Frequency choice of eRHIC SRF linac

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FREQUENCY CHOICE OF ERHIC SRF LINAC
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ABSTRACT
eRHIC is a FFAG lattice based multipass ERL [1]. The eRHIC SRF linac has been
decided to change from 422 MHz 5-cell cavity to 647 MHz 5-cell cavity. There are
several considerations affecting the frequency choice for a high current multipass-
ERL: the beam structure, bunch length, energy spread, beam-break-up (BBU)
threshold, SRF loss considerations. Beyond the physics considerations, cost and
complexity or risk is an important consideration for the frequency choice, especially
when we are designing a machine to be built in a few years.

Although there are some benefits of using a 422 MHz cavity for eRHIC ERL,
however, there are some very critical drawbacks, including lack of facilities to
fabricate a 422 MHz 5-cell cavity, very few facilities to process such a cavity and no
existing facility to test the cavity anywhere. As the cavity size is big and its weight is
large, it is difficult to handle it during fabrication, processing and testing and no one
has experience in this area. As the cavity size is large, the cryomodule becomes big as
well. All of these considerations drive the risk of building eRHIC ERL with 422 MHz
cavities to a very high level. Therefore, a decision was made to change the frequency
of main linac to be 647 MHz 5-cell cavities.

This note will compare these two linacs: 422MHz 5-cell cavity linac and 647Mz 5-
cell cavity SRF linac, from both practical point of view and physics point of view.

1. LOW FREQUENCY AND HIGH FREQUENCY CAVITY

From physics point of view, there are a few benefits of using a low frequency SRF
cavity for ERL [2], and there are also some drawbacks. For example,

(1) The transient voltage is inversely proportional to the square of frequency, thus
favoring a lower frequency.

(2) The Lorentz detuning factor is inversely proportional to frequency so the
LLRF control is easier at higher frequencies.

(3) The loss factor (wakefield) is inversely proportional to the aperture (for a
constant ratio of the bunch length and frequency), thus favoring lower
frequencies in term of induced energy spread and HOM power generation.

(4) The transverse beam-break-up (BBU) threshold is approximately inversely
proportional to the cavity frequency and the linac length, favoring a lower
frequency.

(5) With the same real estate and linac energy, more cavities are required for the
higher frequency linac, so the part count is also higher, driving the cost up
with frequency.

(6) One of the drawbacks for a lower frequency cavity is that N-doping will not
improve the quality factor of a 422 MHz cavity because at this low frequency,
the cavity’s quality factor is already dominated by the residual resistance.
However, experiment results from Fermi Lab shows that the quality factor of 650 MHz cavity improve a factor of 3 [3].

As addressed above, the 422 MHz SRF linac brings various benefits for machine performance. However, from practical/project point of view, there is a large risk of using a 422 MHz 5-cell cavity SRF linac. Until now, most elliptical SRF cavities, made by traditional technologies (deep-drawing and electron-beam welding), were at a frequency higher than the 650 MHz for the Project-X. The single-cell 500 MHz cavities for light sources were made by spinning or hydroforming. In the USA, there is only one example of a single-cell 400 MHz SRF cavity, which was made by JLab last year as the prototype of 3-cell SRF cavity for the BES-CLS project [4]. They encountered various difficulties at almost every step of the cavity fabrication and processing, mostly because of its big size and heavy weight. The vertical test result of this single-cell 400 MHz prototype cavity showed that it quenched at 8 MV/m (Q0 was $3 \times 10^9$ at 4.2 K) and the reason for quench is still not clear, although it is suspected to be due to electron-beam welding of the cavity’s equator. For comparison, the design of the eRHIC ERL requires SRF cavities to operate at 18.5 MV/m with a Q0 of $3 \times 10^{10}$. In contrast, the existing facilities (over the world) are able to handle 5-cell 647 MHz cavity, including cavity fabrication, processing and tests. At BNL, we made 3 704 MHz 5-cell cavities [5,6,7,8], which is very close to 647 MHz 5-cell cavity in terms of cavity, our facilities (BCP, HPR, high temperature bake oven and vertical test facility) were commissioned. Another practical point is the RF amplifier [9], the efficiency of the RF amplifiers between 650 MHz and 422 MHz is not different, but a 50 kW 650 MHz RF amplifier is more conventional than a 50 kW 422 MHz RF amplifier.

From a SRF linac point of view, if the real-estate gradient is the same, the high frequency linac is cheaper because of the cryomodule size is smaller, but extra costs may incurred due to the increase part count of tuners and couplers. The cryomodule size is particularly important for eRHIC because of the limit of the existing RHIC tunnel. Overall, the drawbacks of a 647 MHz 5-cell cavity linac may be compensated by other means. However, the risk of the 422 MHz choice is dramatically high because of the lack of fabrication experience and facilities to deal with it. Therefore, the development of 422 MHz SRF cavities requires a large investment in infrastructure. At the known frequency 647 MHz cavity SRF, the risk is largely alleviated.

2. FUNDAMENTAL MODE

The cavity was initially designed with the frequency of 422 MHz, the 5-cell 647MHz cavity is scaled from the original design, so the fundamental mode’s performance is the same. The 647 MHz 5-cell cavity is named as BNL4 cavity. However, the cavity’s length reduces from 2.56 m to 1.68 m. The fundamental mode’s performance of BNL4 cavities is listed in Table I. Figure 1 (top) shows Superfish model of the 647 BNL4 cavity. The field profile of the fundamental mode by Superfish is shown in Figure 1 (bottom).
Figure 1: BNL4 cavity configuration (top) and fundamental mode field profile (bottom).

