

# Exotic hadrons production in heavy ion collisions

Che-Ming Ko  
Texas A&M University

- Exotic hadrons studies in HIC
- Thermal vs coalescence production
- Pentaquark  $\Theta^+(udud\bar{s})$
- Diomega  $(\Omega\Omega)_0$
- $D_{sJ}(2317)$ : diquark or tetraquark
- Charmed tetraquark mesons and pentaquark baryons
- Other exotic mesons, baryons and dibaryons

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# Exotic hadron studies in HIC

- $\Theta^+(udud\bar{s})$ 
  - Randrup, PRC 68, 031903 (2003); statistical model
  - Letessier et al., PRC 68, 061901(R) (2003); statistical model
  - Chen et al., PLB 601, 34 (2004); coalescence model
  - Nonaka et al., PRC 69, 031902 (2004); coalescence model, elliptic flow
  - Not observed by STAR and PHENIX
- Diomega ( $\Omega\Omega$ )<sub>0</sub>
  - Zhang et al., PRC 61, 065204 (2000); based on chiral quark model
  - Pal et al., PLB 624, 210 (05); hadronic transport model
- $D_{sJ}$ : ( $c\bar{s}$ ) or ( $c\bar{s}q\bar{q}$ )
  - Chen et al., PRC 76, 064903 (2007); coalescence model
- $\Theta_{cs}^+(udus\bar{c})$  and  $T_{cc}(ud\bar{c}\bar{c})$ 
  - Lee et al., Eur. J. Phys. C 54, 259 (08); coalescence model
- Exotic mesons (8), baryons (8), and dibaryons (6)
  - Cho et al. [ExHIC Collaboration], PRL 106, 212001 (2011); PRC 84, 064910 (2011); coalescence model

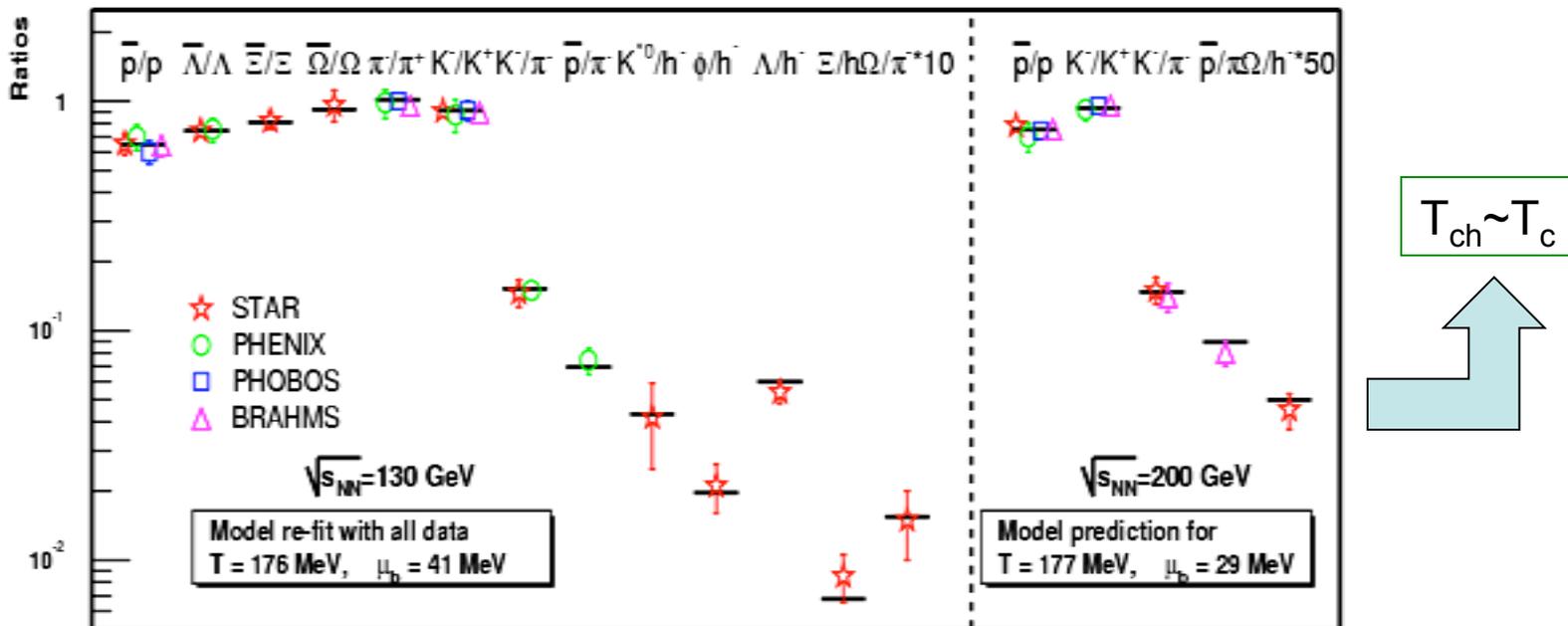
# Statistical model

Andronic et al, NPA 722, 167 (2006); Wheaton et al., Phys. Commun. 180, 84 (2009)

Assume thermally and chemically equilibrated system of non-interacting hadrons and resonances with density

$$n_i = \frac{g}{2\pi^2} \int_0^\infty \frac{p^2 dp}{e^{(E_i(p) - \mu_i)/T} \pm 1}, \quad E_i = \sqrt{p^2 + m_i^2}$$

Determine chemical freeze out temperature  $T_{ch}$  and baryon chemical potential  $\mu_B$  by fitting experimental data after inclusion of feed down from short-lived particles and resonances decay.



# Coalescence model

Greco, Ko & Levai, PRL 90, 202102 (2003);  
PRC 68, 034904 (2003)

Number of hadrons with n quarks and/or antiquarks

$$N_n = g \int \prod_{i=1}^n p_i d\sigma_i \frac{dp_i}{(2\pi)^3 E_i} f_{q_i}(x_i, p_i) f_n(x_1, \dots, x_n; p_1, \dots, p_n)$$

Spin-color  
statistical factor

$g_M$

e.g.  $g_\pi = g_K = 1/36$     $g_\rho = g_{K^*} = 1/12$   
 $g_p = g_{\bar{p}} = 1/108$ ,    $g_\Delta = g_{\bar{\Delta}} = 1/54$

Quark distribution  
function

$f_q(x, p)$

$$\int p \cdot d\sigma \frac{d^3 p}{(2\pi)^3 E} f_q(x, p) = N_q$$

Coalescence  
probability  
function

$$f_M(x_1, x_2; p_1, p_2) = f_2(x_1 - x_2; p_1 - p_2)$$

$$= \exp[(x_1 - x_2)^2 / 2\Delta_x^2]$$

$$\times \exp[\{(p_1 - p_2)^2 - (m_1 - m_2)^2\} / 2\Delta_p^2]$$

$$\Delta_x \cdot \Delta_p \approx \hbar$$

For baryons, Jacobi coordinates for three-body system are used.

