

Large Angle Hadron Correlations from Medium-Induced Gluon Radiation

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**Jet Correlations at RHIC, March 10-11, 2005
Brookhaven National Laboratory, Upton, NY**

- ▶ **Radiative energy loss and jet quenching:**
 - Experimental results
 - Infrared and collinear safety property
 - Large angle emission - the death of the "dead cone"

- ▶ **Nuclear modification of di-hadrons:**
 - Modification of the yields (energy redistribution)
 - Modification of the large angle correlations
 - Sensitivity to subtraction of the elliptic flow

- ▶ **Conclusions:**

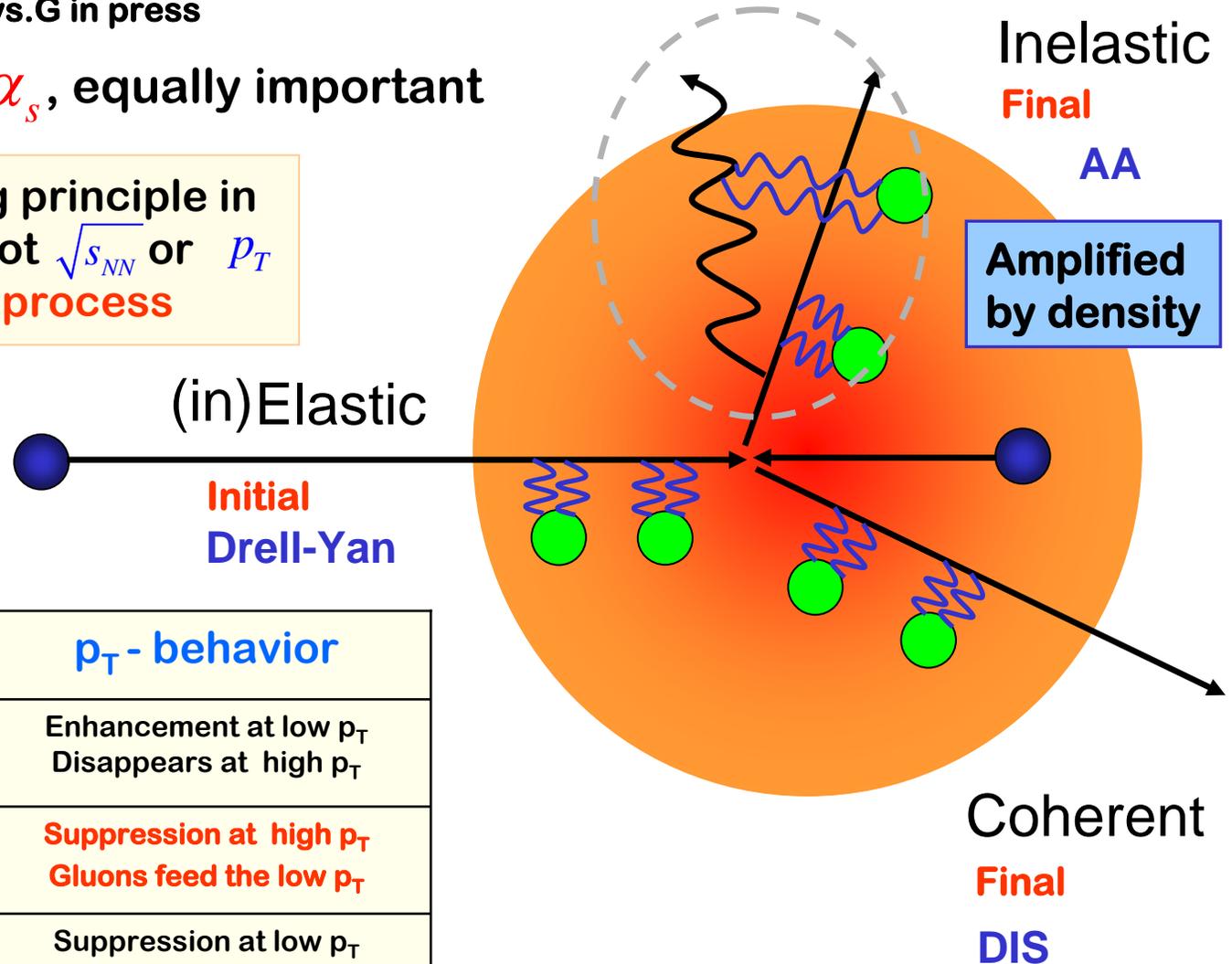
Specific Processes with Nuclei



I.V., J.Phys.G in press

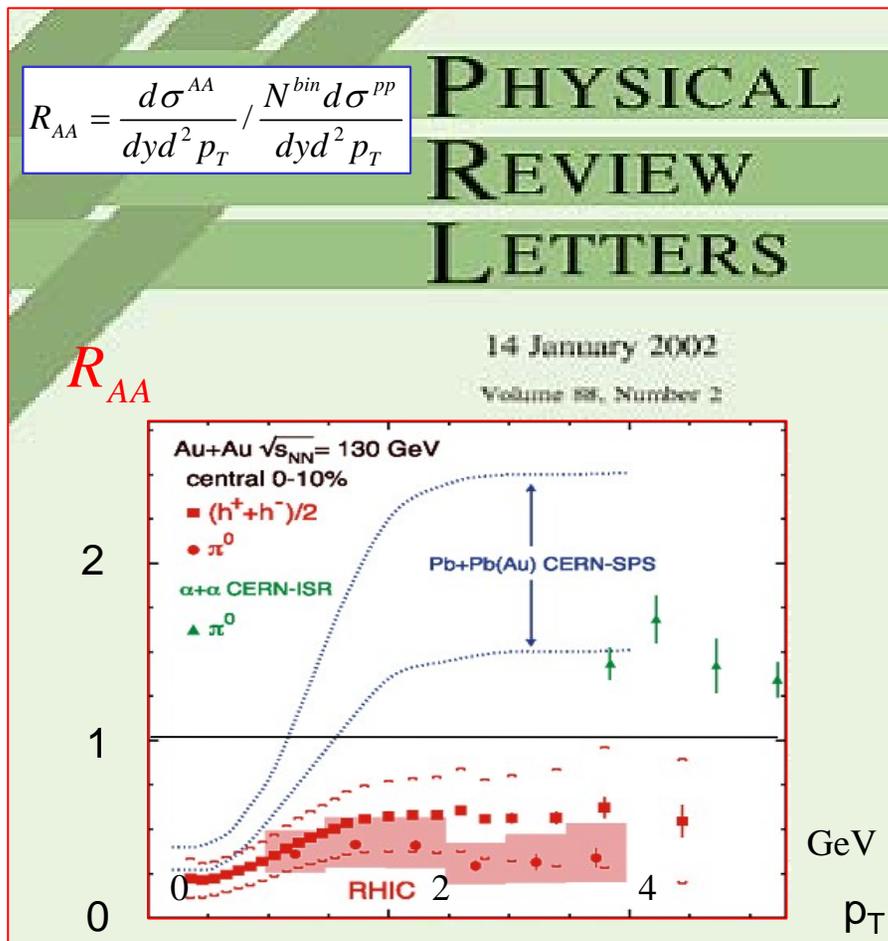
All couplings $\sim \alpha_s$, equally important

- The overarching principle in calculations is not $\sqrt{s_{NN}}$ or p_T but the **physical process**

