

Electric Dipole Moment Goals and “New Physics”

William J. Marciano 12/7/09

**d_p with 10^{-29} e-cm sensitivity!
Why is it important?**

d_p not “just” complementary to d_n

Outstanding Discovery Potential! → Baryogenesis!

(**why do we exist?**)

□ Potential sensitivity an order of magnitude **better** than d_n !

Probes New Physics(NP) at $(1\text{TeV}/\Lambda_{\text{NP}})^2 \tan\phi_{\text{NP}} \leq 10^{-7}$!

or for $\phi_{\text{NP}} \sim O(1) \rightarrow \Lambda_{\text{NP}} \sim \underline{3000\text{TeV}}$! (**well beyond LHC**)

Paves the way for a **new generation** of storage ring experiments $d_p \rightarrow d_D, d(^3\text{He}), d(\text{radioactive nuclei}), d_\mu$

Baryogenesis

- 1928 The Dirac Equation

QM+Special Rel.+Spin+EM Gauge Invariance

$$i(\partial_\mu - ieA_\mu(\mathbf{x}))\gamma^\mu\psi(\mathbf{x}) = m_e\psi(\mathbf{x}) \quad \text{First Order}$$

Mag. Moment: $\boldsymbol{\mu} = g_e Q_e/2m_e \mathbf{s}$ $g_e = 2!$

Great Success-Cornerstone of Modern Physics

Later realized → AntiMatter → positron!

Why is the Universe Matter-Antimatter

Asymmetric?

(1964-CP Violation Discovered-Not Strong Enough)

“New Physics” Source of CP Violation Needed!

Baryogenesis & New Physics CP Violation

Examples of New Physics Models with potentially large CP Violation: Supersymmetry, Multi-Higgs, L-R Models, 4th Generation, Extra Dimensions...

- Generic Manifestation - **Electric Dipole Moments**

What is the “New Physics”?

Look for EDMs!

No Standard Model Background (too small)

1947 Small Anomalous Atomic Fine Structure Effects

We could add extra terms to the Dirac Equation

$$e/4m_e a_e F_{\mu\nu}(x) \sigma^{\mu\nu} \psi(x) + i/2 d_e \gamma_5 F_{\mu\nu}(x) \sigma^{\mu\nu} \psi(x)$$

Anomalous Mag. Mom.

Electric Dipole Mom.

$$g_e = 2(1 + a_e)$$

(Violates P&T(CP))

$$\text{Electron } g_e = 2.002$$

Not Observed

$$\text{Proton } g_p = 5.59$$

$$|d_e| < 2 \times 10^{-27} \text{ e-cm}$$

But It Must Exist!

1948 Schwinger Calculates: $a_e = \alpha/2\pi \approx 0.00116$

Agreed with measurement of Kusch & Foley!

Great Success of QED -Quantum Field Theory

General Formalism (Spin 1/2 Form Factors)

$$\langle f(p') | J_{\mu}^{\text{em}} | f(p) \rangle = \bar{u}_f(p') \Gamma_{\mu} u_f(p)$$

$$\Gamma_{\mu} = F_1(q^2) \gamma_{\mu} + i F_2(q^2) \sigma_{\mu\nu} q^{\nu} - F_3(q^2) \gamma_5 \sigma_{\mu\nu} q^{\nu} \dots$$

$$F_1(0) = Q_f e \quad \text{electric charge}$$

$$F_2(0) = a_f Q_f e / 2m_f \quad \text{anom. mag. mom.}$$

$$F_3(0) = d_f Q_f \quad \text{el. dipole mom.}$$

Effective Dim. 5 Dipole Operators

$$H_{\text{dipole}} = -1/2 [F_2 \bar{f}(x) \sigma_{\mu\nu} f(x) + iF_3 \bar{f}(x) \sigma_{\mu\nu} \gamma_5 f(x)] F^{\mu\nu}(x)$$