# $\Theta^+(\text{u}d\text{u}d\text{s}\bar{\text{b}})$ production in heavy ion collisions

Chen, Greco, Ko, Lee & Liu, PLB 601, 34 (2004)

Using non-relativistic distributions for quarks and harmonic oscillator wave functions for  $\Theta^+$

$$f_q(\eta, y, \vec{p}_\perp) = g_q \delta(\eta - y) \exp(-\vec{p}_\perp^2 / (2m_q T))$$

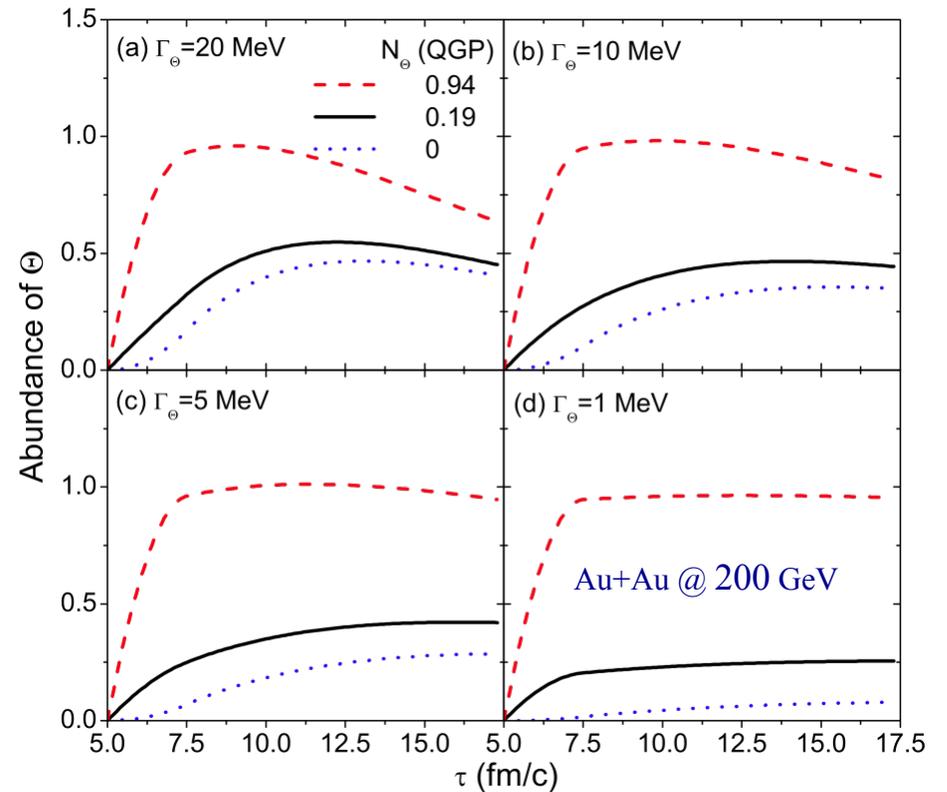
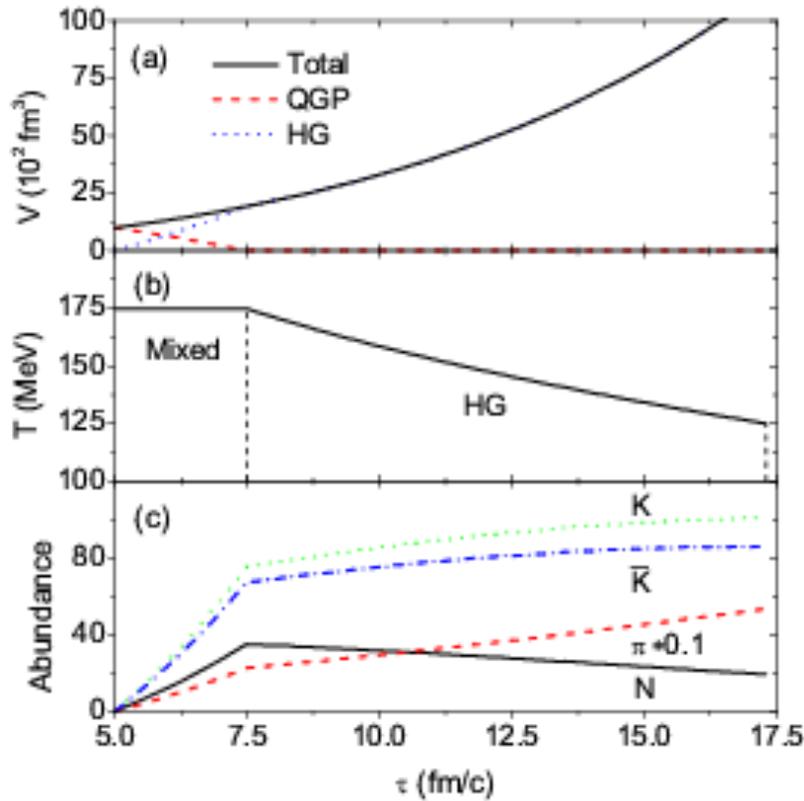
$$f_\Theta(x; p) = 8^4 \exp\left(-\sum_{i=1}^4 \vec{y}_i^2 / \sigma_i^2 - \sum_{i=1}^4 \vec{k}_i^2 \sigma_i^2\right)$$

Number of  $\Theta^+$  produced in quark coalescence model

$$\begin{aligned} N_\Theta &= g_\Theta \int \prod_{i=1}^5 \frac{p_i \cdot d\sigma_i d^3 \vec{p}_i}{(2\pi)^3 E_i} f_q(x_i, p_i) f_\Theta(x_1 \cdots x_5; p_1 \cdots p_5) \\ &= g_\Theta N_u^2 N_d^2 N_{\bar{s}} \left( \frac{4m_q}{5m_s} + \frac{1}{5} \right)^{3/2} \left[ \frac{(4\pi)^{3/2} \sigma^3}{V(1 + 2m_q T \sigma^2)} \right]^4 \end{aligned}$$