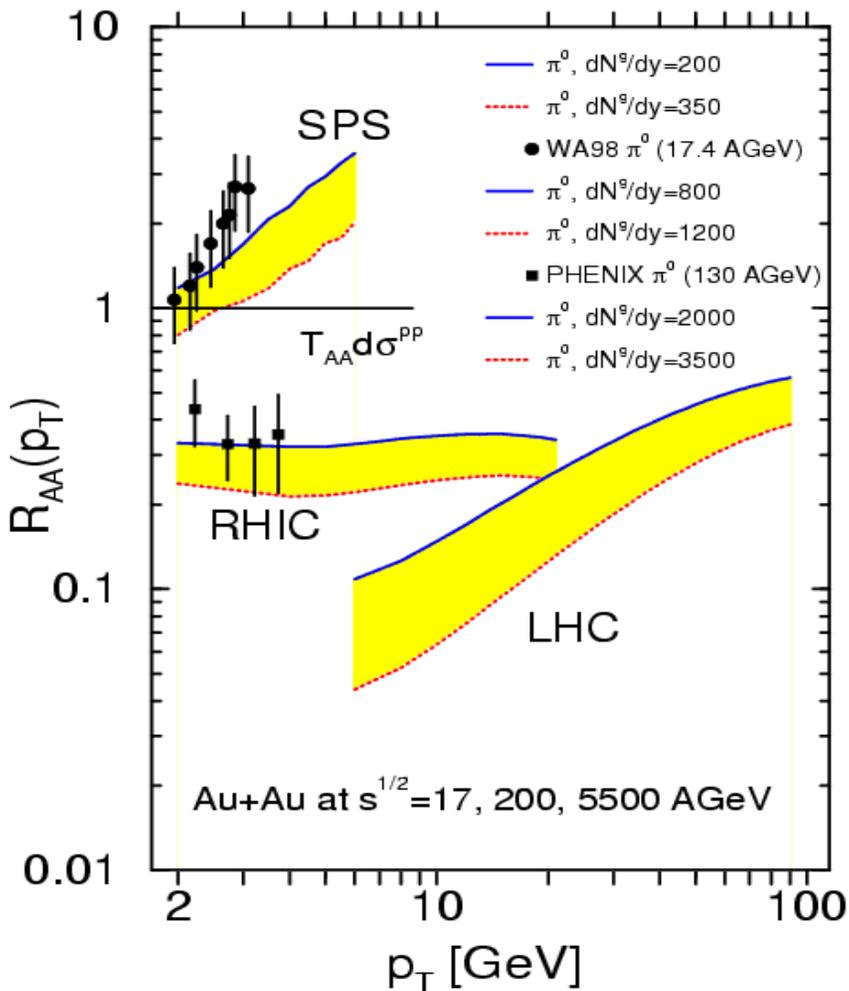


Type	Effect	p_T - behavior
Elastic	Cronin	Enhancement at low p_T Disappears at high p_T
Inelastic	Jet quenching	Suppression at high p_T Gluons feed the low p_T
Coherent	Shadowing	Suppression at low p_T Quickly disappears at high p_T

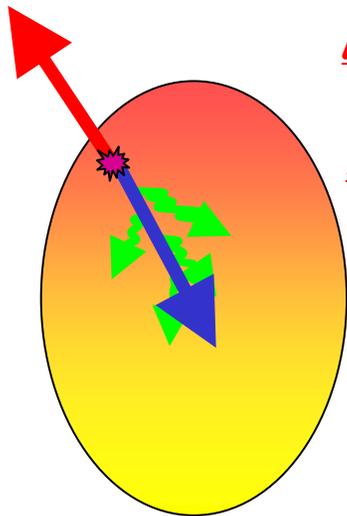
Depletion of high- p_T hadron multiplicities in Au+Au relative to the binary collision scaled p+p result



K.Adcox et al., Phys.Rev.Lett.88, (2002)



I.V., M.Gyulassy, Phys.Rev.Lett. 89 (2002)



Another way to establish

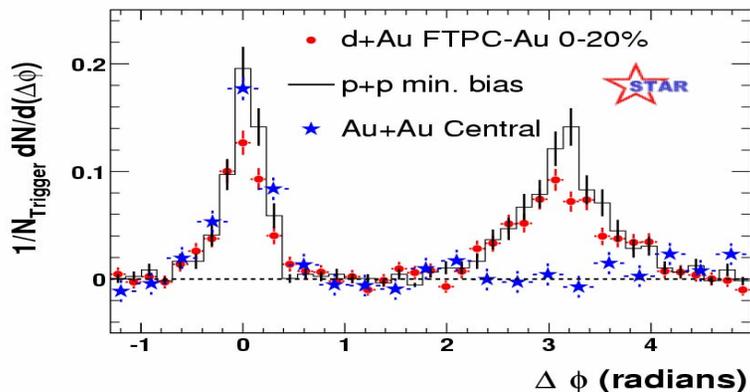
$d+Au \sim p+p$

$Au+Au$ is very different

**Away-side jet gets
"stuck" in the medium**

$$C_2(\Delta\phi) = \frac{1}{N_{trig}} \frac{dN^{h_1 h_2}}{d\Delta\phi}$$

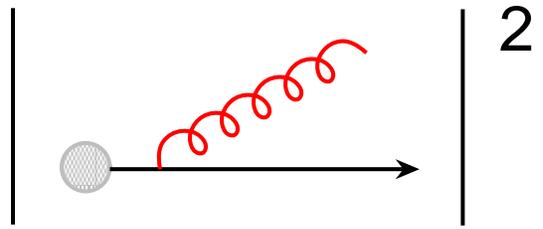
Test against a light system



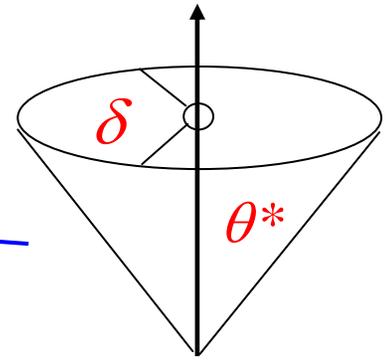
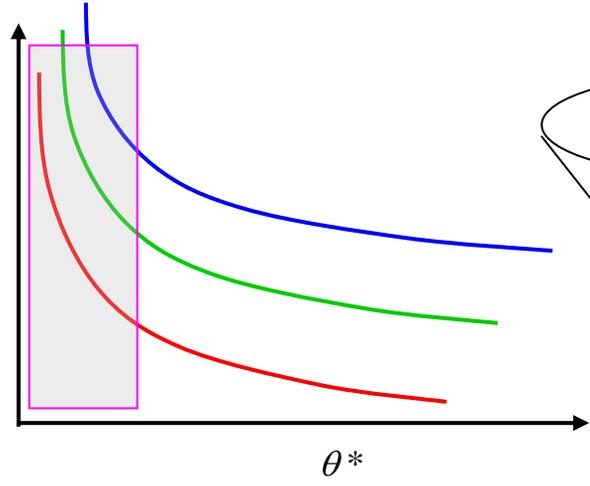
J.Adams *et al.*, Phys.Rev.Lett.91 (2003)



Vacuum Radiation



$$\frac{dN_{vac}^g}{d\omega d\sin\theta^*}$$



If interested in the small angle
small frequency behavior

$$\frac{dN^g}{d\omega d\sin\theta^* d\delta} \propto |M_c|^2$$

$$\frac{dN_{vac}^g}{d\omega d\sin\theta^* d\delta} \approx \frac{C_R \alpha_s}{\pi^2} \frac{1}{\omega \sin\theta^*}$$

