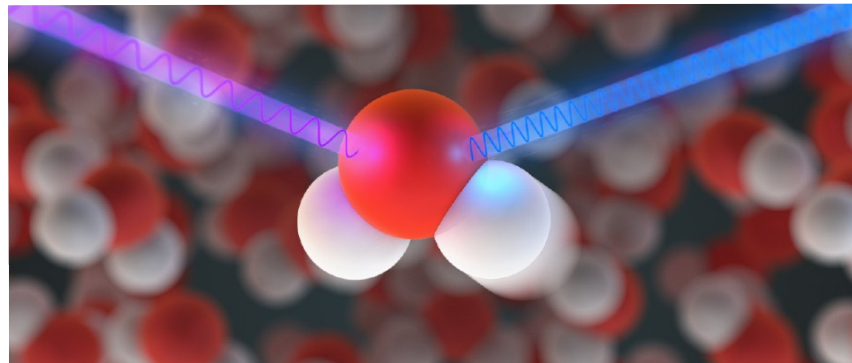


# First-principles modeling of RIXS in liquid water:

Core-excited nuclear dynamics and the  
distribution of local potential energy surfaces



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*The 11<sup>th</sup> International Conference on Inelastic X-ray Scattering*

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## Theory



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## Experiment

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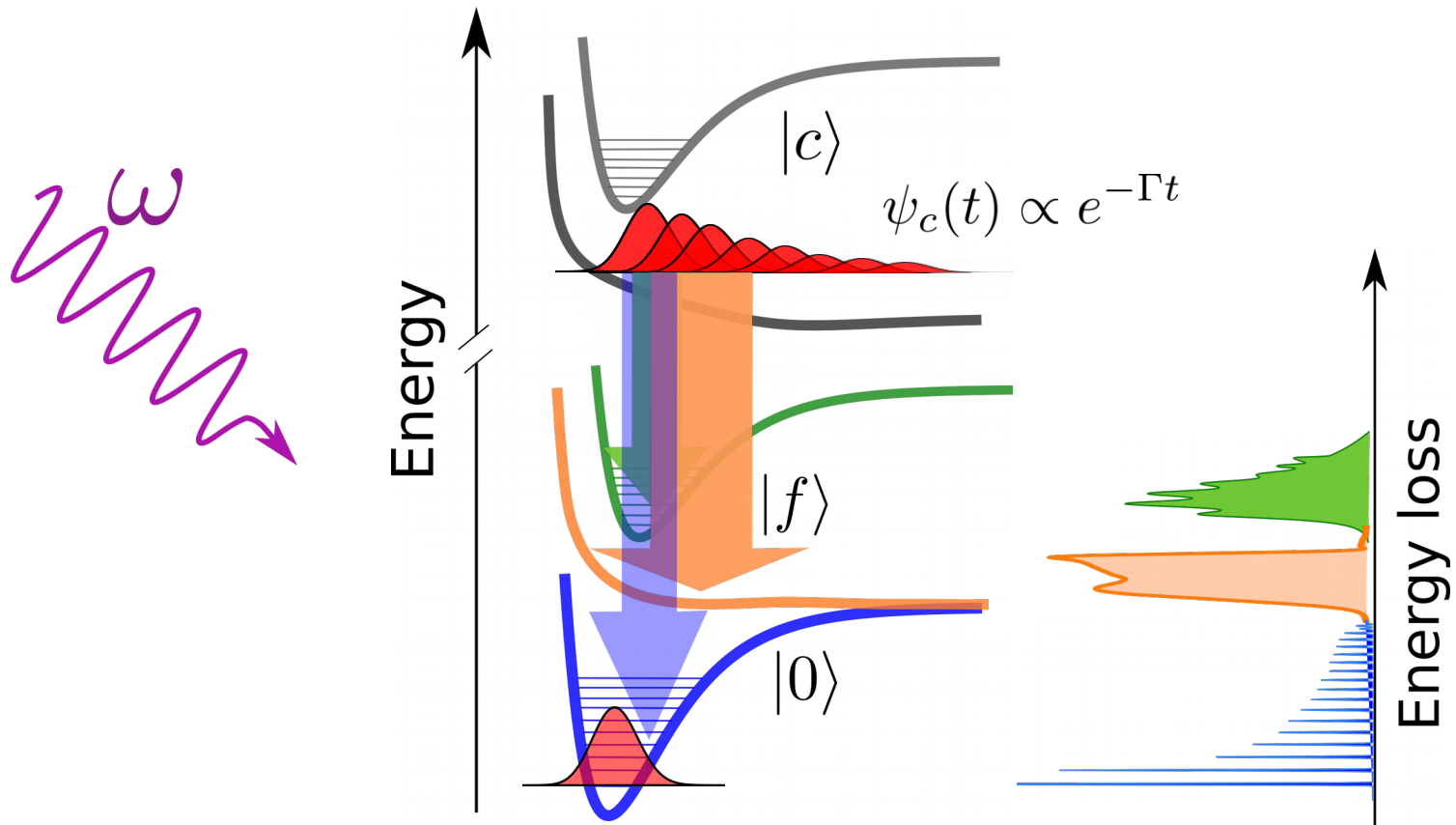
Marcus Dantz  
Xingye Lu  
Daniel McNally  
Thorsten Schmitt

*Measurements done at  
the ADDRESS Beamline at PSI*

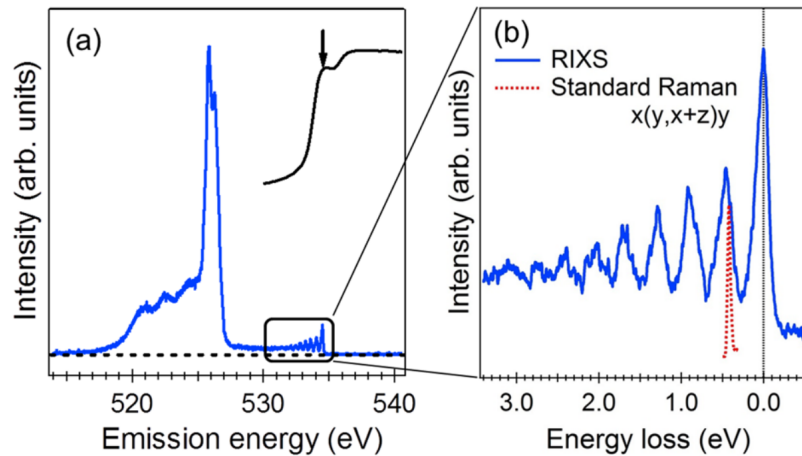
# Outline

- Introduction.
- Theoretical Model.
- Core-excited dynamics in liquid water.
- Vibrational RIXS and HB strength in water.
- The splitting of the  $1b_1$  resonance.
- Summary.