## Time evolution of $\Theta^+$ (udud sbar) abundance

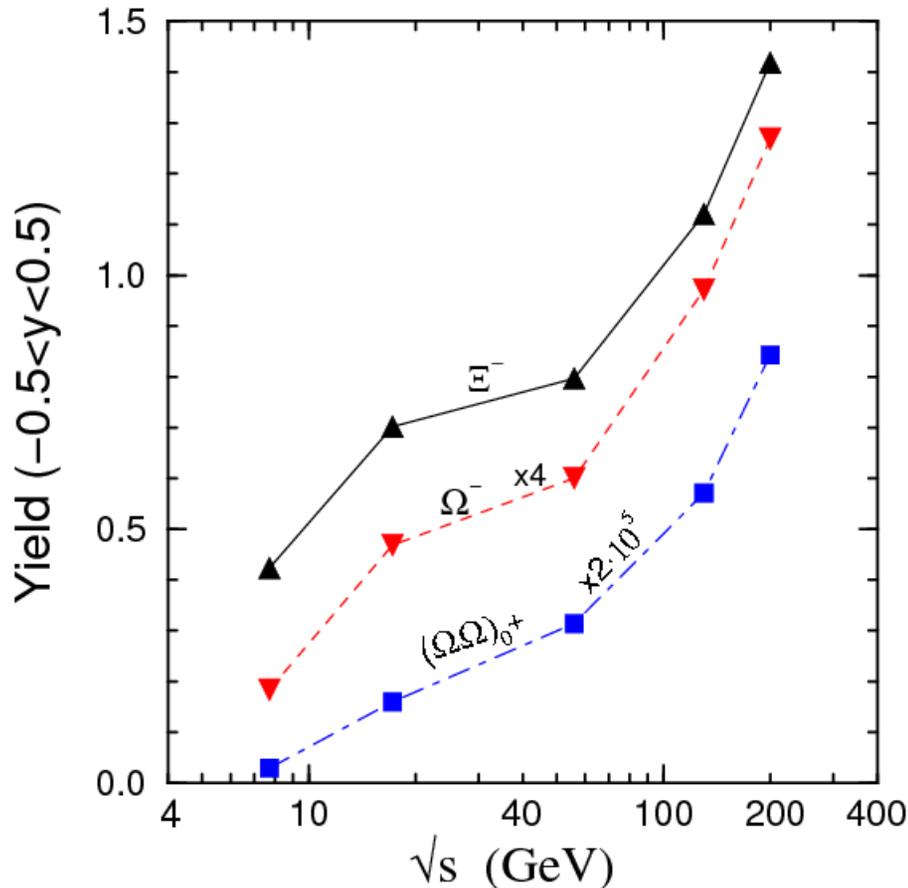
$$\frac{dN_{\Theta}}{d\tau} = R_{QGP}(\tau) + \langle \sigma_{\pi N \rightarrow \bar{K}\Theta} \nu \rangle n_{\pi} n_N V_H + \left( \langle \sigma_{KN \rightarrow \pi\Theta} \nu \rangle + \langle \sigma_{KN \rightarrow \Theta} \nu \rangle \right) n_K n_N V_H - \Gamma_{\Theta} N_{\Theta} - \langle \sigma_{\bar{K}\Theta \rightarrow \pi N} \nu \rangle n_{\bar{K}} N_{\Theta} - \langle \sigma_{\pi\Theta \rightarrow KN} \nu \rangle n_{\pi} N_{\Theta}$$



- About 0.5  $\Theta^+$  ( $\sigma=0.86 \text{ fm}$  and  $\Gamma_{\Theta}=20 \text{ MeV}$ ) in central rapidity per collision, similar to predictions from statistical model (Randrup; Letessier et al.)

# Diomega production in HIC

According to the chiral quark model of Zhang et al. (PRC 61, 065204 (2000)), diomega  $(\Omega\Omega)_{0+}$  is bound by  $\sim 116$  MeV with a root-mean-square radius  $\sim 0.84$  fm and lifetime  $\sim 10^{-10}$  sec.



No.	Channel
I	$\Omega + \Omega \rightarrow (\Omega\Omega)_0 + \gamma$
II	$\Omega + \Omega \rightarrow (\Omega\Omega)_0 + \eta$
III	$\Omega + \Omega \rightarrow (\Omega\Omega)_0 + \eta'$
IV	$\Omega + \Omega \rightarrow (\Omega\Omega)_0 + \phi$
V	$\Omega + \Xi \rightarrow (\Omega\Omega)_0 + K$
VI	$\Omega + \Xi \rightarrow (\Omega\Omega)_0 + K^*$
VII	$\Omega + N \rightarrow (\Omega N)_2 + \gamma$
VIII	$\Omega + N \rightarrow (\Omega N)_2 + \pi$
IX	$\Omega + (\Omega N)_2 \rightarrow (\Omega\Omega)_0 + N$

- Cross sections for I-VI are  $\sim 2-25 \mu\text{b}$  and thus unimportant.
- Production is dominated by two-step processes through VII, VIII ( $\sim 50-175 \mu\text{b}$ ) and IX ( $\sim 20-50 \text{mb}$ ).
- Yield is order of magnitude smaller than in statistical or coalescence model (neglect of three-body process?)

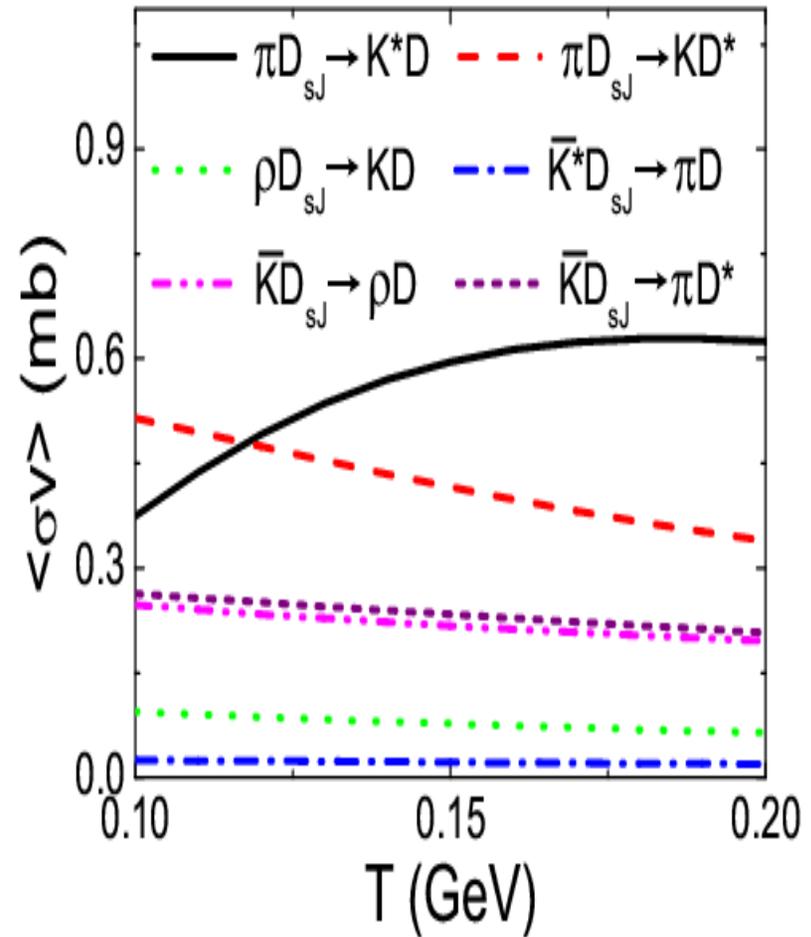
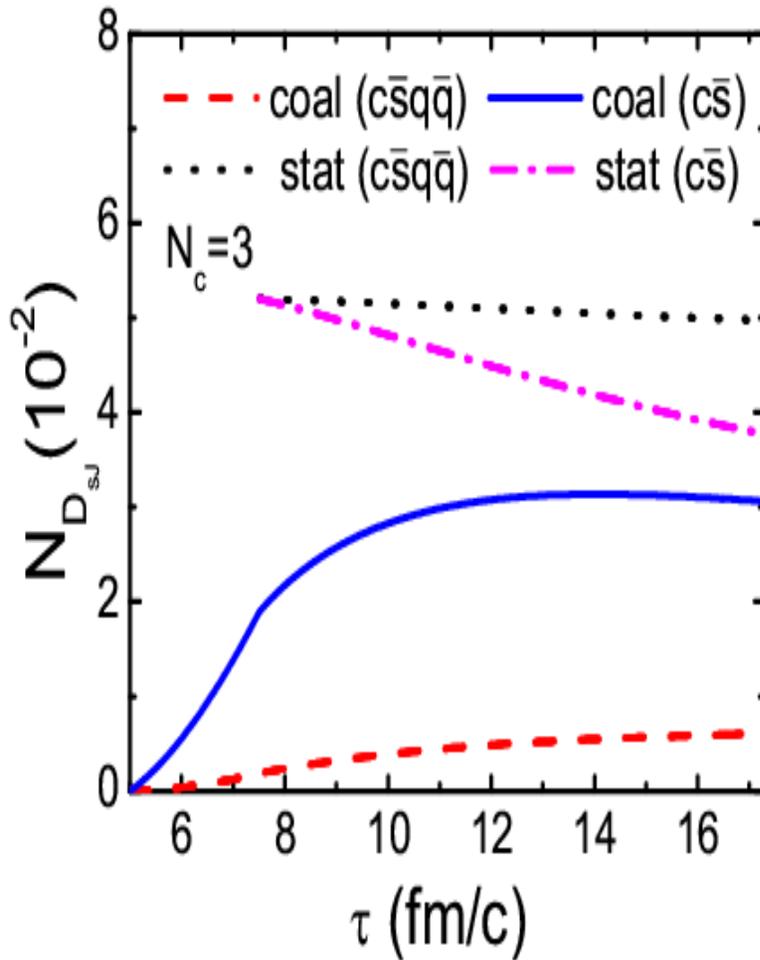
Pal, Ko & Zhang, PLB 624, 210 (05)

