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# Inelastic X-ray scattering at extreme conditions and its geophysical applications

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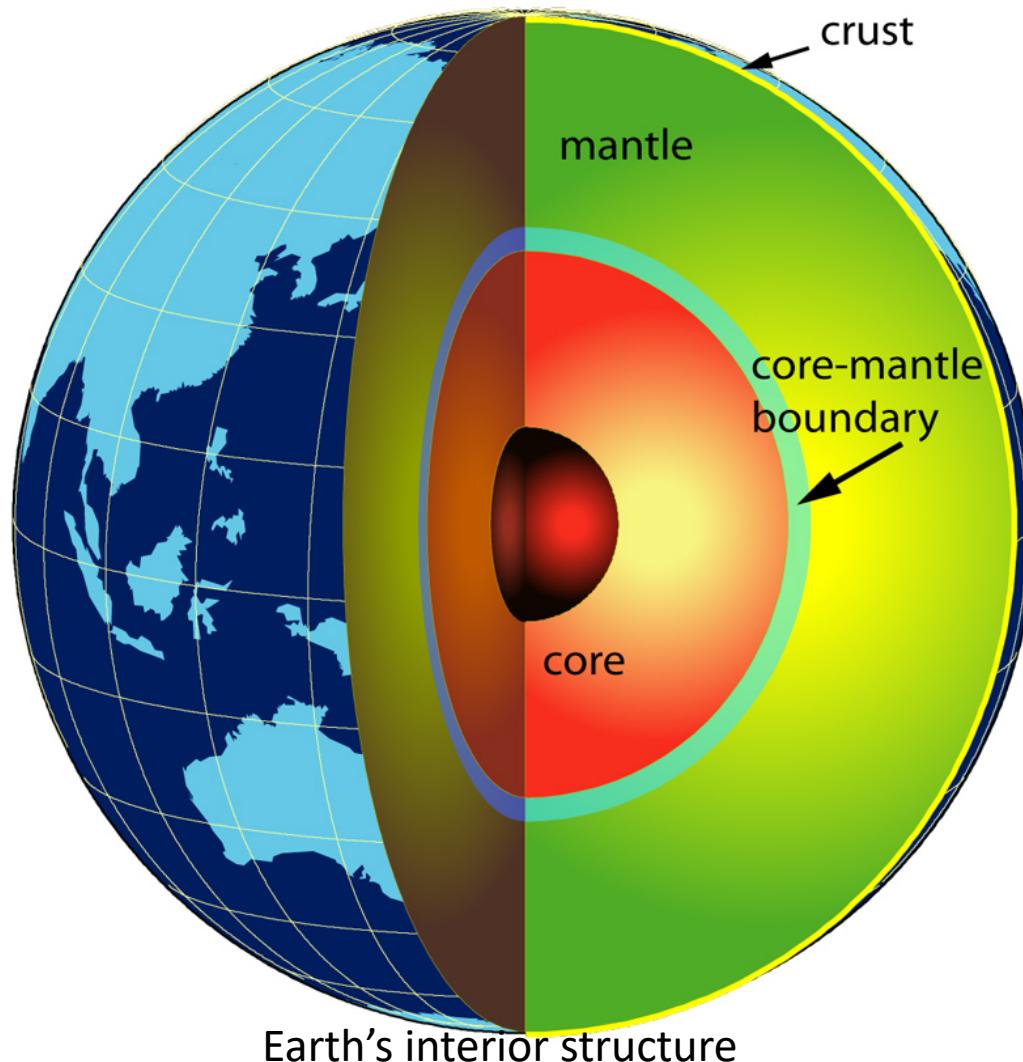
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Email: eohtani@tohoku.ac.jp

