Strong Coupling of the Iron-Quadrupole and Anion-Dipole Polarizations in Ba(Fe$_{1-x}$Co$_x$)$_2$As$_2$

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We use a quantitative convergent beam electron diffraction based method to image the valence electron density distribution in Ba(Fe$_{1-x}$Co$_x$)$_2$As$_2$. We show a remarkable increase in both the charge quadrupole of the Fe cations and the charge dipole of the arsenic anions upon Co doping from $x = 0$ ($T_c = 0$ K) to $x = 0.1$ ($T_c = 22.5$ K). Our data suggest that an unexpected electronic correlation effect, namely strong coupling of Fe orbital fluctuation and anion electronic polarization, is present in iron-based superconductors.

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Iron-pnictide high-temperature superconductivity develops when the “parent” spin-ordered \cite{1} and likely orbital-ordered \cite{2–5} phase is suppressed, typically by introduction of dopant atoms \cite{6}. This phenomenon is similar to cuprate superconductivity but the orbital physics is new. Whether strong orbital fluctuation (electronic oscillation among the Fe 3d orbitals) develops with the doping and creates a novel mechanism for high-$T_c$ superconductivity has been of great interest \cite{7–20}. Strong orbital fluctuation arguably can be induced by phonons (iron \cite{19} or arsenic \cite{20} atomic oscillation) and mediate the $s_{\pm+}$-wave state, in contrast with the “conventional” spin fluctuation-mediated $s_{\pm}$-wave state \cite{21,22}. This problem remains outstanding because direct experimental evidence is lacking. However, orbital fluctuation in principle can be directly measured as a dynamical change in the Fe charge quadrupole \cite{15,19} and its signal can be enhanced by impurities \cite{23}.

Concerning the charge multipole dynamics, there is another unique feature of iron-based superconductors, namely the unusually high electronic polarizability of the anions bonded to the Fe cations \cite{24,25}. Take Ba(Fe$_{1-x}$Co$_x$)$_2$As$_2$ \cite{26} as a prototypical example \cite{6–18}. The electronic polarizability of As$^{3-}$ is 9–12 Å$^3$, which is much larger than 0.5–3.2 Å$^3$ of O$^{2-}$ \cite{24}. In addition, the anions sit considerably out of the Fe plane (the Fe-As-Fe angle is $\sim$71°). Thus the anions’ electron clouds can be readily shifted by the electric field of the Fe charge monopole. Two effects of this Fe monopole-anion dipole interaction have been considered. (i) It weakens the effective electron-electron repulsion on Fe 3d orbitals \cite{24}, driving the system away from the Mott insulator regime \cite{27}. This effect has been taken into account in most theories for iron-based superconductivity, in which the anion degree of freedom is then assumed to be inactive. (ii) However, it was illustrated in a one-orbital model that the electronic oscillation of the anions could dress the electrons moving in the Fe plane to form “electronic polaron”s and mediate them to form Cooper pairs \cite{24,25,28}. The arsenic orbitals were recently reported to be relevant to superconductivity in a spectroscopic ellipsometry study \cite{29}. Yet, there is also a lack of direct experimental evidence of those active roles of anion polarization. In any case, the coupling of the anion-dipole polarization and the Fe-orbital fluctuation (or even the static Fe quadrupole polarization) has not been discussed.

In this Letter, we use a quantitative convergent beam electron diffraction (CBED) based method \cite{30–33} to image the valence electron density distribution in Ba(Fe$_{1-x}$Co$_x$)$_2$As$_2$ single crystals and thus obtain the information about the Co concentration dependence of the Fe charge quadrupole and the anion charge dipole. This method has been successfully applied to describe the valence electron distribution and essential bonding in various systems ranging from copper oxides \cite{30,31} to MgB$_2$ \cite{32} and to CaCu$_3$Ti$_4$O$_{12}$ \cite{33}, etc. Here, we show a remarkable increase in the Fe charge quadrupole in Ba(Fe$_{1-x}$Co$_x$)$_2$As$_2$ upon Co doping from $x = 0$ ($T_c = 0$ K) to $x = 0.1$ ($T_c = 22.5$ K). Unexpectedly, we also observe an obvious boost in the charge dipole of the arsenic anions. Our data reveal a strong coupling between the static Fe quadrupole and anion dipole, and suggest the existence of a novel electronic correlation effect; namely, strong Fe orbital fluctuation can be induced by the optical oscillation of the anions’ electron cloud and vice versa, in iron-based superconductors.

