

# Charm degrees of freedom above deconfinement

Sayantana Sharma



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BNL-Bielefeld collaboration, Physics Letters B 737, 210, (2014),  
S. Mukherjee, P. Petreczky, SS, Phys. Rev. D 93, 014502 (2016).

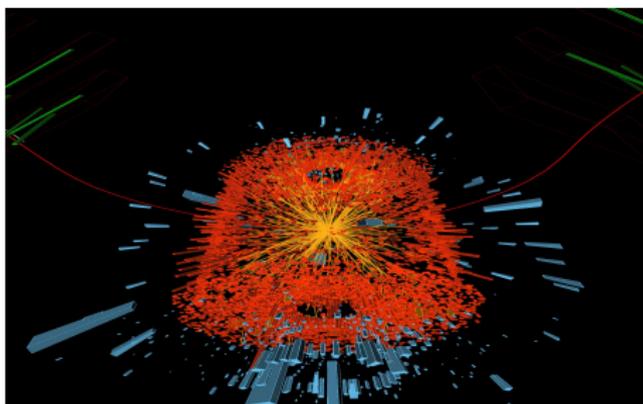
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- 1 The story about charm so far
- 2 Open charm mesons at freezeout
- 3 Relevance of our studies

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# Heavy quark from experiments

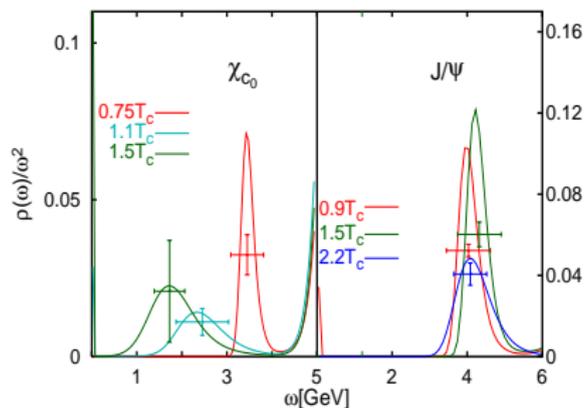


[<http://www.cern.ch/news>]

- The suppression of  $\Upsilon$  states measured  $\rightarrow$  signal of a thermalized QCD medium? [CMS collaboration, QM14]
- Loosely bound excited states melt earlier.
- What happens to heavy-light hadrons?
- $R_{AA}$  and  $v_2$  puzzle for  $D$  mesons exist [ALICE collaboration, 15]. Require more input from first principles for heavy quark phenomenology.

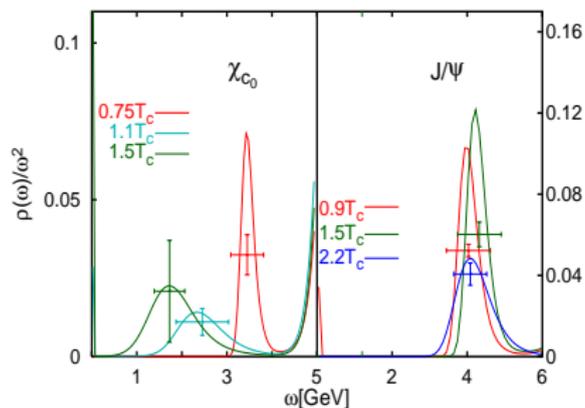
# What is known about the heavy hadrons: theory

- The  $c\bar{c}$  mesons like  $J/\psi$ ,  $\eta_c$  are also created early.
- If **thermalized QGP** is formed the number of  $J/\psi$  produced is much reduced due to screening of inter quark potential [Matsui & Satz, 86]
- First principles study of the spectral functions [Asakawa & Hatsuda, 03, S. Datta et. al., 04, Ding et. al, 12, Swansea collaboration, 07,10, H. Ohno, 13] and variational method [H. Ohno et. al, 11] shows melting of  $J/\psi$  at  $T > 1.5 T_c$ .



