} \text{ eV}^2 \text{ LMA I}$$

$$= 14 \pm 3 \times 10^{-5} \text{ eV}^2 \text{ LMA II}$$

Kamland  $\bar{\nu}_e \rightarrow \bar{\nu}_e$

$$\sin^2 2\theta_{12} \simeq 0.86 \pm 0.10 \quad \theta_{12} \simeq 36^\circ$$

Left to determine  $\theta_{13}$  +  $\delta$   $\sin^2 2\theta_{13} \lesssim 0.2$  (Reactors)  
 $0 \leq \delta < 2\pi$

$$J_{CP}^{\text{leptons}} \simeq 0.23 \sin \theta_{13} \sin \delta \quad \text{Potentially Enormous} \underbrace{\sim 10^{-2}}_{\text{Holy Grail}}$$

$$J_{CP}^{\text{quarks}} \simeq 3 \pm 1 \times 10^{-5} \text{ tiny}$$

### Potential Competition for CP Violation

JPARC (Phase II 2015+) → Hyper K (at 295 km)  
**4MW!**      **1000 kton (H<sub>2</sub>O)!**

$$A_{CP} = \frac{P(\nu_\mu \rightarrow \nu_e) - P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)}{P(\nu_\mu \rightarrow \nu_e) + P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)} \sim \frac{\sin \delta}{\sin \theta_{13}} \frac{\Delta m_{31}^2 L}{E_\nu} \text{ Potentially Large}$$

Proposal: Off-Axis  $\nu_\mu$  &  $\bar{\nu}_\mu$  beams  $E_\nu \approx 0.6 \text{ GeV}$

$$8 \text{ yr} \left\{ \begin{array}{l} 2 \times 10^7 \text{ sec} \\ 6 \times 10^7 \text{ sec} \end{array} \right. \quad \left. \begin{array}{l} \nu_\mu \rightarrow \nu_e \pi^- \rightarrow e^- p \\ \bar{\nu}_\mu \rightarrow \bar{\nu}_e \pi^+ \rightarrow e^+ n \end{array} \right\} \text{Quasi-Elastic}$$

Very Challenging

Detector: Cost  $\sim \$10^9$ , Excavation  $\sim 10 \text{ yr}$ !

Machine: 4MW upgrade very expensive & difficult

Target-Horn: Liquid Target, Heating, Robotics ...

Physics - Not Robust (What if  $\Delta m_{32}^2 < 2 \times 10^{-3} \text{ eV}^2$ )

Untangle  $g\beta$ ,  $\theta_{13}$ , matter effects?

Weakness: 295 km Too Short!

BNL - Homestake 2540 km (1NW, 500kton) much more modest

On-Axis (0°) Wide Band Beam  $0.5 \text{ GeV} \leq E_\nu < 5 \text{ GeV}$

2-2.5 x More Flux

Quasi-Elastic  $\nu n \rightarrow l p$   $2 \times$  cross-section  $E_\nu \geq 16 \text{ eV}$   
 $3 \times$  for  $\bar{\nu} p \rightarrow \bar{l} n$

Run  $\nu_\mu$  alone for  $5 \times 10^7 \text{ sec}$  (or 2yr  $\nu_\mu$  + 3yr  $\bar{\nu}_\mu$ )

Measure  $\sin \delta$  +  $\cos \delta$  (+ all other parameters)

More Robust - Gets better if  $\Delta m_{32}^2$  smaller!

Easier, Much Cheaper, Faster, Better!

Figure of Merit  $\sim \left( \frac{\Delta m_{31}^2}{\Delta m_{32}^2} \right)^2 \sin^2 2\theta_{12} \times \text{Detector Size} \times \text{Power} \times \text{Time}$

Has been increasing! } Factor of 3  
Becoming Easier! } since study start

Basic Features: 1) Measure  $\nu_\mu \rightarrow \nu_\mu$  disappearance  
3 peaks

$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - \sin^2 2\theta_{23} \sin^2 \left( \frac{\Delta m_{34}^2 L}{4E_\nu} \right) + \dots$$

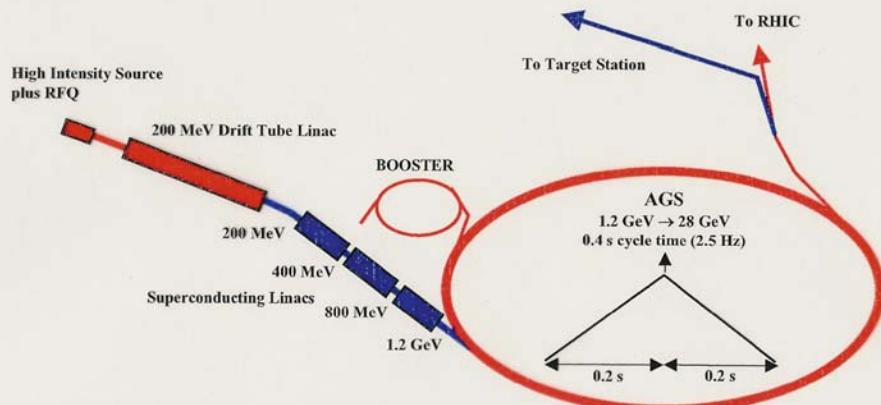
$$\text{Min. } L_{\text{osc}} \approx (2n+1) \times 500 \text{ km} \times E_\nu (\text{GeV}) \quad n=0,1,2$$

at 2500km  $\rightarrow$  peaks at  $\sim 2.5, 1.25, 0.83 \text{ GeV} \dots$

## The Accelerator

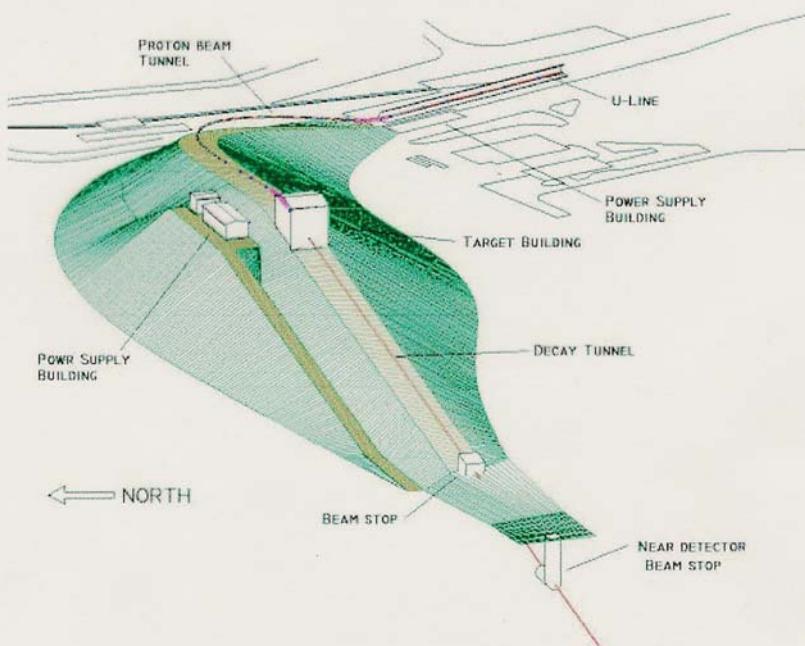
- Conceptually simple upgrade. No magic. Cost  $\sim \$100M$ .
- Run 28 GeV AGS at 2.5 Hz to get 1 MW.
- Need faster proton source: Super Conducting LINAC at 1.2 GeV
- Current:  $7 \times 10^{13} ppp$  at 0.5 Hz  $\Rightarrow$  LINAC:  $10^{14} ppp$  at 2.5 Hz.

