

A SIMPLE MODEL-BASED MAGNET SORTING ALGORITHM FOR PLANAR HYBRID UNDULATORS*

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Abstract

Various magnet sorting strategies have been used to optimize undulator performance, ranging from intuitive pairing of high- and low-strength magnets, to full 3D FEM simulation with 3-axis Helmholtz coil magnet data. In the extreme, swapping magnets in a full field model to minimize trajectory wander and rms phase error can be time consuming. This paper presents a simpler approach, extending the field error signature concept to obtain trajectory displacement, kick angle and phase error signatures for each component of magnetization error from a Radia [1] model of a short hybrid-PM undulator. We demonstrate that steering errors and phase errors are essentially decoupled and scalable from measured X, Y and Z components of magnetization. Then, for any given sequence of magnets, rms trajectory and phase errors are obtained from simple cumulative sums of the scaled displacements and phase errors. The cost function (a weighted sum of these errors) is then minimized by swapping magnets, using one's favorite optimization algorithm. This approach was applied recently at NSLS to a short in-vacuum undulator, which required no subsequent trajectory or phase shimming. Trajectory and phase signatures are also obtained for some mechanical errors, to guide "virtual shimming" and specifying mechanical tolerances. Some simple inhomogeneities are modeled to assess their error contributions.

INTRODUCTION

NSLS-II will have numerous planar in-vacuum hybrid-PM undulators (IVU's), designed to deliver high-brightness multi-kilovolt photon beams. They will have period lengths typically on the order of 20 mm and will be optimized for high brightness at high harmonics. This requires minimizing the deleterious effects of field errors, which cause not only deviations in trajectory straightness, but also introduce phase errors which reduce peak brightness, especially at high harmonics. Strategies for minimizing these errors include imposition of tight dimensional tolerances on poles, magnets, module parts and support beams, on tolerance stack-ups, and on precise mounting of these components. The second is requiring tight magnetic tolerances on the permanent magnet (PM) blocks. Magnet manufacturers now routinely achieve magnet strength errors of $<1\%$ and magnetization angle errors of $<1^\circ$. Still, it is routine practice to measure the X, Y and Z magnetic moments of PM's with Helmholtz coils,

and to apply some kind of sorting algorithm to minimize undulator field errors and their consequences. Characterizing magnet blocks in a Helmholtz coil or by far field measurements yields the average magnetic moments over the magnet. Magnetic inhomogeneities in the small IVU magnets are inherently small and will be ignored here.

Magnet sorting methods and criteria for optimizing undulators range from intuitive pairing of stronger and weaker magnets to minimize field errors (used as recently as 2007 [2]), to multi-objective optimization by Simulated Annealing [3] or Genetic Algorithms [4] to minimize trajectory and phase error. Optimization by shuffling magnets requires constructing a field error model from measurements of individual magnets, and then computing a "cost function" to be minimized. This may be done to good approximation for a pure-PM undulator by superposition of measured fields of individual magnets, since permeability of PM's is close to 1. In hybrid-PM undulators (HPMU'S) with ferromagnetic poles, linear superposition of PM fields is not valid. However, for small errors, "field error signatures" [5] can be obtained, which characterize the change in undulator field due to a small change in a magnetic or mechanical parameter, or of a magnetic shim [6]. Field error signatures may be scaled by Helmholtz data and convolved linearly with the ideal field, then integrated to compute trajectory and phase errors for a cost function to be minimized, by iterating thousands of times – a computationally intense process.

In this paper we extend the error signature concept and directly obtain trajectory kick, displacement and phase error signatures of magnetization errors. We show they are essentially decoupled and can then be simply scaled and summed to obtain a performance cost function. We outline a simple magnet swapping algorithm, written in Mathematica, to optimize spectral performance.

