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Memristors with diffusive dynamics as synaptic emulators for neuromorphic computing

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Abstract

The accumulation and extrusion of Ca^{2+} in the pre- and postsynaptic compartments play a critical role in initiating plastic changes in biological synapses. To emulate this fundamental process in electronic devices, we developed diffusive Ag-in-oxide memristors with a temporal response during and after stimulation similar to that of the synaptic Ca^{2+} dynamics. *In situ* high-resolution transmission electron microscopy and nanoparticle dynamics simulations both demonstrate that Ag atoms disperse under electrical bias and regroup spontaneously under zero bias because of interfacial energy minimization,

closely resembling synaptic influx and extrusion of Ca^{2+} , respectively. The diffusive memristor and its dynamics enable a direct emulation of both short- and long-term plasticity of biological synapses and represent a major advancement in hardware implementation of neuromorphic functionalities.

CMOS circuits have been employed to mimic synaptic Ca^{2+} dynamics, but three-terminal devices bear limited resemblance to bio-counterparts at the mechanism level and require significant numbers and complex circuits to simulate synaptic behavior¹⁻³. A substantial reduction in footprint, complexity and energy consumption can be achieved by building a two-terminal circuit element, such as a memristor directly incorporating Ca^{2+} -like dynamics. Various types of memristors based on ionic drift (drift-type memristor)⁴⁻⁸ have recently been utilized for this purpose in neuromorphic architectures⁹⁻¹⁵. Although qualitative synaptic functionality has been demonstrated, the fast switching and non-volatility of drift memristors optimized for memory applications do not faithfully replicate the nature of plasticity. Similar issues also exist in MOS-based memristor emulators¹⁶⁻¹⁸, although they are capable of simulating a variety of synaptic functions including spike-timing-dependent plasticity (STDP). Recently, Lu's group adopted second-order drift memristors to approximate the Ca^{2+} dynamics of chemical synapses by utilizing thermal dissipation¹⁹ or mobility decay²⁰, which successfully demonstrated STDP with non-overlapping spikes and other synaptic functions, representing a significant step towards bio-realistic synaptic devices. This approach features repeatability and simplicity, but the significant differences of the dynamical response from actual synapses limit the fidelity and variety of desired synaptic functions. A device with similar physical behavior as the biological Ca^{2+} dynamics would enable improved emulation of synaptic function and broad applications to neuromorphic computing. Here we report such an emulator, which is a memristor based on metal atom diffusion and spontaneous nanoparticle formation, as

determined by *in situ* high-resolution transmission electron microscopy (HRTEM) and nanoparticle dynamics simulations. The dynamical properties of the diffusive memristors were confirmed to be functionally equivalent to Ca^{2+} in bio-synapses, and their operating characteristics were experimentally verified by demonstrating both short- and long-term plasticity, including mechanisms that have not been unambiguously demonstrated previously.

The diffusive memristor illustrated in Figure 1a consists of two Au electrodes sandwiching a switching layer of a dielectric film with embedded Ag nanoclusters (Methods). X-ray photoelectron spectroscopy (XPS) revealed that the Ag was metallic, which was further confirmed by HRTEM micrographs showing Ag nanocrystals in $\text{SiO}_x\text{N}_y:\text{Ag}$ (Supplementary Fig. S1-S2). These devices are similar to electrochemical metallization memory (ECM)²¹⁻²⁶ cells in terms of utilizing mobile species of noble metals, but they differ substantially in terms of the structural symmetry and operating voltage polarities, metal concentration and profile, and transient switching behaviour. An applied voltage above an apparent threshold abruptly switched the device to a conductance state limited by an external compliance current (Fig. 1b). To demonstrate that the device spontaneously relaxed back to an insulating configuration upon removing the bias (without applying an opposite polarity voltage), repeatable I-V loops with only positive applied voltages were used in collecting the data in Fig. 1b. Symmetric hysteresis loops were observed with the opposite polarity bias (Supplementary Fig. S3), showing that the threshold switching is unipolar in nature and significantly different from non-volatile drift-type memristors, especially in the OFF-switching process. The micro-devices represented by Fig. 1a have an area of $10\mu\text{m}\times 10\mu\text{m}$ and nano-devices with an area of $100\text{nm}\times 100\text{nm}$ exhibited similar switching behaviours (Supplementary Fig. S4). The resistance ratio between the conducting and insulating states was 5-orders of magnitude in $\text{SiO}_x\text{N}_y:\text{Ag}$ and over 10-orders in $\text{HfO}_x:\text{Ag}$ devices, the highest reported in threshold switching devices so far²⁷⁻³⁰. The volatile

switching had sharp turn-on slopes of $\sim 10\text{mV/decade}$ in $\text{MgO}_x\text{:Ag}$ and $\text{SiO}_x\text{N}_y\text{:Ag}$, and an extraordinary $\sim 1\text{mV/decade}$ in $\text{HfO}_x\text{:Ag}$, the sharpest demonstrated to date²⁷⁻³⁰. The high current capability and large resistance ratio enable diffusive memristors to be utilized as selectors for mitigating sneak current paths in crossbar arrays²⁷⁻³⁰. In Fig. 1c, each 500ns/1.5V switching pulse was followed by a 500ns/0.2V reading pulse to verify that the device had relaxed back to the insulating state under zero bias within 5 μs after switching to the high conductance state. Repeatable and symmetric switching was demonstrated using wider bipolar voltage pulses with over a million switching cycles in Fig. 1d.

To examine the switching mechanism, especially the spontaneous relaxation to the insulating state upon ceasing power, a planar $\text{Au/SiO}_x\text{N}_y\text{:Ag/Au}$ device with a nano-junction was fabricated for *in-situ* HRTEM characterizations (Supplementary Fig. S5a). Reliable threshold switching was observed under a 100nA compliance in ambient conditions with a typical relaxation time constant of $\sim 11\text{ms}$ (Supplementary Fig. S5b-c). In the time sequence of HRTEM images in Fig. 2 (Supplementary Videos), the gap between the Au electrodes first experienced a constant voltage (20V) with an 100nA compliance from 0s to 5s, after which the power was turned off. We observed a delay time of $\sim 2\text{s}$ during which the measured current was $< 5\text{nA}$ and Ag nanoparticles formed in the gap region (indicated by the orange and blue arrows at time 0.1s), followed by an abrupt current jump to the compliance level as nanoparticles grew further to bridge the gap between the electrodes (indicated by the red arrow at 2.5s). At 4.6s, the cluster reached a diameter of $\sim 4.2\text{nm}$.

Up to this point, the behaviour of Ag nanoparticles in SiO_xN_y is similar to previous observations, which have been interpreted as electrochemical reactions at effectively bipolar electrodes²¹⁻²⁶. We next turned off the power at 5.0s to observe the spontaneous relaxation,

which is critical for understanding the dynamics of these devices, but has not been previously reported to the best of our knowledge. The elongated cluster of nanoparticles that had likely formed the conductive bridge rapidly contracted from a length of 14.8nm to a circular profile with a diameter of 7.6nm by 5.7s, indicating Ostwald ripening³¹. These observations demonstrated that minimizing the interfacial energy between the Ag nanoparticles and the dielectric served as the driving force for the relaxation dynamics of these diffusive memristors. The material systems exhibiting a substantial relaxation were those with large wetting contact angles³², such as MgO_x:Ag, SiO_xN_y:Ag, and HfO_x:Ag in Fig. 1b, consistent with the reported pseudoelasticity of silver nanoparticles³³ and the hypothesis that interfacial energy facilitates filament rupture in volatile switching³⁴⁻³⁶.