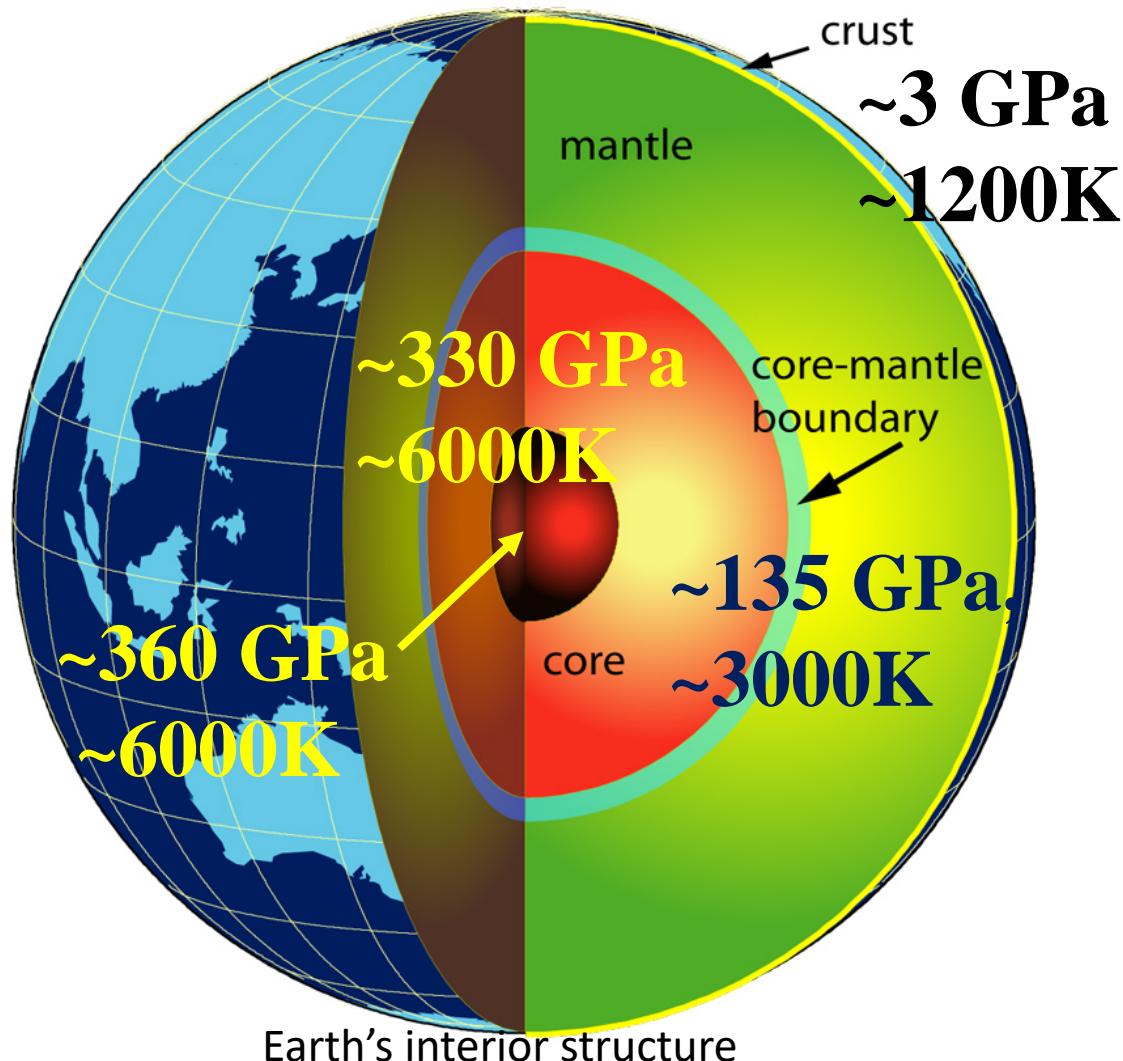
# Topics

- Sound velocity of iron and its alloy compounds and the Earth's core
- Sound velocity measurements at multi-Megabar pressures and the primary pressure scale

# Sound velocity measurements of iron-light element alloys: A challenge to the core conditions

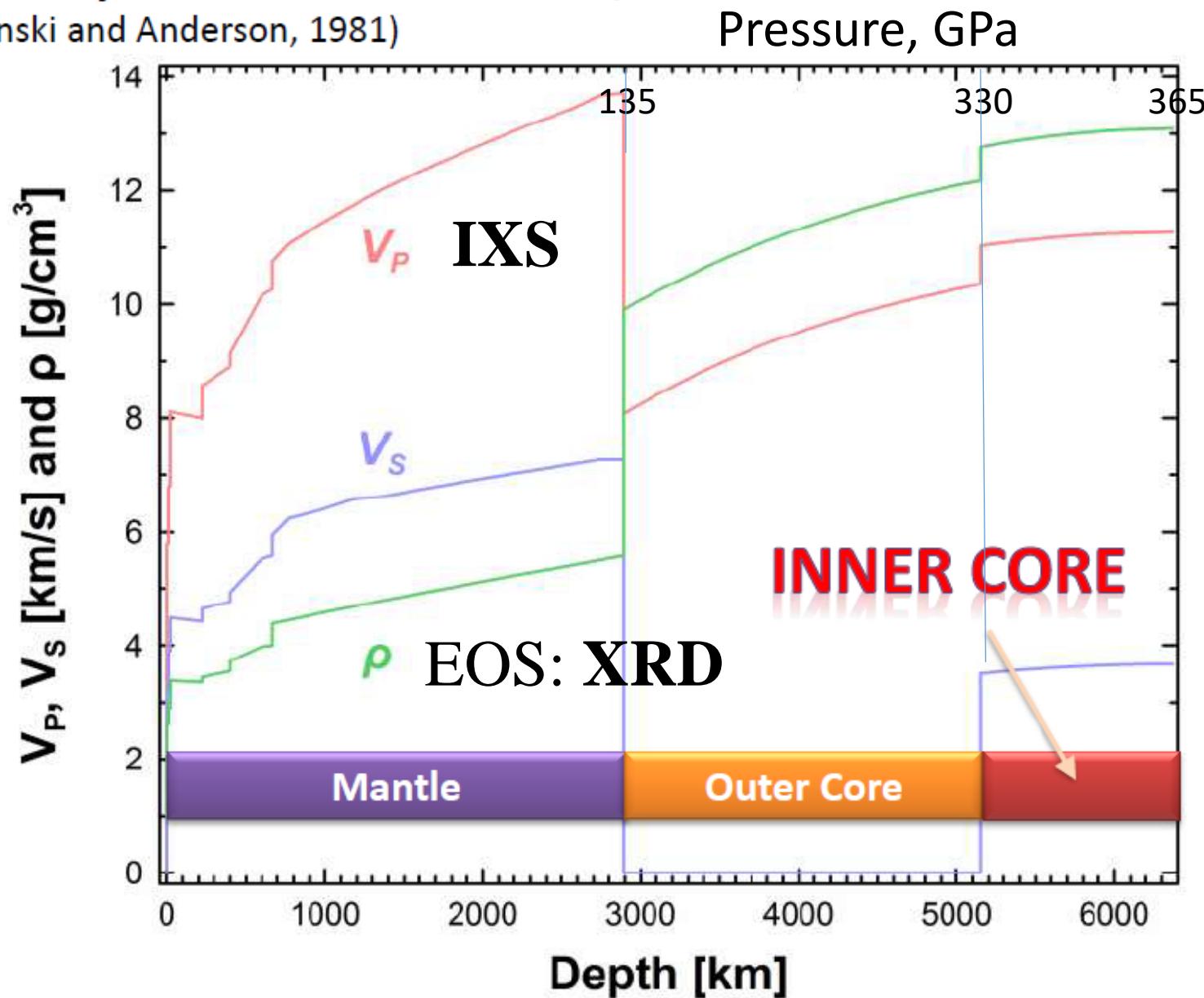


# Sound velocity measurements of iron-light element alloys: A challenge to the core conditions

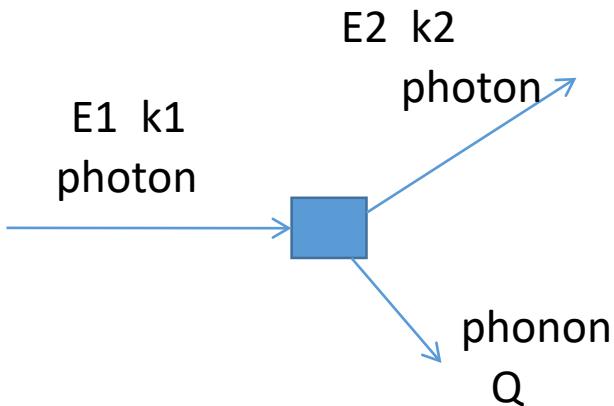


# Preliminary reference Earth model; PREM

(Dziewonski and Anderson, 1981)