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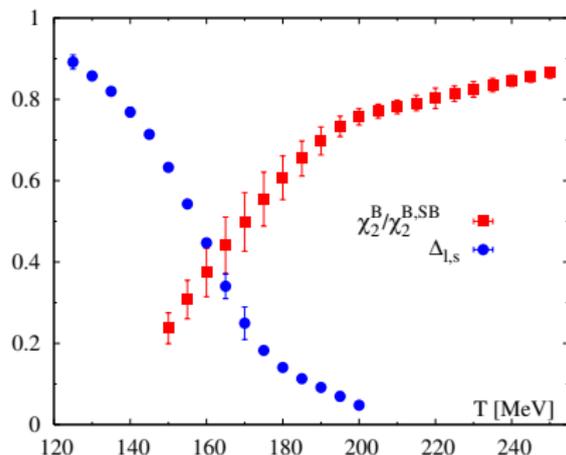
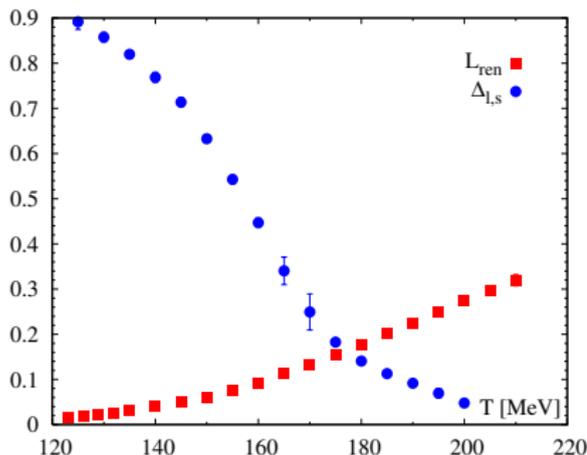
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- Bottomonium states show sequential melting above  $T_c$ .  
[H. Ohno, et. al. 13,14, Swansea 14]



# (De)Confinement

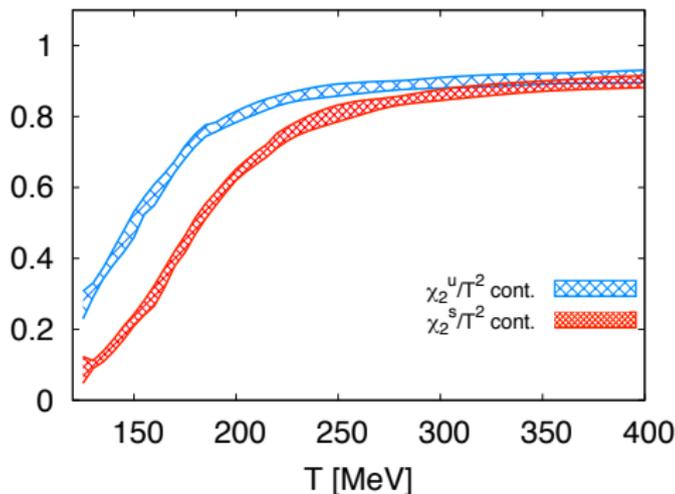
- Deconfinement : Releasing of colored degrees of freedom
- Pure gauge theory: phase transition due to deconfinement  
Polyakov loop  $L_{ren}$
- In QCD with physical masses: no exact order parameter
- $\chi_{SB}$  and deconfinement for light quarks occur simultaneously
- When do the heavier strange and charm quarks deconfine?

Bazavov & Petreczky, 13



# Deconfinement of strangeness and charm

- Lattice QCD is the most effective non-perturbative tool that can provide answer to such questions
- Looking at the fluctuations of  $s$  and  $u$  quark numbers in the thermal medium gives an apparent impression of different  $T_d$  [C. Ratti et. al, 12, Bellweid, 12]
- Important to look at good “order parameters” that clearly separates the deconfined phase.



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# Motivation for HRG

- At freezeout no more inelastic collisions  $\Rightarrow$  the ensemble can be described by a gas of all measured hadrons and possible resonances (HRG) [Dashen, Ma and Bernstein, 69,71]

$$\ln \mathcal{Z} = \pm \sum_i g_i \frac{V}{2\pi^2} \int_0^\infty dp p^2 \ln \left( 1 \pm e^{\beta(\epsilon_i - \mu_i)} \right),$$

$$\epsilon_i = \sqrt{p^2 + m_i^2} \simeq m_i \quad \& \quad \mu_i = \mu_B B_i + \mu_S S_i + \mu_C C_i + \mu_I I_i.$$

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- HRG a good approximation if resonances very near to two particle threshold.

[Prakash & Venugopalan, 92]

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- Summary: any residual hadron interactions at the freezeout is taken into account by considering all known resonances [ Braun-Munzinger, Cleymans, Oeschler, Redlich, 02].