The dynamical properties of diffusive memristors were further studied by applying voltage pulses and measuring resulting currents. Under an applied pulse, the device exhibited threshold switching to a low resistance state after an incubation period τ_d , as shown in Fig. 3a. This τ_d is related to the growth and clustering of silver nanoparticles to eventually form conduction channels. Upon channel formation, the current jumped abruptly by several orders of magnitude, and then slowly increased further under bias as the channel thickened. As the voltage pulse ended, the device relaxed back to its original high resistance state over a characteristic time τ_r . As shown in Fig. 3b, τ_r decreased as the ambient temperature increased, consistent with a diffusion activation energy of 0.27eV (inset of Fig. 3b), and the characteristic time was on the same order as the response of bio-synapses, i.e., tens of ms. In addition to the temperature, τ_d and τ_r were also functions of the voltage pulse parameters, operation history, Ag concentration, host lattice, device geometry, humidity, and other factors³⁷⁻⁴⁰, which alone or combined could be used to tune the desired dynamics for neuromorphic systems (Supplementary Fig. S6).

To better understand the switching mechanism, we performed simulations using a generalized model similar to the one utilized for non-volatile switching and current noise in TaO_x memristors⁴¹. This model links electrical, nano-mechanical and thermal degrees of freedom (Methods). The model results here did not include redox reactions, although they can be added in order to more closely resemble the electrochemical models proposed previously²¹⁻²⁶.

In our simulations, two large clusters of metallic nanoparticles are located near each terminal of the device (Fig. 4a1). When a voltage pulse is applied (Fig. 4a), the local temperature increases due to Joule heating and the potential is tilted by electric forces acting on particles with induced charge, both of which cause larger clusters to break up. As the nanoparticles become more uniformly distributed in the gap, the resistance drops, the current and temperature increase, and a positive feedback results in the formation of a conductive channel (Fig. 4a2). As soon as the power is turned off, the temperature drops, and the nanoparticles start to coalesce (Fig. 4a3), i.e. particles slowly diffuse to their minimum energy positions near the device terminals. Eventually, most of the nanoparticles have merged into larger clusters to minimize interfacial energy, and the high resistance state is re-established along with the original particle distribution almost restored (compare Fig. 4a1 and Fig. 4a4), leading to the observed volatility in Fig. 2. The model predicts interesting conductance evolution similar to synaptic behavior when a train of pulses is applied (Fig. 4b). First, when the initial voltage pulse is applied, electric field-assisted diffusion pumps some of the Ag-particles out of the ‘left’ cluster and they start to bridge terminals. However, a single short pulse cannot excite enough particles to form a complete conducting path between the two terminals (Fig 4b2). If a subsequent pulse arrives before particles are re-absorbed, i.e., if the time between pulses is shorter than the diffusion relaxation time, more particles are pushed into the gap between terminals resulting in a gradual increase in device conductance, similar to the paired-pulse facilitation (PPF) phenomenon in

bio-synapses. The result is that when high frequency pulses are applied, the device conductance increases with the number of pulses (Fig. 4b) until a conducting bridge is formed (Fig. 4b1-b4). Second, as the electric field pumps more and more particles towards one of the device terminals, the number of particles at the other terminal decreases (Fig 4b4-4b5, where the distribution peak at the left terminal decreases as more and more pulses arrive). As a result, the number of particles in the gap decreases (Fig 4b5-4b6) and the device conductance starts to decay. This results in an inflection of the device conductance due to excessive stimulation, capturing another synaptic behaviour, i.e., PPF followed by PPD (paired pulse depression). Third, sequential high voltage pulses with a long enough interval (low frequency) may form a conducting bridge first, but before the next pulse arrives the bridge breaks and the particles are re-absorbed at the terminals. Due to the electric field, the Ag particles gradually deplete at one terminal and accumulate at the other. Consequently, the conductance of the device starts to decrease from the initial state without showing facilitation first (PPD). (Supplementary Fig. S7c).

The simulations for Ag in dielectric agreed well with the experimental HRTEM observations. In addition, significant similarities exist between the Ag dynamics and that of synaptic Ca^{2+} , not only in the diffusion mechanism but also in their dynamical balance of concentration and regulating roles in their respective systems. Ca^{2+} dynamics is responsible for initiating both short- and long-term plasticity of synapses, forming the basis of memory and learning⁴²⁻⁴⁴. In chemical synapses, the dynamical balance of the Ca^{2+} concentration is shaped by both influx via voltage-sensitive calcium channels (VSCC) and N-methyl-D-aspartate receptors (NMDAR)^{42,43}, and extrusion via the plasma membrane Ca^{2+} -ATPase (PMCA) and $\text{Na}^+/\text{Ca}^{2+}$ exchanger (NCE)^{43,44} that restores $[\text{Ca}^{2+}]_i$ to the basal concentration. The Ca^{2+} dynamics naturally leads to short-term plasticity in which residual elevation of presynaptic $[\text{Ca}^{2+}]_i$

directly correlates to the enhancement of synaptic transmission⁴³⁻⁴⁵. The calcium inside the postsynaptic membrane also plays important regulating roles in long-term potentiation and depression where Ca^{2+} accumulation is necessary to regulate enzymes, i.e. Ca^{2+} /calmodulin-dependent protein kinase II (CaMKII), calcineurin, and protein phosphatase 1^{42,43,46,47}, which in turn triggers rapid and persistent modification of synaptic strengths by changing the number and/or conductance of α -amino-3-hydroxy-5-methyl-4-isoxazolepropionic acid receptors (AMPA)^{43,46,47}. The Ag diffusion into the gap region between Ag nanoclusters with field assistance (Fig. 2 and Fig. 4), resembles the influx processes of Ca^{2+} . The clearance of bridging Ag nanoparticles from the gap region by Ostwald ripening when electrical stimulus is removed replicates the extrusion processes of Ca^{2+} . Thus, the Ag dynamics of the diffusive memristor is a functional emulation of bio-synapses (Fig. 5a). An expected characteristic of diffusive memristors is short-term plasticity, where application of paired pulses to synapses can induce an increase or decrease in postsynaptic responses, depending on the frequency of applied pulses. As shown in Fig. 5b, when the time interval between pulses (t_{zero}) is short (high frequency), the device conductance increases (PPF) from its initial conductance (steady state of the diffusive memristor) as the number of pulses increases. In contrast, a long t_{zero} (low frequency) leads to a reduced rate of increment or even a decrease in conductance (PPD) from the same initial conductance (Inset of Fig. 5b and Supplementary Fig. S7a-b)^{45,48}. Moreover, it has also been shown in bio-synapses that prolonged or excessive stimulations with high-frequency (short t_{zero}) pulses will eventually lead to an inflection from facilitation to depression, an effect solely induced by an increased number of stimulation pulses at the same frequency⁴⁵. This important feature of bio-synapses, which has not been clearly demonstrated previously on two terminal devices, was predicted in Fig. 4b and observed experimentally in Fig. 5c. The device in its steady state shows PPD upon low frequency (196Hz) stimulation and experiences an increase in current (facilitation) once the stimulation frequency is raised (5000Hz). The facilitation turns

into depression (current decrease) with more pulses having identical frequency (5000Hz) due to the gradual depletion of silver at one electrode and accumulation at the other. The depression continues with the low-frequency (196Hz) pulses, which eventually bring the device back to a state close to its initial steady state, implying the potential for autonomic computing^{48,49}.