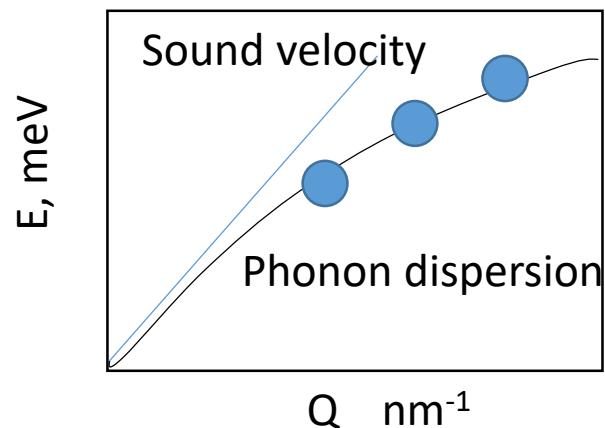


# Sound velocity of Fe and Iron-light element alloys



Energy transfer  $E_1 - E_2 = E$

Momentum transfer  $k_1 - k_2 = Q$



## Sound velocity of Earth materials

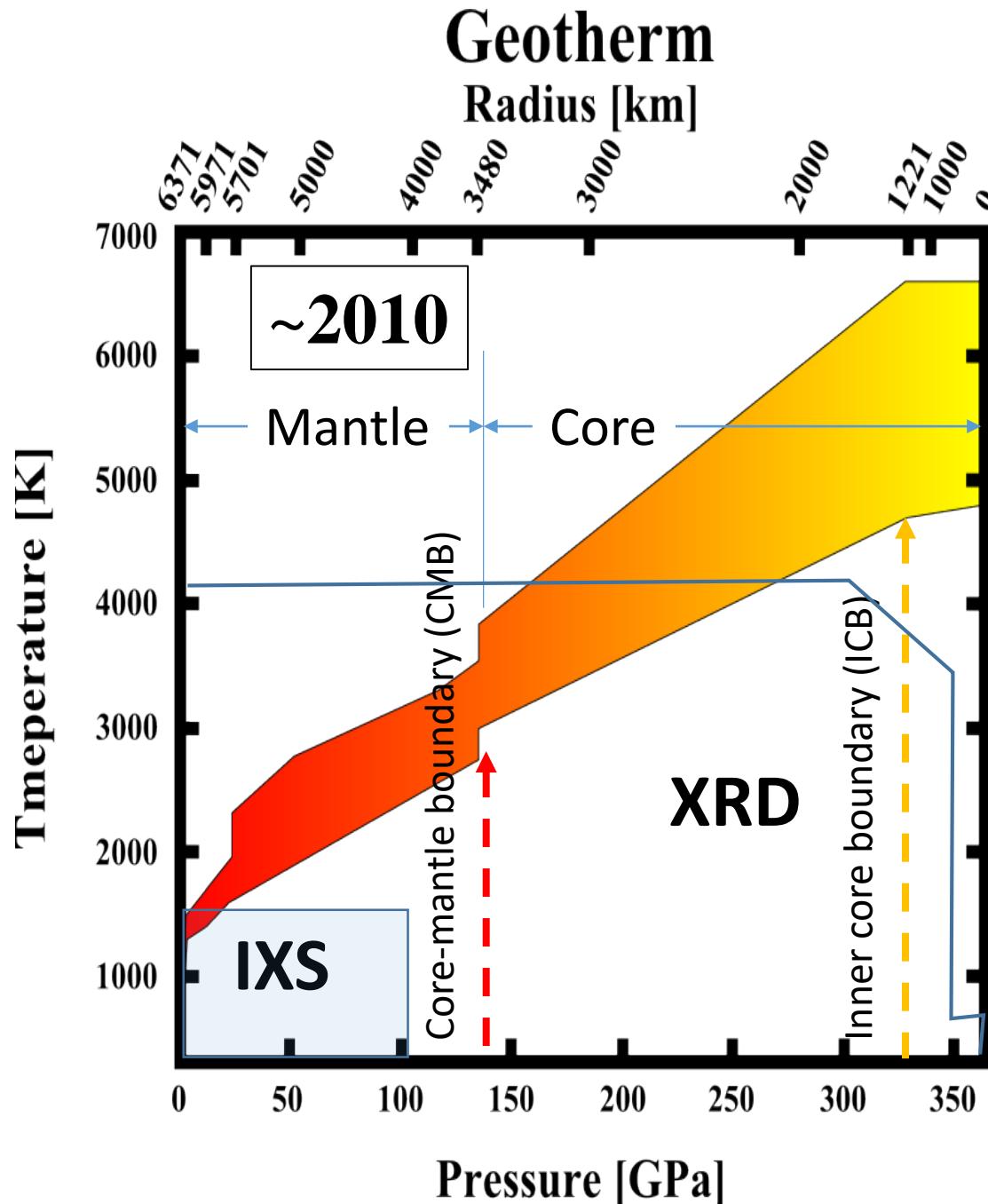
Ultrasonic

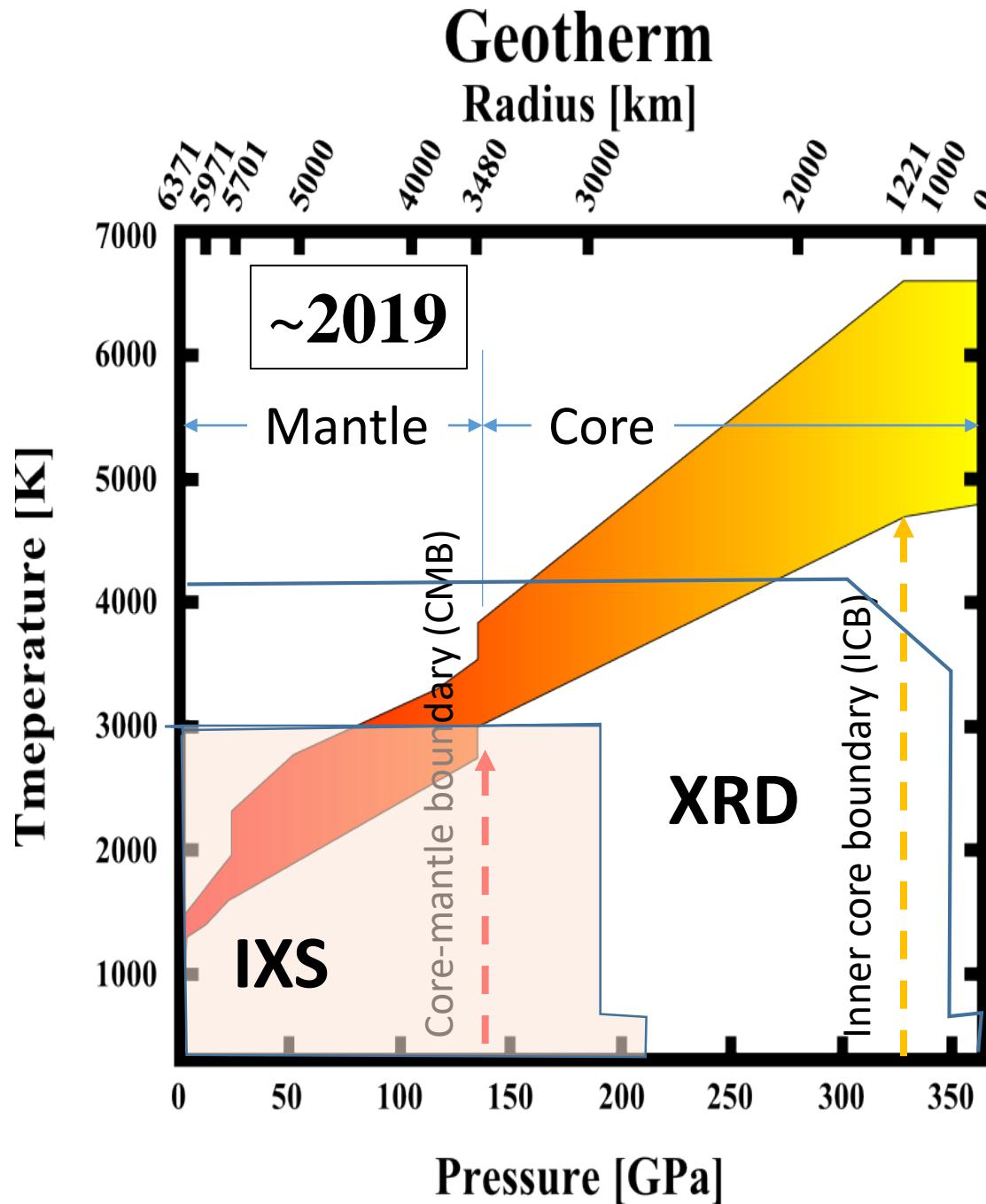
Brillouin scattering

NRIXS (NIS, Nuclear Resonance Inelastic X-ray Scattering)

**IXS (Inelastic X-ray scattering)**

- Fiquet et al. (2001) Fe-Vp @ESRF
- Antonangeli et al. (2004) :  
Fe Anisotropy of Vp
- Z.Mao et al. (2012) Fe and FeSi  
at HP and HT @APS