# Schematic description of RIXS



## Earliest measurements of water

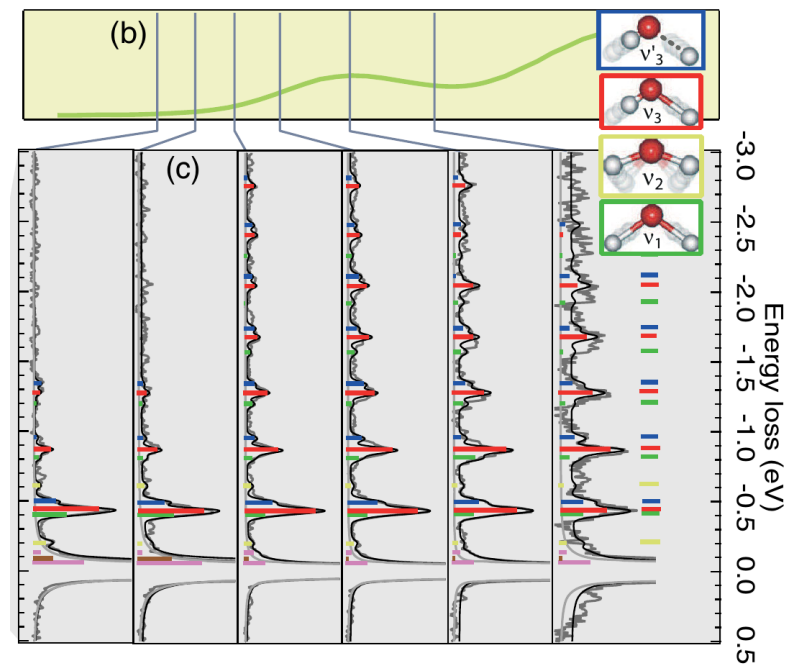


Harada *et al.* Phys. Rev. Lett., 111,193001 (2013).

- “The monotonic reduction of the energy separation between the various overtones can be explained by assuming a simple Morse function for the ground state potential surface.”
- “For H<sub>2</sub>O and D<sub>2</sub>O  $\nu_{0 \rightarrow 1}$  coincides closely with the energy of the stretching vibrational mode of gas-phase water rather than that of liquid water, clearly indicating the contribution to the XAS pre-edge peak of molecules with a highly weakened or broken donating H-bond.”

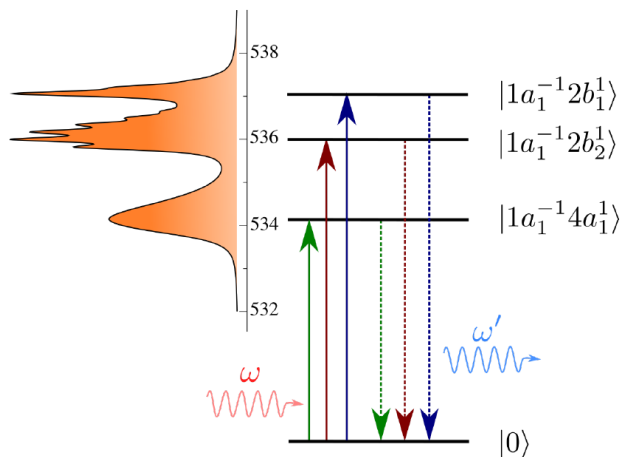
## Earliest measurements of water

- “The profile of the vibrational peaks gets broader with larger energy loss.”
- “The peak maximum positions, however, correspond to those of the asymmetric stretch mode of liquid water”
- “... we observe the presence of an additional mode which we assign to H-O---H molecules where one OH bond has lost its covalency due to bond elongation.”



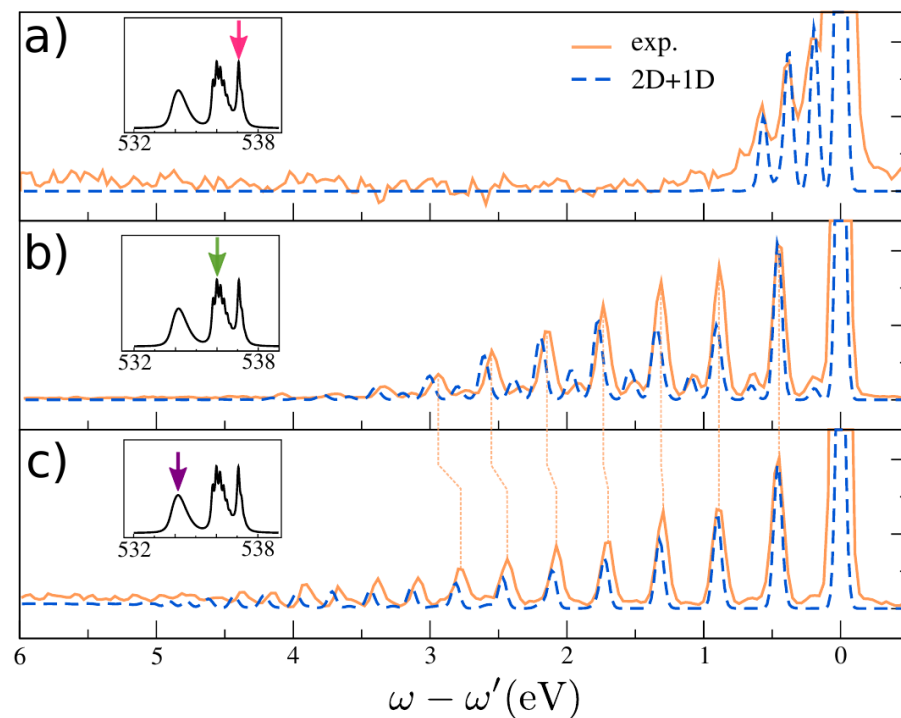
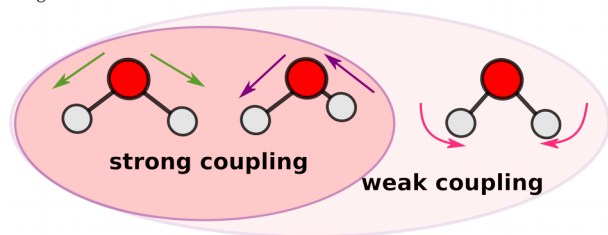
Pietzsch et al. Phys. Rev. Lett., 114, 88302 (2015).