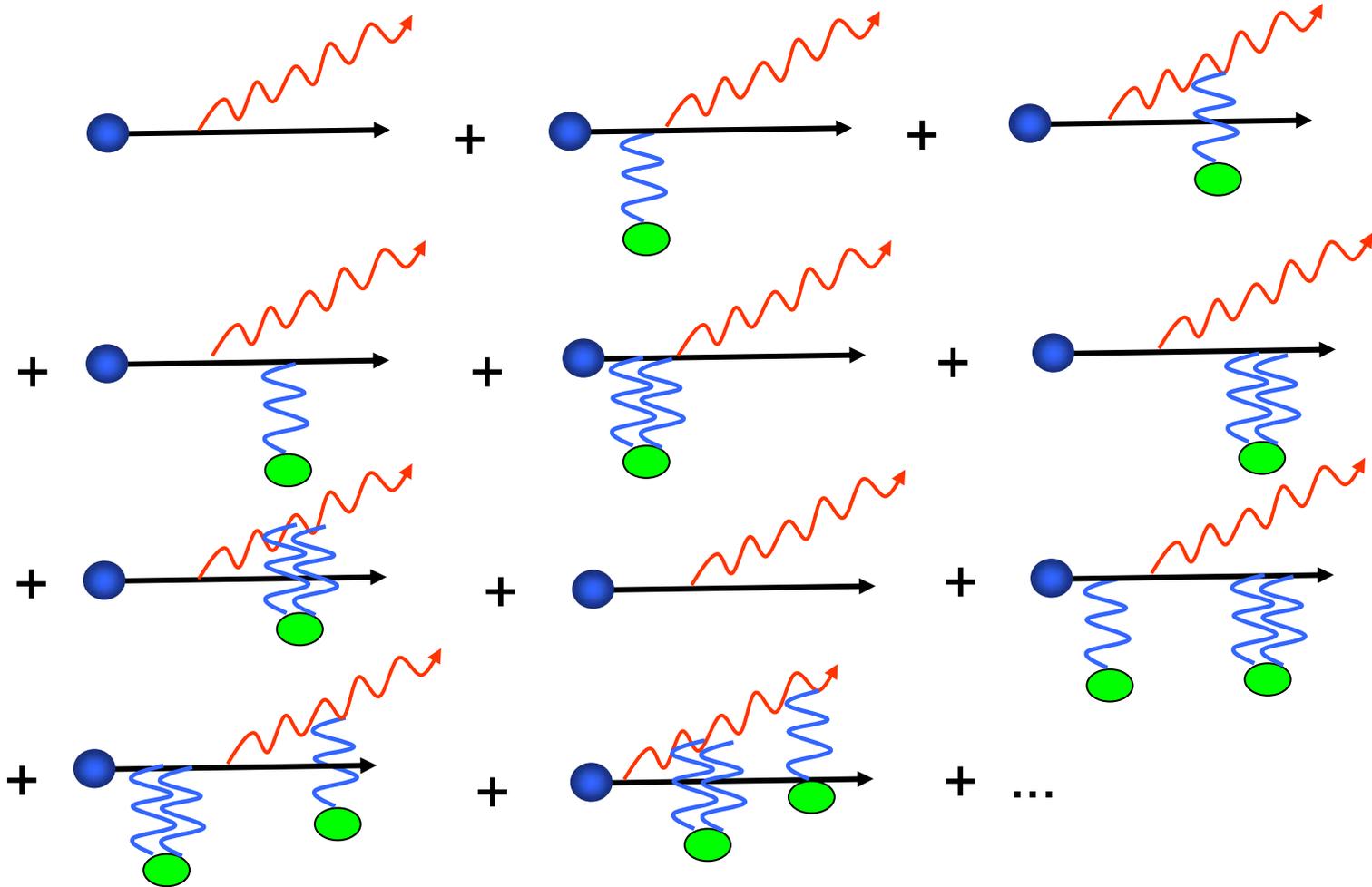
For massive quarks - "dead cone effect"

- Takes care of the collinear

$$\frac{dN_{vac}^g}{d\omega d\sin\theta^* d\delta} \approx \frac{C_R \alpha_s}{\pi^2} \frac{\sin\theta^*}{\omega (\sin^2\theta^* + M^2/E^2)}$$

Cuts part of phase space $0 \leq \theta^* \leq M/E$

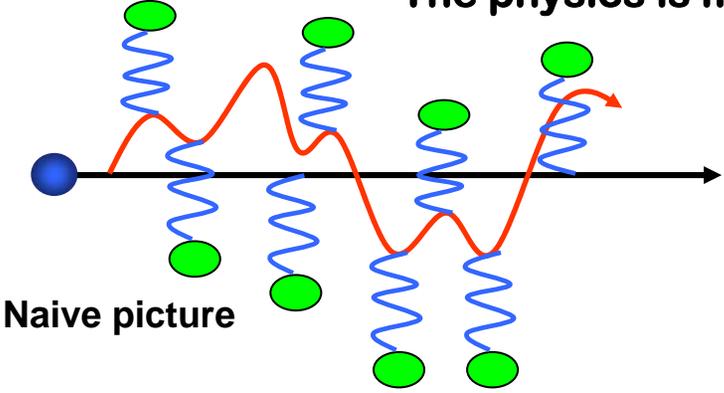
- Both **collinear** and **infrared** divergent
- **Collinear** persists. At fixed order requires subtraction in the PDFs and FFs



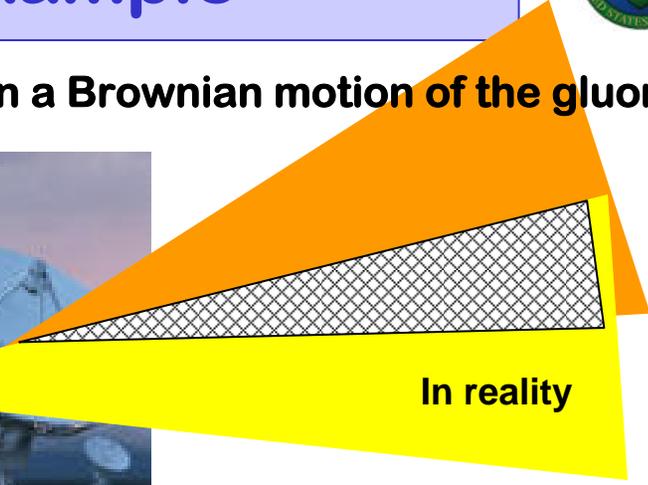
Need an organizing principle!

Instructive Example

The physics is more interesting than a Brownian motion of the gluon



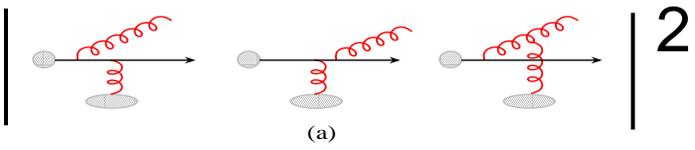
Naive picture



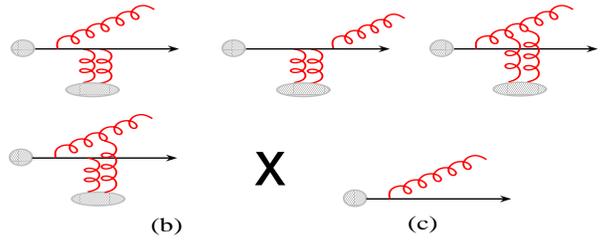
In reality

$$i(-i) = 1 \quad i(i) = -1 = \cos(\pi)$$

$$\frac{dN_{med}^g}{d\omega d\sin\theta^* d\delta} \propto (|M_a|^2 + 2\text{Re} M_b^* M_c) + \dots$$



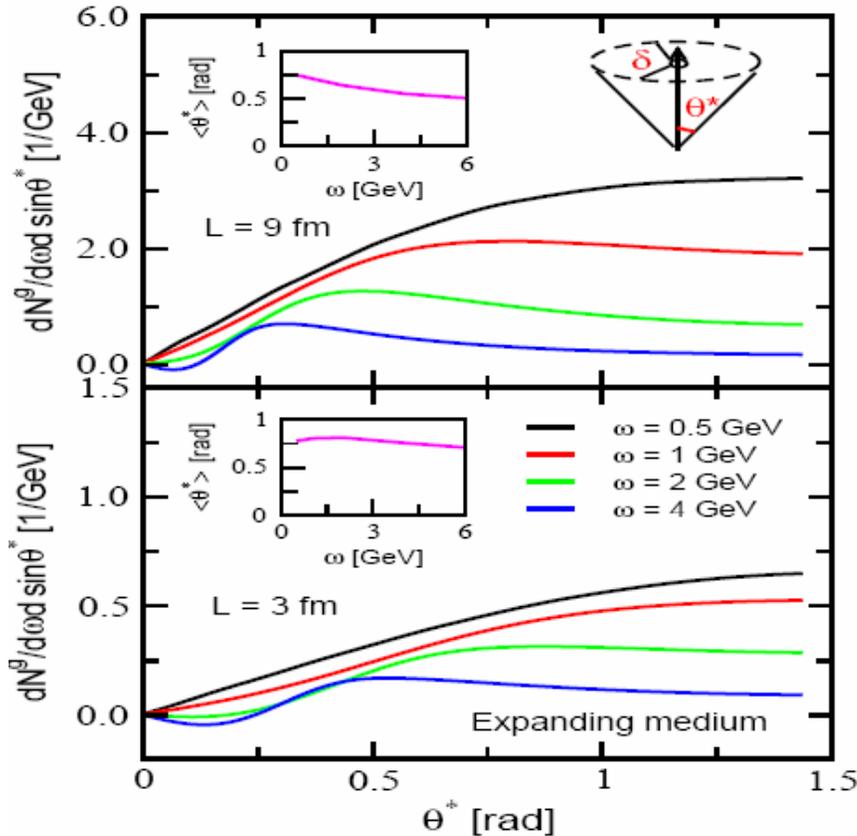
+2Re



Solution to first order in the mean # of scatterings

$$\frac{dN_{med}^g}{d\omega d\sin\theta^* d\delta} \approx \frac{2C_R\alpha_s}{\pi^2} \int_{z_0}^L \frac{d\Delta z}{\lambda_g(z)} \int_0^\infty dq_\perp q_\perp^2 \frac{1}{\sigma_{el}} \frac{d\sigma_{el}}{d^2q_\perp} \times \int_0^{2\pi} d\alpha \frac{\cos\alpha}{(\omega^2 \sin^2\theta^* - 2q_\perp \omega \sin\theta^* \cos\alpha + q_\perp^2)} \times \left[1 - \cos \frac{(\omega^2 \sin^2\theta^* - 2q_\perp \omega \sin\theta^* \cos\alpha + q_\perp^2) \Delta z}{2\omega} \right]$$