The above PPF and PPD demonstrations were realized with diffusive memristors only, resembling short-term plasticity⁴⁵ in synapses because any conductance change from the OFF state of diffusive memristors will vanish over time. When combined with a non-volatile element, i.e., a drift-type memristor, long-term plasticity⁵⁰ following the spike-rate-dependent plasticity and STDP^{47,50} learning rules can be realized. For demonstration purposes, we created a combined circuit element using a diffusive memristor in series with a Pt/TaO_x/Ta/Pt drift memristor (Supplementary Fig. S8). This combined element was connected to pulsed voltage sources similar to a synapse between pre- and post-synaptic neurons (Fig. 6a). The spike-rate-dependent potentiation demonstration is illustrated in Fig. 6b, where the drift memristor weight (conductance) change is a function of the frequency of the applied pulses. Similar to Fig. 5b, a shorter t_{zero} resulted in a greater increase in the conductance of the diffusive memristor and thus a larger voltage drop across the drift memristor, which thereby switched due to the voltage divider effect. A longer t_{zero} resulted in a smaller increase in the diffusive memristor conductance and thus a smaller voltage drop across the drift memristor, leading to a smaller or non-detectable resistance change in the drift memristor.

To demonstrate STDP learning rules with non-overlapping spikes, pre and post-synaptic spikes (Fig. 6c) were applied to the combined element. The two spikes were separated by a time difference Δt , which determined how much conductance change was programmed in the drift memristor. Each spike consisted of two parts, a high voltage short pulse and a low voltage long

pulse. The pre-spike and post-spike were equal in magnitude but opposite in voltage polarity (Fig. 6c). In the combined element, the resistance of the diffusive memristor in its OFF state is much larger than that of the drift memristor, while the resistance of its ON state is much smaller than that of the drift memristor. Because the diffusive memristor has a finite delay time, the short high voltage pulse will not turn it ON. In contrast, the long voltage pulse with a lower amplitude will turn ON the diffusive memristor. The drift memristor is not switched by the first spike, because the majority of the voltage drops across the diffusive memristor and turns it ON first. After the spike ends, the resistance of the diffusive memristor gradually increases from its ON state over time, regulated by the diffusive dynamics. The second spike occurs at a time Δt from the end of the first spike, and it may or may not switch the drift memristor depending on how much voltage drops on the drift memristor, which is determined by the conductance of the diffusive memristor at that moment, a function of Δt . A smaller Δt corresponds to a smaller diffusive memristor resistance and results in a greater resistance change in the drift memristor and vice versa (Fig. 6d). If the pre-spike appears before the post-spike, the drift memristor conductance increases (potentiation). If the pre-spike follows the post-spike, depression occurs. (Supplementary Fig. S9) Because the dynamics of the diffusive memristor provides an intrinsic timing mechanism for the combined element, the spike-rate-dependent plasticity and STDP do not require complex pulse engineering or spike overlapping. This substantially reduces the complexity of both circuit and algorithm design and enables low-energy operations. In addition, depending on the application, any non-volatile memristor (low/high retention, analog/digital) can be used along with the diffusive memristor, allowing a significantly broader choice of materials rather than relying on the properties of the drift memristor when used alone. (See Supplementary Fig. S10 for STDP demonstration with a Pt/HfO_x/TiN drift memristor)

In conclusion, we have constructed and demonstrated a new class of memristors as synaptic emulators that function primarily based on diffusion (rather than drift) dynamics. The microscopic nature of both the threshold switching and relaxation of the diffusive memristor is revealed for the first time by *in situ* HRTEM and explained by nanoparticle dynamics simulation. The Ag dynamics of the diffusive memristors functionally resemble the synaptic Ca^{2+} behavior in chemical synapses and lead to a direct and natural emulation of multiple synaptic functions for both short-term and long-term plasticity, such as PPF, PPD, PPD following PPF, SRDP and STDP. In addition to providing a synapse emulator, the diffusive memristor can also serve as a selector with a large transient nonlinearity that is critical for the operation of a large crossbar array as a neural network. The results here provide an encouraging pathway toward synaptic emulation using diffusive memristors for neuromorphic computing.

Methods

Preparation of crossbar samples. The diffusive memristor devices were grown on p-type (100) Si wafer with 100nm thermal oxide. The bottom electrodes were patterned by photolithography followed by evaporation and liftoff of a ~20nm thick Pt(Au) layer. The ~15nm thick doped dielectric was deposited at room temperature by reactively co-sputtering MgO or HfO_2 (99.99%, Kurt Lesker) and Ag (99.99%, Kurt Lesker) in an ambient of mixed Ar and O_2 , or co-sputtering Si (99.99%, Kurt Lesker) and Ag in Ar, N_2 , and O_2 . The ~30nm Pt(Au) top electrodes were subsequently patterned by photolithography followed by evaporation and liftoff processes. Electrical contact pads of the bottom electrodes were first patterned by photolithography and then subjected to reactive ion etching with mixed CHF_3 and O_2 gases.

The drift memristor devices used the same substrates and bottom electrodes as the diffusive memristor devices. The switching layer was grown by sputtering Ta_2O_5 (HfO_2) for a thickness

of ~10(5)nm in Ar gas followed by photolithography. Top electrodes were deposited by evaporating Ta(5nm)/Pt(20nm) (sputtering TiN(50nm)/Pd(30nm)) and liftoff.

Electrical Measurements. Electrical measurements were performed with the Keysight B1500A semiconductor device analyser using two of its modules: DC measurements were carried out using the source and measure units (B1517A) and the B1530A waveform generator/fast measurement unit (WGFMU) was used to perform the pulse measurements. Using a two-probe (W tips) configuration, we applied DC and pulse voltages between the top and bottom electrodes of the device and measured current through one of the measurement units. The same units were used to perform measurements at different temperatures on the Variable Temperature Micro Probe System (MMR technologies, K2000 Digital Temperature Controller) in ambient atmosphere. We performed the rate-dependent plasticity and the STDP experiments with the diffusive memristor in series with a Pt/TaO_x/Ta/Pt drift memristor. The B1530A WGFMU was used for applying the pre and spike-post-synaptic voltage spikes. The conductance of the drift memristor was read using a small DC voltage between each programming operation to determine the change in its weight. For each data point of the spike-rate-dependent plasticity measurement, the drift memristor was first initialized to its high resistance state, and then we applied 15 voltage pulses across the combined series memristors with the same pulse amplitude (2.5V), duration (40μs) and a particular t_{zero} value, and finally read the drift memristor to determine the change in its state induced by the train of 15 pulses.