The single crystals used in the present study were prepared by the high-temperature solution method using FeAs as flux \cite{34}. For high-energy electron probes we can easily find regions with perfect crystal integrity that satisfy...
To yield a three-dimensional charge density distribution, CBED and x-ray or DFT data (the DFT data are used here) or density-functional theory (DFT) electronic structure calculations can be obtained from x-ray diffraction [30] (which are dominantly contributed by atomic position and core charge) can be obtained from x-ray diffraction [30].

The Co substitution disorder is treated in the multipole refinement using a posterior virtual crystal approximation (see the Supplemental Material [35]). Since the total density map is dominated by the core electrons, the valence electron distribution is presented by the difference map between the aspherical crystal charge density and superimposed spherical atomic charge density [36].

The resulting room-temperature three-dimensional difference charge density in Ba(Fe1−xCo)x2As2 is shown in Fig. 2(a) for x = 0 and Fig. 2(b) for x = 0.1, the near optimally doped sample. The essential crystal structure of Ba(Fe1−xCo)x2As2 is the FeAs trilayer: the As anions form a two-dimensional network of edge-shared tetrahedra; the center of each tetrahedron is occupied by an Fe cation, forming the conducting Fe square lattice [26]. The valence electron distribution is characterized by a significant increase in both the charge quadrupole around the Fe cations and the charge dipole around the As anions upon Co substitution, echoing the significant increase in Tc, as elaborated below.

The charge quadrupole moments inside a sphere centered at the Fe cation are given by Qij = e ∫ ∆ρ(r)[(r − RFe)(r − RFe) − I(r − RFe) · (r − RFe)]ij dR, where r and RFe are the positions of the electrons and the Fe ion, respectively, e is the electron charge, ∆ρ(r) is the difference electron density at r, and I is the 3×3 identity matrix. Its diagonal [37] quadrupole moments Qxx and Qyy, as a function of the radius of the Fe sphere r, are shown in Fig. 2(f). Upon Co substitution, Qxx decreases and Qzz increases, both by a remarkable amount, indicating a strong interorbital charge transfer of about 0.25 electrons from the in-plane Fe 3d orbitals (x² − y² and xy) to the out-of-plane Fe 3d orbitals (z², xz, and yz). As a result, the electronic structure of Ba(Fe1−xCo)x2As2 would be more three-dimensional upon Co substitution, in agreement with angle-resolved photoemission spectroscopy [38]. This observation points to an unusual character of iron-based superconductors, namely, the rather weak crystal-field splitting of the Fe 3d orbital levels. Usually, the layered structure hosts a strong crystal-field splitting between the in-plane and out-of-plane d orbitals; therefore, charge fluctuation between them is suppressed. However, in iron-based superconductors the largest 3d splitting is about 0.5 eV, which is comparable to the interorbital electron hopping strength [3]. Therefore, the Fe-orbital degree of freedom is nearly unquenched and strong orbital fluctuation involving all the five Fe 3d orbitals can take place.