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- Related work by Fermi [50]  $\Rightarrow$  for strong interaction particle production determined by statistical weights indep. of the details on hadron interactions.
- **Expected to work in the charm sector!**

# Why charm?

- The heavy charm quarks produced before QGP is formed.
- Maximum  $T \sim 500$  MeV at the LHC
- $m_c > T$ : charm is not thermally generated in the hot medium
- Have a near thermal distribution of momenta [S.Gupta & R. Sharma, 14]
- At LHC energies charm abundances are quite high  $\rightarrow$  statistical hadronization similar to the light quarks? [Braun-Munzinger, Redlich, Stachel, 06]
- Hadronization would imply existence of deconfined medium

# Our Setup

- We want to understand where heavy quarks deconfine from properties of **heavy-light hadrons**.  $c\bar{c}$  states not considered.
- The analysis of bound states through the study of spectral functions difficult on the lattice.
- If the charm hadron ensemble near the freezeout well described as a **hadron resonance gas** characterized by  $T, \mu_B, \mu_C$ ,

$$P(\hat{\mu}_C, \hat{\mu}_B) = P_M \cosh(\hat{\mu}_C) + P_{B,C=1} \cosh(\hat{\mu}_B + \hat{\mu}_C) \\ + P_{B,C=2} \cosh(\hat{\mu}_B + 2\hat{\mu}_C) + P_{B,C=3} \cosh(\hat{\mu}_B + 3\hat{\mu}_C) .$$

- The ground state  $m_{C=2} - m_{C=1} = 1$  GeV : effect on thermodynamics of  $C = 2, 3$  baryons is negligible.

# Our Setup

- It is comparatively easy to calculate the fluctuations + correlations of  $B, C$

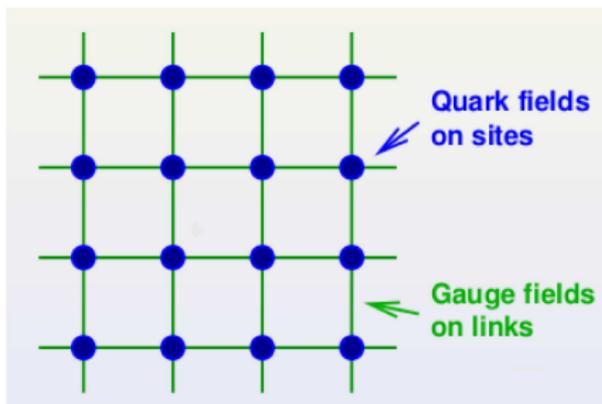
$$\chi_{ij}^{BC} = \frac{\partial^{i+j}}{\partial \hat{\mu}_i^B \partial \hat{\mu}_j^C} P_{tot} / T^4$$

- The partial pressures can be constructed out of  $\chi_2^C, \chi_{11}^{BC}$  and  $\chi_4^C, \chi_{31}^{BC}, \chi_{22}^{BC}, \chi_{13}^{BC}$ . [Bielefeld-BNL collaboration, 13]

- Setting  $\mu = 0$  one can rewrite the partial pressures in terms of these quantities like

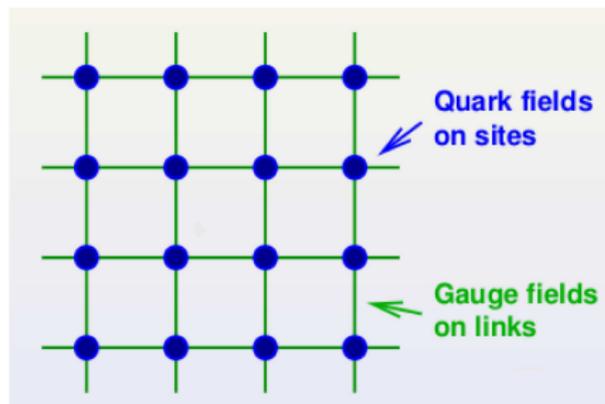
$$P_M = \chi_2^C - \chi_{22}^{BC}, P_{B,C=1} \sim \chi_{mn}^{BC}, m+n=4$$

# A glimpse of what goes into computations



- Two different lattice  $24^3 \times 6$ ,  $32^3 \times 8$  to check the cut-off effects
- Large enough for thermodynamic limit
- The light and strange quarks are dynamical  $\rightarrow$  nearly-physical
- Charm quarks are like external probes  $\rightarrow$  quenched
- $m_c$  determined by setting  $1/4 (3m_{J/\psi} + m_{\eta_c})$  to its physical value

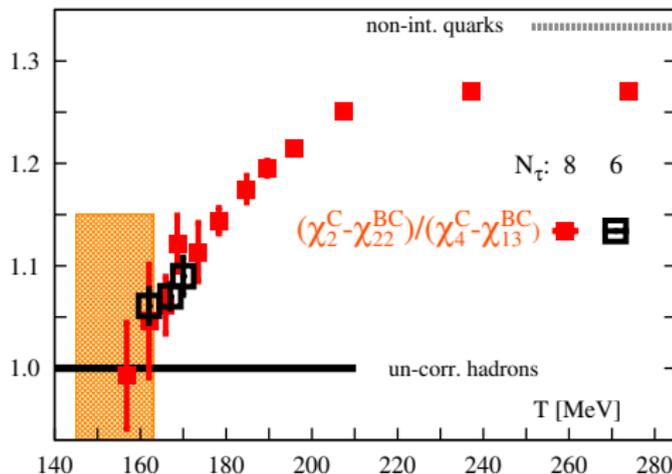
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- $m_c$  determined by setting  $1/4 (3m_{J/\psi} + m_{\eta_c})$  to its physical value
- On the lattice measuring susceptibilities is complimentary to the spectral function method.