Preparation of planar samples for TEM. The specimen for in situ HRTEM was grown on the Aduro E-chip with pre-built Au connections (Model E-AEL00-LN, Protochip). Au electrodes are patterned by electron beam lithography followed by evaporation and liftoff of a ~20nm thick Au layer. The doped dielectric layer of SiO_xN_y:Ag was deposited by reactively

co-sputtering of both Si and Ag targets in an ambient of Ar, N₂, and O₂ at room temperature with a thickness of ~30nm.

***in situ* TEM.** The *in situ* HRTEM was performed at Brookhaven National Laboratory with the FEI Titan 80-300 operating at 300keV. The sample was grown on a Aduro E-chip (Model E-AEL00-LN, Protochip) which was mounted on a corresponding Aduro TEM holder for FEI (Protochip). Current was monitored in real-time on a Keithley 2602B System SourceMeter which exerted electrical bias.

Diffusive memristor dynamical simulations.

The diffusive memristor model links electrical, nano-mechanical and heat degrees of freedom: (a) the growth, shape change and decay of clusters of nanoparticles identified by their positions x_i inside a device (i is the nanoparticle label), (b) the electric current through the device governed by a sequence of tunnelling resistances between nanoparticles, and (c) the local temperature controlling the nanoparticle diffusion, determined by Joule heating and the thermal conductivity of the memristor.

The mathematical definition for a *generic memristor*⁴ has two components, the quasi-static conduction equation relating voltage v and current i , or Ohm's law for the element

$$v = iR(\mathbf{x}), \quad (1)$$

where R is the state-dependent resistance and \mathbf{x} represents one or more *state variables* that define the physical properties of the memristor, and the dynamical equation(s) that define the evolution of the state variables with time in the presence of a current and affected by local temperature T :

$$\frac{d\mathbf{x}}{dt} = f(\mathbf{x}; i, T), \quad (2)$$

For the state-dependent resistance we assume sequential electron tunnelling: first from the input terminal to the nearest metallic nanoparticle, and then from this nanoparticle to the next

one and so on with the last tunnelling event to the output terminal. The total resistance of the memristor is the sum of tunnelling resistances between $N-1$ adjacent nanoparticles/islands:

$$R_M = \sum_0^N R_t \exp[(x_{i+1} - x_i)/\lambda], \quad (3)$$

with λ the effective tunnelling length, R_t the tunneling resistance amplitude (assumed the same for all islands), x_0 and x_N the spatial coordinates of the input and output terminals, respectively, and we order the island positions as $x_0 < x_1 < x_2 < \dots < x_{N-1} < x_N$. The minimum resistance can be estimated as $R_{min} = \min R_M = NR_t \exp[2/N\lambda]$.

To describe the nanoparticle diffusion, and thus the memristor dynamics, we employed an overdamped Langevin equation for each mobile metallic nanoparticle trapped by a potential U and subject to a random force ξ_i , the magnitude of which is determined by the device local temperature T ,

$$\eta \frac{dx_i}{dt} = -\frac{\partial U(x_i)}{\partial x_i} + \alpha \frac{V(t)}{L} + \sqrt{2\eta k_B T} \xi_i, \quad (4)$$

In the equation (4) the friction term (left hand side), proportional to the particle velocity and viscosity η , is balanced by all other forces acting on nanoparticles. The first term on the right hand side of Eq. 4 forces the nanoparticle to approach the minimum potential energy with a speed that is proportional to minus the local gradient of the potential energy. The drift term $\alpha V(t)/L$ represents a bias in the electric field $E = V(t)/L$ affecting nanoparticle with induced charge α when the voltage is on. The electrical bias together with diffusion is responsible for switching to a high conducting state and depletion of nanoparticles at one of the device terminals. The random force, $\sqrt{2\eta k_B T} \xi_i$, which is driven by the instantaneous temperature, describes diffusion of the nanoparticles that occurs both when voltage is on and when the system relaxes with no bias toward the potential minimum after the power to the device is off and the local temperature cools. In other words, since T is nonzero, there will always be some

diffusion of the nanoparticles modelled by adding random thermal fluctuations ξ_i , which are δ -correlated white noise characterized by $\langle \xi \rangle = 0$ and $\langle \xi(0)\xi(t) \rangle = \delta(t)$.

The potential $U = U_I + U_p$ has two energy scales – the interfacial energy U_I responsible for formation of large metallic clusters near the device terminals and a weaker nanoparticle-pinning energy U_p with many smaller wells between the electrodes. Pinning can occur through interactions of the nanoparticles with impurities, the substrate and/or the ionic lattice⁴¹. For

our simulations we used $U_I = -w_I \left[\exp\left(-\frac{(x_i+x_0)^2}{R_I^2}\right) + \exp\left(-\frac{(x_i-x_0)^2}{R_I^2}\right) \right]$ and $U_p =$

$\frac{w_p}{2} \sin\left(2\pi \frac{x}{R_p}\right)$, with the interfacial energy barrier w_I and the amplitude w_p of the pinning

potential. The particular shape of neither the interfacial potential nor the pinning energy profile are essential; the only property that matters is that the potential U has two different energy scales and the weaker pinning potential has many wells (for example it can be random with fluctuating w_p and R_p). At high enough temperature during a voltage pulse, the increased diffusion assisted by the electrical force breaks up the large nanoparticle clusters and populates the pinning sites. At lower temperatures after the power is off and the potential bias disappears, the nanoparticles re-aggregate to form clusters at the electrodes. Moreover, a qualitatively similar result (although requiring considerably more computational resources) has been obtained when we modelled the interfacial energy as an interaction between particles⁴¹.

The temperature dynamics are determined by Newton's law of cooling:

$$\frac{dT}{dt} = C_T Q - \kappa(T - T_0), \quad (5)$$

with the Joule heating power $Q = V^2/R_M$ increasing the temperature of the system and thermal conductivity acting as a damping factor by removing energy from the system. Here, κ and C_T are the heat transfer coefficient and heat capacitance respectively, while the background temperature is T_0 . Equations (4) and (5) are sufficient to describe the memristor dynamics

subject to the current through the device, which is controlled by the electric circuit in which it is embedded. Thus, the model described above enables the simulation of a complex system consisting of both volatile and non-volatile memristors.