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Very long baselines with a superbeam

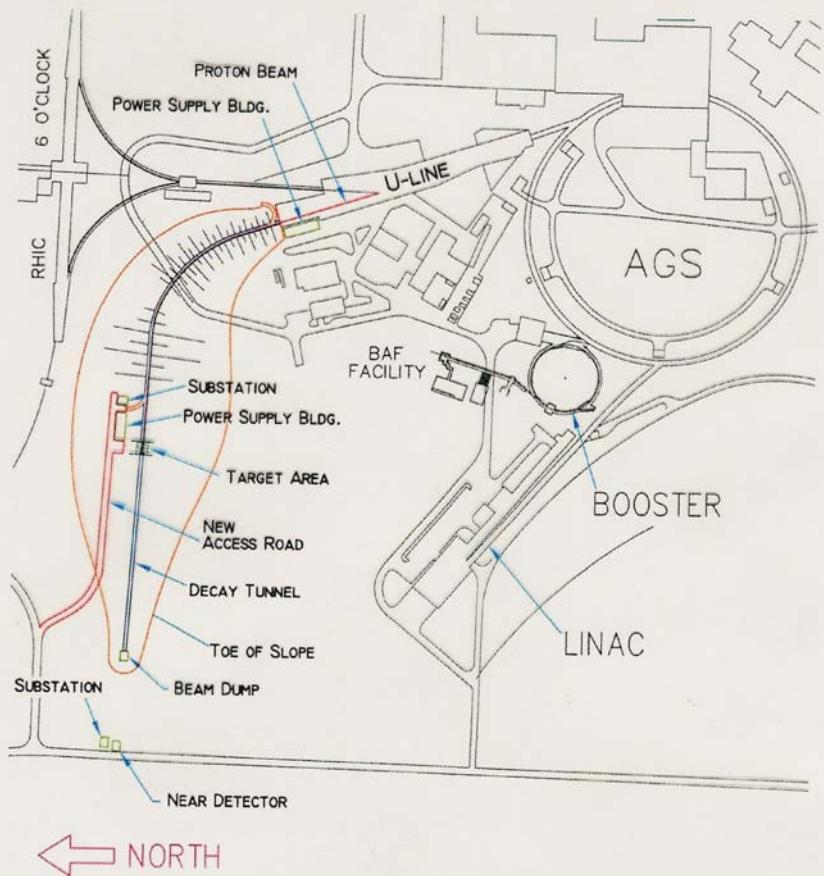
## Beam 3d



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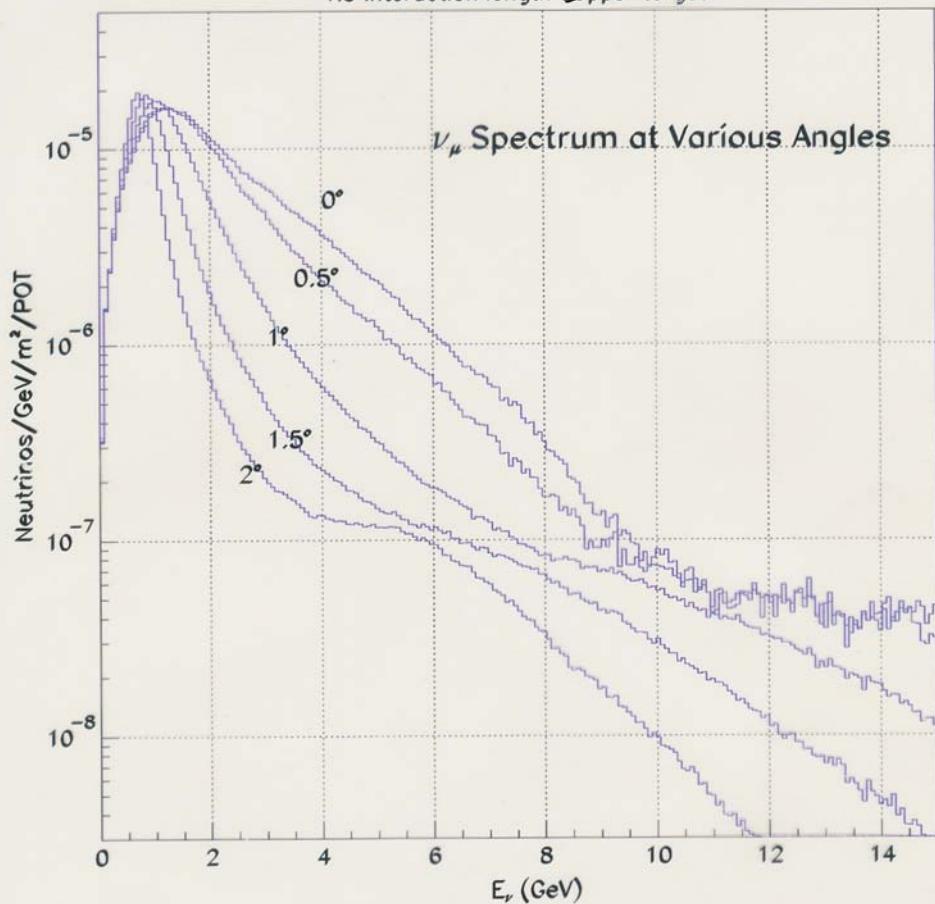
## Beam Layout