# Our approach for the charm mesons

- We consider two equivalent definitions of  $P_M = \chi_2^C - \chi_{22}^{BC} = \chi_4^C - \chi_{13}^{BC}$
- Ratio is like an **order parameter**
- Insensitive to lattice cut-off, mass effects
- Diagonal fluctuations dominated by mesons  $\rightarrow$  **not a good observable.**



- Open charm mesons melt at  $T_c$  independent of the details of the hadron spectrum [ Bielefeld-BNL collaboration, PLB, 14]

# A first glimpse at the charm baryons

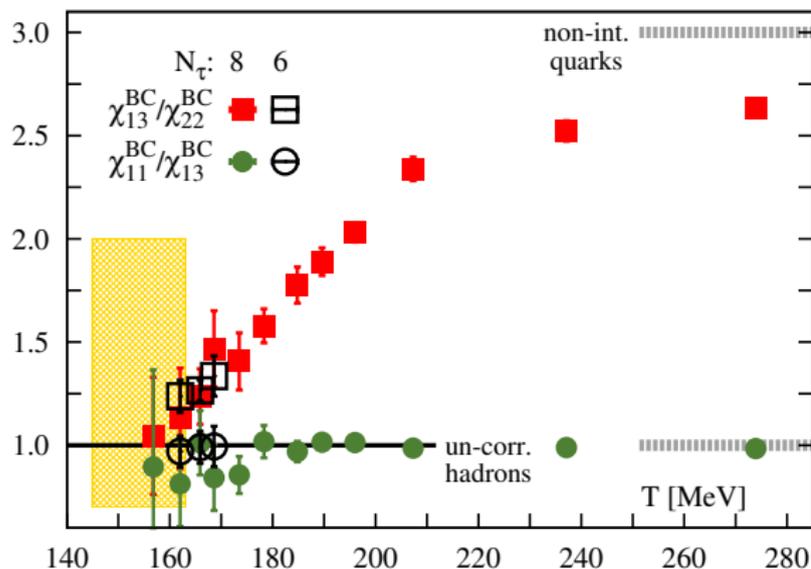
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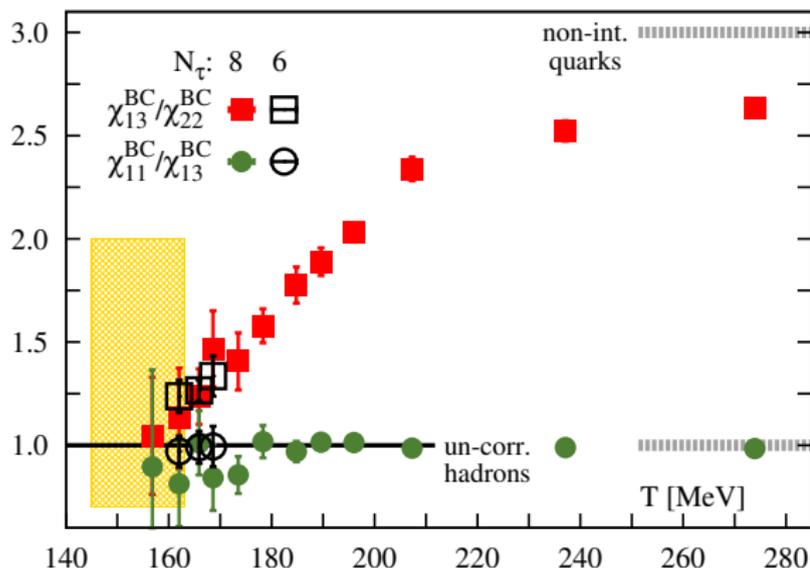
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- These melt near  $T_c$  too!