# BL35XU@ SPring-8: High pressure and temperature:

IXS Optics [Baron et al., 2000]

- Kirkpatrick-Baez mirror pair: **16 × 16 μm** beam size

XRD: Flat panel area detector

Heating: Portable laser heating system **COMPAT** (Fukui et al., 2013)

# BL43XU@SPring-8: Higher pressure: P>200 GPa

IXS Optics [Baron et al., 2016]

- Multilayer Kirkpatrick-Baez (**KB**) mirror: **5 × 5 μm** beam size
- Soller screen [Baron, 2019]:

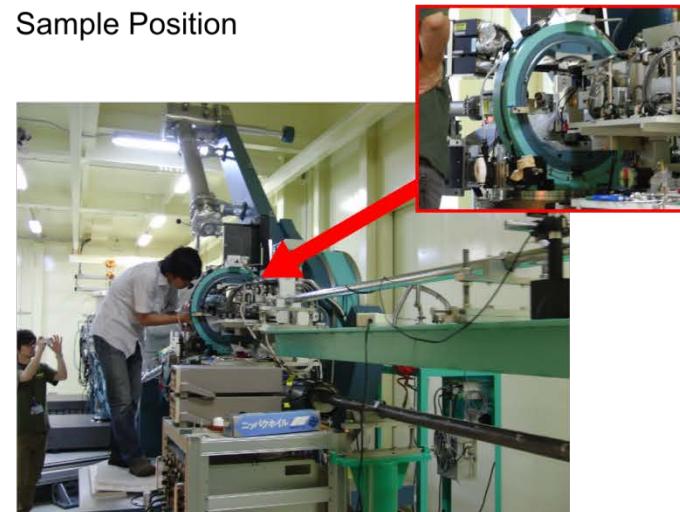
XRD: Flat panel area detector

# BL35XU Optics

Simultaneous measurements of sound velocity and density: **Flat panel detector**, Image plate