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2002/07/22 13.30

Carbon  
1.5 interaction length Copper target

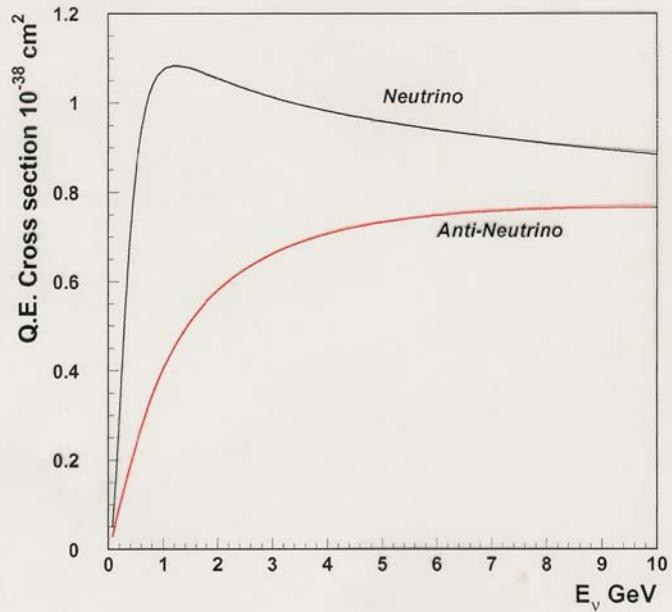


$$L = 1 \text{ km} \quad T = 200 \text{ m}$$

Very long baselines with a superbeam

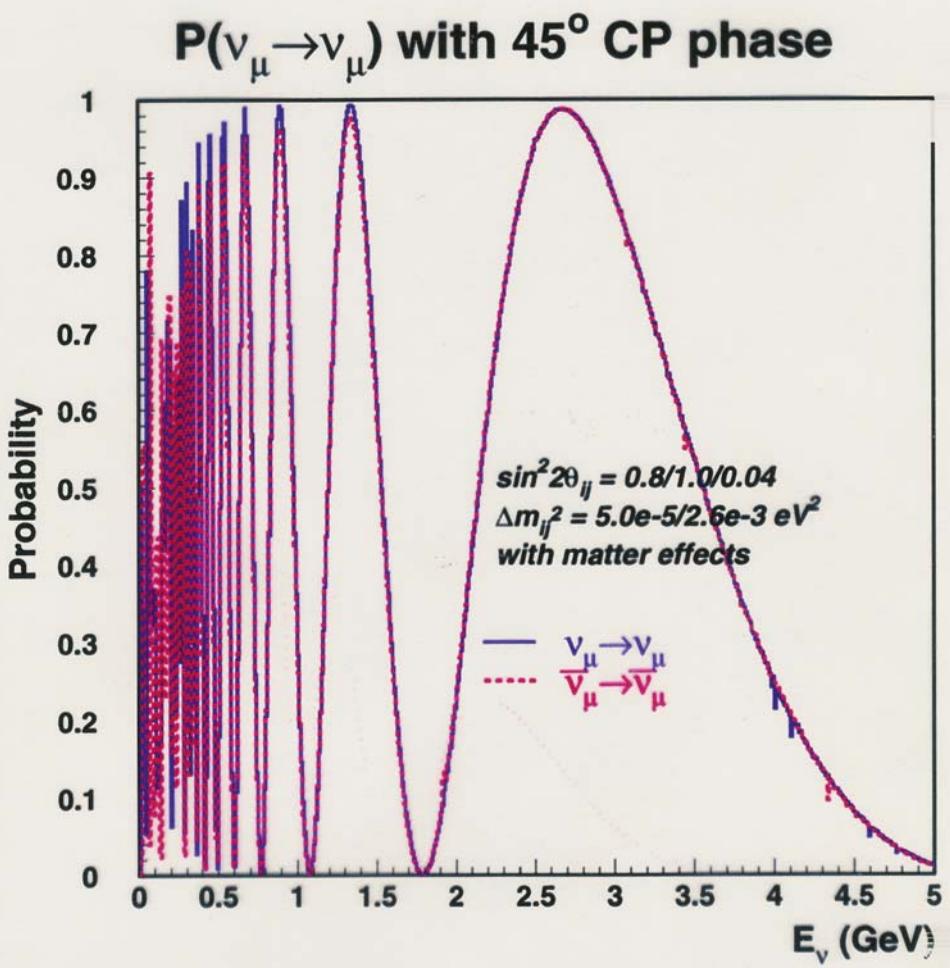
### Quasielastic cross section

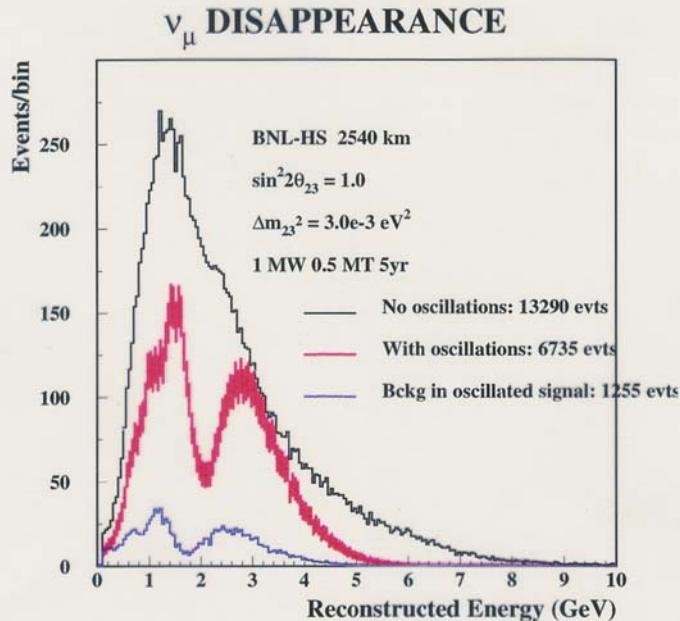
$$\nu_{\mu} e \rightarrow \mu^- \bar{P}, \bar{\nu}_{\mu} P \rightarrow \mu^+ e \rightarrow E_{\nu}$$



An experiment searching for signal at high energies may not need much more anti-neutrino running than neutrino running.

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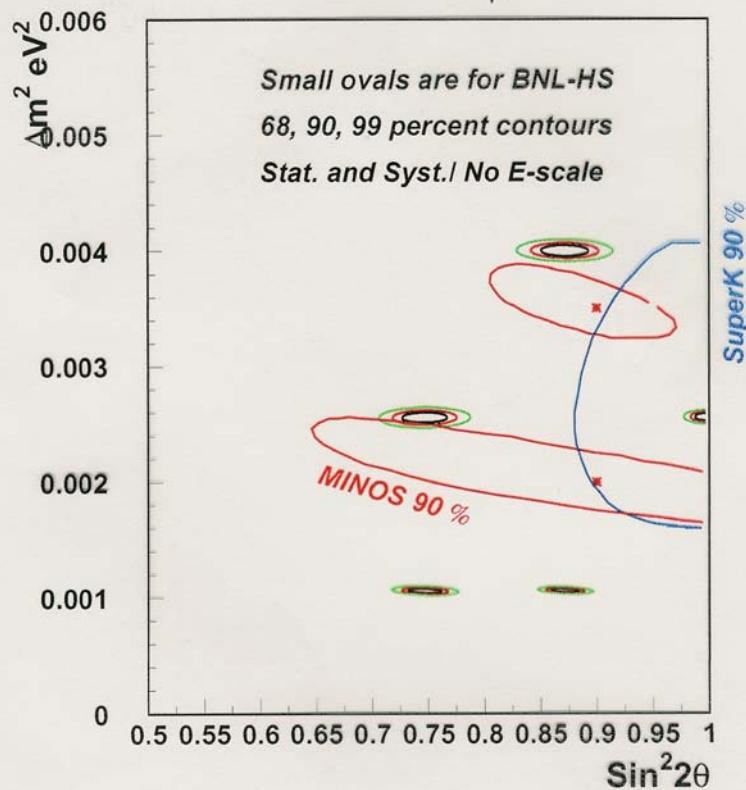
Node pattern provides high  $\Delta m_{23}^2$  resolution.  
Energy calibration is very important.