I.V., hep-ph/0501255

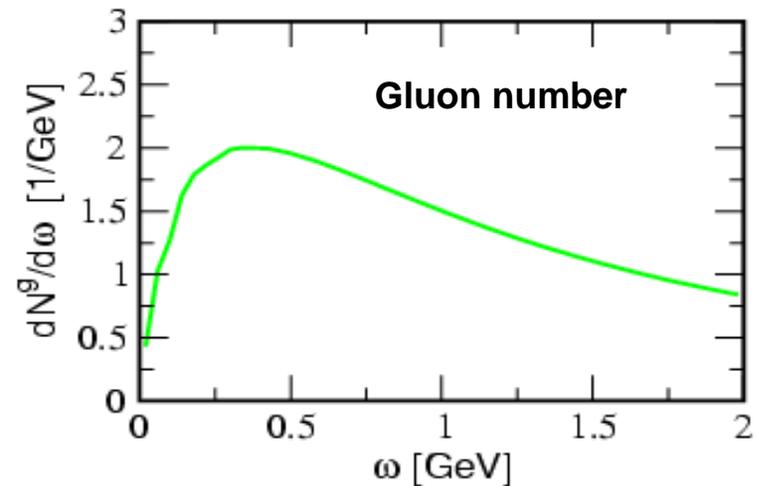


I.V., hep-ph/0501255

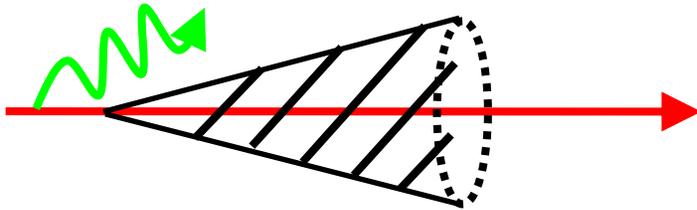
- Radiation is **moderately large angle** (cancellation near the jet axis)

- **Finite** gluon number

$$l_f = \frac{2\omega}{(\omega^2 \sin^2 \theta^* - 2q_{\perp} \omega \sin \theta^* \cos \alpha + q_{\perp}^2)} \sim \Delta z \sim L/2$$



- The small angle $\theta^* \rightarrow 0$ and small frequency $\omega \rightarrow 0$ behavior of the radiative spectrum is under perturbative control



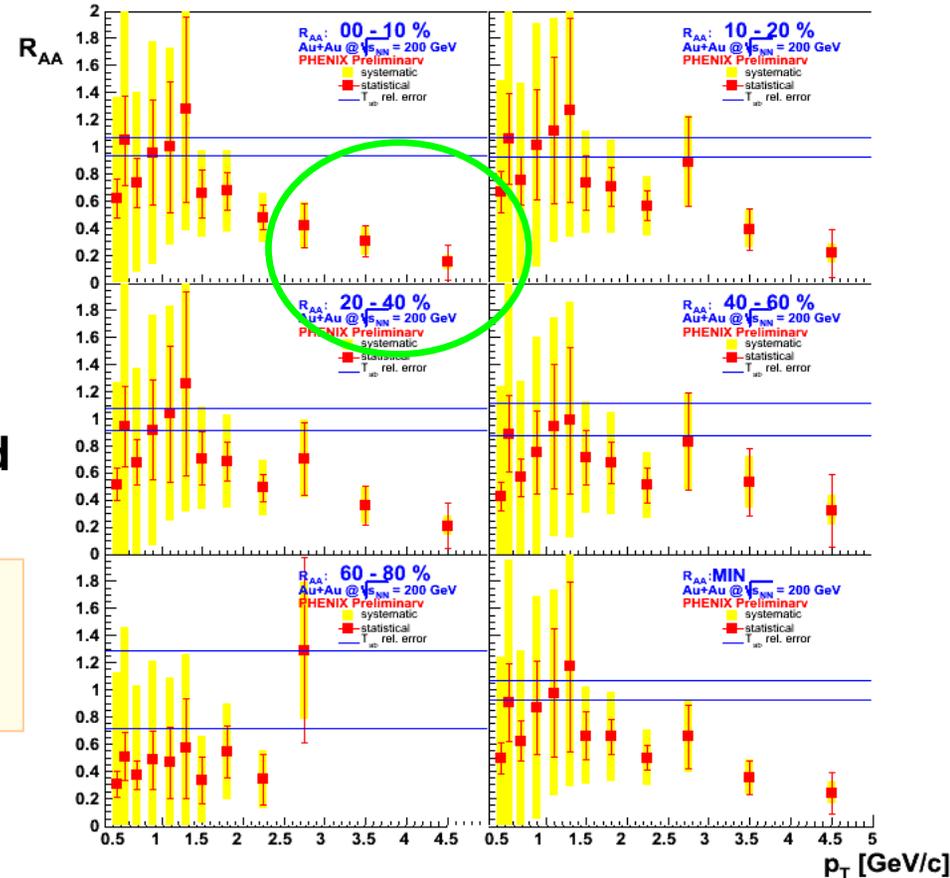
Y. Dokshitzer, D. Kharzeev, Phys. Lett. B519 (2001)

- Of course the "dead cone" will be important **if** the medium induced radiation is still dominated by forward emission

Key point: It is difficult to suppress what is not there in the first place

Not the whole story! (In preparation)
Stay tuned!

Preliminary PHENIX non-photonic electrons



- Quenching of **heavy q** ~ **light q**

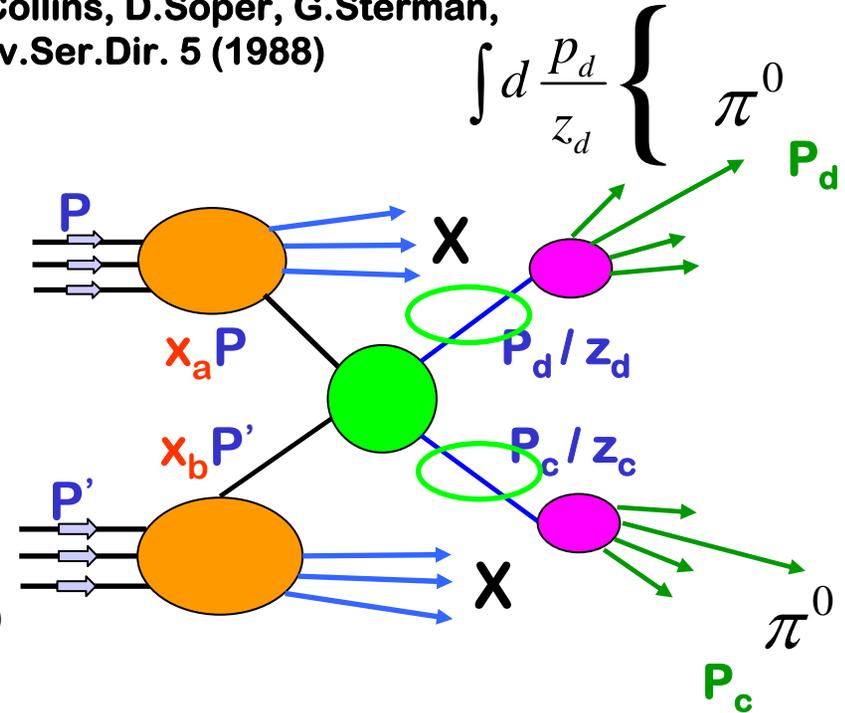
- **Reliable** formalism with **predictive power**