Sample Position



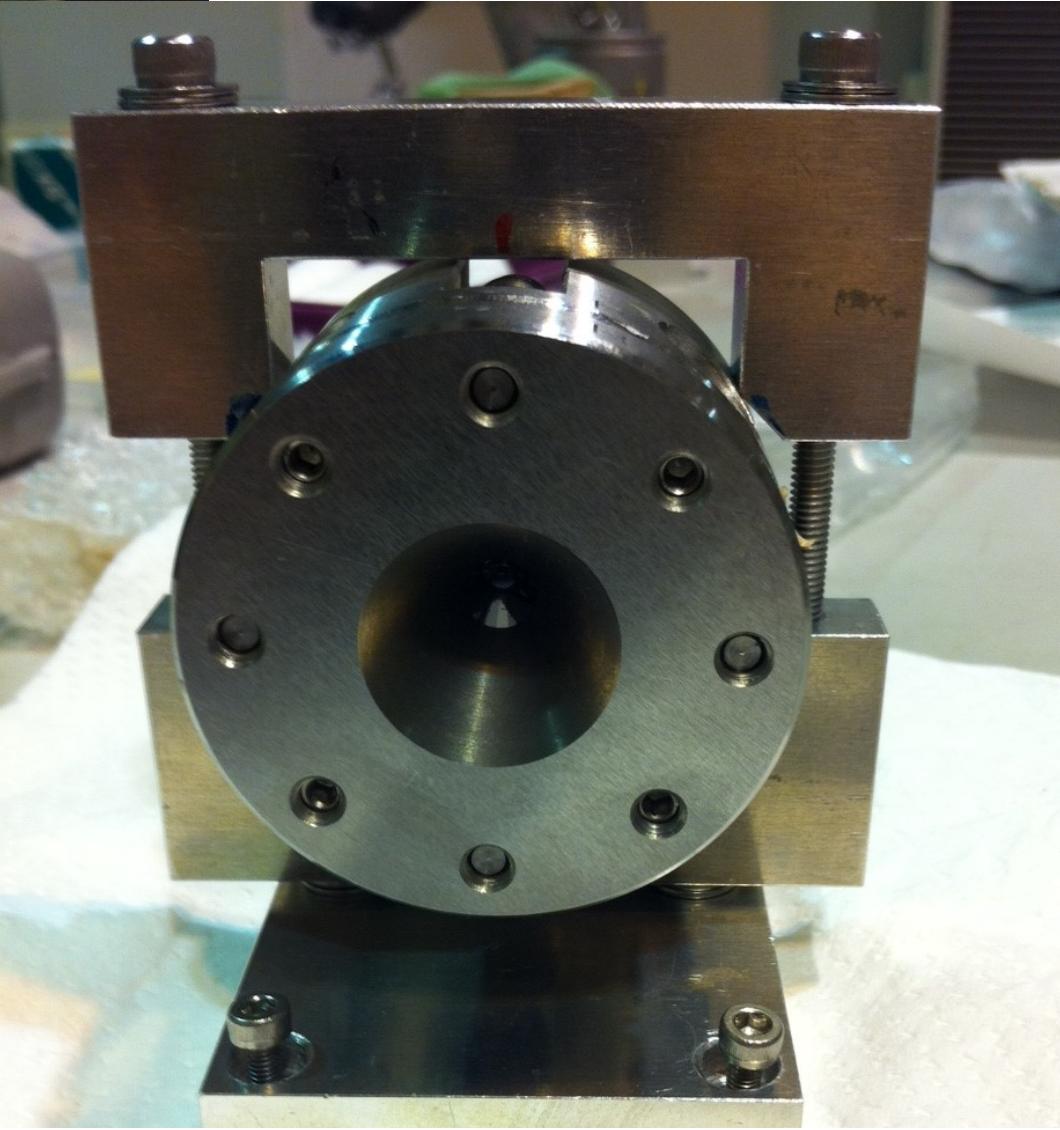
## BL35XU for High pressure and temperature:

IXS Optics [Baron et al., 2000]

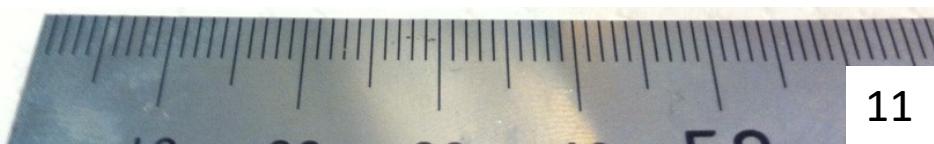
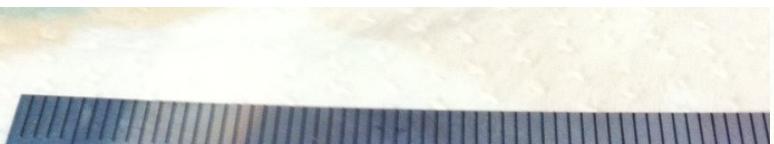
- Si (9 9 9) reflection: 2.8 meV resolution at 17.794 keV:
- Kirkpatrick-Baez mirror pair: **16 × 16 μm** beam size

XRD: Flat panel area detector

Heating: Portable laser heating system **COMPAT** (Fukui et al., 2013)