Flux normalization not important for  
measurement of  $\sin^2 2\theta_{23}$

Background shape can be measured independently  
Minimum systematics in  $\nu_\mu$  and  $\bar{\nu}_\mu$  comparison

Very long baselines with a superbeam

## Test points for $\nu_\mu$ disapp



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Measure  $\Delta m_{32}^2 + \sin^2 2\theta_{23}$  to  $\pm 1\%$  (or better)!

No. Osc.  $\nu_\mu \pi \rightarrow \mu^- p$  15,000 events  
 $\sin^2 2\theta_{23} \approx 1$  Osc.  $\rightarrow$  7,500 events } 1 event/hr  
 (Sterile  $\nu$  mixing, Extra Dim, Exotic Int...)

2)  $\nu_\mu \rightarrow \nu_e$  Appearance (Rich Structure) (3-4 peaks)

$$P(\nu_\mu \rightarrow \nu_e) = \frac{0.5 \sin^2 2\theta_{13} \sin^2 \left( \frac{\Delta m_{31}^2 L}{4E_\nu} \right)}{+ 0.93 \sin \theta_{13} \sin \left( \frac{\Delta m_{31}^2 L}{4E_\nu} \right) \left\{ \sin \frac{\Delta m_{31}^2 L}{4E_\nu} \sin \delta + \cos \frac{\Delta m_{31}^2 L}{4E_\nu} \cos \delta \right\} \frac{\Delta m_{21}^2 L}{2E_\nu}} + 0.36 \left( \frac{\Delta m_{21}^2 L}{4E_\nu} \right)^2 + \text{matter effects} + \text{small terms}$$

Term 2 :  $\cos \left( \frac{\Delta m_{31}^2 L}{4E_\nu} - \delta \right)$

To explore  $0 \leq \delta < 2\pi \rightarrow \frac{\Delta m_{31}^2 L}{4E_\nu} \simeq \underbrace{\frac{\pi}{2}, \frac{3\pi}{2}, \frac{5\pi}{2}}_{3 \text{ peaks}}$   
 $(L = 2540 \text{ km})$

$$E_\nu \simeq 5, \frac{5}{3}, 1 \text{ GeV}$$

Broad Band (On-Axis) Beam  $0.5 \text{ GeV} < E_\nu < 5 \text{ GeV}$

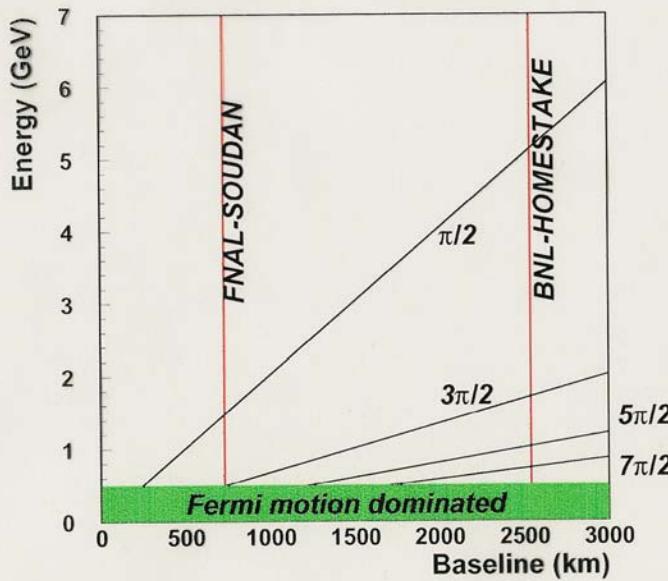
i)  $3 \text{ GeV} < E_\nu < 5 \text{ GeV}$  (very sensitive to matter)

$\text{sgn } \Delta m_{32}^2$  easy

measure  $\theta_{13}$   $0.01 \leq \sin^2 2\theta_{13} \leq 0.2$  Factor  $\approx 20$ !

Bound  $\rightarrow 0.003$

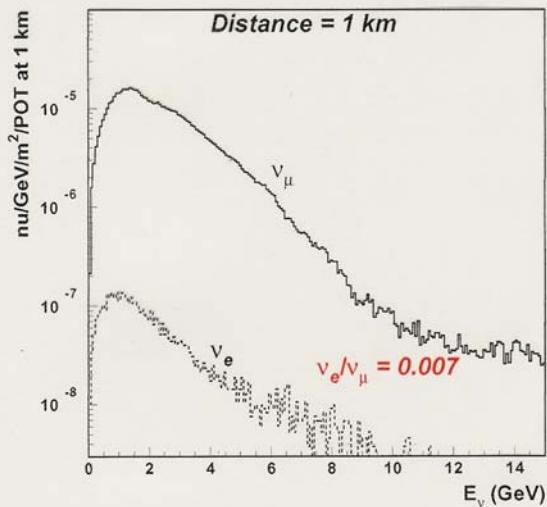
### Oscillation Nodes for $\Delta m^2 = 0.0025 \text{ eV}^2$



- Large effects: Multiple oscillation nodes.
- Low cross section at low energies
- Fermi motion limits resolution at low energies: wide band beam ( $0.5 \rightarrow 8 \text{ GeV}$ ).
- $\Delta m^2 \approx 0.0025 \text{ eV}^2$ : Baseline  $> 2000 \text{ km}$ .