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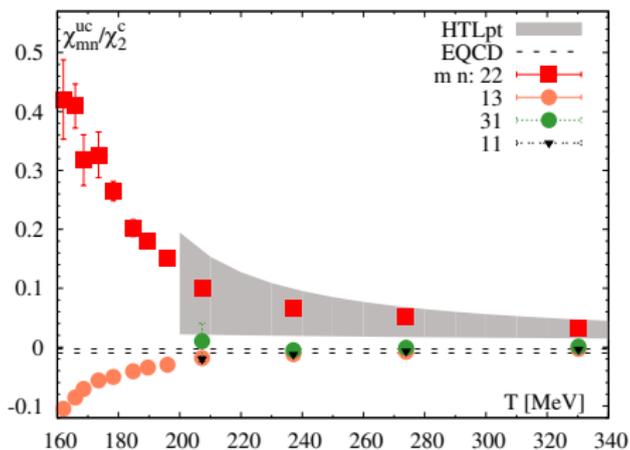
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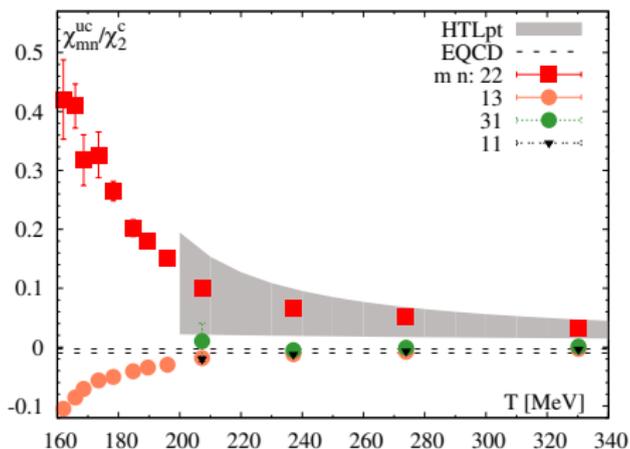
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# What does it imply for medium properties



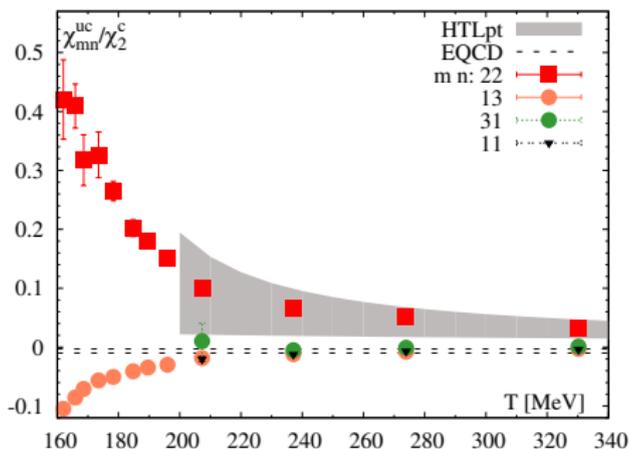
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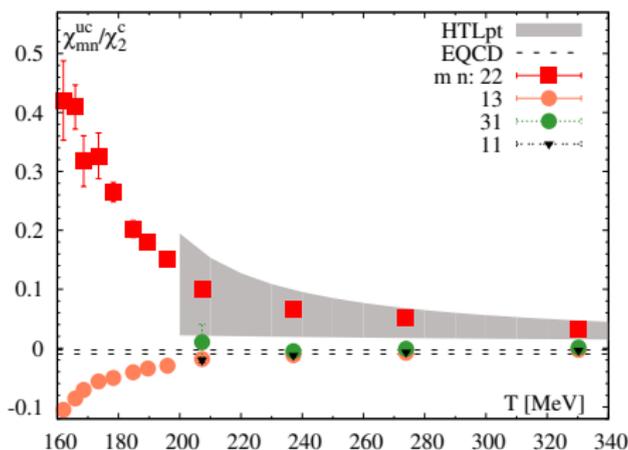
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- Hadrons melt but may survive as broad excitations till  $1.2T_c$
- Pressure for broad “resonances” considerably lower than sharp width QP [Biro & Jakovac, 14]
- Charm spectral function may have a broad asymmetric peak  $\rightarrow$  not a good quasi-particle below 200 MeV.

# Charm d.o.f at deconfinement

- Considering charm mesons+baryon+quark-like excitations

$$p_C(T, \mu_B, \mu_C) = p_M(T) \cosh\left(\frac{\mu_C}{T}\right) + p_{B,C=1}(T) \cosh\left(\frac{\mu_C + \mu_B}{T}\right) + p_q(T) \cosh\left(\frac{\mu_C + \mu_B/3}{T}\right).$$