# Gas-phase data weighs in!



## Nuclear degrees of freedom

$$\omega_s = 0.453 \text{ eV} \quad \omega_a = 0.466 \text{ eV} \quad \omega_b = 0.198 \text{ eV}$$



## RASPT2 potential energy surfaces 2D+1D Quantum wave packet model

V. Vaz da Cruz *et al* PCCP **19**, 19573 (2017).  
R.C. Couto *et al* Nature Communications, **8**, 14165 (2017)

## Main questions for the theory

1. Does O1s pre-edge RIXS probe **only** a sub-set of molecules with **weak/broken hydrogen bonds**?
2. Can the vibrational progression in liquid water be explained by a simple **Morse potential**, a **normal-mode** fit, or even a **gas-phase** model?
3. Is the associated channel to the  **$1b_1$  electronic state** a reliable probe of **local structure** and **hydrogen bonding**?

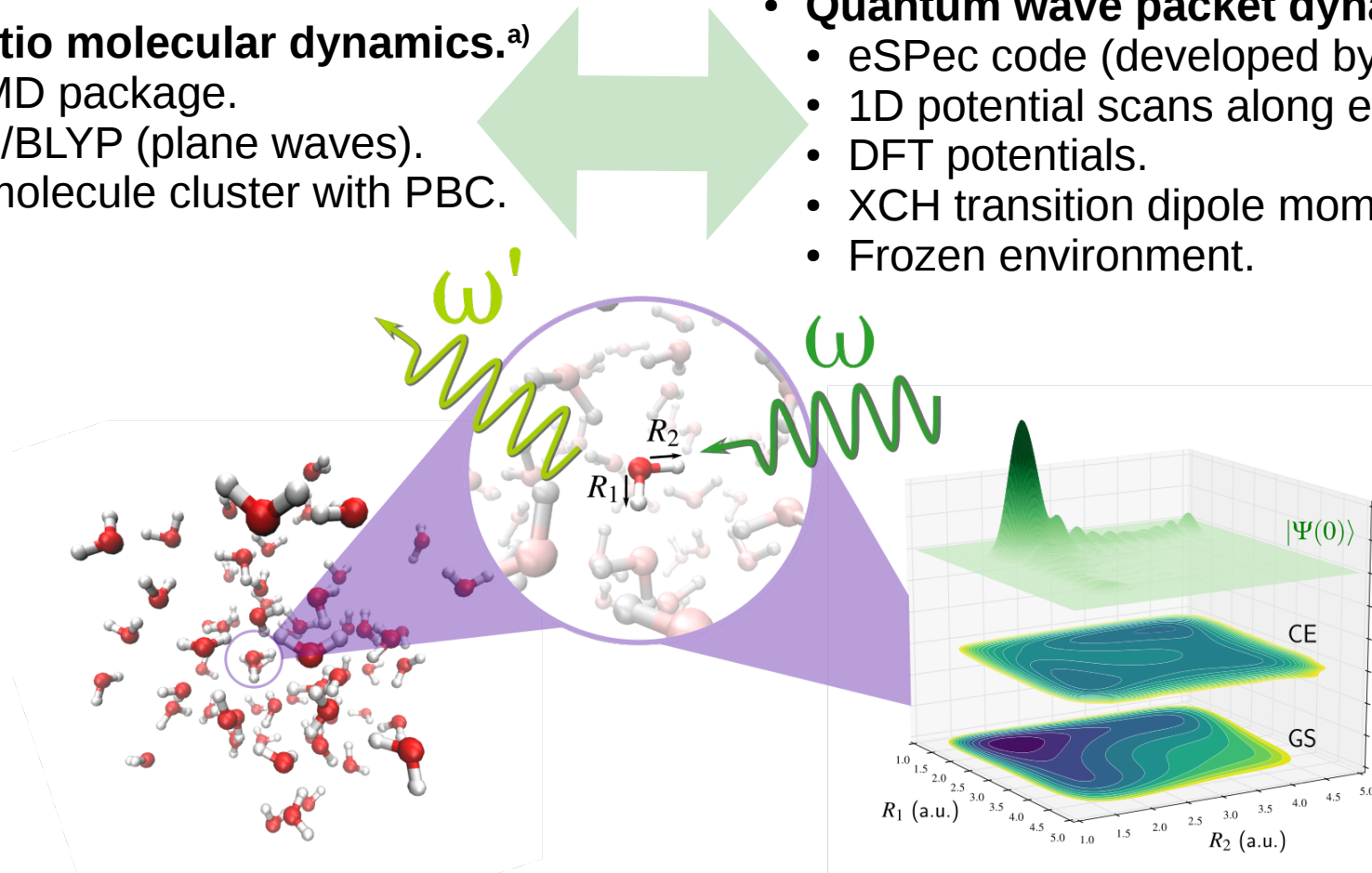
# Proposed Model of Bulk Liquid Water

## • Ab-initio molecular dynamics.<sup>a)</sup>

- CPMD package.
- DFT/BLYP (plane waves).
- 64-molecule cluster with PBC.