F_2 & F_3 Real, Finite & Calculable in Ren. QFT

Complex Formalism: $F_D = F_2 + iF_3$

$$H_{\text{dipole}} = -1/2 [F_D \bar{f}_L \sigma_{\mu\nu} f_R + F_D^* \bar{f}_R \sigma_{\mu\nu} f_L] F^{\mu\nu}$$

$$F_D = |F_D| e^{i\phi} \text{ (Relative to } m_f)$$

$$|F_D| = (F_2^2 + F_3^2)^{1/2}, \quad \tan\phi = F_3/F_2$$

$\tan\phi =$ Relative Degree of CP Violation

$$\text{egs. } |\tan\phi_e|^{\text{SM}} \approx 10^{-24} \quad |\tan\phi_n|^{\text{SM}} \approx 10^{-20}$$

Anomalous Magnetic Dipole Moments

fermion	a_f^{exp}	$ d_f(e/2m_f)^{\text{exp}} $
e	0.00115965218073(28)	$<1 \times 10^{-16}$
μ	0.00116592089(63)	$<3 \times 10^{-6}$
p	1.792158142(28)	$<3 \times 10^{-12}$ (new d_{Hg})
n	-1.9130427(5)	$<1 \times 10^{-13}$

“New Physics” expected to scale as $(m_f/\Lambda)^2$

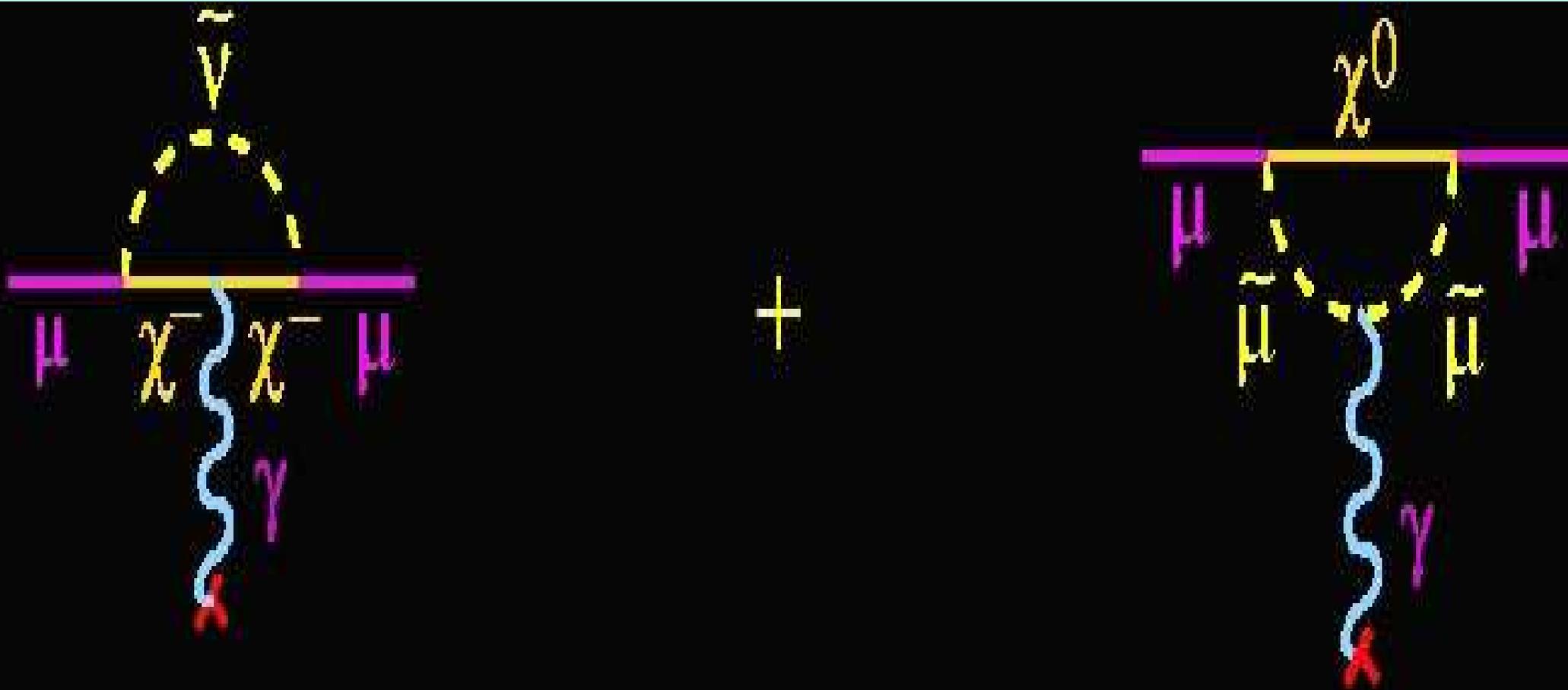
$(m_\mu/m_e)^2 \approx 43000$ Muon only a_f sensitive to high $\Lambda \sim 2\text{TeV}$!