Very long baselines with a superbeam

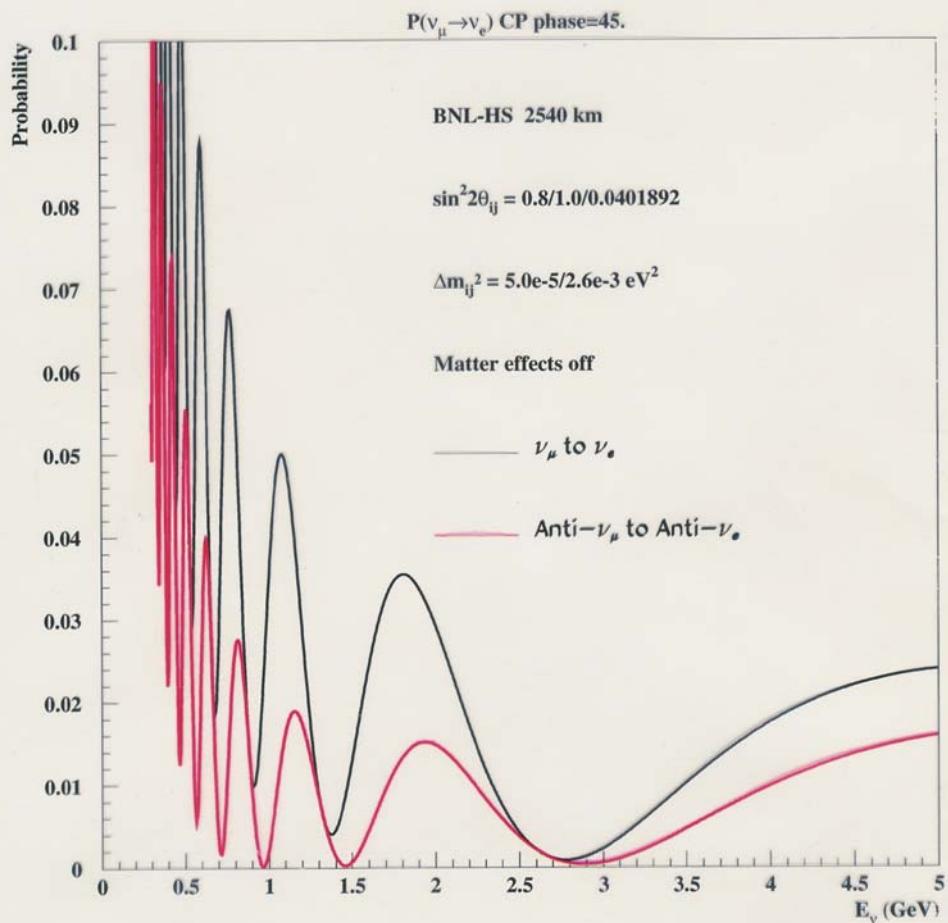
BNL Wide Band. Proton Energy = 28 GeV



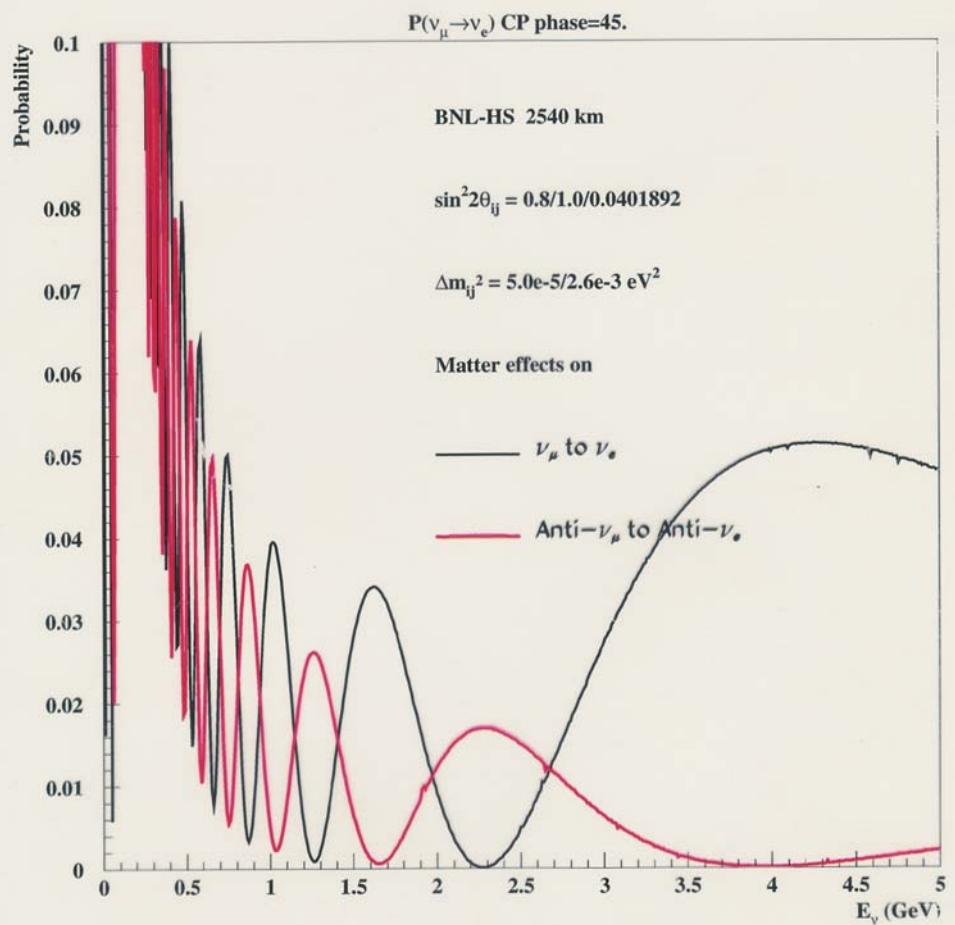
- New design spans 0.5-6 GeV
- Low  $\nu_e$  background 0.7%  
 $0.0073 \pm 0.0014$  (E734 1986).
- Low background from high energies (NC and  $\nu_\tau$  for  $\nu_e$ )
- 200 m decay tunnel
- Graphite target embedded in horn
- Target cooling achievable for 1 MW

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2002/07/19 18.08



2002/07/22 11.00



$1 \text{ GeV} < E_\nu < 3 \text{ GeV}$       Measure  $\delta$  ( $\sin \delta, \cos \delta$ )

If inverted hierarchy    2 yr  $\bar{\nu}_\mu$  + 3 yr  $\bar{\nu}_\mu$

$0.5 \text{ GeV} < E_\nu < 1 \text{ GeV}$       Measure  $\Delta m_{21}^2 \sin 2\theta_{12}$  to  $\pm 5\%$ !

special feature of long dist  
(unique)

Statistical Figure of Merit (for  $CP, \delta$ )

In sensitive to  $L$  &  $\sin^2 2\theta_{13}$

Asym. grows  $\sim L$        $N_\nu \sim 1/L^2$

$$\text{F.O.M.} \sim A_{CP}^2 N_\nu$$

with about 300-400  $\bar{\nu}_e n \rightarrow e^- p$  quasi-elastic events

measure

$$\text{sgr } \Delta m_{32}^2$$

$$\Delta m_{21}^2 \sin 2\theta_{12} \text{ to } \pm 5\%$$

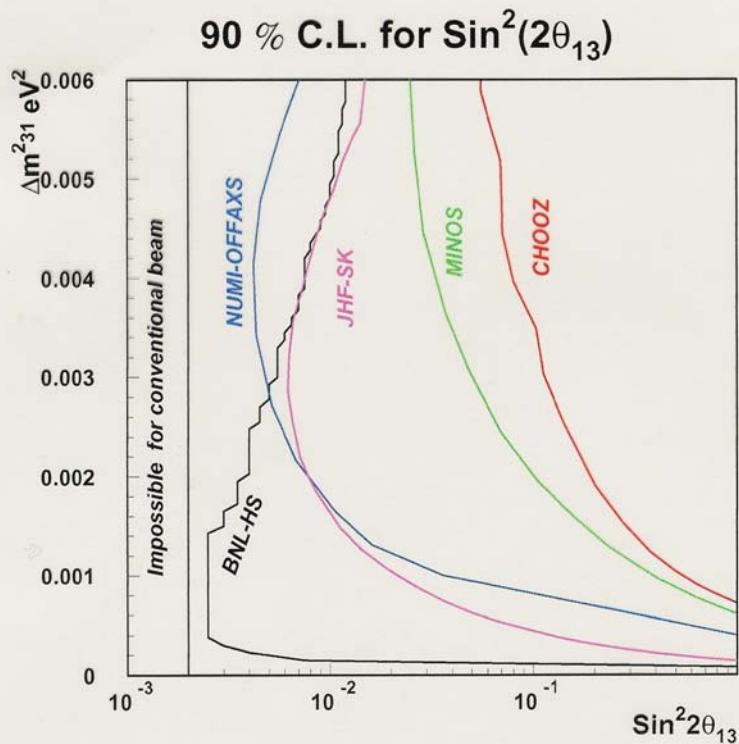
$$0.01 < \sin^2 2\theta_{13} < 0.2 \rightarrow \sin^2 2\theta_{13} \text{ to } \pm 10\%$$