There are two time scales in the model, the diffusion time scale and the characteristic scale of temperature relaxation. The first one depends on temperature, potential profile, and electric drift, thus, this time scale changes depending on voltage pulse intensity and temperature. For this reason, we measure all time in the simulations in units of the temperature relaxation time $1/\kappa$. As one can see from Fig. 4, the relaxation occurs on time scales of the order 10-20 $1/\kappa$, thus, the simulated system is clearly governed by diffusion rather than the temperature relaxation¹⁹. There are two conductance states with low and high conductance. We used the conductance $1/R_{min}$ in the high conductance state as a normalization factor. The normalization enabled the simulated conductance to be plotted as a percentage of its maximum conductance after each applied pulse, for instance, from Fig 4b we conclude that the conductance reached 25% of the maximum after 4 pulses and about 75% after 7 pulses. To provide a better link to the experimental data, we normalized the voltages to the threshold voltage V_{th} , which was assumed to be the voltage where the conductance reached 10% of its maximum value. These quantities can be easily obtained from both simulations (averaged over 30 realizations) and experimental I-V hysteresis loops, thus directly linking the units in the simulations and the experiments. For the sake of consistency, we normalized all voltages to V_{th} at the highest simulated temperature, $\frac{k_B T}{w_p} = 0.45$. The temperature $\frac{k_B T}{w_p}$ in the simulations was varied from 0.3 to 0.45 (i.e, the same relative range as in Fig. 3b). In this range the characteristic single hopping time scale $e^{w_p/k_B T}$ changed from about $2/\kappa$ to $6/\kappa$ and the diffusion relaxation time (estimated as a characteristic jump time multiplied by the number of jumps to reach the interfacial minimum near the device terminal) was about $20/\kappa$ to $60/\kappa$. The ratio of interfacial and pinning potentials w_l/w_p was assumed to be 4.5 in the simulations to ensure that the

interfacial potential was strong enough to re-trap the Ag nanoparticles after the voltage was switched off and the thermal fluctuations were too weak to destroy the large clusters near the terminals in the absence of excess heating. Conversely, the electric force ($\alpha V_{th} R_p / w_I = 0.3$ in the simulations) was used to suppress the interfacial barrier $k_B w_I / T$ to about 3.6, which enabled the enhanced thermal fluctuations induced by Joule heating to activate the positive thermal feedback. The stronger fluctuations support larger Joule heating and vice versa, breaking up the large Ag clusters to form a string of smaller nanoparticles and thus a conductive path between the terminals, as observed experimentally in the HRTEM studies. Note that we also linked some model parameters with experimentally measurable ones, e.g., $C_T \approx \kappa w_p R_t / V_{th}^2 k_B$, $\eta \approx w_p / \kappa L^2$, and $\alpha \approx \eta \kappa L^2 / V_{th}$.

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Author contributions:

J.J.Y. conceived the concept. J.J.Y., Q.X., Z.W. and S.J. designed the experiments. Z.W. fabricated the devices and S.J. performed electrical measurements. S.E.S. performed the simulation. H.L.X. carried out the in-situ TEM characterizations. H.J., R.M., P.L., M.H., N.G., J.P.S., Z.L., Q.W., M.B., G.-L.L., and R.S.W. helped with experiments and data analysis. J.J.Y., Q.X., Z.W., S.J., S.E.S., and R.S.W. wrote the paper. All authors discussed the results and implications and commented on the manuscript at all stages.

Additional information

Supplementary information is available in the online version of the paper. Reprints and permissions information is available online at www.nature.com/reprints. Correspondence and requests for materials should be addressed to J.J.Y.

Competing financial interests

The authors declare no competing financial interests.

Figure Captions

Figure 1 Highly non-linear, fast, and repeatable threshold switching behaviours of diffusive memristors (a) Pseudo-colour scanning electron micrograph of a crossbar device. Top electrodes are depicted by the red dashed line and bottom contacts by the blue dashed line. Biasing is applied on the top electrode with the bottom electrode grounded. The inset shows an atomic force microscopy (AFM) image of the junction. (b) Repeatable highly non-linear threshold switching I-V loops for devices with different host lattices doped with silver. (c) High-speed switching characteristics of the $\text{SiO}_x\text{N}_y:\text{Ag}$ device at an elevated temperature of 600K. The programming pulse width is 500 ns and the voltage is 1.5V. (d) Endurance-cycling performance test of the $\text{SiO}_x\text{N}_y:\text{Ag}$ device for 1 million cycles at room temperature. The inset shows the shape of the applied voltage pulse, which consists of four segments: a 1.4V/200 μs programming voltage and a 0.14V/200 μs read voltage, followed by a -1.4V/200 μs programming voltage and a -0.14V/200 μs read voltage. We sampled one voltage and one current data point from each of the four segments of the pulse. The voltage samples are shown in red, while the purple dots and green dots correspond to device current due to positive and negative programming pulses, respectively. The read current for both positive and negative

programming is at the instrument noise level ($<100\text{nA}$) for the current measurement range used. The device did not fail during the measurement, demonstrating high robustness.

Figure 2 *In situ* TEM observation of the threshold switching process suggesting the relaxation is a diffusion process driven by interfacial energy minimization. External electric field is exerted at the point of time zero. Ag migration is observed at time 0.1s when two nanocrystals started to form. A clear arc-shaped filament is visible at 2.5s. When the external biasing is removed at 5.0s, the filament starts to deform, shrinking to a round spherical nanocluster implying an interfacial energy driven diffusion mechanism. All scale bars, 20nm.

Figure 3 Timing mechanism of $\text{SiO}_x\text{N}_y:\text{Ag}$ diffusive memristor. (a) Delay and relaxation characteristics of the device showing variation of current (blue) with applied voltage (red) pulses. Multiple read voltage pulses of (0.05V, $10\mu\text{s}$) are used to study the device relaxation current after the switching pulse (0.75V, 5ms). The device requires a finite delay time to turn ON and has a finite relaxation time before it goes to the high resistance state after the switching pulse is removed. (b) Device relaxation performance showing the variation of current with applied voltage at different temperatures. The relaxation time decreases with increasing temperature. Inset shows the Arrhenius plot of the temperature dependence of the relaxation time. Each data point (black circles) is an average over 10-15 measured relaxation times, and are fitted to the blue line. The activation energy for the material system is calculated to be 0.27eV.

Figure 4 Simulated operation of a diffusive memristor device. (a) The conductance response (blue curve) induced by a voltage pulse (red curve) shows a delay in the response and a gradual relaxation towards the low conducting state, consistent with the experimental threshold switching property in Fig. 3a. Panels (a1-a4) show evolution of metallic nanoparticle density distributions. Blue curves represent particle distributions. Each curve was averaged over temporal interval $0.2/\kappa$ around time moments indicated by orange dots (in (a)) when

instantaneous particle snapshots (red dots) are plotted. The inset shows the temperature dependence of the relaxation time τ defined as the time needed for the conductance to drop to value $0.02G_{max}$ after switching the voltage, which agrees with that of Fig. 3b. The red curve is the fitting of $\ln(\kappa\tau_r)$ by the function $A + B w_p/k_B T$ with $A = 0.1$, $B = 1$. (b) The simulated conductance response (blue curve) showing both facilitation and then depression upon a sequence of short and frequent pulses (red curve). Panels (b1-b6) show evolution of metallic nanoparticle density. Blue curves represent particle distributions, each curve was averaged over temporal interval $0.02/\kappa$, around time moments indicated by orange dots (in (b)) when instantaneous particle snapshots (red dots) are plotted. The conductance initially increases with number of pulses until a conducting-bridge between terminals is formed. The conductance eventually saturates and drops as the number of pulses increase further, which captures an advanced synaptic behaviour, i.e., PPF followed by PPD. Other simulation parameters are $\lambda/2 = R_I = 2R_p/3 = L/10$, $x_0 = 0.85L$, we simulate a hundred of nano-metallic particles and the simulation step was $dt = 2 \times 10^{-6}$ resulting in 10^7 steps during each simulation run; the reasoning of parameters choice and pinning parameters are discussed in the method section.