<table>
<thead>
<tr>
<th>Parameters</th>
<th>422 MHz 5-cell cavity</th>
<th>647 MHz 5-cell cavity</th>
</tr>
</thead>
<tbody>
<tr>
<td>Frequency [MHz]</td>
<td>647</td>
<td>647</td>
</tr>
<tr>
<td>Number of cells</td>
<td>5</td>
<td>5</td>
</tr>
<tr>
<td>Geometry factor [Ω]</td>
<td>273</td>
<td>273</td>
</tr>
<tr>
<td>(R/Q)/Cavity [Ω]</td>
<td>502</td>
<td>502</td>
</tr>
<tr>
<td>Epeak/Eacc [mT/MV/m]</td>
<td>2.27</td>
<td>2.27</td>
</tr>
<tr>
<td>Bpeak/Eacc [mT/MV/m]</td>
<td>4.42</td>
<td>4.42</td>
</tr>
<tr>
<td>Coupling factor [%]</td>
<td>2.8</td>
<td>2.8</td>
</tr>
<tr>
<td>Cavity length [m]</td>
<td>2.56</td>
<td>1.68</td>
</tr>
</tbody>
</table>

### 3. MONOPOLE MODES AND HOM POWER

An average monopole mode HOM power generated by a single bunch travelling through a cavity is proportional to the bunch charge $Q_b$, beam current $I_b$, and the longitudinal loss factor $k_p$:

$$P_{\text{ave}} = k_p I_b Q_b$$  \(1\)
As the average HOM power is linear with the loss factor. The loss factor should be an important optimization factor for high current ERL machine. Calculated by ABCI [10], the loss factor for a 3 mm (rms) bunch excluding the fundamental mode was 2.55 V/pC, which can be handled by the reduction of the number of eRHIC ERL passes. As the bunch length for the eRHIC design may change, various bunch lengths were used to calculate for 647 MHz 5-cell cavity, which is shown in Figure 2.

With the nominal eRHIC beam parameters (7 passes at the maximum beam current of 26 mA ERL, 3 nC per bunch) for an intermediate energy, where the HOM power is maximal, an average value of monopole mode HOM power in one BNL4 cavity is 2.78 kW per cavity. However, this power can be higher or lower if one considers the beam spectrum. This presents a big challenge for removing it out of the cryostat and it has to be damped outside the cryomodule, so bunch pattern should be optimized for HOM power during the ERL design.

Figure 2: Integrated loss factors of the 647 MHz 5-cell BNL4 cavity for different rms bunch length.

4. TRANSVERSE BEAM-BREAK-UP (BBU)

The FFAG lattice based eRHIC design is a multi-pass (up to 12), high current ERL design. One important concern for the linac cavity design is to increase the beam break up (BBU) threshold current. The transverse BBU threshold beam current depends mainly on the strength of dipole HOMs. Assuming that HOMs behave independently and do not interfere with each other, the threshold current in the presence of a single HOM can be approximated as [11]

\[
I_{th} = \frac{2pc}{ek(R_d/Q)Q_{ext}M_{12}\sin(\omega T_r)} \tag{2}
\]

Where p is the particle momentum, c is the speed of light, e is the electron charge, k is the higher-order-mode’s wave number, R_d/Q is the shunt impedance and Q_{ext} is the quality factor, M_{12} is the transport matrix parameter, and T_r is the bunch return time. From the threshold current formula (2), it is clear that a small R_d/Q and/or Q_{ext} can
increase the threshold current. A smaller $Q_{\text{ext}}$ means shorter damping time and larger current needed to deposit enough energy to disturb the beam.

One should notice that this formula fits for one cavity, one pass case. Although it is inversely proportional to the frequency, the threshold current reduces, in the worst case approximately as the square of number of passes. BBU code simulation shows that the threshold current of BNL4 cavity for eRHIC has at least a factor of 4 above the operation beam current, for a zero frequency spread due to fabrication (usually it is around a few MHz spread) in the HOM spectrum.

5. MECHANICAL DESIGN AND PROTOTYPE CAVITY

In eRHIC design, the electron beams will collide with different proton energies from 40 GeV to 250 GeV, which corresponds to a frequency shift up to 174 kHz for 647 MHz cavity. ANSYS simulation shows that the cavity’s tuning sensitivity is 84 kHz/mm, so the tuning range requirement for BNL4 cavity is 2 mm. With a 4 mm thickness of Nb sheet, the cavity can be tuned up to 2.0 mm without exceeding the yield strength of Nb: 7000 psi, which is shown in Figure 5.

![Figure 5: 5-cell prototype of the BNL4 cavity, 4mm thick without stiffness ring.](image)

6. SUMMARY

The first part of this paper describes the frequency considerations for the eRHIC ERL. Although there are a few physics benefits by using a low frequency (422 MHz 5-cell cavity) linac, there are critical practical issues that increase the risk of the project. So, 647 MHz 5-cell cavity is the baseline of the eRHIC SRF ERL. The second part of this paper discusses the physics and mechanical design of the 5-cell 647 MHz cavity.
REFERENCES
2. S. Belomestnykh, et al., “On the frequency choice for the eRHIC SRF linac,” IPAC2014, p. 1547
9. Private communication with Alexander Zaltsman.