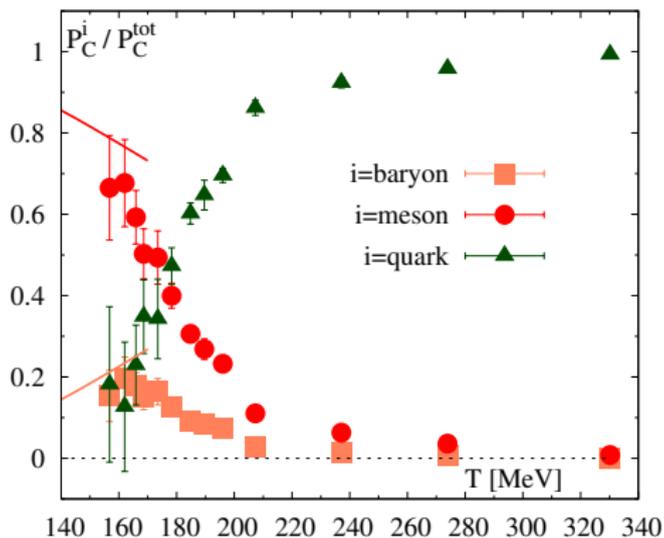
- Considering fluctuations upto 4th order we have 2 trivial constraints

$$\chi_4^C = \chi_2^C, \quad \chi_{11}^{BC} = \chi_{13}^{BC}.$$

- A more non-trivial constraint:

$$c_1 \equiv \chi_{13}^{BC} - 4\chi_{22}^{BC} + 3\chi_{31}^{BC} = 0.$$

# Charm d.o.f at deconfinement



- Meson and baryon like excitations survive upto  $1.2T_c$ .
- Quark-quasiparticles start dominating the pressure beyond  $T \gtrsim 200$  MeV  $\Rightarrow$  hints of strongly coupled QGP [Mukherjee, Petreczky, SS, 15]

# Do diquarks exist beyond $T_c$ ?

- We look specifically at the sector of strange and charm hadrons.
- Upto 4th order derivatives additionally one has 3 more measurements

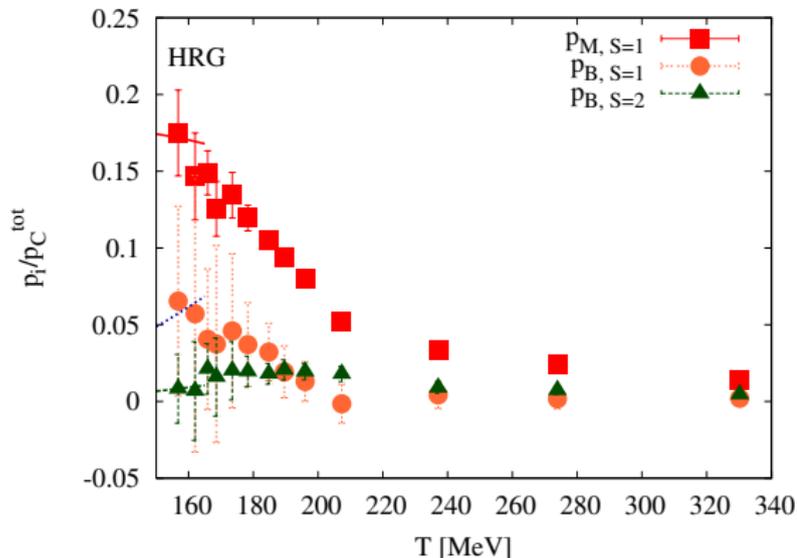
$\chi_{[112]}^{BSC}$

$$p_{SC}(T, \mu_B, \mu_C) = \sum_{j=0}^1 p_{B,S=j}(T) \cosh\left(\frac{\mu_C + \mu_B - j\mu_S}{T}\right) + p_M(T) \cosh\left(\frac{\mu_C + \mu_S}{T}\right) + p_D(T) \cosh\left(\frac{\mu_C + \mu_B/3 - \mu_S}{T}\right).$$

- Di-quarks carry color quantum number...should disappear when quark d.o.f start dominating around 200 MeV.

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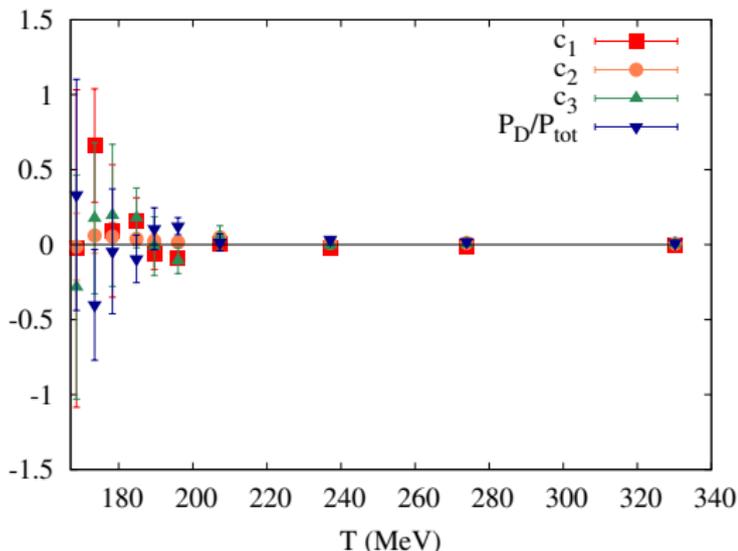
- $\rho_D = \chi_{[211]}^{BSC} - \chi_{[112]}^{BSC} = 0$  for our data.