To facilitate the discussion about the anion polarization, we present the difference charge density maps in the (100) plane in Figs. 2(c) and 2(d) for x = 0 and 0.1, respectively. Apparently, when x is increased from 0 (Tc = 0 K) to 0.1 (Tc = 22.5 K), remarkably more electrons [more reddish area in Fig. 2(d)] appear in between the layers of arsenic anions. The number of valence electrons within the

FIG. 1 (color online). Measurement of the low-order electron structure factors using CBED. (a) Experimental energy-filtered CBED pattern of BaFe2As2 showing the 110 systematical row (reflection of 2 2 0, 1 1 0, 0 0 0, 1 1 0, and 2 2 0) at room temperature. (b) Calculated pattern using the dynamical Bloch wave method. (c) Line scans of the intensity profile from the experimental pattern (open circle) and calculated one (solid line) after the structure factor refinement.
difference charge density on the isosurface are shown in Figs. 2(c) and 2(d) dramatically increases from 0.008 at the interstitial sphere illustrated as the white dotted circles in Fig. 2(a) (black solid and dashed lines). It increases substantially from −0.009 eÅ for $x = 0$ to 0.020 eÅ for $x = 0.1$ when the radius is 1.0 Å (half of the Fe-As distance is 1.2 Å).

The remarkable simultaneous redistribution of the valence electrons around the arsenic anion, its out-of-plane component as a function of the radius of the sphere is shown in Fig. 2(e) (black solid and dashed lines). It increases substantially from −0.009 eÅ for $x = 0$ to 0.020 eÅ for $x = 0.1$ when the radius is 1.0 Å (half of the Fe-As distance is 1.2 Å).

FIG. 2. Valence electron density map in Ba(Fe$_{1-x}$Co$_x$)$_2$As$_2$ for (a) $x = 0$ and (b) $x = 0.1$ as well as the two-dimensional map in the (100) plane for (c) $x = 0$ and (d) $x = 0.1$. The isovalue of difference charge density on the isosurface are 0.1 eÅ$^{-3}$ (red) and −0.1 eÅ$^{-3}$ (blue), respectively. The color legend indicates the magnitude of the charge density and the contour plot has an interval of 0.05 eÅ$^{-3}$. The red line denotes the shortest As-As distance between the FeAs layers. (e) The radius dependence of the out-of-plane dipole moment inside the sphere centered at the Fe anion (black solid and dashed lines) and inside the sphere centered at the middle point of the next-nearest Fe-Fe bond illustrated as the white dashed circle in (c) and (d) (red solid and dashed lines). (f) The radius dependence of the quadrupole moments inside the sphere centered at the Fe anion.

interstitial sphere illustrated as the white dotted circles in Figs. 2(c) and 2(d)] dramatically increases from 0.008 at $x = 0$ to 0.114 at $x = 0.1$ when the diameter is half of the interlayer As-As distance, while the As-As overlap remains weak. This means that Co substitution induces a substantial shift of the electron cloud of the arsenic anion. This shift, i.e., the anion polarization, can be quantified by the charge dipole inside the sphere centered at the arsenic anion.

$\bar{P} = e \int \Delta \rho(\vec{r}) (\vec{r} - \vec{R}_A) d\vec{r} = (0, 0, P)$, where $\vec{R}_A$ is the position of the arsenic anion. Its out-of-plane component as a function of the radius of the sphere is shown in Fig. 2(e) (black solid and dashed lines). It increases substantially from −0.009 eÅ for $x = 0$ to 0.020 eÅ for $x = 0.1$ when the radius is 1.0 Å (half of the Fe-As distance is 1.2 Å).

The considerable accumulation of valence electrons in between the FeAs layers at optimal doping [Fig. 2(d)] may lead to the impression that the interlayer As-As bonding [red line in Fig. 2(d)] appears. This is reminiscent of the pressure experiment on CaFe$_2$As$_2$, where the interlayer As-As distance collapses from 3.78 to 3.0 Å, accompanied by the vanishing of the Fe spin moment and the emerging of superconductivity [39]. By contrast, the interlayer As-As distance in Ba(Fe$_{1-x}$Co$_x$)$_2$As$_2$ for $x = 0$–0.1 remains nearly unchanged at 3.78 Å (see Ref. [26]), which is too distant for a real bonding to occur. Indeed, we found that the number of electrons is still vanishing at the middle of the As-As “bond” [the red line in Figs. 2(c) and 2(d)], indicative of little overlap of the As-As atoms along the $c$ axis. We thus conclude that the shift of the anion’s electron cloud in Ba(Fe$_{1-x}$Co$_x$)$_2$As$_2$ is caused by the Fe electrical field, not by the As-As bonding. In addition, since the structural change induced with Co doping is rather small, it is ruled out as a driving force for the observed large change in the electron redistribution (see the Supplemental Material [35]).