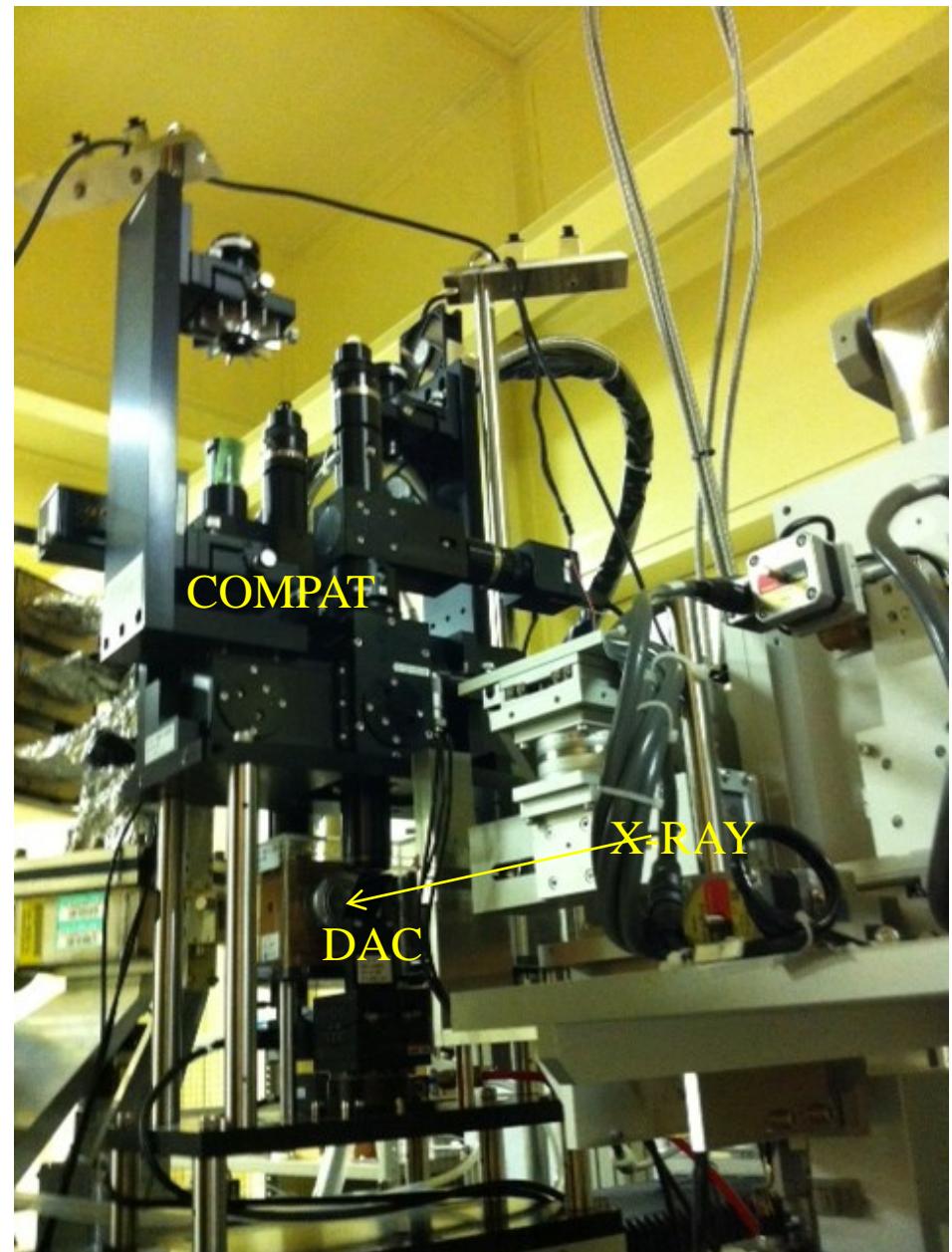


Symmetric diamond anvil cell used for IXS measurement at very high pressures: Culet size of **0.10 mm** for **174 GPa** and **300 K**



**Portable Laser heating  
system for IXS:  
COMPAT (COMpact system  
for generating extreme  
Pressures And Temperatures  
(Fukui et al., 2013)**

31 hours stable heating at  
2300 K and 10 hours heating  
at 3000 K



# Sound velocity measurements:

## **Light elements in the inner core (BL35XU)**

1. FeH: ~70 GPa at 300 K, Shibasaki et al (2012)
2. hcp-Fe : ~174 GPa, 300 K, Ohtani et al (2013)
3.  $\text{Fe}_3\text{S}$ : ~84.5 GPa, 300 K, Kamada et al. (2014)
4. hcp-Fe: ~88GPa, 1000 K, Ohtani et al (2015)
5. hcp-Fe: ~164 GPa, 3000 K. Sakamaki et al (2016)
6.  $\text{Fe}_3\text{C}$ : ~86 GPa, 2300 K, Takahashi et al. (2018)
7.  $\text{Fe}_{0.89}\text{Si}_{0.11}$  alloy: 90 GPa, 1800 K Sakairi et al. (2018)
8. Fe-Ni alloy: ~160 GPa, 2500 K (in prep.)

## **Higher Pressure and Pressure scale to multi-Megabar (BL43XU)**

1. Re: Primary scale of Rhenium ~ 210 GPa

# Sound velocity measurements:

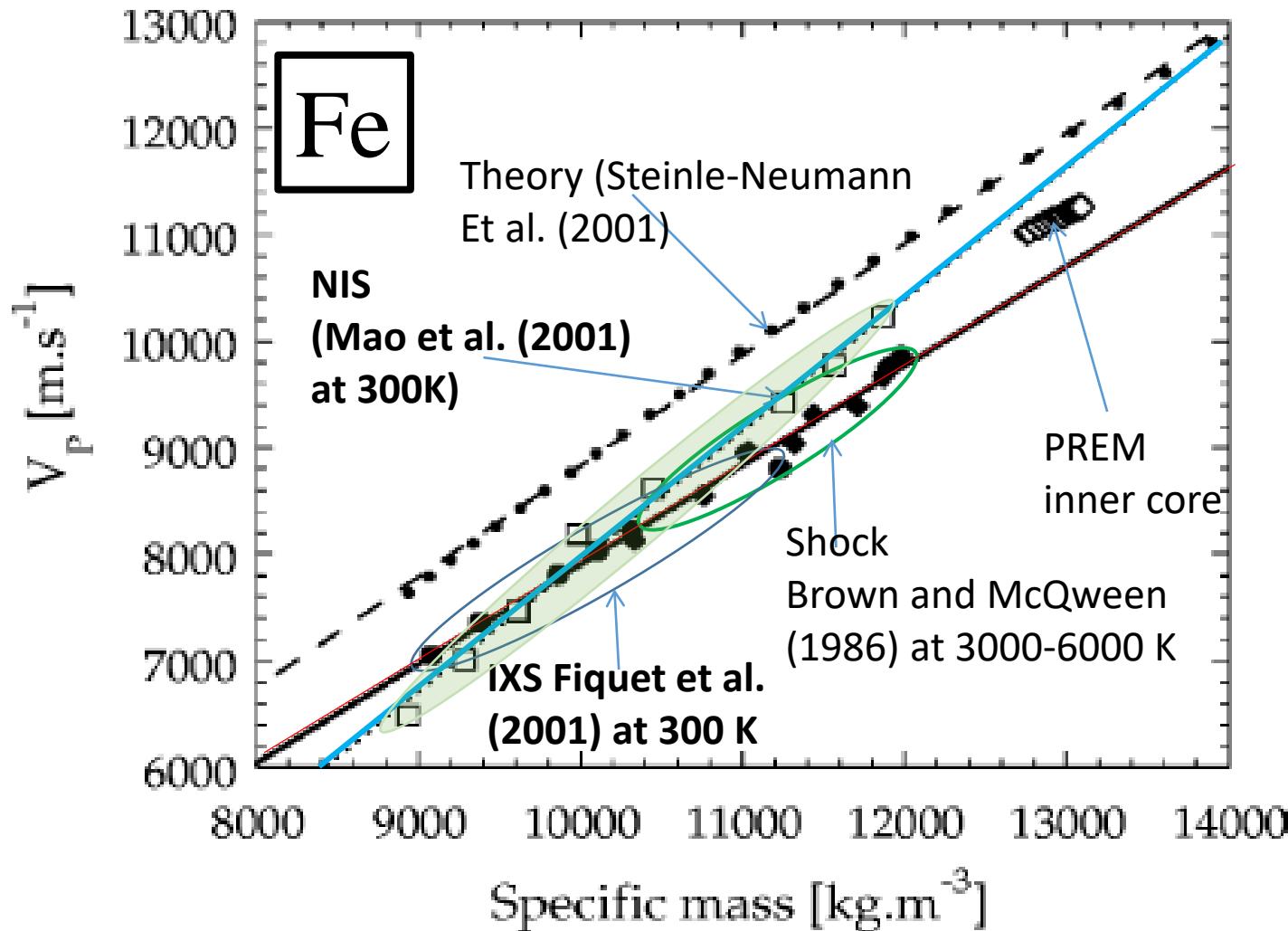
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## Higher Pressure and Pressure scale to multi-Megabar (BL43XU)