$$\delta \text{ to } \pm 15-20^\circ$$

$\left. \begin{array}{l} \text{Very Powerful} \\ (\text{Robust}) \end{array} \right\}$

Very long baselines with a superbeam

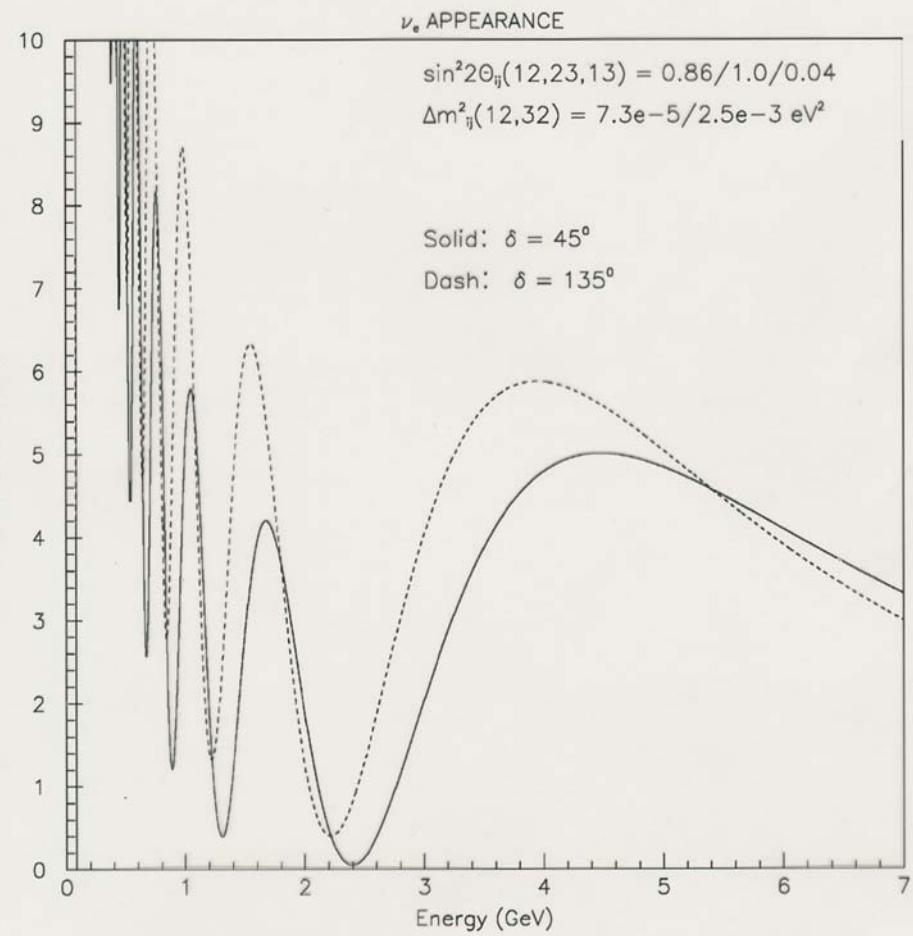
Measurement of  $\sin^2 2\theta_{13}$  90% C.L.



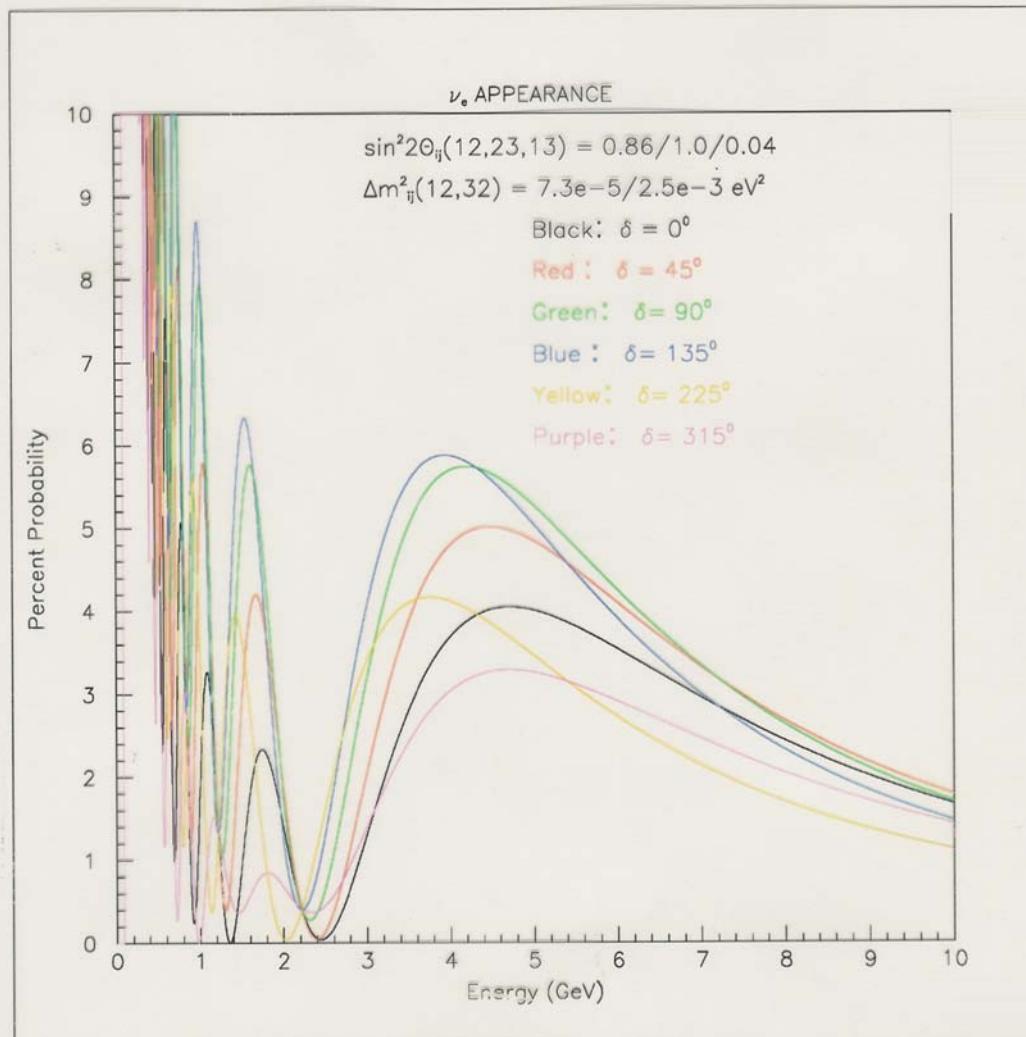
Distinctive signature with multiple oscillations  
above  $0.001 \text{ eV}^2$