## • Quantum wave packet dynamics

- eSPec code (developed by us).
- 1D potential scans along each bond.
- DFT potentials.
- XCH transition dipole moments.
- Frozen environment.



a) Similar to: M. Odelius J. Phys. Chem. A, **113**, 8176-8181 (2009)

## Details of the Quantum Model

### Hamiltonian:

$$h^k = -\frac{1}{2\mu} \frac{\partial^2}{\partial R_1^2} - \frac{1}{2\mu} \frac{\partial^2}{\partial R_2^2} - \frac{\cos \theta_{eq}}{m_O} \frac{\partial^2}{\partial R_1 R_2} + V_k(R_1, R_2, \theta_{eq}),$$

$$V_k(R_1, R_2, \theta_{eq}) = V_k(R_1, R_{eq}, \theta_{eq}) + V_k(R_{eq}, R_2, \theta_{eq}) - V_k(R_{eq}, R_{eq}, \theta_{eq}),$$

### Individual cross-sections:

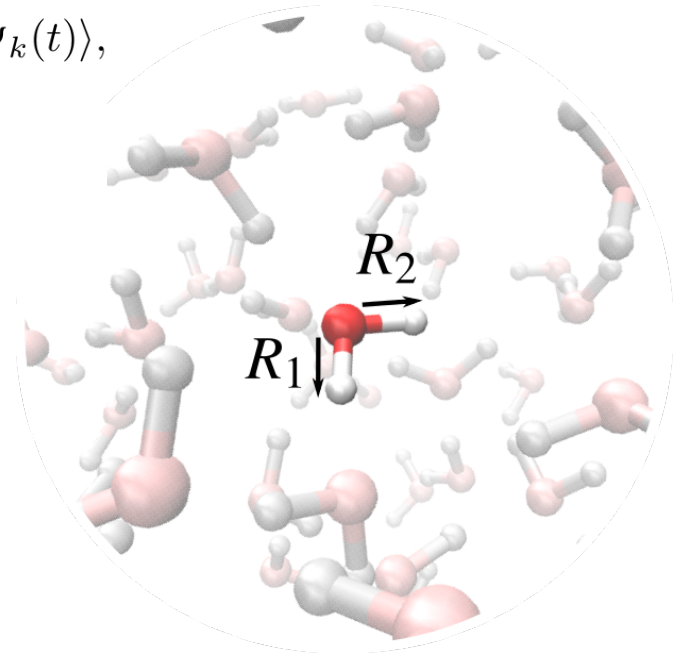
$$\sigma_k(\omega, \omega') = \frac{1}{\pi} \text{Re} \int_0^\infty dt e^{i(\omega - \omega' - \omega_{f0}^k + \epsilon_0^k + i\Gamma)t} \langle \Psi_k(0) | \Psi_k(t) \rangle,$$

$$|\Psi_k(0)\rangle = \int_0^\infty dt e^{i(\omega - \omega_{i0}^k + \epsilon_0^k + i\Gamma)t} |\psi_k(t)\rangle,$$

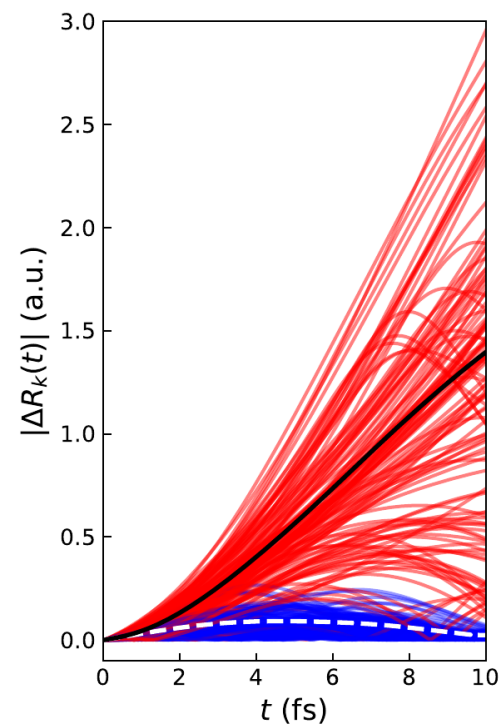
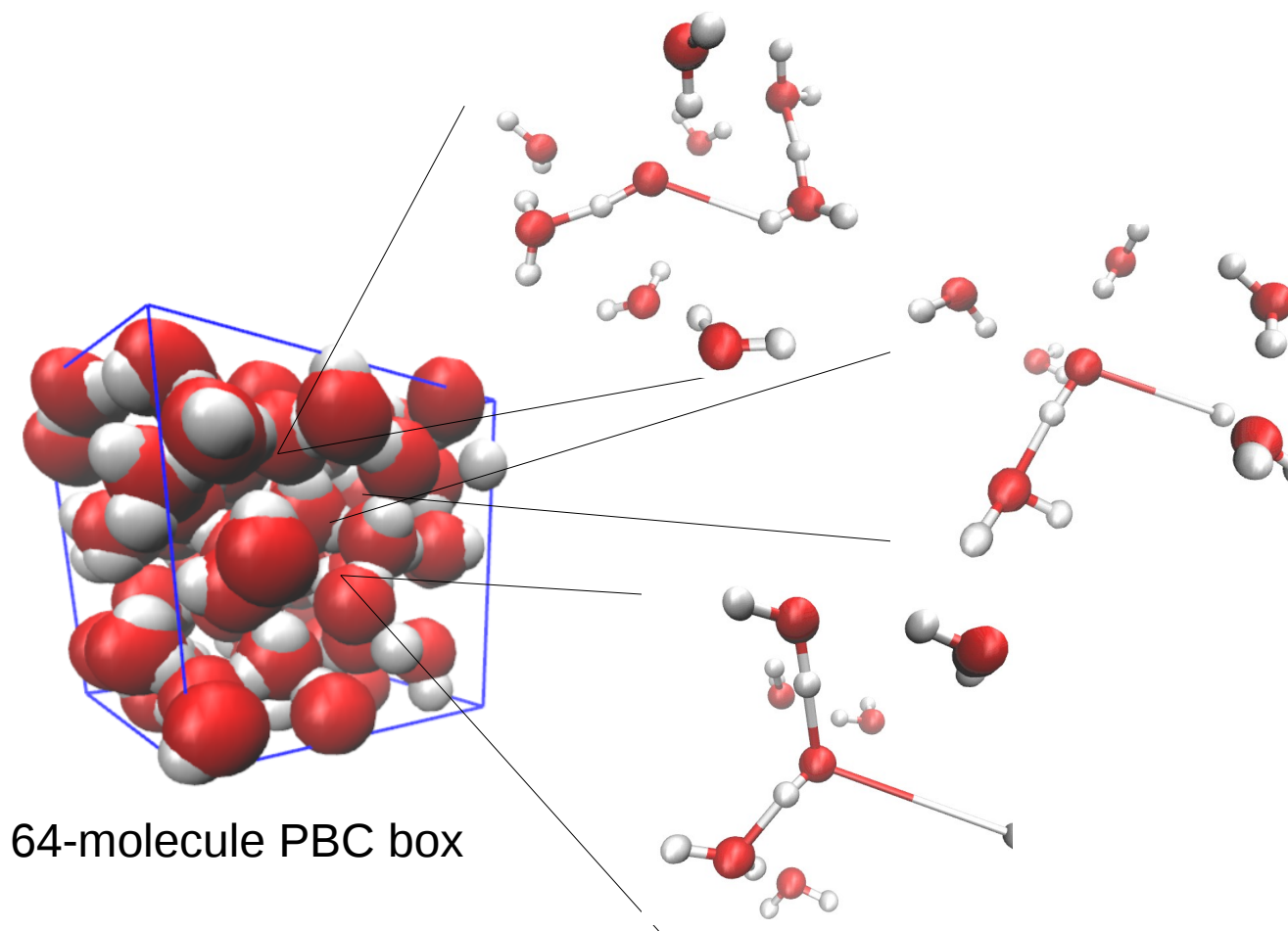
$$|\psi_k(t)\rangle = e^{-i\hbar_i^k t} |0_k\rangle, \quad |\Psi_k(t)\rangle = e^{-i\hbar_f^k t} |\Psi_k(0)\rangle$$