1. Re: Primary scale of Rhenium ~ 210 GPa

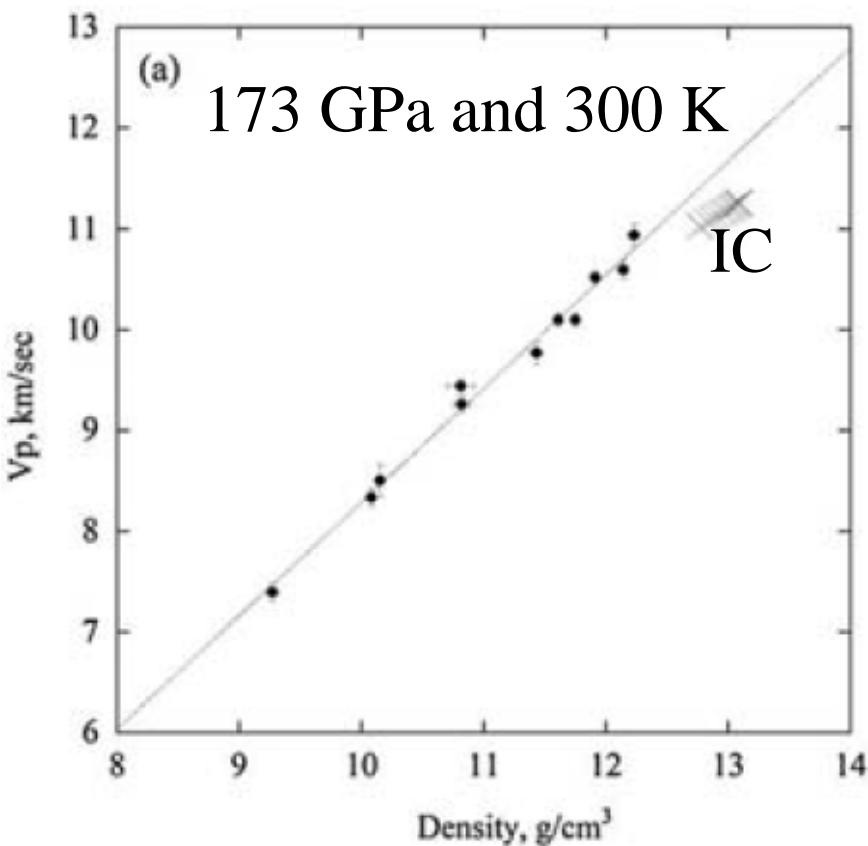
# After Fiquet et al. (2004)



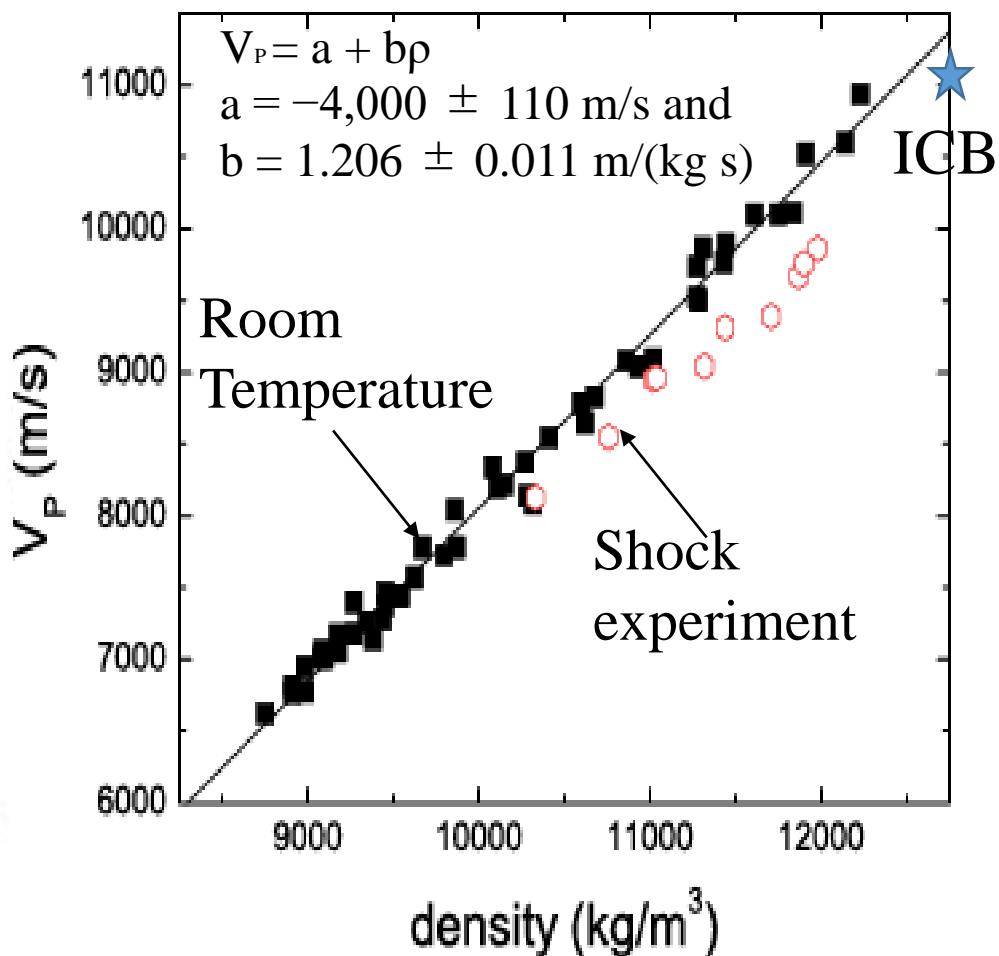
Discrepancy:  
IXS and Shock vs NIS (NRIXS) ?  
Temperature effect on Birch law ?