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*From Z. Parsa*



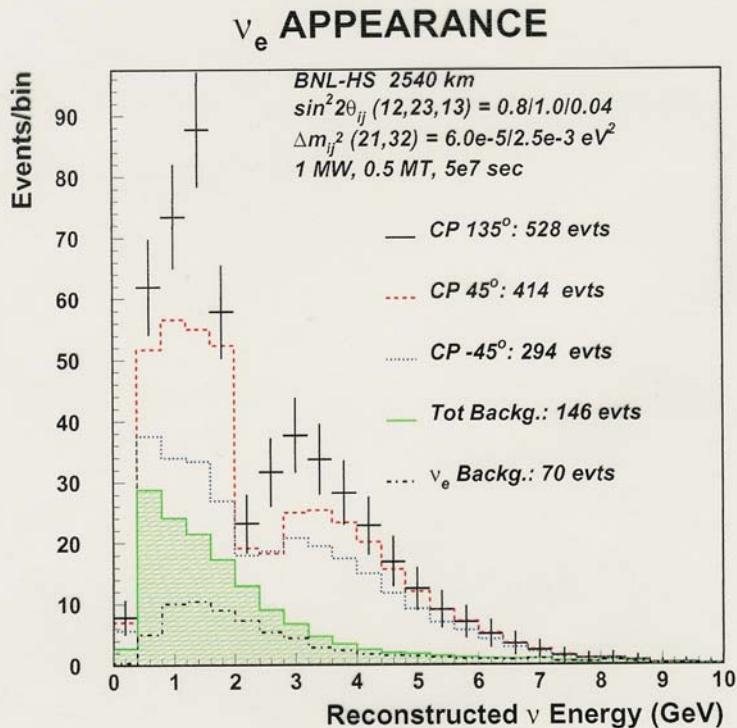
Zohreh Parsa  
BNL - Feb 03



$[\bar{\nu}_e + \tau, 10 \text{ GeV}]$

Very long baselines with a superbeam

$\delta_{CP}$  Measurement. BNL-to-HS,  
2540 km, 1 MW, 500kT,  $5 \times 10^7$  sec

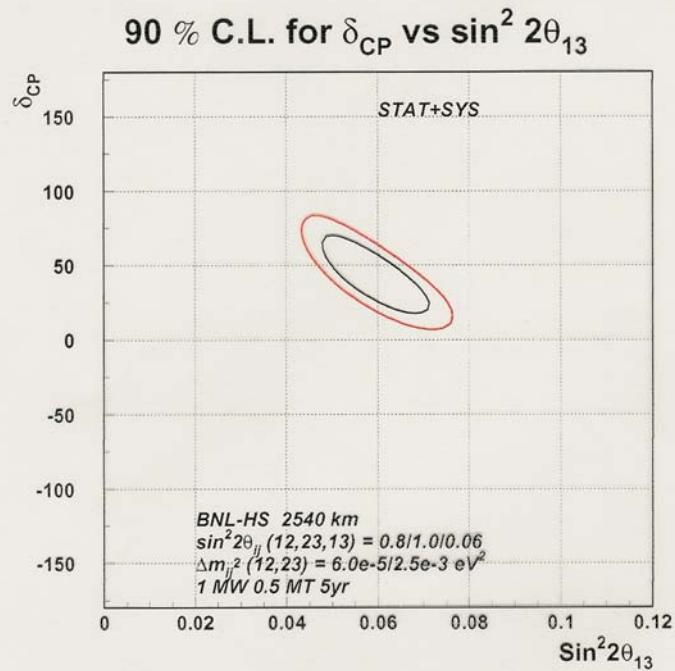


CP parameter can be determined from only neutrino data.  
Good background subtraction can help.

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Very long baselines with a superbeam

Measurement of  $\delta_{CP} = 45^\circ$   
No anti-neutrino running.



Systematic error of 10% on backg.

$$\Delta m_{21}^2 = 6 \times 10^{-5} \text{ eV}^2, \Delta m_{31}^2 = 2.5 \times 10^{-3} \text{ eV}^2$$

$$\sin^2 2\theta_{12} = 0.8, \sin^2 2\theta_{23} = 1.0$$

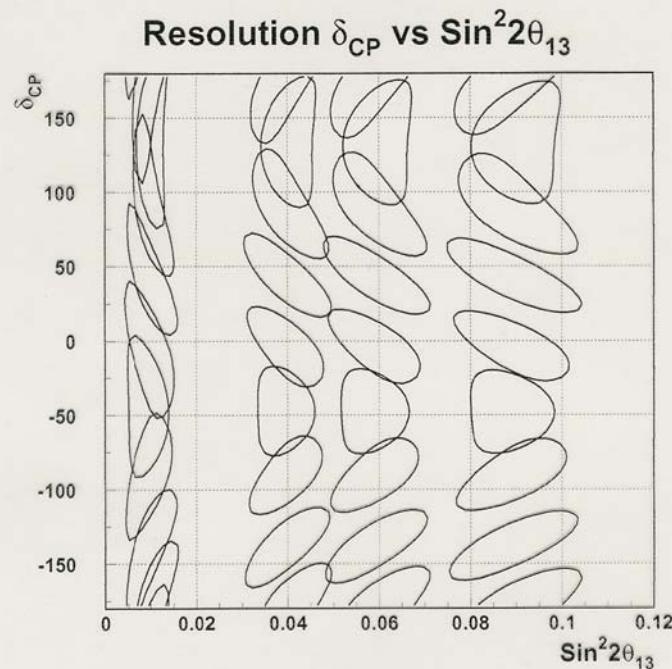
$$\delta_{CP} = 45^\circ, \sin^2 2\theta_{13} = 0.06$$

68%, and 90% C.L.

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Error on  $\delta_{CP}$  vs  $\sin^2 2\theta_{13}$



Assume all other parameters are well-known.