The strong anion polarization should in turn polarize the Fe-Fe bonds. We notice that the middle points of the nearest-neighbor (NN) and next-nearest-neighbor (NNN) Fe-Fe bonds are distinct in symmetry: the former is an inversion center and the latter is not. Therefore, the NNN Fe-Fe bond should be much more affected by anion polarization than the NN one. We calculated the electric dipole moment $\bar{P}$ within the sphere centered at the middle point of the NNN Fe-Fe bond [the white dashed circles in Figs. 2(c) and 2(d)]; this is the Fe-Fe plane point directly under an As anion. We found that its out-of-plane component changes substantially in a similar manner as the anion polarization, e.g., from −0.016 for $x = 0$ to 0.060 eÅ for $x = 0.1$ when the diameter is half of the NNN Fe-Fe distance, being consistent with dipole-dipole interaction. This effect may be relevant to iron-based superconductivity, since the NNN Fe-Fe superexchange $J_2$ was correlated with $T_c$ [40].

The remarkable simultaneous redistribution of the valence electrons around the As and Fe atoms should be reflected in a large change in phonon modes that involve both Fe and As atoms. Indeed, the infrared-active in-plane $E_g$ mode observed at about 258 cm$^{-1}$ in BaFe$_2$As$_2$ (above the magnetic transition) disappears in optimally Co-doped samples [41-43]. To better understand the nature of the lattice vibrations, $ab$ initio calculations were performed using the direct method for the zone-center phonons (see the Supplemental Material [35]). We found that the atomic character of this particular in-plane mode is almost evenly distributed between the Fe and As atoms (55% Fe, 45%
Co substitution, providing Ba and As remain respectively, a significant change in the Fe plane. For example, the charge nonlinearity of anion polarization is enhanced by intersite charge redistribution among the Fe atoms assuming Co (the nominal count of Fe electrons assuming that one Co atom dopes one electron) is comparable to but changes noticeably more than the benchmark, meaning that the observed change is substantial. Our EELS data thus favor the picture that Co substitution introduces charge carriers.

As). However, this should simply lead to line broadening, not the almost total extinction of this feature. For this reason, the change in the atomic charge distribution and the commensurate increase in the screening from electron polarization may be an explanation.

To understand these surprising observations, we note that the As\(^{3-}\) polarization \(P\) is mainly caused by the asymmetrical positioning of Fe cations around the As\(^{3-}\) anion along the \(z\) axis. Thus, \(P\) can be generally expressed in the polynomials of Fe/Co charge \(n_i\): \(P = \beta_1 \langle n_i \rangle + \beta_2 \langle n_i^2 \rangle + \cdots\). Since \(\langle n_i \rangle\), the average Fe/Co charge monopole, remains unchanged upon Co substitution, providing Ba and As remain 2+ and 3–, respectively, a significant change in \(\langle n_i^2 \rangle\) must be responsible for the observed substantial change in \(P\). This implies a significant change in the degree of electronic correlation, which we found is unsurprisingly beyond the capability of local density approximation of the density functional theory (see the Supplemental Material [35]). Furthermore, the nonlinearity of anion polarization is enhanced by intersite charge fluctuation in the Fe plane. For example, the charge fluctuation between two Fe sites \(i\) and \(j\), say one electron hops from \(j\) to \(i\), satisfies the inequality \((n_i + 1)^2 + (n_j - 1)^2 > n_i^2 + n_j^2\) and changes \(P\) by \(2\beta_2\). The nonlinearity of the anion polarization was found in a recent one-orbital theoretical study [24,25]. We expect that a multiorbital model in which the Fe orbital fluctuation can “resonate” with the anion polarization is necessary to explain the observed extraordinary charge response to the Co doping.