MAGNETIZATION ERROR SIGNATURES

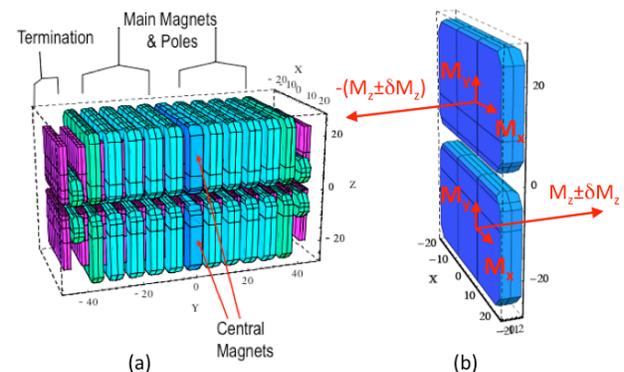
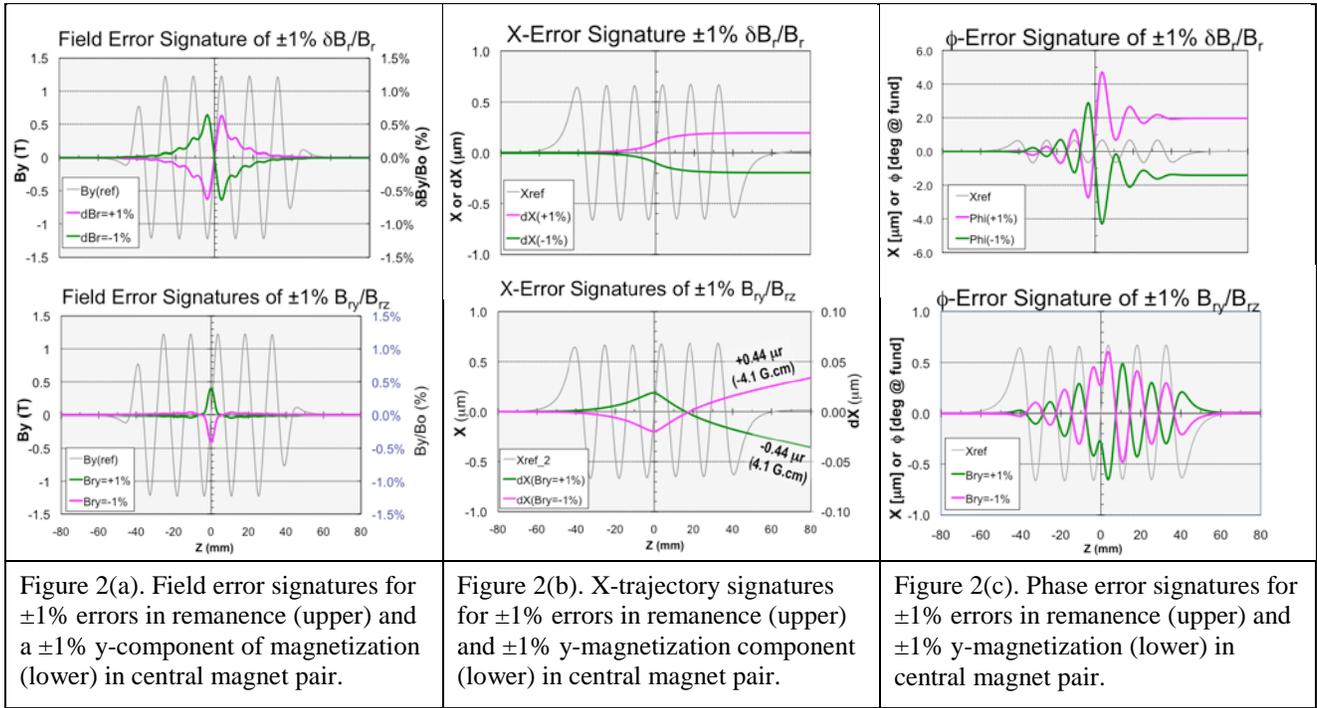


Figure 1. (a) Radia model of HPMU. (b) Central magnet pair with magnetization error components δM_z , M_y and M_x .