### Liquid phase cross-section

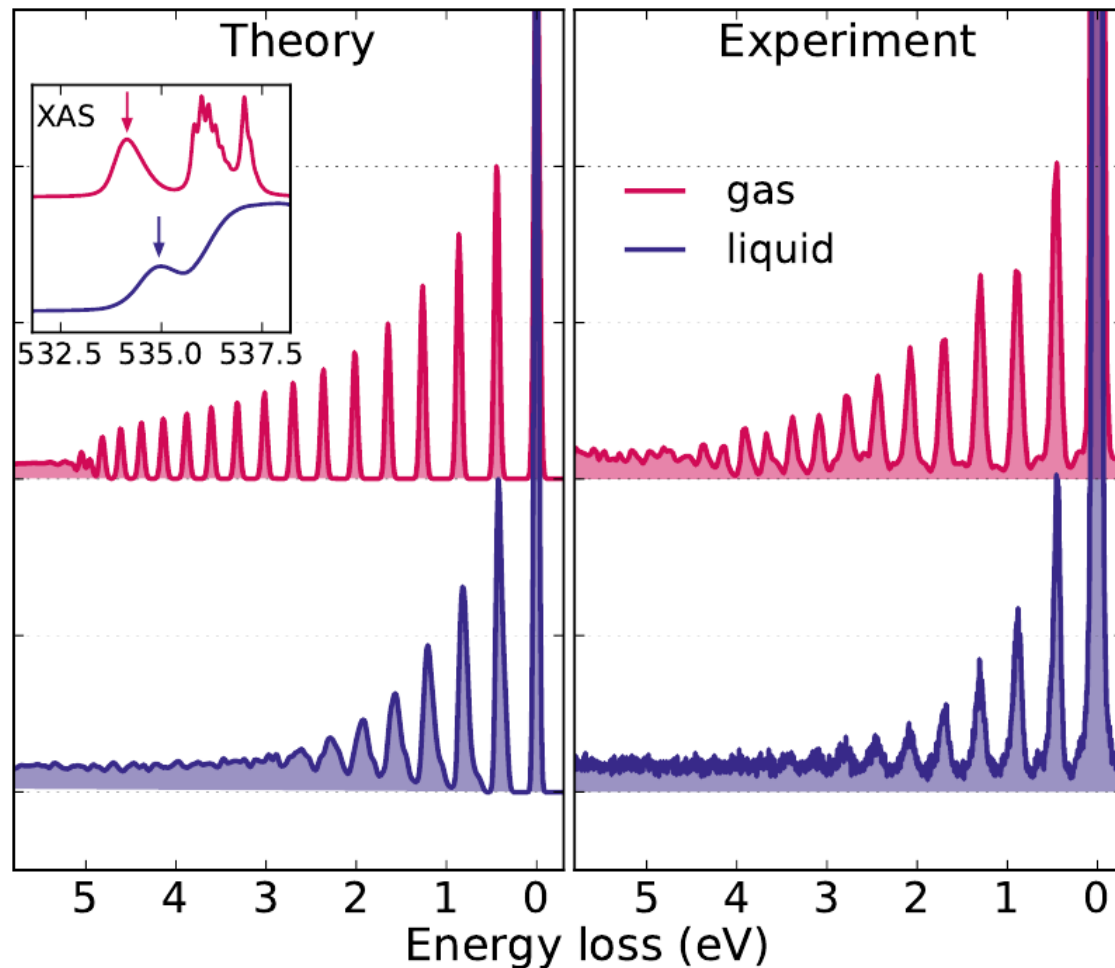
$$\sigma_{liq}(\omega', \omega) \approx \bar{\sigma}(\omega', \omega) = \sum_{k=0}^{64} (d_{i,0}^k)^2 (d_{f,i}^k)^2 \sigma_k(\omega', \omega)$$