Since \(\langle n_i^2 \rangle\) and intersite charge fluctuation are usually enhanced by charge doping away from the stoichiometric limit \(x = 0\), the above analysis implies that substituting Co for Fe effectively dopes charge carriers into the Fe planes. This Co-doping effect is actually a controversial issue (see the Supplemental Material [35] and Refs. [38], [44–49]). To get more insight, we study the room-temperature Co concentration dependence of Fe \(L_{2,3}\) edges EELS. As shown in Fig. 3, two peak areas marked as Fe \(L_2\) and \(L_3\) appear at about 719.6 and 707 eV, respectively. They originate from 2\(p\)-3\(d\) dipole transitions with the well-separated spin-orbit-splitting 2\(p\) states 2\(p_{1/2}\) (\(L_2\)) and 2\(p_{3/2}\) (\(L_3\)). The spectra, not exhibiting any multiplet peak structures, are similar to those for metallic Fe, but much different from those for the iron oxides known as Mott insulators. Upon Co substitution, the \(L_3/L_2\) ratio drops from 2.55 at \(x = 0\) to 2.43 at \(x = 0.08\). Note that this drop implies a slight decrease of the Fe local moment with Co substitution [50,51], in agreement with x-ray emission spectroscopy [52]. To properly evaluate how significant this change is, we employ the theoretical \(L_3/L_2\) ratio for 3\(d\) transition-metal compounds [50,51] to benchmark it. As shown in the inset of Fig. 3, the measured \(L_3/L_2\) ratio as a function of \(n = 6 + x\) (the nominal count of Fe 3\(d\) electrons assuming that one Co atom dopes one electron) is comparable to but changes noticeably more than the benchmark, meaning that the observed change is substantial. Our EELS data thus favor the picture that Co substitution introduces charge carriers.

Our observations suggest a unified picture for the orbital fluctuation [19,20] and electronic polaron [24,25] physics in Ba(Fe\(_{1-x}\)Co\(_x\))\(_2\)As\(_2\): the Co substitution in Ba(Fe\(_{1-x}\)Co\(_x\))\(_2\)As\(_2\) effectively dopes charge carriers into the system. This enhances intersite charge fluctuation in the Fe plane and \(\langle n_i^2 \rangle\). In accordance, the nonlinear electronic polarization of the As anions is strengthened. In turn, the enhanced anion polarization reduces the electron-electron repulsion in the Fe plane, which enlarges \(\langle n_i^2 \rangle\) and induces charge redistribution among the Fe 3\(d\) orbitals via the As dipole-Fe quadrupole interaction. This positive feedback gives rise to a purely electronic mechanism for boosting Fe-orbital fluctuation. The present results also suggest that the fluctuating Fe quadrupole moment \(Q_{xy-yy}\) is considered important to superconductivity [14–16,19,20] could be induced by in-plane optical oscillation of the anions’ electron cloud [37].

In summary, we have studied the Co concentration dependence of the valence electron distribution in Ba(Fe\(_{1-x}\)Co\(_x\))\(_2\)As\(_2\) using advanced electron probes. Our data provide the first experimental evidence that the charge redistribution among the iron 3\(d\) orbitals is strongly coupled with anion polarization. The mechanism that leads to superconductivity in iron pnictides and chalcogenides will only be fully understood once the charge, spin, orbital, lattice, and anion polarization are all together considered in a consistent theory.

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Note added in proof.—The relevance of the orbital fluctuation between the Fe in-plane and out-of-plane orbitals to superconductivity was shown very recently in a theoretical paper by Onari, Yamakawa, and Kontani [53].

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[26] Constrained by the symmetry of space group 14/mmm used in our multipole refinement, the Fe dipole moment and off-diagonal $Q_{ij}$ are vanishing and $Q_{xx} = Q_{yy}$, while the anion in-plane dipole moments are zero.