Figure 5 Schematic illustration of the analogy between Ca^{2+} and Ag dynamics, and short term synaptic plasticity of the diffusive memristor. (a) (left) Diffusion of Ca^{2+} from extracellular sources via VSCC and NMDAR, and the removal of Ca^{2+} via PMCA and NCE. (right) Ag diffusion into the gap region between Ag nanoclusters with field assistance and clearance of Ag filament from the gap region by the interfacial energy or mechanical stress once the voltage signal is removed, which is a close emulation of Ca^{2+} dynamics. (b) Experimental demonstration of short-term synaptic paired-pulse facilitation (PPF) and depression (PPD) behaviour with the diffusive $\text{SiO}_x\text{N}_y\text{:Ag}$ memristor. Device current response (blue) to multiple subsequent voltage pulses (3V, 1ms). The duration between two pulses when the applied

voltage is 0V is denoted as t_{zero} . For small t_{zero} , the current increases with the number of pulses giving larger conductance (weight) change, demonstrating paired-pulse facilitation. Inset shows the percentage change in conductance (weight) for different t_{zero} values. As the t_{zero} increases from 1 ms to 160ms, the weight change slows down with increasing pulse number and eventually becomes negative. (c) Experimental demonstration of PPD following PPF in the diffusive $\text{SiO}_x\text{N}_y\text{:Ag}$ memristor. Device current (blue) response to a train of voltage pulses (2.8V, 100 μs) of the same amplitude but different frequencies. The device begins with PPD (depression) upon low frequency (196Hz) stimulation and experiences an increase in current (facilitation) once the stimulation frequency is raised (5000Hz). The brief facilitation is followed by depressed current under identical stimulation frequency (5000Hz) but excessive pulse number, as a result of the gradual depletion of silver at one electrode and accumulation at the other. The current relaxes to its initial value with subsequent low frequency stimulation (196Hz), implying potential for autonomic computing^{48,49}.

Figure 6 Long-term spike-rate-dependent potentiation and bio-realistic spike-timing dependent plasticity (SRDP and true STDP) behaviour of a combined device consisting of a diffusive and a drift memristor. (a) Illustration of a biological synaptic junction between the pre- and post-synaptic neurons. Also shown is the electrical implementation, a circuit diagram of the electronic synapse consisting of the $\text{SiO}_x\text{N}_y\text{:Ag}$ diffusive memristor connected in series with the TaO_x drift memristor and between pulsed voltage sources, which act as neurons that send voltage spikes to the synaptic junction. (b) Spike-rate-dependent potentiation showing the change in the conductance (weight) of the drift memristor in the electronic synapse with change in the duration t_{zero} between the applied pulses. For long t_{zero} , the change in the conductance of the diffusive memristor is lower (see Fig. 5b), resulting in a lower weight change of the drift memristor. As the t_{zero} decreases, the weight change increases. The dotted red line represents a fit of the average conductance change with change in t_{zero} . (c) Schematic of the pulses applied

to the combined device for STDP demonstration. The long low voltage pulse in each spike turns the diffusive memristor ON, and the short high voltage pulse switches the drift memristor. When the post-spike precedes the pre-spike, the device is reset (depressed), and when the pre-spike precedes the post-spike, the device is set (potentiated). The timing (Δt) between the two spikes determines the voltage drop across the drift memristor. (d) Plot of the conductance (weight) change of the drift memristor with variation in Δt showing the spike-timing dependent plasticity of the electronic synapse. This response is characteristic of the timing-dependent response of biological synapses. The inset shows the spike-timing-dependent plasticity of a typical chemical synapse (reprinted from Fig. 7 of Ref. 50).