# What happens upon excitation at the O1s pre-edge?



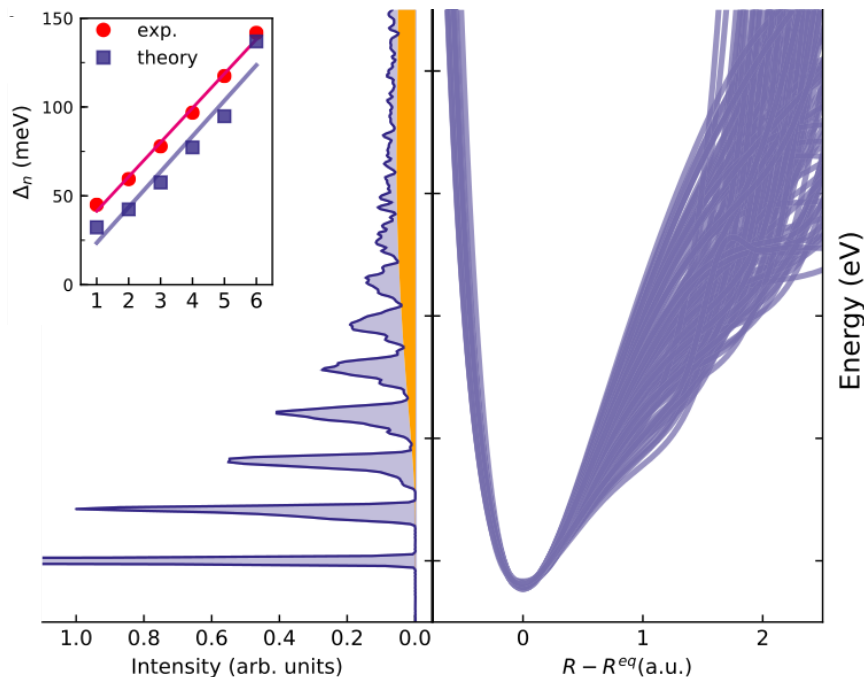
## Calculated RIXS spectra for gas and liquid



- Gas and Liquid phase have similar peak positions.
- Shortening of the vibrational progression in the liquid and formation of a background in the  $> 3$  eV region.

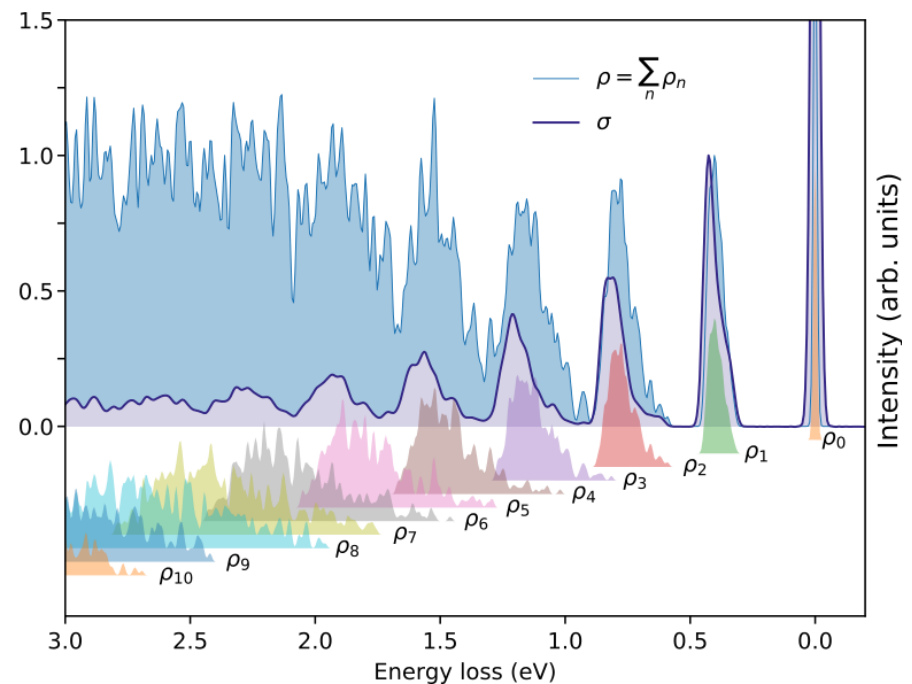
# Formation of the smooth background

DFT/BLYP  
XCH potentials



Peak width increases  
High energy part is smeared out

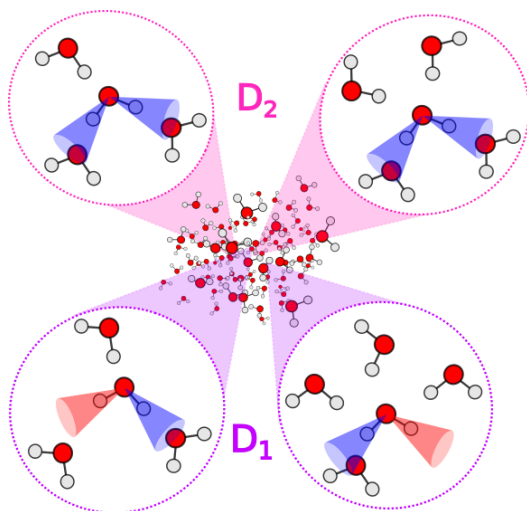
$$\rho_m(\epsilon) = \sum_{k=1}^{64} \sum_{n_1+n_2=m} \Phi(\epsilon - \epsilon_{n_1,n_2}^k + \epsilon_{0,0}^k)$$