J. Collins, D. Soper, G. Sterman,
Adv. Ser. Dir. 5 (1988)

QCD factorization

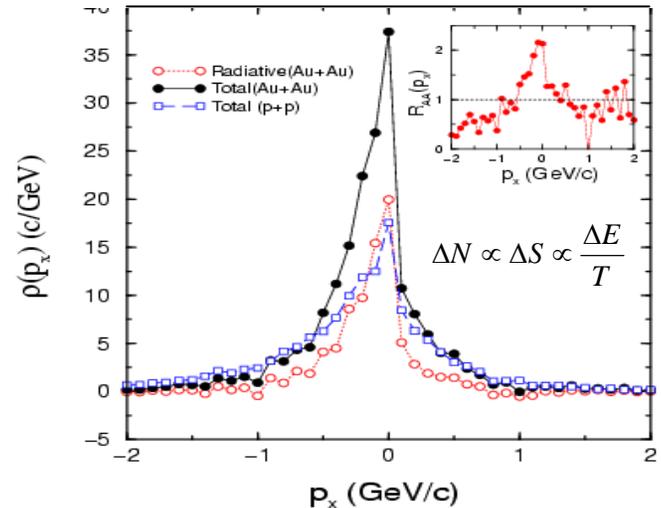
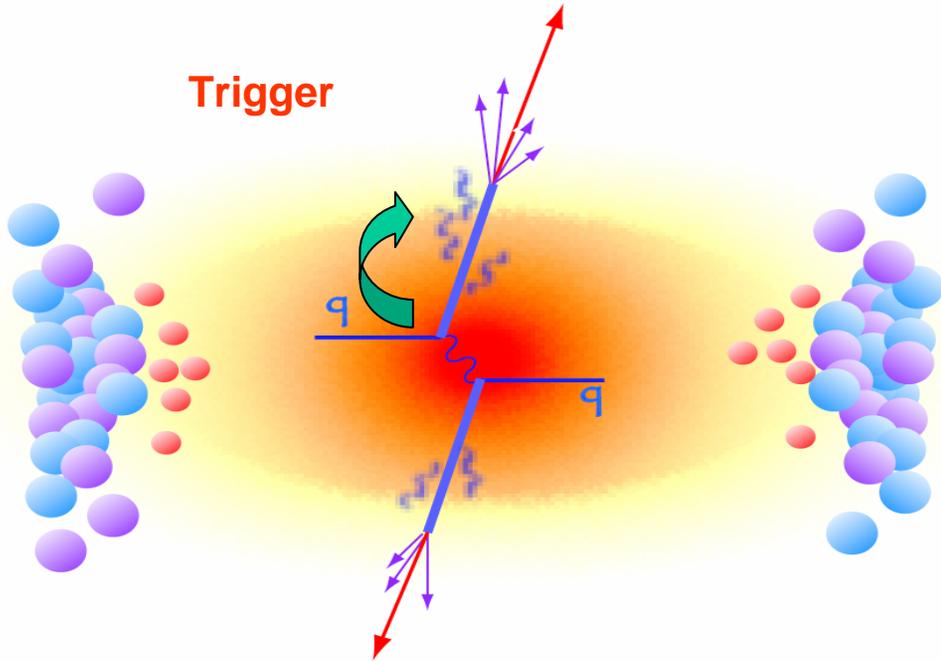
- To LO (2 to 2 scattering) - single and double inclusive hadron production

Can also incorporate **Cronin effect**: $\int d^2k_T f_{med}(k_T)$



$$\frac{d\sigma_{NN}^{h_1}}{dy_1 d^2 p_{T1}} = \sum_{abcd} \int_{x_a \min}^1 dx_a \int_{x_b \min}^1 dx_b \phi(x_a) \phi(x_b) \frac{\alpha_s^2}{(x_a x_b S)^2} \left| \bar{M}^2_{ab \rightarrow cd} \right| \frac{D_{h_1/c}(z_1)}{z_1}$$

$$\frac{d\sigma_{NN}^{h_1 h_2}}{dy_1 dy_2 d^2 p_{T1} d^2 p_{T2}} = \frac{\delta(\Delta\varphi - \pi)}{p_{T1} p_{T2}} \sum_{abcd} \int_{z_1 \min}^1 dz_1 \frac{D_{h_1/c}(z_1)}{z_1} D_{h_2/d}(z_2) \frac{\phi(\bar{x}_a) \phi(\bar{x}_b)}{\bar{x}_a \bar{x}_b} \frac{\alpha_s^2}{S^2} \left| \bar{M}^2_{ab \rightarrow cd} \right|$$



S.Pal, S.Pratt, Phys.Lett.B574 (2003)

- In the context of a **transport model**

But the formation length is $\sim L/2$. May fragment outside the medium

$$D_{h_1/d}(z_2)\delta(\Delta\varphi - \pi) \rightarrow \frac{1}{1-\epsilon} D_{h_1/d}\left(\frac{z_2}{1-\epsilon}\right) f_{med}(\Delta\varphi) \quad \text{Quenched parent parton}$$

$$+ \frac{p_{T_1}}{z_1} \int_0^1 \frac{dz_g}{z_g} D_{h_1/d}(z_g) \int_{-\pi/2}^{\pi/2} d\phi \frac{dN^g(\phi)}{d\omega d\phi} f_{vac}(\Delta\varphi - \phi)$$

Feedback gluons (not DGLAP)

- Use **energy conservation** to verify the fragmentation sum rule

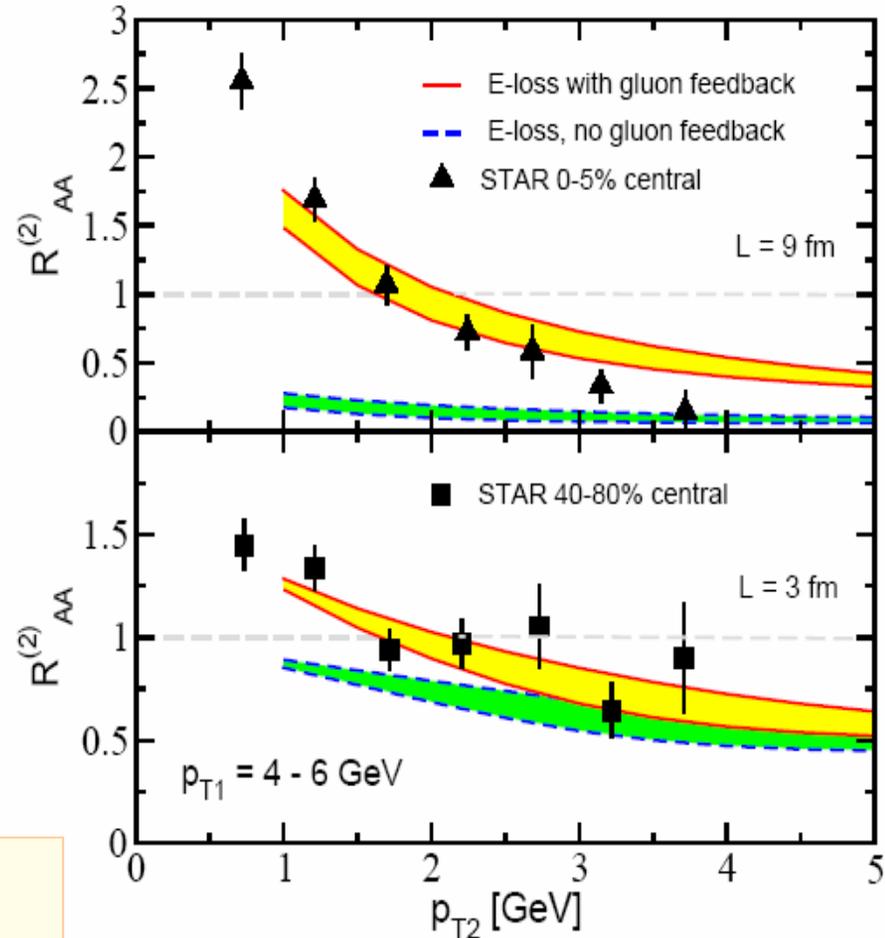
Define a measure for nuclear modifications to di-hadron correlations:

$$R_{AA}^{(2)} = \frac{d\sigma_{AA}^{h_1 h_2} / dy_1 dy_2 dp_{T1} dp_{T2}}{\langle N_{bin} \rangle d\sigma_{pp}^{h_1 h_2} / dy_1 dy_2 dp_{T1} dp_{T2}}$$

P_{T1} trigger:

- Fix the energy
- Ensure high Q^2 ,
- Minimize the effect on the near side
- Maximize the effect on the away side

- The redistribution of the energy is a parameter free prediction
- For large energy loss - the **radiative** gluons dominate to unexpectedly high $p_{T2} \sim 10 \text{ GeV}$