## $D_{sJ}(2317): J^{\pi}=0^+$

- Mass of 2317 MeV less than those predicted by quark model and QCD sum rule for two-quark state ( $c\bar{s}$ , p-wave) but comparable to those for four-quark state ( $c\bar{s}q\bar{q}$ , s-wave)
- Width of a few (four-quark) to a few tens (two-quark) keV from decay to  $D_s\pi$ , empirically less than 4.6 MeV limited by experimental resolution.
- Observed in elementary reactions:
  - BABAR: from  $D_s+\pi^0$  inclusive invariant mass distribution in  $e^+e^-$  annihilation (PRL 90, 242001 (03))
  - Belle: from B decay (PRL 91, 262002 (03))

# $D_{sJ}$ production at RHIC

Chen, Liu, Nielsen & Ko, PRC 76, 064903 (2007))



- Cross sections are for four-quark state and larger by  $\sim 9$  for two-quark state.
- Final yield is sensitive to the quark structure of  $D_{sJ}$

# Orbital angular momentum dependence of coalescence probability

- Hadron Wigner functions

$$f_s^w(\vec{y}, \vec{k}) = 8 \exp\left(-\frac{y^2}{\sigma^2} - k^2 \sigma^2\right)$$

$$f_p^w(\vec{y}, \vec{k}) = \left(\frac{16}{3} \frac{y^2}{\sigma^2} - 8 + \frac{16}{3} k^2 \sigma^2\right) \exp\left(-\frac{y^2}{\sigma^2} - k^2 \sigma^2\right)$$

- Coalescence factors

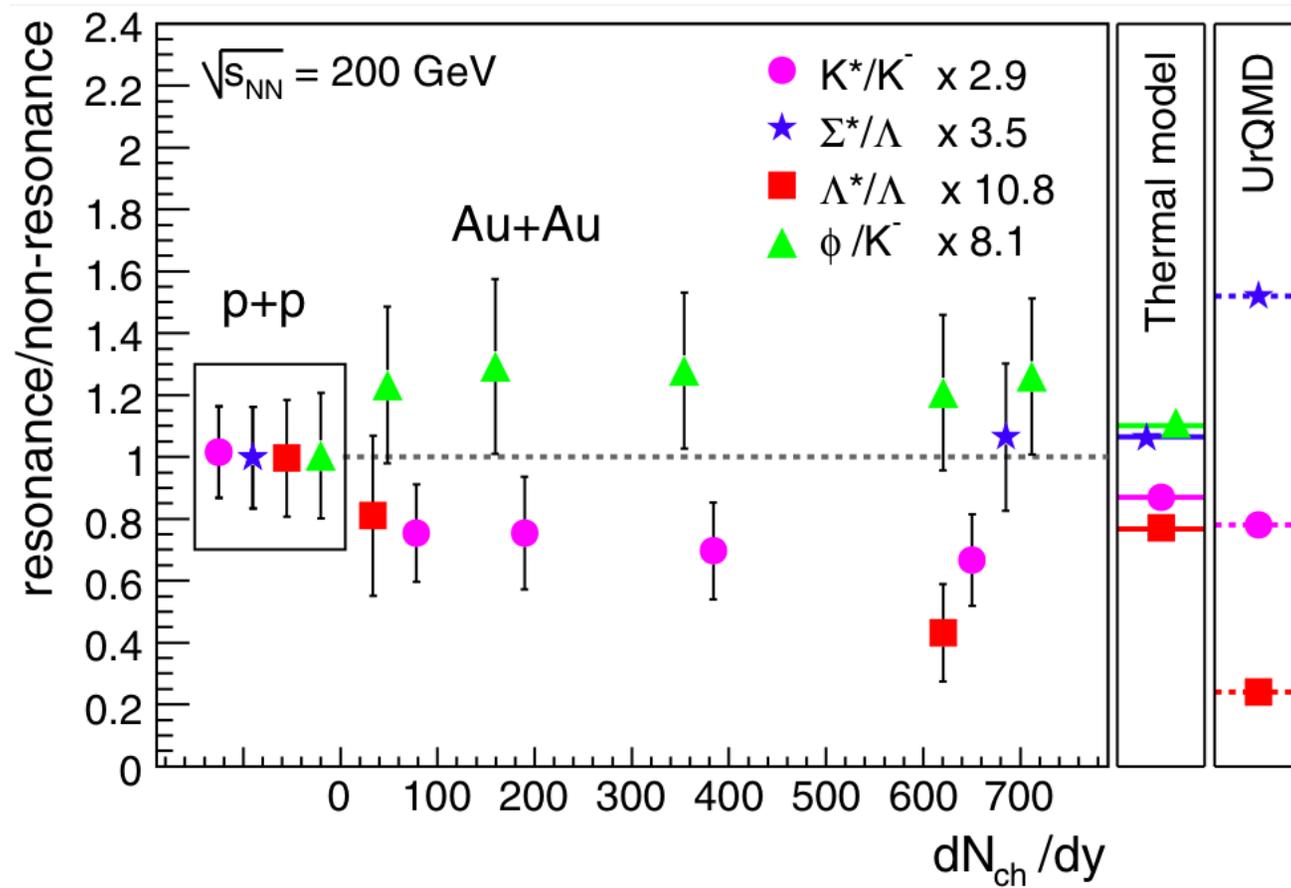
$$\frac{1}{g} \frac{N}{V} \frac{(4\pi\sigma^2)^{3/2}}{(1+2\mu T\sigma^2)^2} \approx 0.360 \quad \text{for s - wave}$$

$$\frac{1}{g} \frac{N}{V} \frac{2}{3} \frac{(4\pi\sigma^2)^{3/2} 2\mu T\sigma^2}{(1+2\mu T\sigma^2)^2} \approx 0.093 \quad \text{for p - wave}$$

- p-wave coalescence is suppressed by a factor of  $\sim 4$  compared to s-wave coalescence.