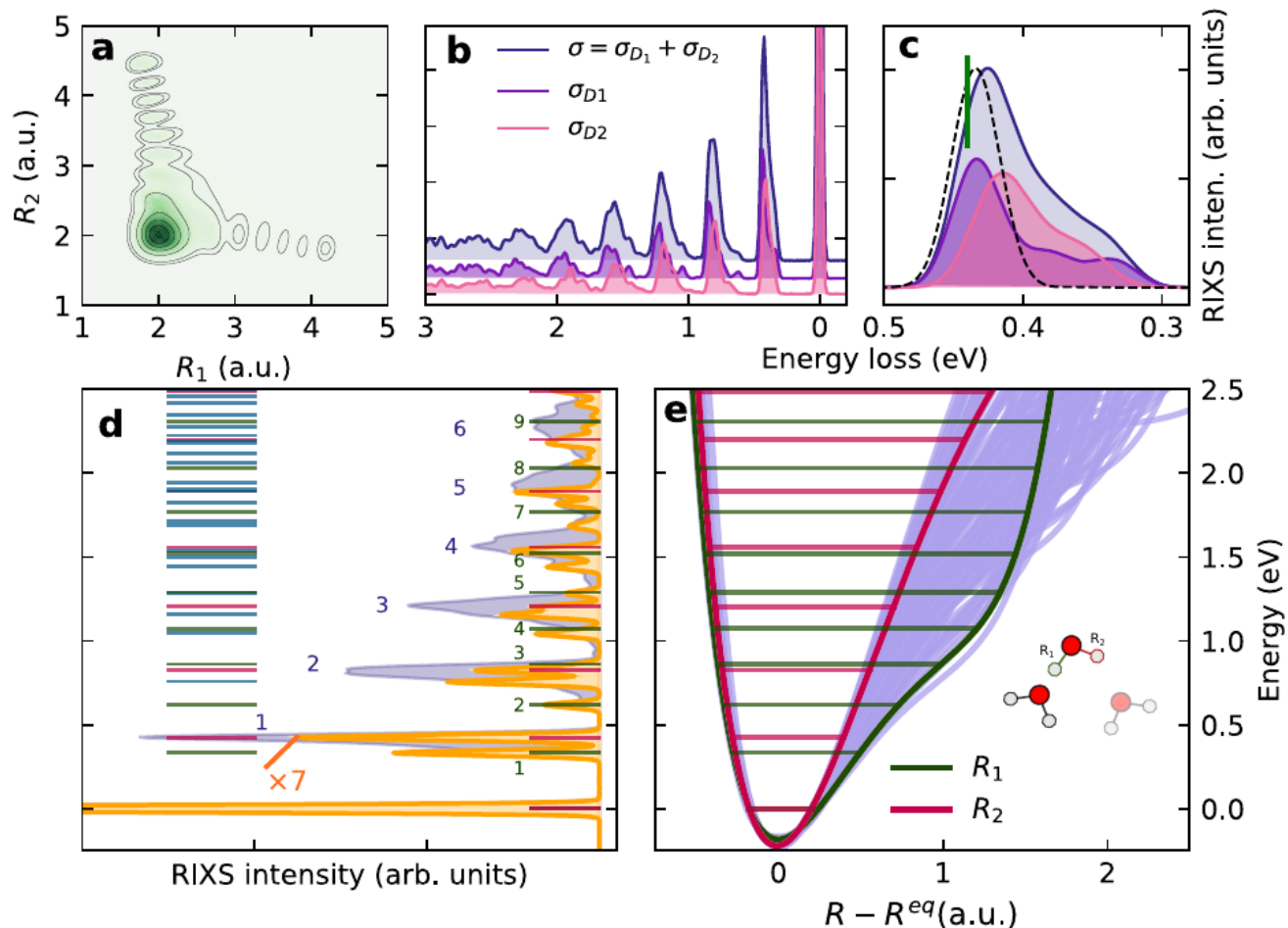
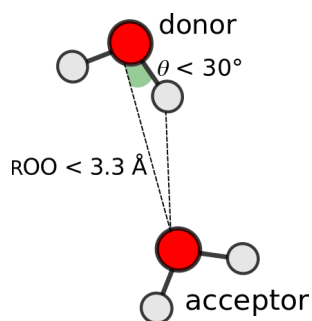
Strong overlap between the  
partial densities of states