I.V., hep-ph/0501255

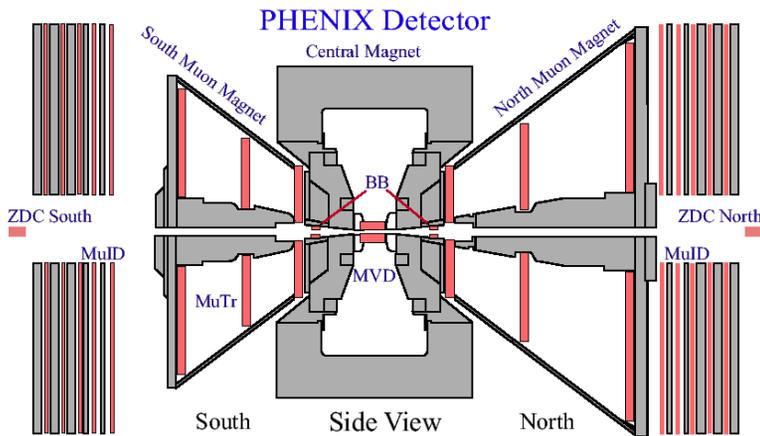
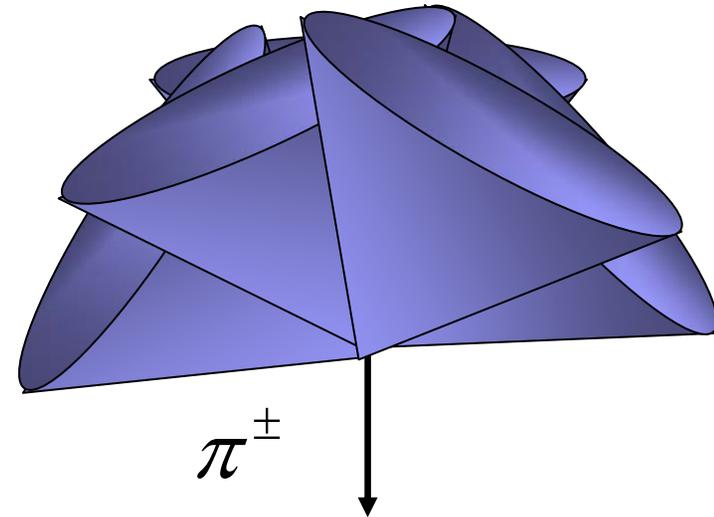
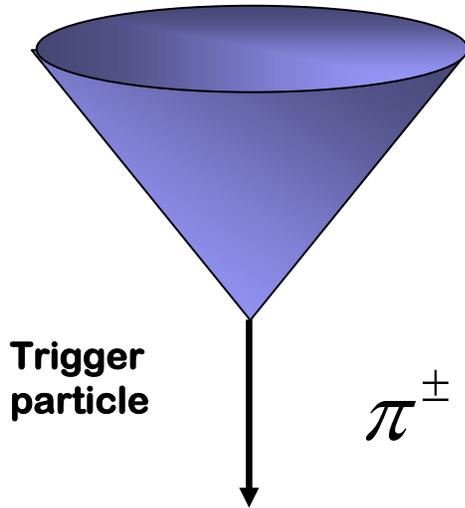
Data is from:

J.Adams *et al.*, nucl-ex/0501016

Superposition of Jet Cones



Some mechanism of jet cone production



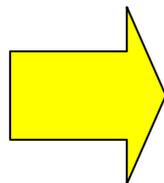
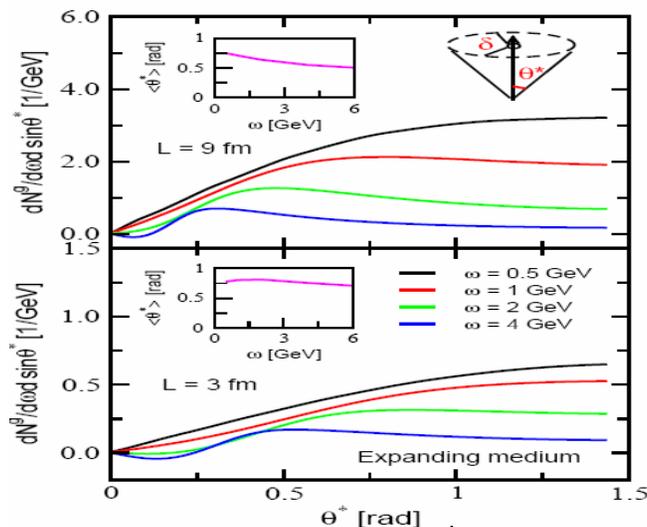
$\Delta\eta = \pm 0.35$

Experiments measure in the plane ϕ
(to make the life of theorists difficult)

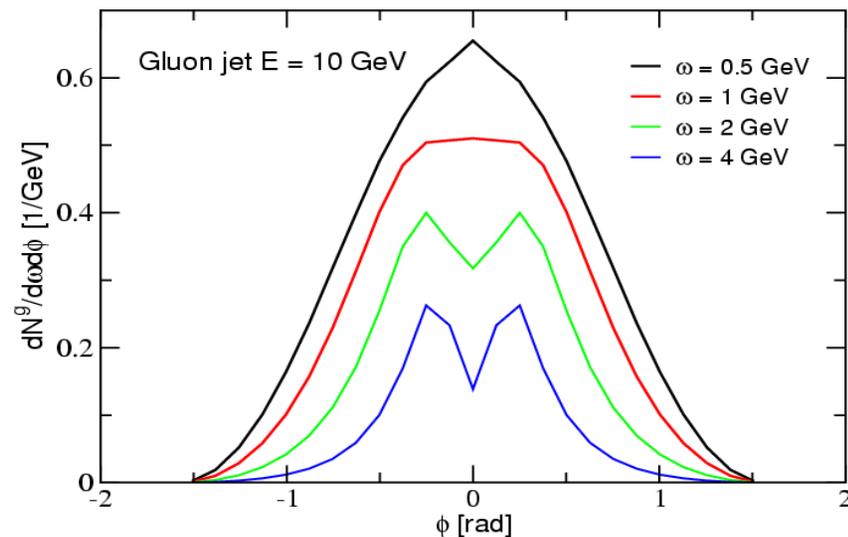
- Surprisingly flat dijets in a wide rapidity range $\Delta y \approx 2 - 3$
- One has to filter through the di-jet rapidity distribution