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A short HPMU was modeled in Radia, with parameters of the NSLS X9 in-vacuum undulator: period $\lambda_u=14.5$ mm, 3.4 mm gap, NdFeB with $B_r=1.3\text{T}$. (Figure 1a.) On-axis fields $B_{y0}(z)$ and $B_{x0}(z)$ as well as trajectories $x_0(z)$ and $y_0(z)$ were computed with no errors applied. Nominal errors of $\pm 1\%$ in each component of magnetization were introduced in turn in the central magnet pair (Figure 1b): $\pm \delta M_z/M_z$ (the principal component) was simulated by changing B_r by $\pm 1\%$; (b) M_y or M_x errors were modeled by adding ± 0.01 transverse (x or y) components to the principal (z) magnetization unit vector. The transverse components were oriented to add on-axis. Again, on-axis fields and trajectories were computed for each case. Subtracting the no-error fields and trajectories, we obtain *field error signatures* and *trajectory error signatures* for each magnetization component. Finally, by computing the path length difference $\delta S(z)$ between the trajectories with and without the error, normalized by the resonant optical wavelength, times $180^\circ/\pi$, we obtained phase error signatures (in degrees) for each error component.

Magnetization Strength Error

Figure 2 (upper row) shows the signatures of field error (%), X-trajectory error (μm) and phase error (degrees) due to $\pm 1\%$ error in B_r in the central magnet pair. Although the field error “bleeds” into 3 or 4 neighboring poles, it produces a net x-displacement of $\sim 0.2 \mu\text{m}$ ($\sim 1/3$ of the wiggle amplitude) with *no steering*. This gives us a scale factor of $\delta x = \sim 0.1 \mu\text{m}$ per 1% $\delta B_r/B_r$ per magnet. The phase error profile exhibits local over- and undershoots, but the *net* error is $\sim 1.8^\circ$, or $\delta\phi = \sim 0.9^\circ/1\%$ $\delta B_r/B_r$ per magnet.

Magnetization Angle Errors

Figure 2 (lower row) shows the signatures of a $\pm 1\%$ y-component of magnetization in both central magnets. The peak y-field error is $\sim 0.3\%$, mostly localized at the magnet, and results in a net steering kick $\delta x'$ of $\sim \pm 0.44 \mu\text{r}$ ($\sim 2 \text{ G.cm}$), or about $-2 \mu\text{r}/1\%$ M_y/M_z per magnet. The phase error becomes oscillatory after the deflection, but the *average* phase shift is zero.

Not shown, a $\pm 1\%$ x-component of magnetization produces peak B_x field error of only 0.003% , a y-kick of $0.14 \mu\text{r}$, or $0.07 \mu\text{r}/1\%$ M_x/M_z per magnet, and negligible phase error.

Performance Cost Function

These models reveal a simple scaling from Helmholtz or 3-axis far-field data of the magnet blocks:

- δM_z produces displacement δx and phase shift $\delta\phi$.
- M_y produces only an x-kick $\delta x'$.
- M_x produces only a y-kick $\delta y'$.

For small errors the scaling is linear. The models also reveal that the three magnetization error components produce effects that are essentially decoupled. For any arrangement of magnets we can now construct x and y error trajectories and phase error profiles by simple recursion. (The \pm means that the appropriate sign must be applied depending on magnet location and orientation.)

- $x'_{i+1} = x'_i \pm \delta x'_{i+1}; \quad x_{i+1} = x_i \pm \delta x_{i+1} + x'_{i+1} \lambda_u/2$
- $y'_{i+1} = y'_i \pm \delta y'_{i+1}; \quad y_{i+1} = y_i + y'_{i+1} \lambda_u/2$
- $\phi_{i+1} = \phi_i + \delta\phi_{i+1}$ (independent of orientation)

The results are *net* error trajectories (minus local details), from which we can compute rms values, and combine them into a weighted multi-parameter cost function W :