- Strange baryon-like excitations suppressed than meson-like excitations.
- These studies consistent with screening mass of  $sc$ -mesons [Y. Maizawa et. al., PRD 2015].

# Do diquarks exist beyond $T_c$ ?

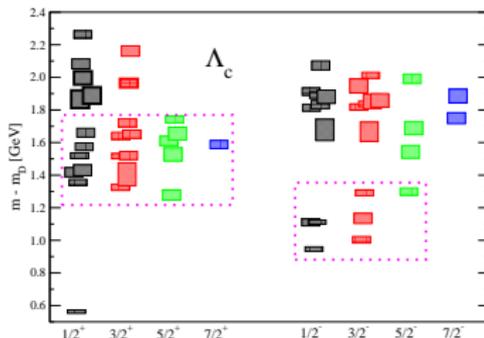
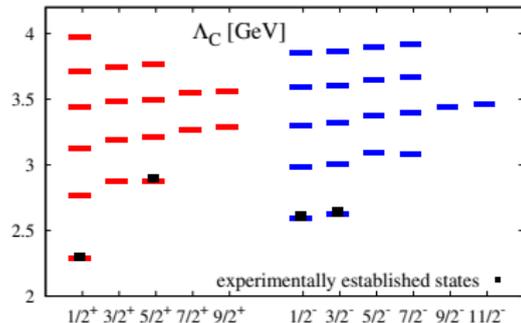
- For these calculations to be valid one should satisfy constraint relations  $\rightarrow$  smoothly connect to HRG and free gas at low and high  $T$ .



- LQCD data agree with the constraints imposed by our proposed model.

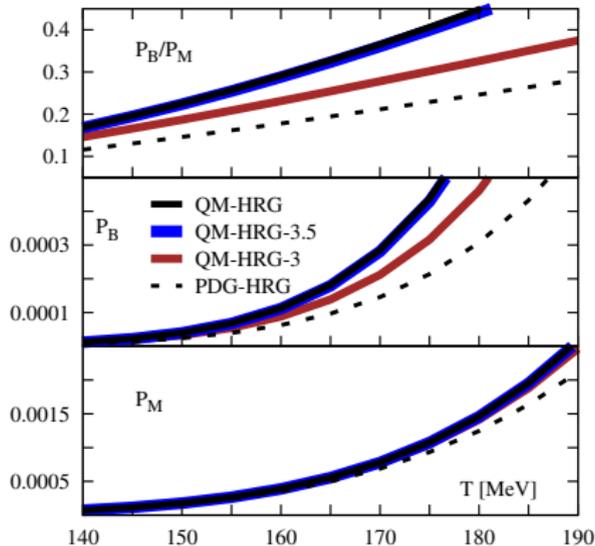
# Charm hadron spectrum...story about missing states

- The charm meson sector is measured experimentally to high precision.
- Many charm baryons states not measured yet predicted from lattice and quark models [ Ebert et. al, 10, Padmanath et. al., 13]
- Even spin-parity of ground state  $\Lambda_c$  not measured!



# Relevance for QCD thermodynamics at freezeout

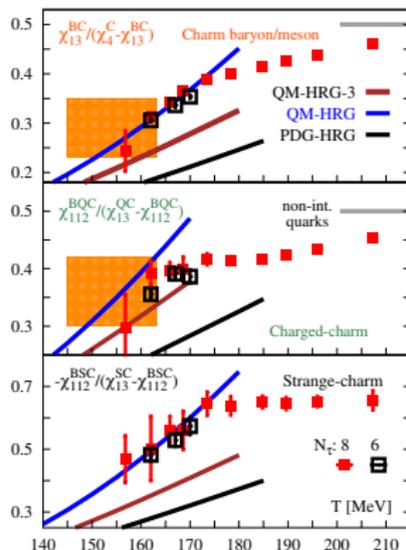
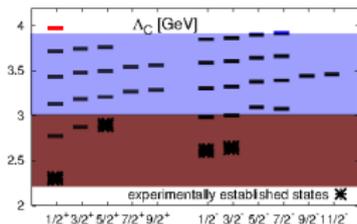
- We construct hadron resonance gas model with **experimentally known states: PDG-HRG**
- Compare with HRG with experimental+additional states: **QM-HRG**
- The partial pressure of mesons are similar
- In the baryon sector the difference starts showing up [ Bielefeld-BNL collaboration, 14]