# Suppression of $\Lambda(1520)$ in HIC

Abelev [Star Collaboration],  
PRL 97, 132301 (2006)



- Measured  $\Lambda(1520)/\Lambda(1115)$  ratio is significantly smaller than thermal model prediction, but can be explained by the coalescence model after taking into account the p-wave state of strang quark in  $\Lambda(1520)$  (Kanada-En'yo and Meuller, PRC 74, 061901(R) (2006).

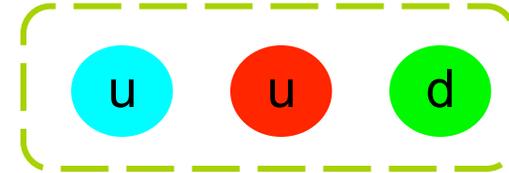
# Quark color-spin interaction and hadron masses

Lee, Yasui, Liu, and Ko, EJPC 54, 259 (2008)

## ■ Baryon mass differences

Mass Difference	$M_\Delta - M_N$	$M_\Sigma - M_\Lambda$	$M_{\Sigma_c} - M_{\Lambda_c}$
Formula	$\frac{3C_B}{2m_u^2}$	$\frac{C_B}{m_u^2} \left(1 - \frac{m_u}{m_s}\right)$	$\frac{C_B}{m_u^2} \left(1 - \frac{m_u}{m_c}\right)$
Fit	290 MeV	77 MeV	154 MeV
Experiment	290 MeV	75 MeV	170 MeV

$$\text{Diquark} \quad \sum \frac{C_B}{m_i m_j} [s_i \cdot s_j]$$

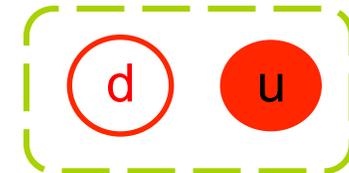


$$m_u = m_d = 300 \text{ MeV}, \quad m_s = 500 \text{ MeV}, \quad m_c = 1500 \text{ MeV}, \quad m_b = 4700 \text{ MeV}$$

## ■ Meson mass differences

Mass Difference	$M_\rho - M_\pi$	$M_{K^*} - M_K$	$M_{D^*} - M_D$	$M_{B^*} - M_B$
Formula	$\frac{C_M}{m_u^2}$	$\frac{C_M}{m_u m_s}$	$\frac{C_M}{m_u m_c}$	$\frac{C_M}{m_u m_b}$
Fit	635 MeV	381 MeV	127 MeV	41 MeV
Experiment	635 MeV	397 MeV	137 MeV	46 MeV

$$\text{Quark-antiquark} \quad \sum \frac{C_M}{m_i m_j} [s_i \cdot s_j]$$



Works very well with  $3 \times C_B = C_M = 635 m_u^2$

# Charm exotics production in HIC

Lee, Yasui, Liu & Ko  
Eur. J. Phys. C 54, 259 (08)

- Charm tetraquark mesons
  - $T_{cc}(ud\bar{c}\bar{c})$  is  $\sim 80$  MeV below  $D+D^*$
  - Coalescence model predicts a yield of  $\sim 5.5 \times 10^{-6}$  in central Au+Au collisions at RHIC and  $\sim 9 \times 10^{-5}$  in central Pb+Pb collisions at LHC if total charm quark numbers at mid-rapidity are 3 and 20, respectively
  - Yields increase to  $7.5 \times 10^{-4}$  and  $8.6 \times 10^{-3}$ , respectively, in the statistical model
  
- Charmed pentaquark baryons
  - $\Theta_{cs}(udus\bar{c})$  is  $\sim 70$  MeV below  $D+\Sigma$ ,  $\sim 30$  MeV below  $N+D_s$ , but  $\sim 8$  MeV above  $\Lambda+D$
  - Yield is  $\sim 1.2 \times 10^{-4}$  at RHIC and  $\sim 7.9 \times 10^{-4}$  at LHC from the coalescence model for total charm quark numbers of 3 and 20, respectively
  - Statistical model predicts much larger yields of  $\sim 4.5 \times 10^{-3}$  at RHIC and  $\sim 2.7 \times 10^{-2}$  at LHC

## Decay modes of $T_{cc}$ and $\Theta_{cs}$

**Table 8.** Possible decay modes of  $T_{cc}$ . In the bottom row, we would observe the correlations  $(K^+\pi^-)(K^+\pi^-)\pi^-$  and  $(K^+\pi^+\pi^+\pi^-)(K^+\pi^-)\pi^-$  in the final states. See the text for details

Threshold	Decay mode	Lifetime
$M_{T_{cc}} > M_{D^*} + M_D$	$D^{*-} \bar{D}^0$	hadronic decay
$2M_D + M_\pi < M_{T_{cc}} < M_{D^*} + M_D$	$\bar{D}^0 \bar{D}^0 \pi^-$	hadronic decay
$M_{T_{cc}} < 2M_D + M_\pi$	$D^{*-} K^+ \pi^-, D^{*-} K^+ \pi^+ \pi^- \pi^-$	$0.41 \times 10^{-12}$ s

**Table 9.** Possible decay modes of  $\Theta_{cs}$

Threshold	Decay mode	Lifetime
$M_{\Theta_{cs}} > M_N + M_{D_s}$	$pD_s^-$	hadronic decay
$M_\Lambda + M_D < M_{\Theta_{cs}} < M_N + M_{D_s}$	$\Lambda \bar{D}^0$	hadronic decay
	$\Lambda D^-$	hadronic decay
$M_{\Theta_{cs}} < M_\Lambda + M_D$	$\Lambda K^+ \pi^-, \Lambda K^+ \pi^+ \pi^- \pi^-$	$0.41 \times 10^{-12}$ s
	$\Lambda K^+ \pi^- \pi^-$	$1.0 \times 10^{-12}$ s

# Exotic mesons, baryons and dibaryons

Cho, Furumoto, Hyodo, Jido, Ko, Lee, Nielsen, Ohnishi, Sekihara, Yasui, and Yazaki [ExHIC Collaboration],  
PRL 106, 212001 (2011); PRC 84, 064910 (2011)