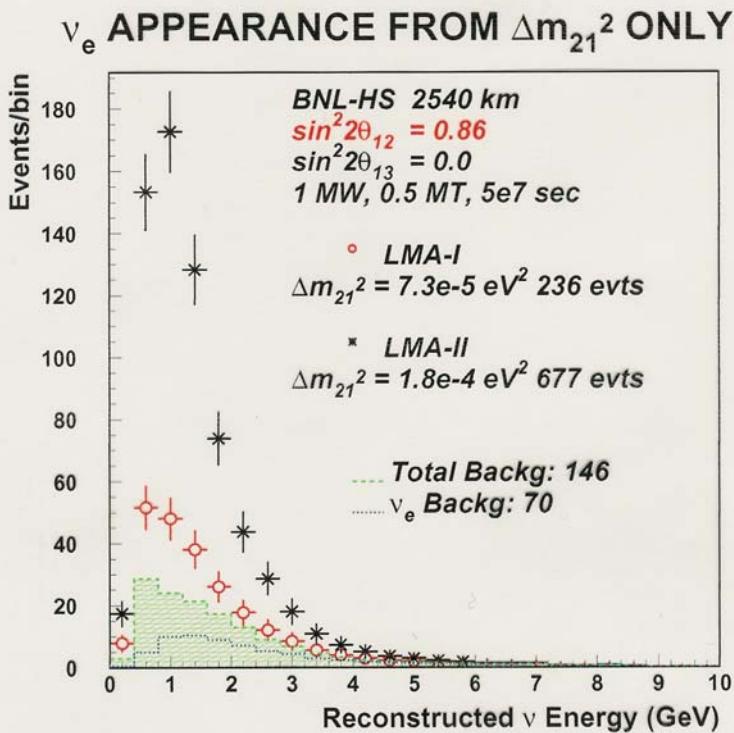
$$\Delta m_{21}^2 = 6 \times 10^{-5} eV^2, \Delta m_{31}^2 = 2.5 \times 10^{-3} eV^2$$

$$\sin^2 2\theta_{12} = 0.8, \sin^2 2\theta_{23} = 1.0$$

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## Measurement of $\Delta m_{12}^2$

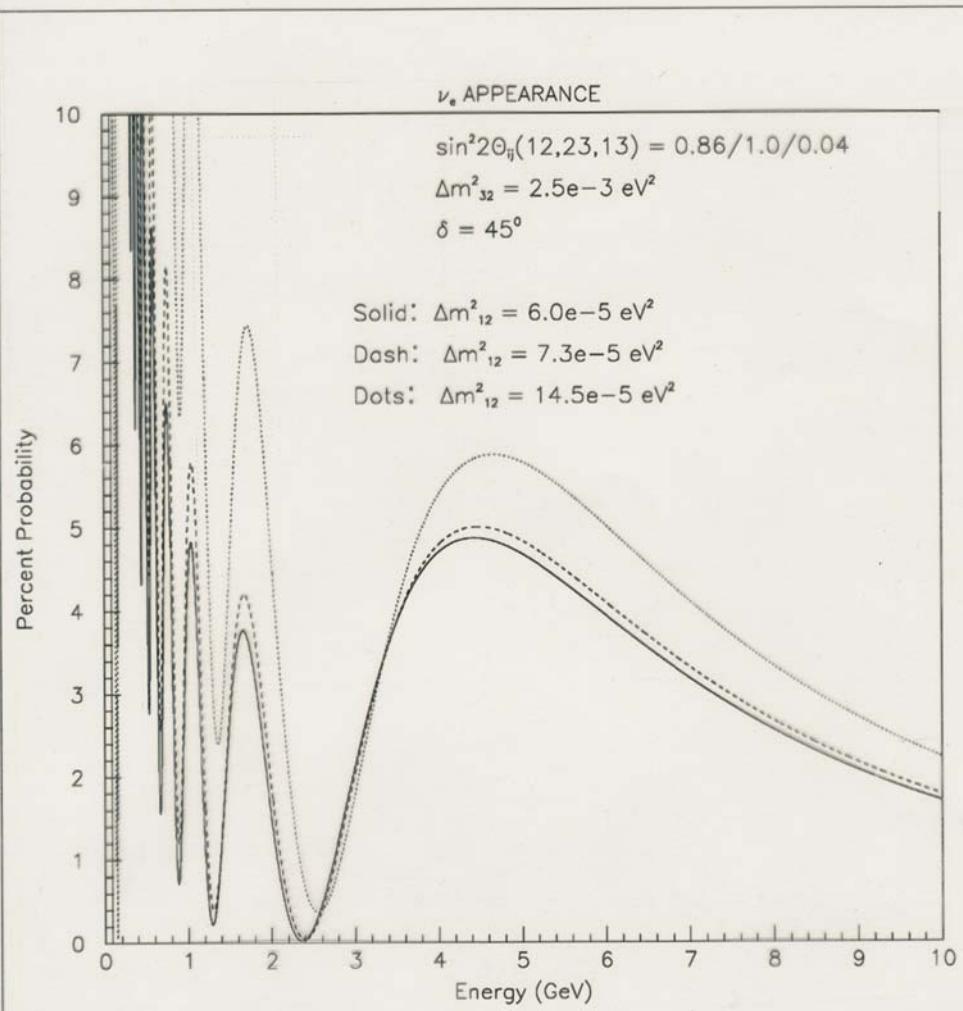


$$\theta_{13} = 0, \Delta m_{12}^2 = 7.3 \times 10^{-5} \text{ eV}^2$$

Excess of  $\sim 90$  events. Must know background

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Zohreh Parsa  
Feb 28, 2003



### Outlook

We have shown: 1MW AGS + 500 kton H<sub>2</sub>O Detector

$$L \approx 2000-3000 \text{ km}$$

(Homestake, WIPP, Henderson)

$\nu_\mu \rightarrow \nu_\mu, \nu_e \rightarrow$  Measure:  $\Delta m_{ij}^2, \theta_{ij}, \delta \dots$  (May do  $\bar{\nu}_\mu$  as well.)

Detector (Work with UNO Collaboration & Others)

Cost 300-500 Million

R&D to Reduce

Note: 50yr Physics Facility ( $\gamma_p, \nu \dots$ )  
Could Start Soon!

AGS Upgrade (see study) Straightforward  $0.14 \text{ MW} \rightarrow 1 \text{ MW}$   
 $1 \text{ MW} \rightarrow 2 \text{ MW}$

Neutrino Beam Hill better than Hole (Cheaper, Clearer)

Study Continues (Backgrounds etc.)

Best Idea for  $\nu$  Future (No real competition)

An Idea Whose Time Has Come (straightforward)

Should be supported & pursued!

## Accelerator Based Experiments in the USA

### FNAL

CDF & DΦ  
MiniBOONE  
MINOS  
BTeV  
CKM  
Off-Axis ν } Future 2008 →

### SLAC

Ba Bar  
Pol. e<sup>+</sup>e<sup>-</sup>  
Pol. eD  
Super b?

### CESR

CLEO-C

### BNL-AGS

$g_\mu - 2$   
 $K^+ \rightarrow \pi^+ \nu \bar{\nu}$   
MECO ( $\mu^- N \rightarrow e^- N$ )  
KOPIO ( $K_L \rightarrow \pi^0 \nu \bar{\nu}$ )  
VLB ν osc.  
EDM } Future 2008 →

Future BNL Program is an Essential Component!