# Thermodynamic imprints of charm baryons!

- Our methodology allows us to look at charm baryon sector exclusively
- Also look into the specific quantum number channels

- all hadrons:  $\frac{\chi_{13}^{BC}}{\chi_4^C - \chi_{13}^{BC}}$
- S=1,2 hadrons:  $\frac{\chi_{112}^{BSC}}{\chi_{13}^{SC} - \chi_{112}^{BSC}}$
- Q=1,2 hadrons:  $\frac{\chi_{112}^{BQC}}{\chi_{13}^{QC} - \chi_{112}^{BQC}}$



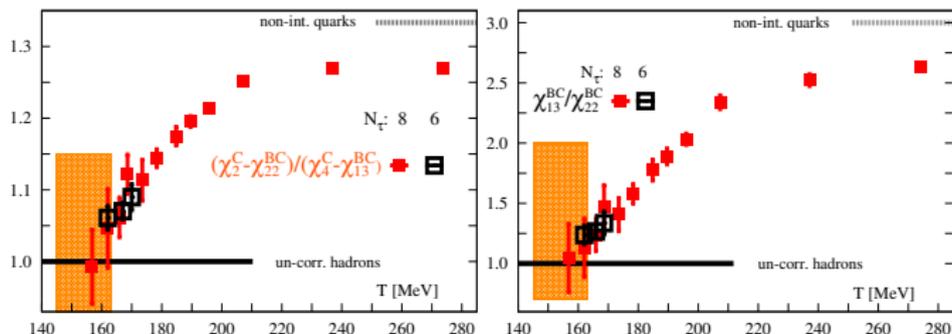
Our data from QCD seems to support the existence of these additional baryon states!

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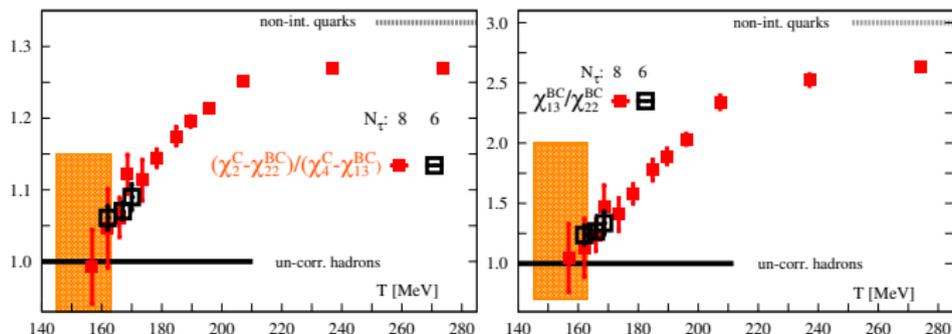
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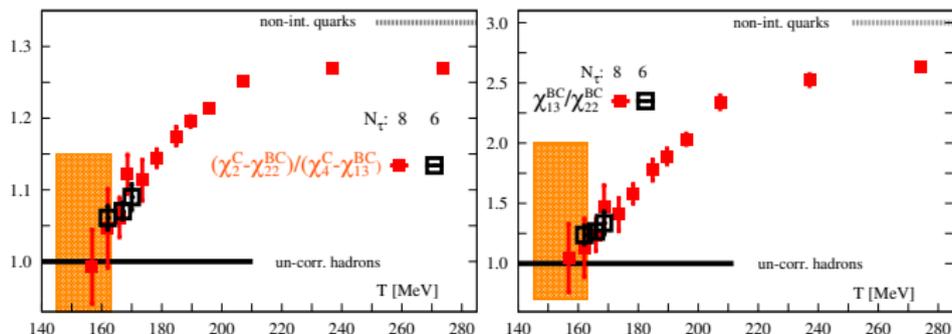
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- The charm mesons and baryons melt near  $T_c \rightarrow$  similar to the light quarks.
- Interpret experiments to theory it is crucial to account for hadron abundances correctly



- Open charm hadrons melt at  $T_c \Rightarrow$  freezeout temperature for  $D_s$  is now well known  
Input for heavy flavour transport models [ A. Beraudo et. al., 12]
- Additional baryons may contribute to hadronic interactions near the freezeout  $\rightarrow$  can it explain the discrepancy for between flow and suppression for  $D$  mesons?
- Charm baryon and meson-like excitations surviving in the medium till  $1.2 T_c$ .
- Our study more in favour for resonant scattering of heavy quarks in the medium [ M. He, R. J. Fries, R. Rapp, 12].