Particle	$m$ (MeV)	$g$	$I$	$J^P$	$2q/3q/6q$	$4q/5q/8q$	Mol.	$\omega_{\text{Mol.}}$ (MeV)	decay mode
<b>Mesons</b>									
$f_0(980)$	980	1	0	$0^+$	$q\bar{q}, s\bar{s} (L=1)$	$q\bar{q}s\bar{s}$	$\bar{K}K$	67.8(B)	$\pi\pi$ (strong decay)
$a_0(980)$	980	3	1	$0^+$	$q\bar{q} (L=1)$	$q\bar{q}s\bar{s}$	$\bar{K}K$	67.8(B)	$\eta\pi$ (strong decay)
$K(1460)$	1460	2	1/2	$0^-$	$q\bar{s}$	$q\bar{q}q\bar{s}$	$\bar{K}KK$	69.0(R)	$K\pi\pi$ (strong decay)
$D_s(2317)$	2317	1	0	$0^+$	$c\bar{s} (L=1)$	$q\bar{q}c\bar{s}$	$DK$	273(B)	$D_s\pi$ (strong decay)
$T_{cc}^1 \dagger$	3797	3	0	$1^+$	—	$qq\bar{c}\bar{c}$	$\bar{D}\bar{D}^*$	476(B)	$K^+\pi^- + K^+\pi^- + \pi^-$
$X(3872)$	3872	3	0	$1^+, 2^-^*)$	$c\bar{c} (L=2)$	$q\bar{q}c\bar{c}$	$\bar{D}D^*$	3.6(B)	$J/\psi\pi\pi$ (strong decay)
$Z^+(4430) \ddagger$	4430	3	1	$0^-^*)$	—	$q\bar{q}c\bar{c} (L=1)$	$D_1\bar{D}^*$	13.5(B)	$J/\psi\pi$ (strong decay)
$T_{cb}^0 \dagger$	7123	1	0	$0^+$	—	$qq\bar{c}\bar{b}$	$\bar{D}B$	128(B)	$K^+\pi^- + K^+\pi^-$
<b>Baryons</b>									
$\Lambda(1405)$	1405	2	0	$1/2^-$	$qqq (L=1)$	$qqqs\bar{q}$	$\bar{K}N$	20.5(R)-174(B)	$\pi\Sigma$ (strong decay)
$\Theta^+(1530) \ddagger$	1530	2	0	$1/2^+^*)$	—	$qqqq\bar{s} (L=1)$	—	—	$KN$ (strong decay)
$\bar{K}KN \dagger$	1920	4	1/2	$1/2^+$	—	$qqqs\bar{s} (L=1)$	$\bar{K}KN$	42(R)	$K\pi\Sigma, \pi\eta N$ (strong decay)
$\bar{D}N \dagger$	2790	2	0	$1/2^-$	—	$qqqq\bar{c}$	$\bar{D}N$	6.48(R)	$K^+\pi^-\pi^- + p$
$\bar{D}^*N \dagger$	2919	4	0	$3/2^-$	—	$qqqq\bar{c} (L=2)$	$\bar{D}^*N$	6.48(R)	$\bar{D} + N$ (strong decay)
$\Theta_{cs} \dagger$	2980	4	1/2	$1/2^+$	—	$qqqs\bar{c} (L=1)$	—	—	$\Lambda + K^+\pi^-$
$BN \dagger$	6200	2	0	$1/2^-$	—	$qqqq\bar{b}$	$BN$	25.4(R)	$K^+\pi^-\pi^- + \pi^+ + p$
$B^*N \dagger$	6226	4	0	$3/2^-$	—	$qqqq\bar{b} (L=2)$	$B^*N$	25.4(R)	$B + N$ (strong decay)
<b>Dibaryons</b>									
$H \dagger$	2245	1	0	$0^+$	$qqqqss$	—	$\Xi N$	73.2(B)	$\Lambda\Lambda$ (strong decay)
$\bar{K}NN \ddagger$	2352	2	1/2	$0^-^*)$	$qqqqqs (L=1)$	$qqqqq\bar{q}s\bar{q}$	$\bar{K}NN$	20.5(T)-174(T)	$\Lambda N$ (strong decay)
$\Omega\Omega \dagger$	3228	1	0	$0^+$	$ssssss$	—	$\Omega\Omega$	98.8(R)	$\Lambda K^- + \Lambda K^-$
$H_c^{++} \dagger$	3377	3	1	$0^+$	$qqqqsc$	—	$\Xi_c N$	187(B)	$\Lambda K^- \pi^+ \pi^+ + p$
$\bar{D}NN \dagger$	3734	2	1/2	$0^-$	—	$qqqqq\bar{q}c\bar{c}$	$\bar{D}NN$	6.48(T)	$K^+\pi^- + d, K^+\pi^-\pi^- + p$
$BNN \dagger$	7147	2	1/2	$0^-$	—	$qqqqq\bar{q}b\bar{b}$	$BNN$	25.4(T)	$K^+\pi^- + d, K^+\pi^- + p + p$

# Parameters in fireball model & in hadron Wigner functions

$$V(\tau) = \pi \left[ R_C + v_C (\tau - \tau_C) + a/2 (\tau - \tau_C)^2 \right]^2 \tau c$$

$$\sigma = (\mu\omega)^{-1/2} \text{ fixed by normal hadrons}$$

TABLE I. Quark numbers at hadronization temperature  $T_C$  and volume  $V_C$ , the volume  $V_H$  at the end of hadronization, and the thermal freeze-out temperature  $T_F$  and volume  $V_F$  in central heavy ion collisions at RHIC and LHC.

	RHIC	LHC
$N_u = N_d$	245	662
$N_s = N_{\bar{s}}$	150	405
$N_c = N_{\bar{c}}$	3	20
$N_b = N_{\bar{b}}$	0.02	0.8
$V_C$	1000 fm <sup>3</sup>	2700 fm <sup>3</sup>
$T_C = T_H$	175 MeV	175 MeV
$V_H$	1908 fm <sup>3</sup>	5152 fm <sup>3</sup>
$\mu_B$	20 MeV	0 MeV
$\mu_s$	10 MeV	0 MeV
$V_F$	11322 fm <sup>3</sup>	30569 fm <sup>3</sup>
$T_F$	125 MeV	125 MeV

TABLE III. Yields of normal hadrons at RHIC and LHC in the coalescence and statistical models with oscillator frequencies  $\omega = 550$  MeV,  $\omega_s = 519$  MeV,  $\omega_c = 385$  MeV, and  $\omega_b = 338$  MeV are determined by fitting the statistical model results for  $\Lambda(1115)$ ,  $\Lambda_c(2286)$ , and  $\Lambda_b(5620)$  marked with \* at RHIC after taking account of resonance decays. Numbers in the parentheses are those without the decay contribution.

Configuration	Particle	RHIC		LHC	
		Coalescence	Statistical	Coalescence	Statistical
$\bar{q}q$	$\omega(782)$	44.2	40.2	119	108
	$\rho(770)$	132	127	358	342
	$\bar{K}^*(892)$	41.2	47.2	111	135
	$K^*(892)$	41.2	52.9	111	135
$qq_s$	$\Lambda(1115)$	29.8*	29.8	80.5	77.5
		(3.0)	(6.5)	(8.1)	(16.5)
$qqQ$	$\Lambda(1520)$	1.6	1.9	4.4	4.8
	$\Lambda_c(2286)$	0.60*	0.60	4.0	3.6
		(0.058)	(0.14)	(0.39)	(0.83)
	$\Lambda_b(5620)$	$3.6 \times 10^{-3}$ *	$3.6 \times 10^{-3}$	0.14	0.13
	( $3.6 \times 10^{-4}$ )	( $9.2 \times 10^{-4}$ )	(0.014)	0.033	

# Exotic hadron yields at RHIC and LHC

TABLE V. Exotic hadron yields in central Au + Au collisions at  $\sqrt{s_{NN}} = 200$  GeV at RHIC and in central Pb + Pb collisions at  $\sqrt{s_{NN}} = 5.5$  TeV at LHC from the quark coalescence ( $2q/3q/6q$  and  $4q/5q/8q$ ) and the hadron coalescence (Mol.), as well as from the statistical model (Stat.)