All d_f sensitive to “New Physics” if $\tan\phi^{\text{NP}}$ not too small

Nucleon edms Isovector or isoscalar? Mixed?

Both d_n and d_p need to be measured!

“New Physics” Effects
_SUSY 1 loop a_μ Corrections
(Most Likely Scenario)



- SUSY Loops are like EW, but depend on:
- 2 spin 1/2 χ^- (charginos)
- 4 spin 1/2 χ^0 (neutralinos) including dark matter!
- spin 0 sneutrinos and sleptons with mixing

Enhancement $\tan\beta = \langle\phi_2\rangle/\langle\phi_1\rangle \sim 3-40!$

- **Potentially large CP Violating Phases**

$$\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = 255(63)(49) \times 10^{-11} \quad (3.2\sigma!)$$

- New Physics? Nearly 2x Standard Model EW!

Most Natural Explanation: **SUSY Loops**

Generic 1 loop SUSY Contribution:

$$a_\mu^{\text{SUSY}} = (\text{sgn}\mu) 130 \times 10^{-11} (100 \text{ GeV} / m_{\text{susy}})^2 \tan\beta$$

$\tan\beta \approx 3-40$, $m_{\text{susy}} \approx 100-500 \text{ GeV}$ Natural Explanation

Other Explanations: Hadronic? $\tau \rightarrow \pi^- \pi^0 \nu_\tau$ + isospin data

$$(\Delta a_\mu = \sim 157(63)(52) \times 10^{-11} \quad (2\sigma))$$

Other New Physics $\leq 2 \text{ TeV}$

eg **Extra Dimensions**

If SUSY is responsible for $g_\mu - 2$ Happy Days

Implications: $\text{sgn}\mu > 0$ (dark matter searches easier)

SUSY at LHC very likely

edms, $\mu \rightarrow e\gamma$, ... Good Bets

All chiral changing amplitudes $L \leftrightarrow R$

Enhanced by $\tan\beta \sim 3-40$ factor

But, why haven't we seen edms if susy is correct?

Electric Dipole Moments: $d_e, d_n, d_p, d_\mu, d_{\text{Hg}}$ (new)

Many d_n searches, starting with pioneering exp. Purcell & Ramsey
Recent improvement in Atomic edn exps.

- Griffith, Swallows, Loftus, Romalis, Heckel & Fortson
PRL102, 101601 (2009)
- **Some Implications of $|d_{\text{Hg}}| < 3.1 \times 10^{-29} \text{ e-cm}$**
 - $d_p (\text{e-cm}) < 7.9 \times 10^{-25}$ **Best**
 - $d_n (\text{e-cm}) < 5.8 \times 10^{-26}$ (Direct $d_n < 2.9 \times 10^{-26}$ Best)
 - $d_e (\text{e-cm}) < 3 \times 10^{-27}$ (TI: $d_e < 1.6 \times 10^{-27}$ Best)

Further factor 3-5 Improvement Expected!

Future Expectations

- $d_n \rightarrow 10^{-27} - 10^{-28} \text{e-cm}$ Spallation Neutron Sources
- $d_p \rightarrow 10^{-28} - 10^{-29} \text{e-cm}$ **Storage Ring Proposal (BNL)**
- $d_D \rightarrow 10^{-29} \text{e-cm}$ Storage Ring Proposal
- $d_e \rightarrow 10^{-30} \text{e-cm}$ or better
- $d_\mu \rightarrow 10^{-24} \text{e-cm}$ Storage Ring Proposal

If SUSY is responsible for Δa_μ deviation, then a susy loop induced observable edm may be right around the corner!