# Role of inequivalent bonds

## Local structures



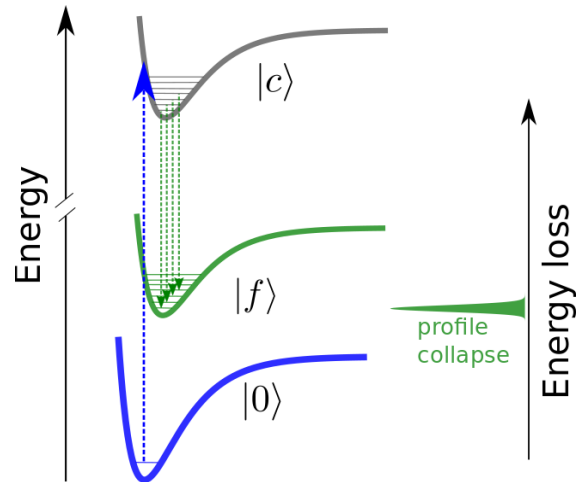
## HB definition



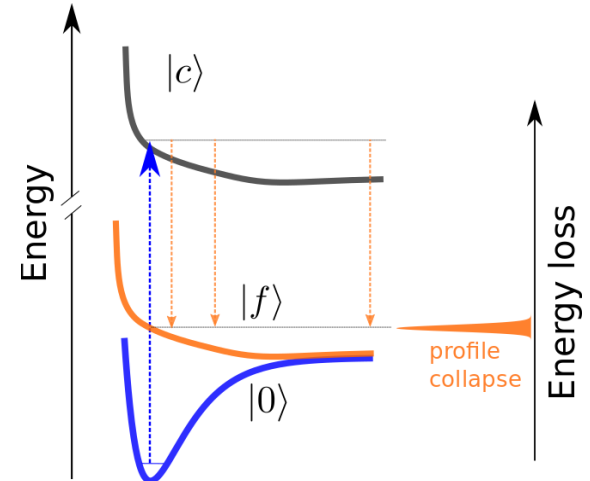
# The $1b_1$ splitting at the pre-edge

# Atomic peaks revisited

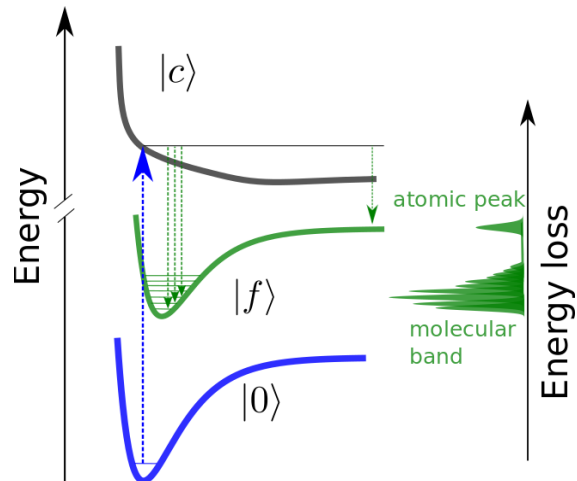
## Case 1



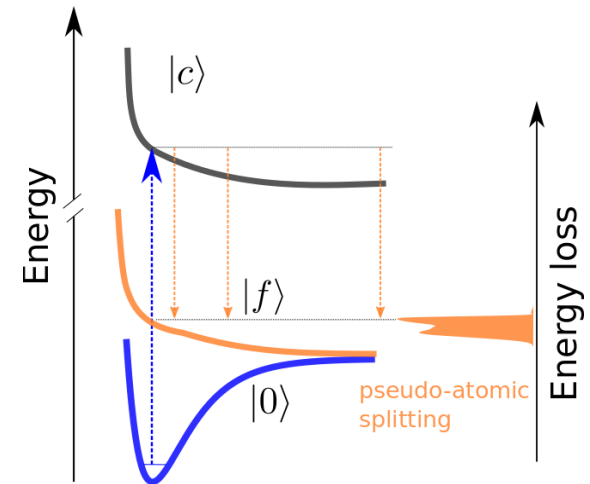
## Case 2



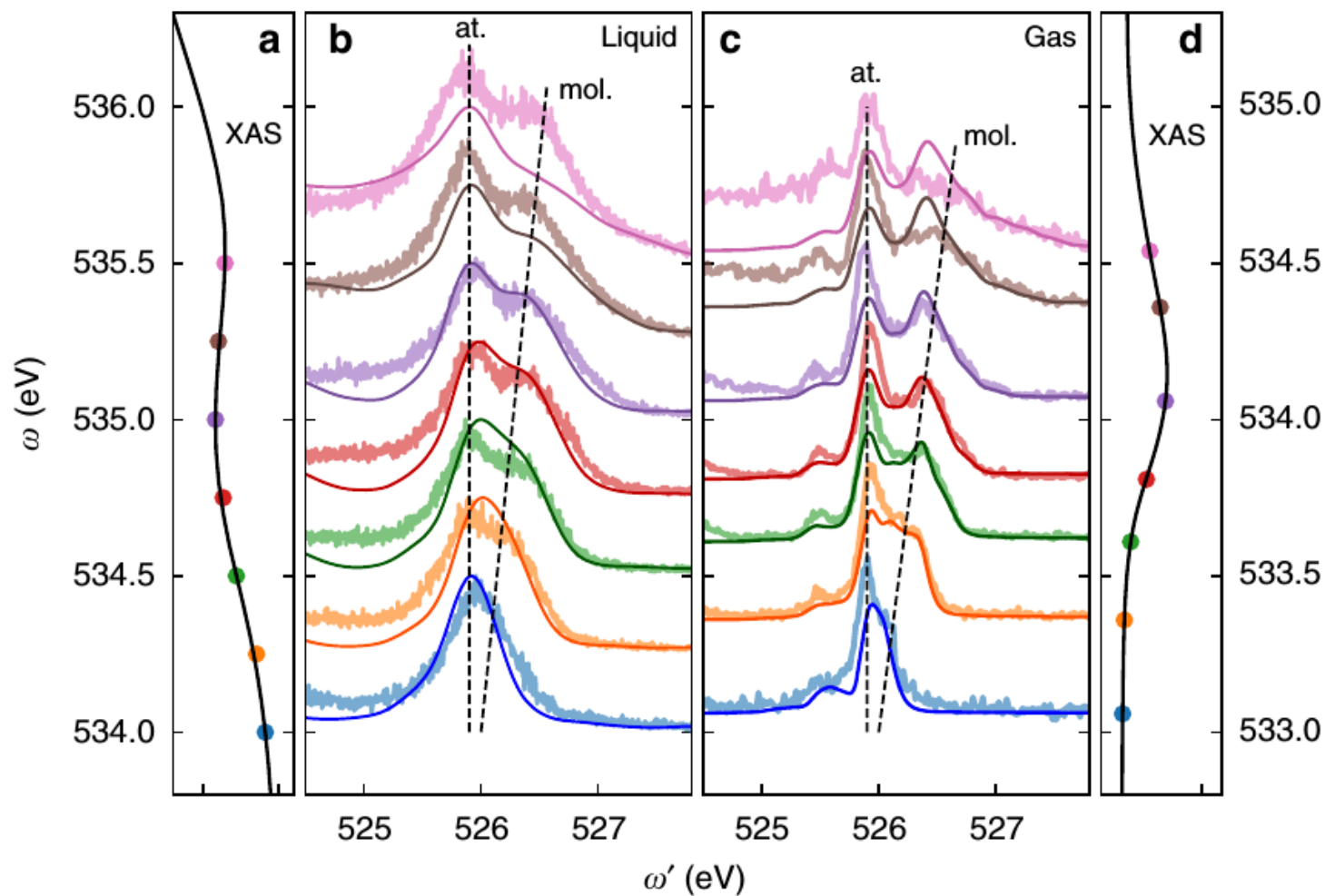
## Case 3



## Case 4



# The emergence of the $1b_1$ split-peak



# For more details on the split peak and the structure of water...



## Compatibility of quantitative X-ray spectroscopy with continuous distribution models of water at ambient conditions

Johannes Niskanen<sup>a,b</sup>, Mattis Fondell<sup>a</sup>, Christoph J. Sahle<sup>c</sup>, Sebastian Eckert<sup>d,a</sup>, Raphael M. Jay<sup>d,a</sup>, Keith Gilmore<sup>c</sup>, Annette Pietzsch<sup>a</sup>, Marcus Dantz<sup>e</sup>, Xingye Lu<sup>e</sup>, Daniel E. McNally<sup>e</sup>, Thorsten Schmitt<sup>e</sup>, Vinicius Vaz da Cruz<sup>f,a</sup>, Victor Kimberg<sup>f,g</sup>, Faris Gel'mukhanov<sup>f,g</sup>, and Alexander Föhlisch<sup>a,d,1</sup>

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Niskanen *et al.* PNAS, **116**, 4058 (March. 2019).

## Summary

- We have found that a broad distribution of local structures is probed at the O1s pre-edge of liquid water.
- The differences between the progression in gas-phase and liquid reflect the variations in local HB environment.
- The core-excited ultra-fast dynamics is an effective probe of hydrogen-bonds strength of in liquid water via the distribution of potential energy surfaces accessed.
- The  $1b_1$  split-peak is caused by nuclear dynamics, however it is formed by transitions close to the equilibrium geometry being much less sensitive to hydrogen bonding.

# Thank you!