Projected Medium-Induced Radiation

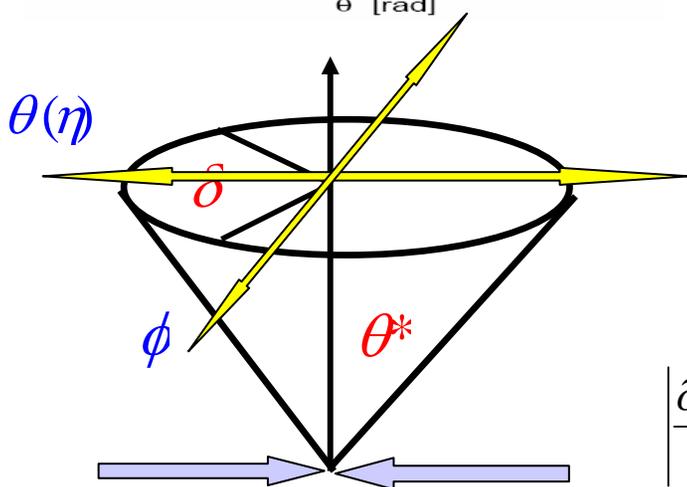
From this



to that



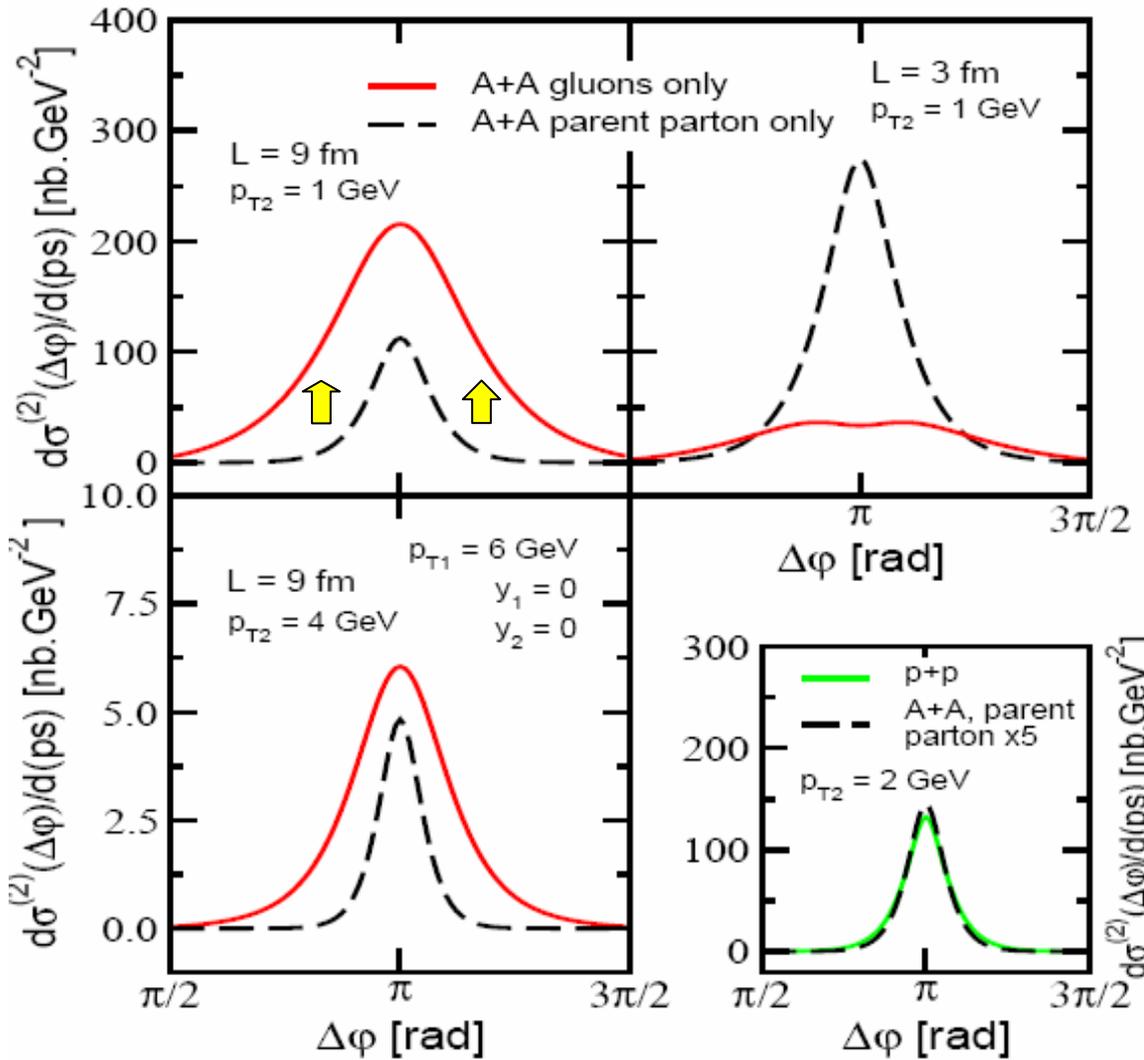
The double hump structure is gone



$$y \approx \eta = -\ln \text{tg}(\theta/2)$$

$$\left| \begin{array}{l} \text{tg}^2 \theta^* = \text{ctg}^2 \theta + \text{tg}^2 \phi \\ \text{tg} \delta = -\frac{\text{ctg} \theta}{\text{tg} \phi} \end{array} \right.$$

$$\left| \frac{\partial(\sin \theta^*, \delta)}{\partial(\theta, \phi)} \right| = \frac{1}{\sin^2 \theta \cos^2 \phi} \frac{(\text{ctg}^2 \theta + \text{tg}^2 \phi)^{-1/2}}{(1 + \text{ctg}^2 \theta + \text{tg}^2 \phi)^{3/2}}$$



I.V., hep-ph/0501255

$$\sigma_{Far}(AA) > \sigma_{Far}(pp)$$

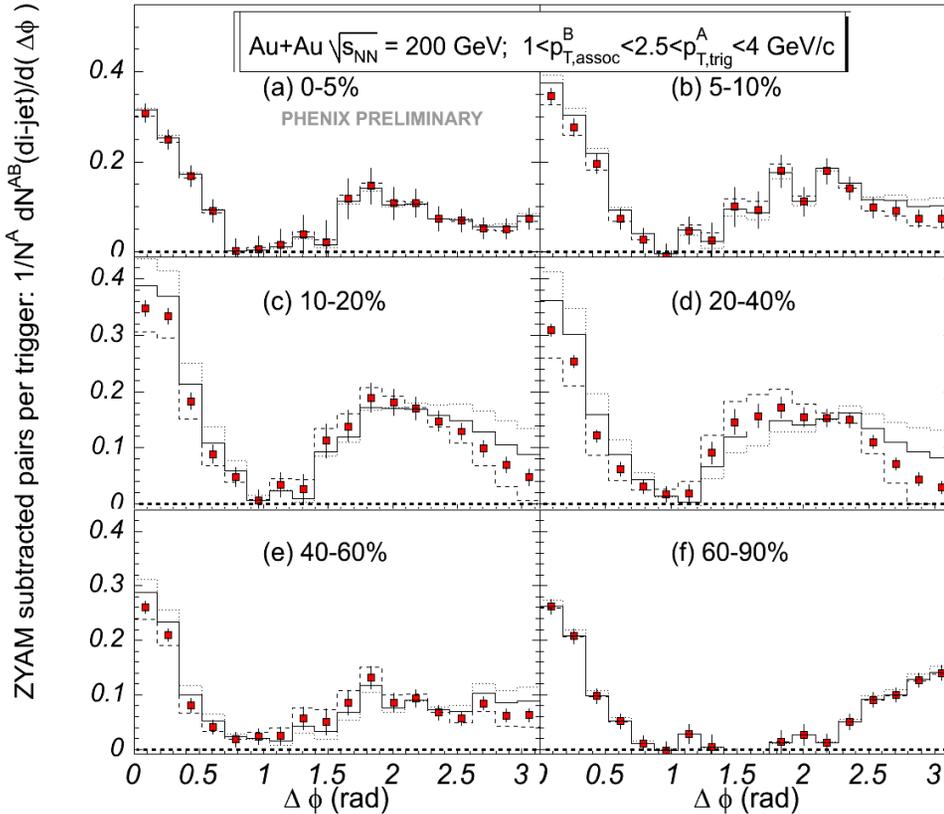
- The width $|\Delta\phi - \pi|$ of the large-angle correlations is dominated by medium induced gluon radiation
- Reassessment of the origin of small and moderate p_T away triggered hadrons

The quenched parton is not wider

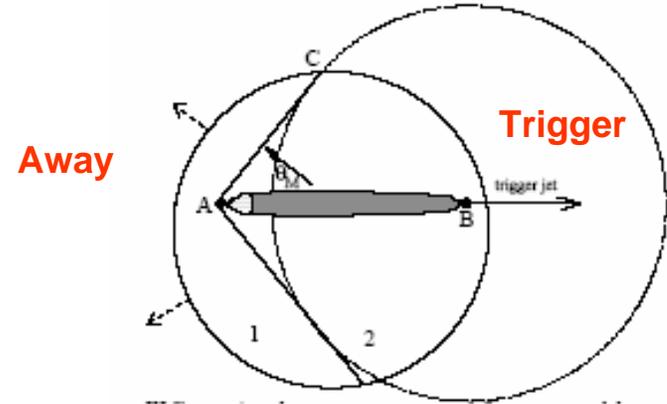
Because:

$$\sigma_{Far} \approx \frac{\sqrt{\langle k_T^2 \rangle_{vac}}}{p_{Tc}} \rightarrow \frac{\sqrt{\langle k_T^2 \rangle_{tot}}}{[p_{Tc}/(1-\epsilon)]}$$

PHENIX preliminary:



• What's going on with this hole in the middle?