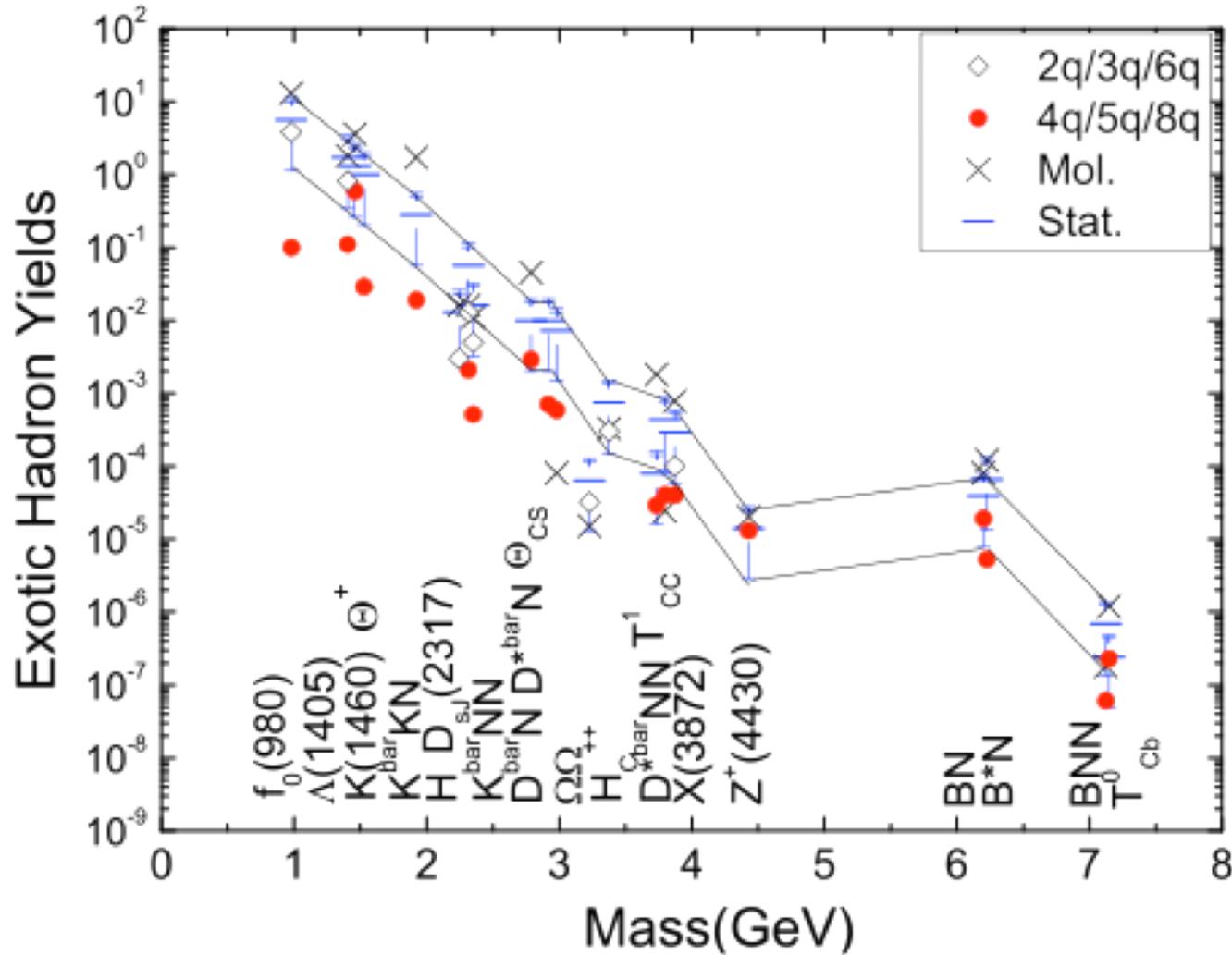
	RHIC				LHC			
	$2q/3q/6q$	$4q/5q/8q$	Mol.	Stat.	$2q/3q/6q$	$4q/5q/8q$	Mol.	Stat.
<b>Mesons</b>								
$f_0(980)$	3.8, 0.73( $s\bar{s}$ )	0.10	13	5.6	10, 2.0 ( $s\bar{s}$ )	0.28	36	15
$a_0(980)$	11	0.31	40	17	31	0.83	$1.1 \times 10^2$	46
$K(1460)$	—	0.59	3.6	1.3	—	1.6	9.3	3.2
$D_s(2317)$	$1.3 \times 10^{-2}$	$2.1 \times 10^{-3}$	$1.6 \times 10^{-2}$	$5.6 \times 10^{-2}$	$8.7 \times 10^{-2}$	$1.4 \times 10^{-2}$	0.10	0.35
$T_{cc}^{1a}$	—	$4.0 \times 10^{-5}$	$2.4 \times 10^{-5}$	$4.3 \times 10^{-4}$	—	$6.6 \times 10^{-4}$	$4.1 \times 10^{-4}$	$7.1 \times 10^{-3}$
$X(3872)$	$1.0 \times 10^{-4}$	$4.0 \times 10^{-5}$	$7.8 \times 10^{-4}$	$2.9 \times 10^{-4}$	$1.7 \times 10^{-3}$	$6.6 \times 10^{-4}$	$1.3 \times 10^{-2}$	$4.7 \times 10^{-3}$
$Z^+(4430)^b$	—	$1.3 \times 10^{-5}$	$2.0 \times 10^{-5}$	$1.4 \times 10^{-5}$	—	$2.1 \times 10^{-4}$	$3.4 \times 10^{-4}$	$2.4 \times 10^{-4}$
$T_{cb}^{0a}$	—	$6.1 \times 10^{-8}$	$1.8 \times 10^{-7}$	$6.9 \times 10^{-7}$	—	$6.1 \times 10^{-6}$	$1.9 \times 10^{-5}$	$6.8 \times 10^{-5}$
<b>Baryons</b>								
$\Lambda(1405)$	0.81	0.11	1.8–8.3	1.7	2.2	0.29	4.7–21	4.2
$\Theta^{+b}$	—	$2.9 \times 10^{-2}$	—	1.0	—	$7.8 \times 10^{-2}$	—	2.3
$\bar{K}KN^a$	—	$1.9 \times 10^{-2}$	1.7	0.28	—	$5.2 \times 10^{-2}$	4.2	0.67
$\bar{D}N^a$	—	$2.9 \times 10^{-3}$	$4.6 \times 10^{-2}$	$1.0 \times 10^{-2}$	—	$2.0 \times 10^{-2}$	0.28	$6.1 \times 10^{-2}$
$\bar{D}^*N^a$	—	$7.1 \times 10^{-4}$	$4.5 \times 10^{-2}$	$1.0 \times 10^{-2}$	—	$4.7 \times 10^{-3}$	0.27	$6.2 \times 10^{-2}$
$\Theta_{cs}^a$	—	$5.9 \times 10^{-4}$	—	$7.2 \times 10^{-3}$	—	$3.9 \times 10^{-3}$	—	$4.5 \times 10^{-2}$
$BN^a$	—	$1.9 \times 10^{-5}$	$8.0 \times 10^{-5}$	$3.9 \times 10^{-5}$	—	$7.7 \times 10^{-4}$	$2.8 \times 10^{-3}$	$1.4 \times 10^{-3}$
$B^*N^a$	—	$5.3 \times 10^{-6}$	$1.2 \times 10^{-4}$	$6.6 \times 10^{-5}$	—	$2.1 \times 10^{-4}$	$4.4 \times 10^{-3}$	$2.4 \times 10^{-3}$
<b>Dibaryons</b>								
$H^a$	$3.0 \times 10^{-3}$	—	$1.6 \times 10^{-2}$	$1.3 \times 10^{-2}$	$8.2 \times 10^{-3}$	—	$3.8 \times 10^{-2}$	$3.2 \times 10^{-2}$
$\bar{K}NN^b$	$5.0 \times 10^{-3}$	$5.1 \times 10^{-4}$	0.011–0.24	$1.6 \times 10^{-2}$	$1.3 \times 10^{-2}$	$1.4 \times 10^{-3}$	0.026 – 0.54	$3.7 \times 10^{-2}$
$\Omega\Omega^a$	$3.2 \times 10^{-5}$	—	$1.5 \times 10^{-5}$	$6.4 \times 10^{-5}$	$8.6 \times 10^{-5}$	—	$4.4 \times 10^{-5}$	$1.9 \times 10^{-4}$
$H_c^{++a}$	$3.0 \times 10^{-4}$	—	$3.3 \times 10^{-4}$	$7.5 \times 10^{-4}$	$2.0 \times 10^{-3}$	—	$1.9 \times 10^{-3}$	$4.2 \times 10^{-3}$
$\bar{D}NN^a$	—	$2.9 \times 10^{-5}$	$1.8 \times 10^{-3}$	$7.9 \times 10^{-5}$	—	$2.0 \times 10^{-4}$	$9.8 \times 10^{-3}$	$4.2 \times 10^{-4}$
$BNN^a$	—	$2.3 \times 10^{-7}$	$1.2 \times 10^{-6}$	$2.4 \times 10^{-7}$	—	$9.2 \times 10^{-6}$	$3.7 \times 10^{-5}$	$7.6 \times 10^{-6}$