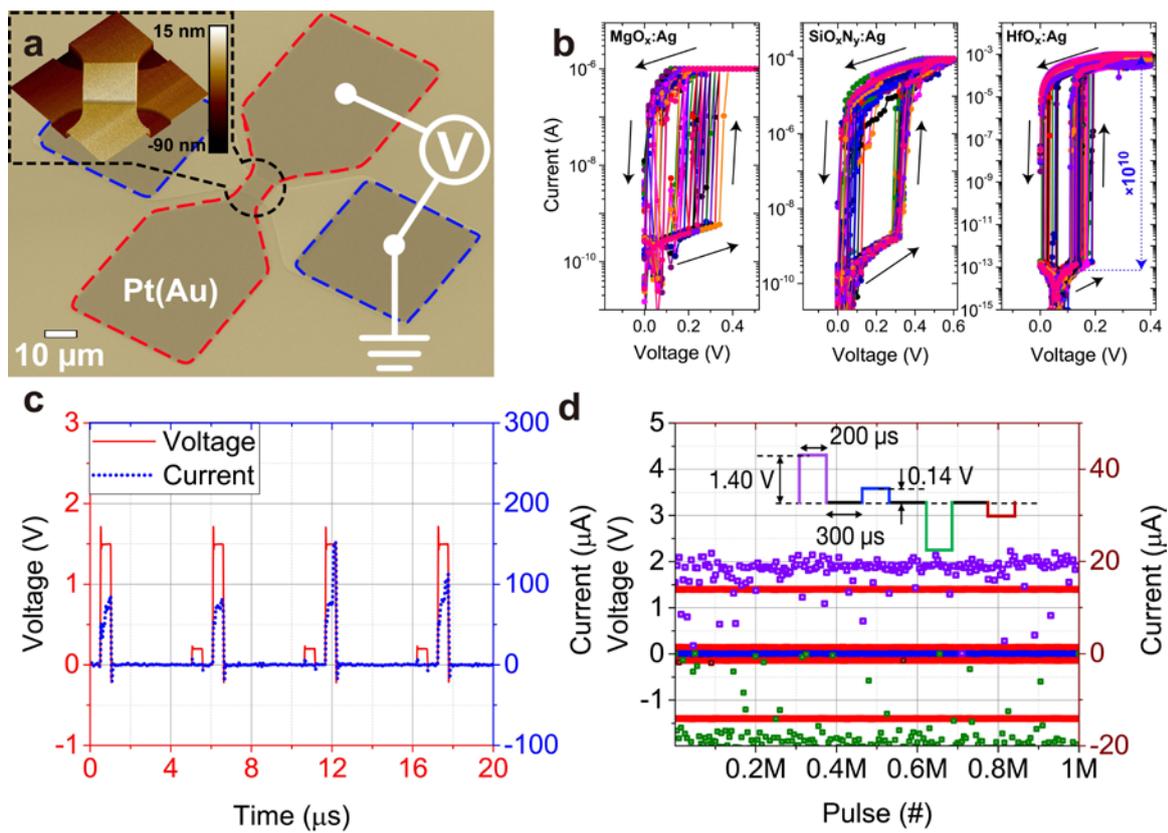


Figure 1

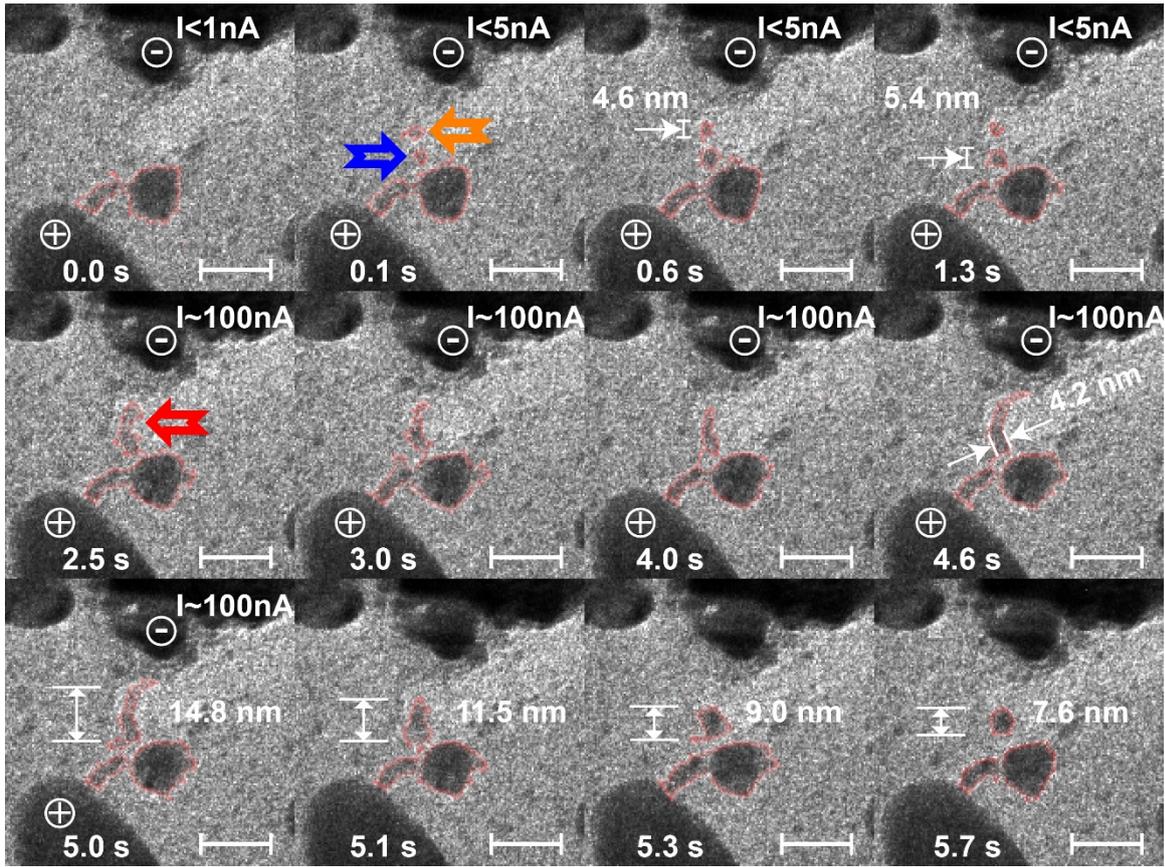


Figure 2

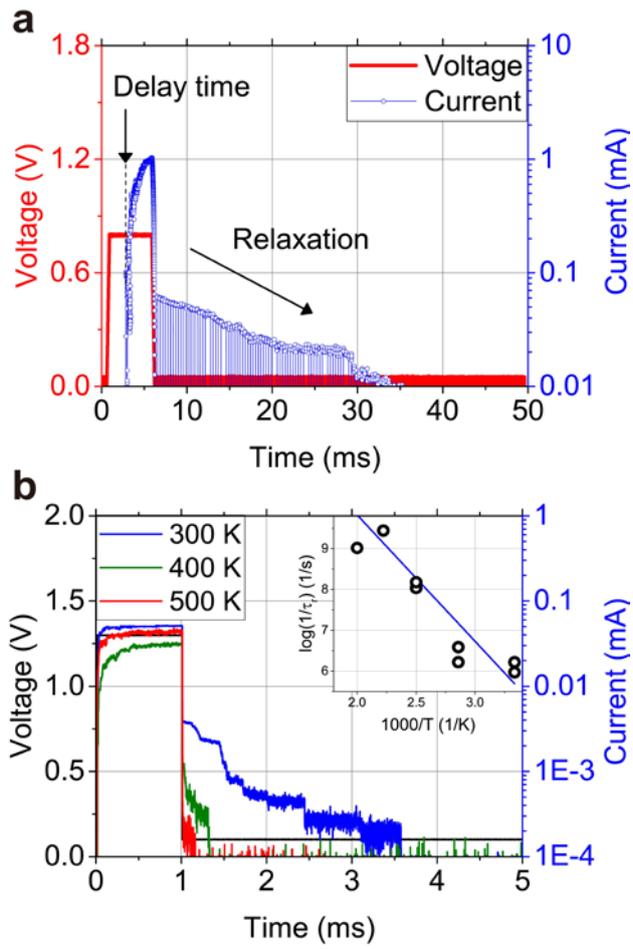


Figure 3