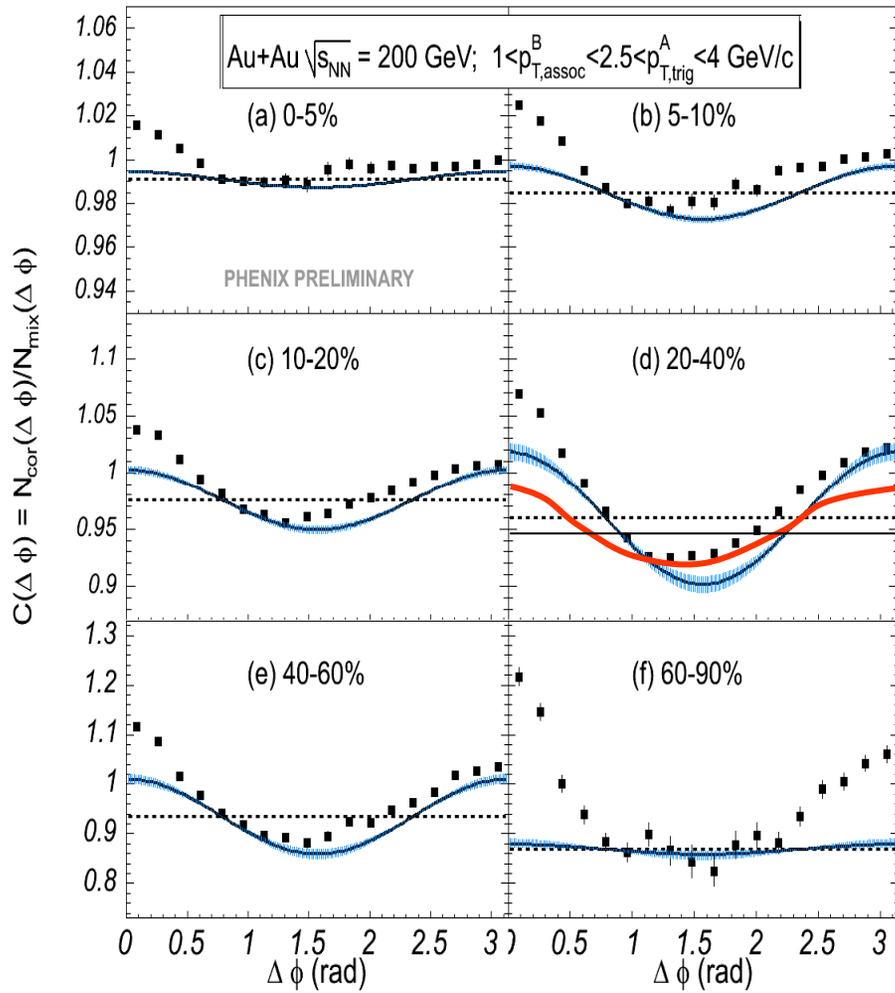
Solana, Shuryak, Teaney, hep-ph/0411315

Did not do the averaging over the away-side di-jet distribution

• Figure taken from B. Jacak, ICPAQGP 2005

$$\sigma_{Far}(AA) > \sigma_{Far}(pp)$$

• Confirmation of a very broad distributions of away-side triggered hadrons



Two source model gives :

$$C(\Delta\phi) = a_0 \left[\begin{matrix} \textit{Flow} & \textit{Jet} \\ H(\Delta\phi) & + J(\Delta\phi) \end{matrix} \right]$$

- Assumption, which I think is incorrect
- There is no constraint on how big of a harmonic is subtracted in this method

The v_2 used by PHENIX seems to differ from STAR

There may be an uncertainty associated with the amplitude of flow and jets ZYAM

- Figure taken from N.N.Ajitanand ICPAQGP 2005

• PHENIX says: Both (di-) jet correlations and flow are evident

The Rapidity Story is Known

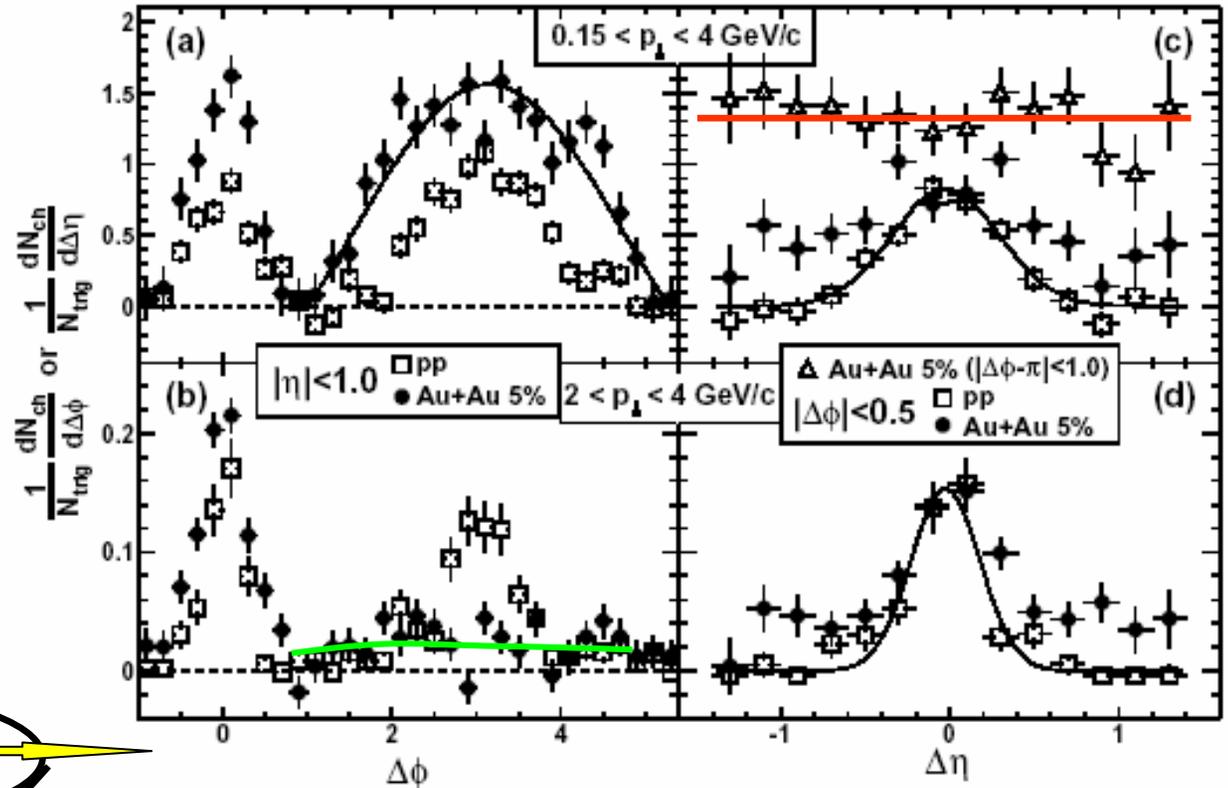
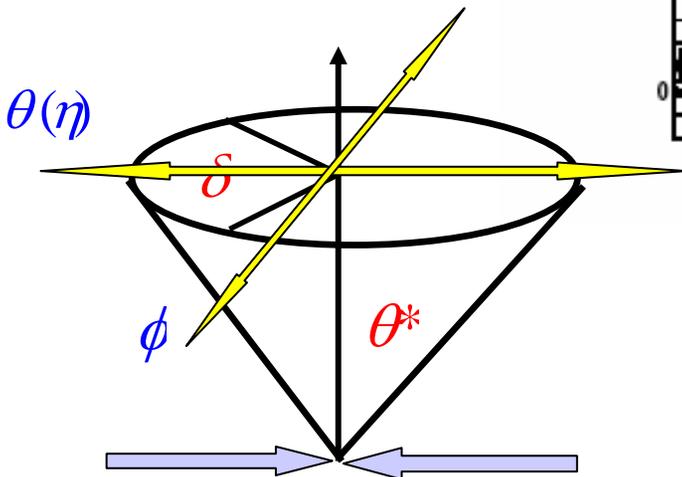


Rapidity coverage $\eta = \pm 1.4$

$$y \approx \eta = -\ln \operatorname{tg}(\theta/2)$$

$$\theta \in (28^\circ, 152^\circ)$$

No (curious) structure in rapidity or azimuth



J.Adams *et al.*, nucl-ex/0501016, submitted to Phys.Rev.Lett.

- Slicing in ϕ and slicing in $\theta(\eta)$ is the same

- ▶ New jet quenching studies demonstrated the **large angle hadron production** from and the possible **disappearance of the dead cone effect**. Possible evidence from single electrons (not the full story!)
- ▶ A **parameter free description** of the **redistribution** of the lost energy for tagged jets can be obtained in the perturbative approach. The medium parameters only specify $-dE$
- ▶ **Significant broadening** of the away side correlations confirmed by PHENIX. The extra structure is possibly from over subtraction of v_2 . Checked against STAR results and rapidity