<sup>a</sup>Particles that are newly predicted by theoretical model.

<sup>b</sup>Particles that are not yet established.

■ Most yields are sufficient large ( $>10^{-5}$ ) 17

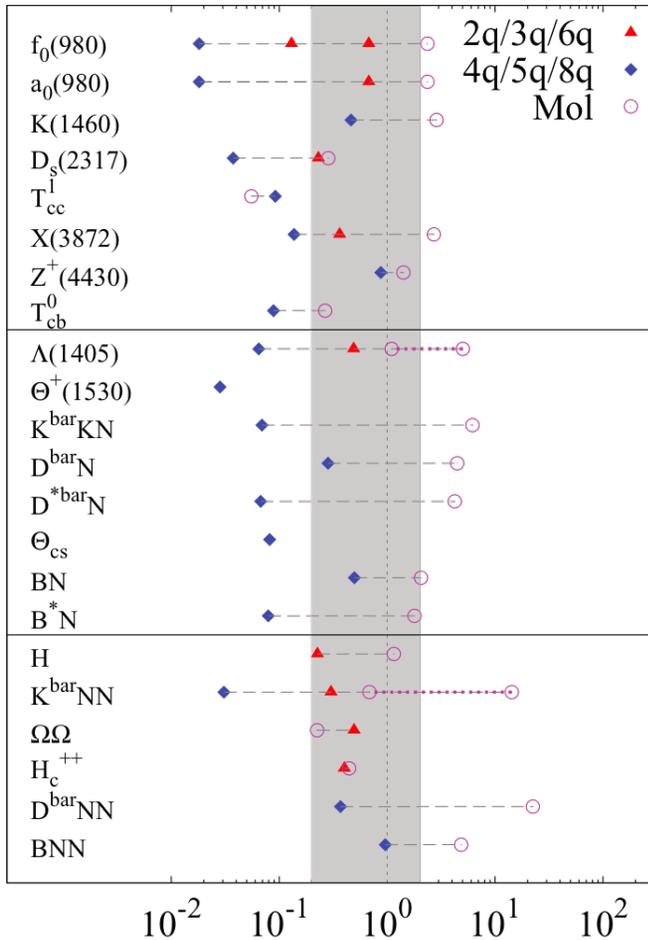
# Yields of exotic hadrons at RHIC



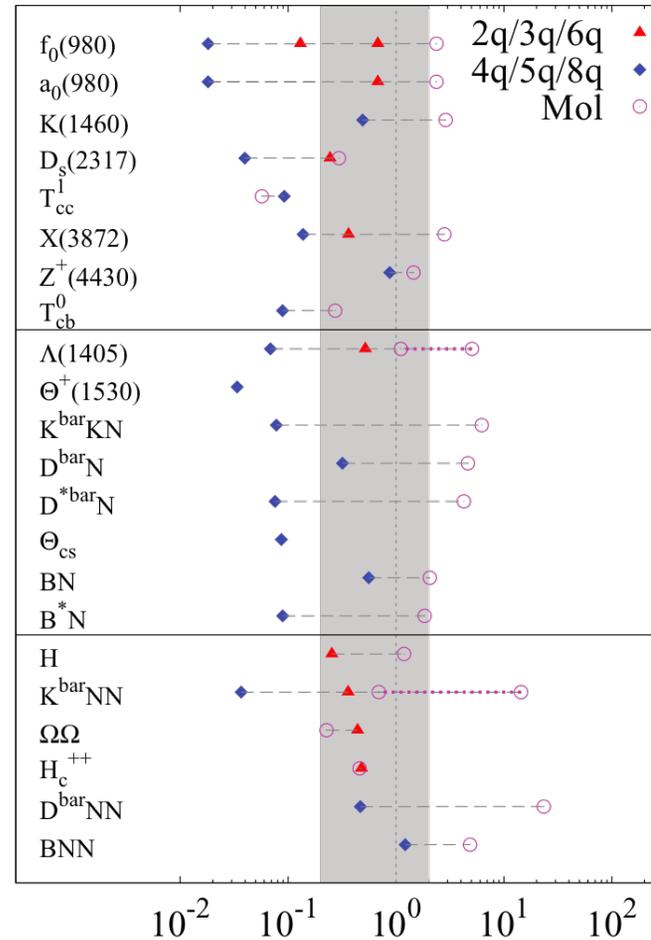
- Most exotic hadrons are abundantly produced ( $>10^{-5}$ )

# Ratio of exotic hadron yields from coalescence and statistical models

Coalescence / Statistical model ratio at RHIC



Coalescence / Statistical model ratio at LHC



- Multiquark hadrons are suppressed while hadronic molecules are enhanced in coalescence model, compared to the statistical model predictions

## Summary

- Expected yield of  $\Theta^+(udud\bar{s})$  in HIC is large but it is not observed.
- Possible existence of tetraquark meson  $T_{cc}(ud\bar{c}\bar{c})$  and pentaquark baryon  $\Theta_{cs}(udus\bar{c})$  due to attractive diquark spin-spin interaction
- HIC allows for the study of  $\Omega\Omega$  interaction and possible existence of  $(\Omega\Omega)_{0+}$
- Yield of  $D_{sj}$  (2317) in HIC is sensitive to its quark structure
- Yields of exotic hadrons are appreciable in HIC ( $>10^{-5}$ )
- In the coalescence model, yields of exotic hadrons are sensitive to their structures with molecular-state configurations enhanced and multiquark configurations suppressed relative to statistical production