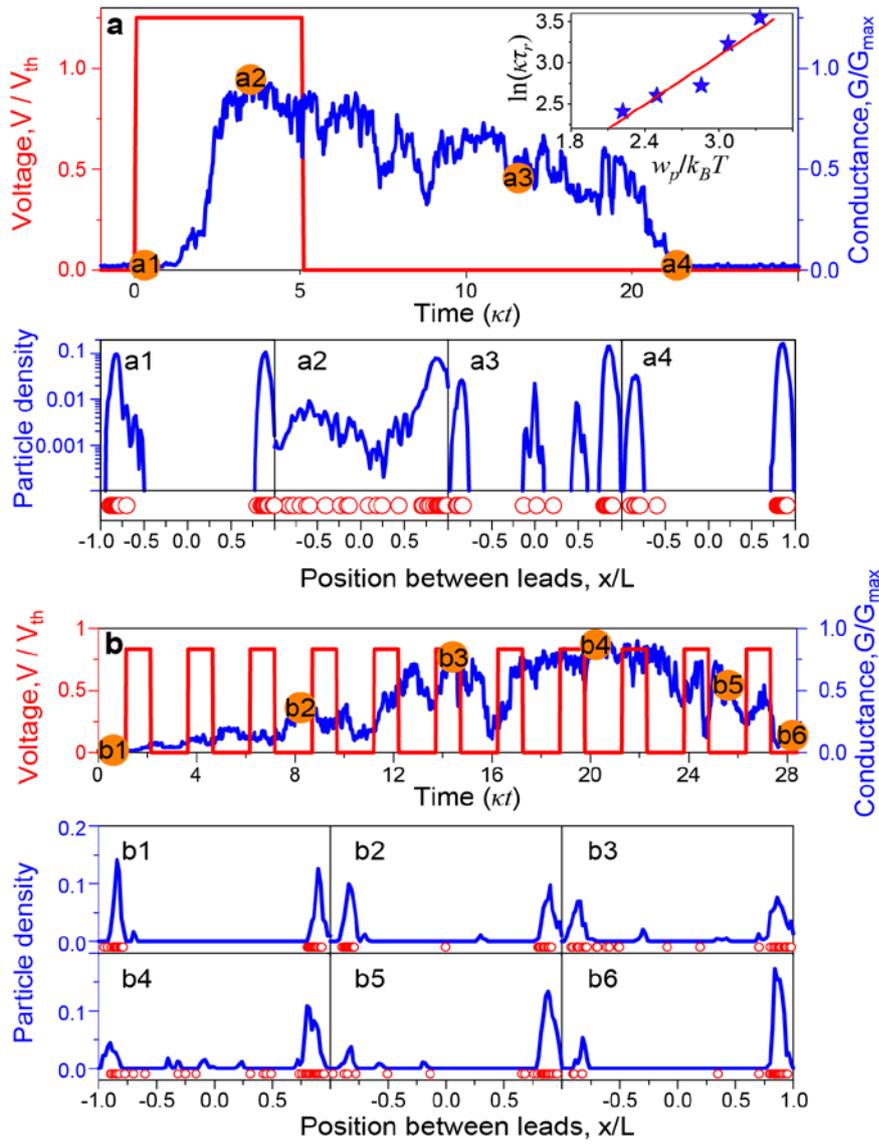


Figure 4

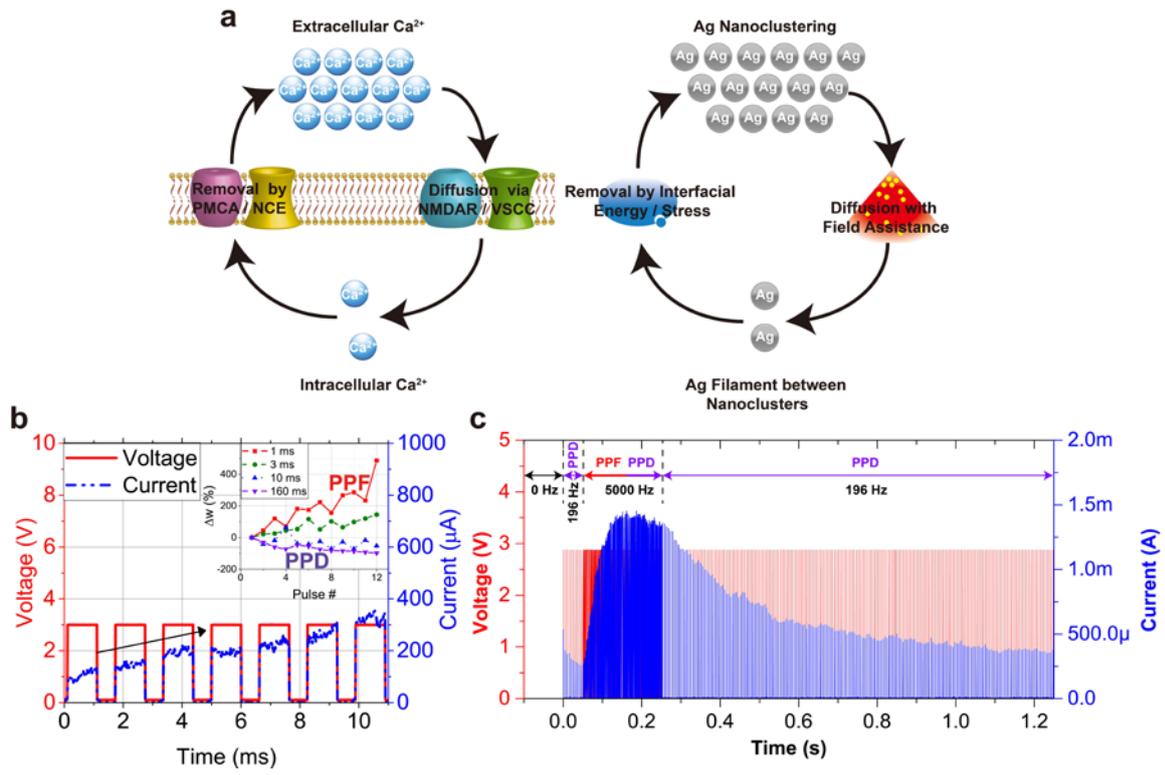


Figure 5

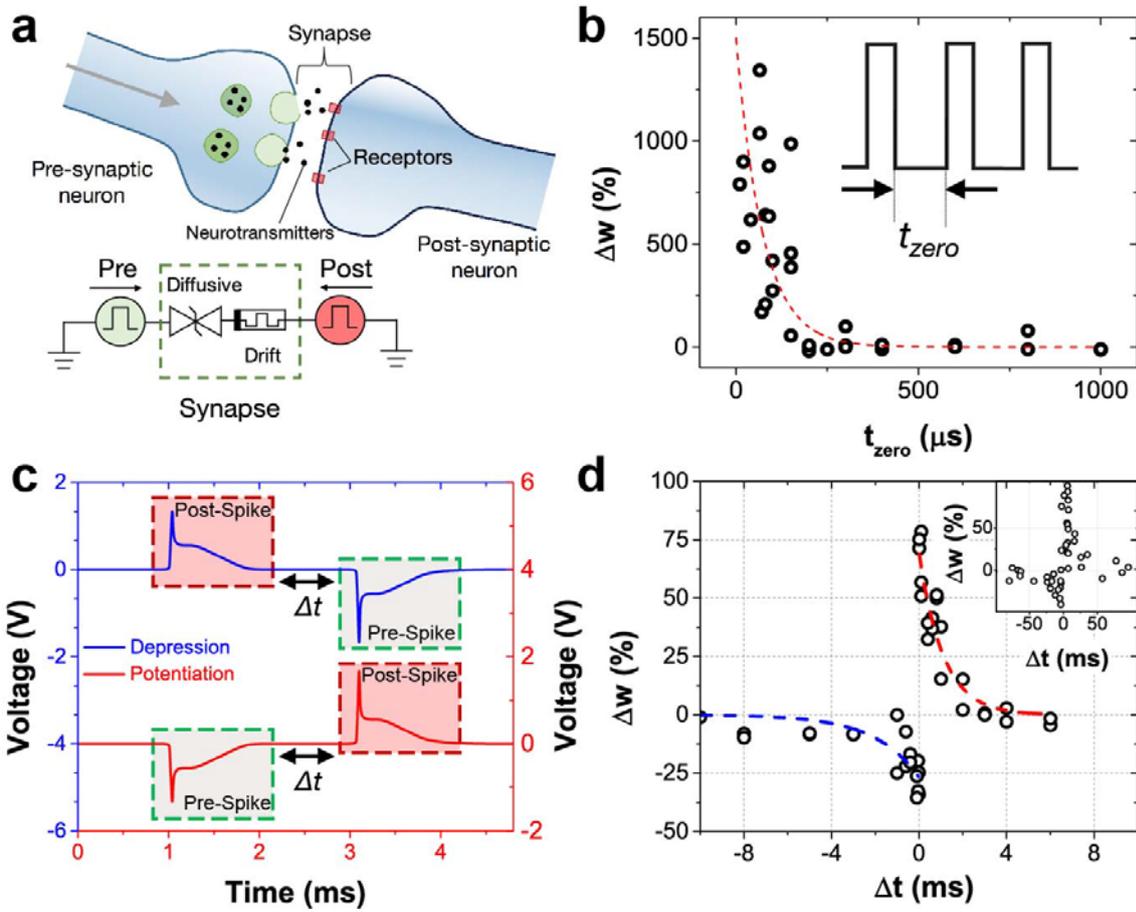


Figure 6