Source of CP Violation in Baryogenesis?

If the same “New Physics” ($\Lambda_{\text{NP}}=100\text{-}1000\text{GeV}$) responsible for Δa_μ is also giving edms, we expect (scaling with m_f):

$$|d_\mu^{\text{NP}}| \sim 3 \times 10^{-22} \tan\phi_\mu^{\text{NP}} \text{e-cm}$$

$$|d_e^{\text{NP}}| \sim 2 \times 10^{-24} \tan\phi_e^{\text{NP}} \text{e-cm}$$

$$|d_n^{\text{NP}}| \sim 10^{-22} \tan\phi_n^{\text{NP}} \text{e-cm}$$

$$|d_p^{\text{NP}}| \sim 10^{-22} \tan\phi_p^{\text{NP}} \text{e-cm}$$

Future Experiments will have sensitivity:

$$\phi_\mu^{\text{NP}} \sim 10^{-2} - 10^{-3}$$

$$\phi_e^{\text{NP}} \sim \phi_n^{\text{NP}} \sim \mathbf{10^{-6}}$$

$$\phi_p^{\text{NP}} \sim \mathbf{10^{-7}!}$$

d_p & d_n Relationship

Constituent Quark Model: $d_n = 4/3d_d - 1/3d_u$
 $d_p = 4/3d_u - 1/3d_d$

Roughly $1/4 < |d_p/d_n| < 4$ Similar Magnitudes
Isovector $(d_p - d_n)/2$ or Isoscalar $(d_p + d_n)/2$?
Need both d_n & $d_p \rightarrow d_d$ & d_u (Relationship?)

$\bar{\theta}_{\text{QCD}}$ leading effect isovector (χ PT)
 $d_n = -d_p \sim 3.6 \times 10^{-16} \bar{\theta}_{\text{QCD}} \text{e-cm}$

Currently: $d_n \rightarrow \bar{\theta}_{\text{QCD}} < 10^{-10}$! Future: 10^{-12}

d_p at 10^{-29} e-cm explores $\bar{\theta}_{\text{QCD}} < 10^{-13}$

If a non-zero d_n is discovered, the first thing we want to do is know d_p

Opposite sign? Isovector, $\bar{\theta}_{\text{QCD}}$ Interpretation

Same Sign? $\bar{\theta}_{\text{QCD}}$ Unlikely

More Likely: strangeness, gluonic, susy...

Both d_n & d_p needed!

Physics Reach of $d_p \sim 10^{-29} \text{e-cm}$

$$d_p \sim 0.01 (m_p / \Lambda_{\text{NP}})^2 \tan \phi^{\text{NP}} \text{e} / 2m_p$$
$$\sim \mathbf{10^{-22} (1 \text{TeV} / \Lambda_{\text{NP}})^2 \tan \phi^{\text{NP}} \text{e-cm}}$$

If ϕ^{NP} is of $O(1)$, $\Lambda_{\text{NP}} \sim \underline{3000 \text{TeV}}$ Probed!

If $\Lambda_{\text{NP}} \sim O(1 \text{TeV})$, $\phi_{\text{NP}} \sim 10^{-7}$ Probed!

Unique Capabilities!

Conclusion

1. Measurements of d_n & d_p with similar sensitivity essential to unfold underlying physics. Explain Baryogenesis

2. d_p has potential to do (10x) better than d_n

3. d_p at 10^{-29} e-cm must do exp. if possible.

Explores physics up to scales $O(3000\text{TeV})$

for $\phi^{NP} \sim O(1)$ i.e. beyond LHC or $\phi^{NP} \sim 10^{-7}$

at LHC discovery scales!

4. Sets stage for $d_D = d_n + d_p + d(2 \text{ body}), d(^3\text{He}) \dots$