# Compressional velocity of hcp-Fe at room temperature

Ohtani et al. (GRL, 2013)



Antonangeli and Ohtani (PEPS, 2015)

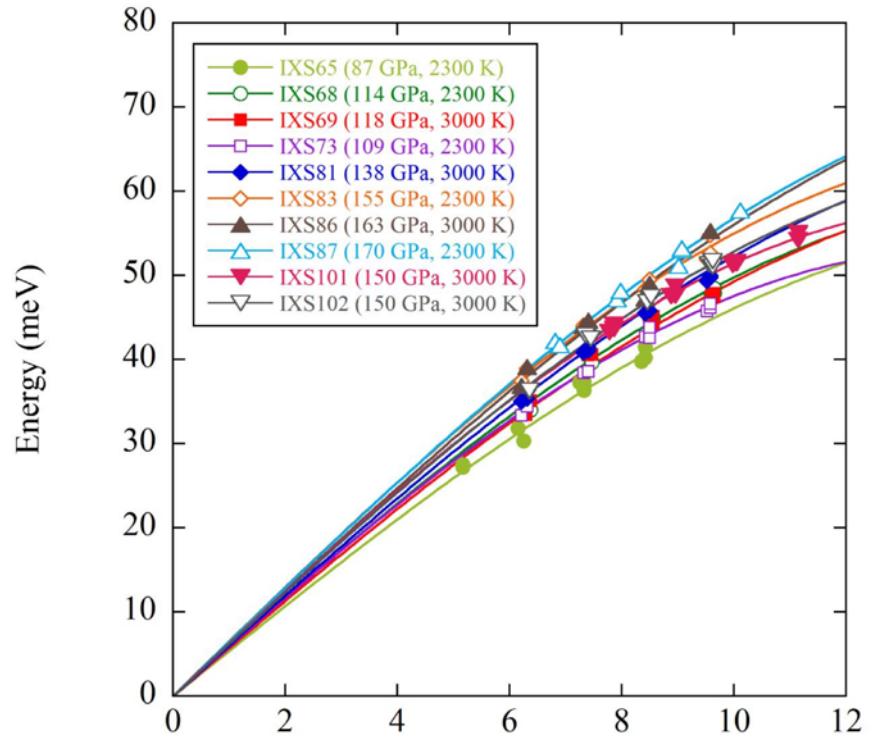
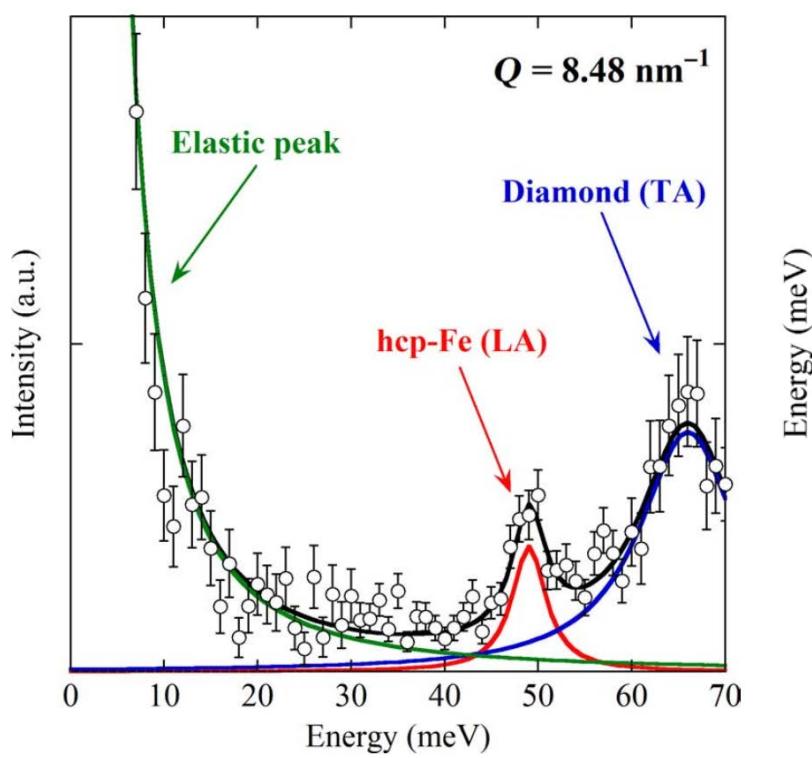


Data from Mao et al., 1998; Crowhurst et al., 2004;  
Antonangeli et al., 2004b; 2012; Ohtani et al., 2013;  
Decremps et al., 2014).



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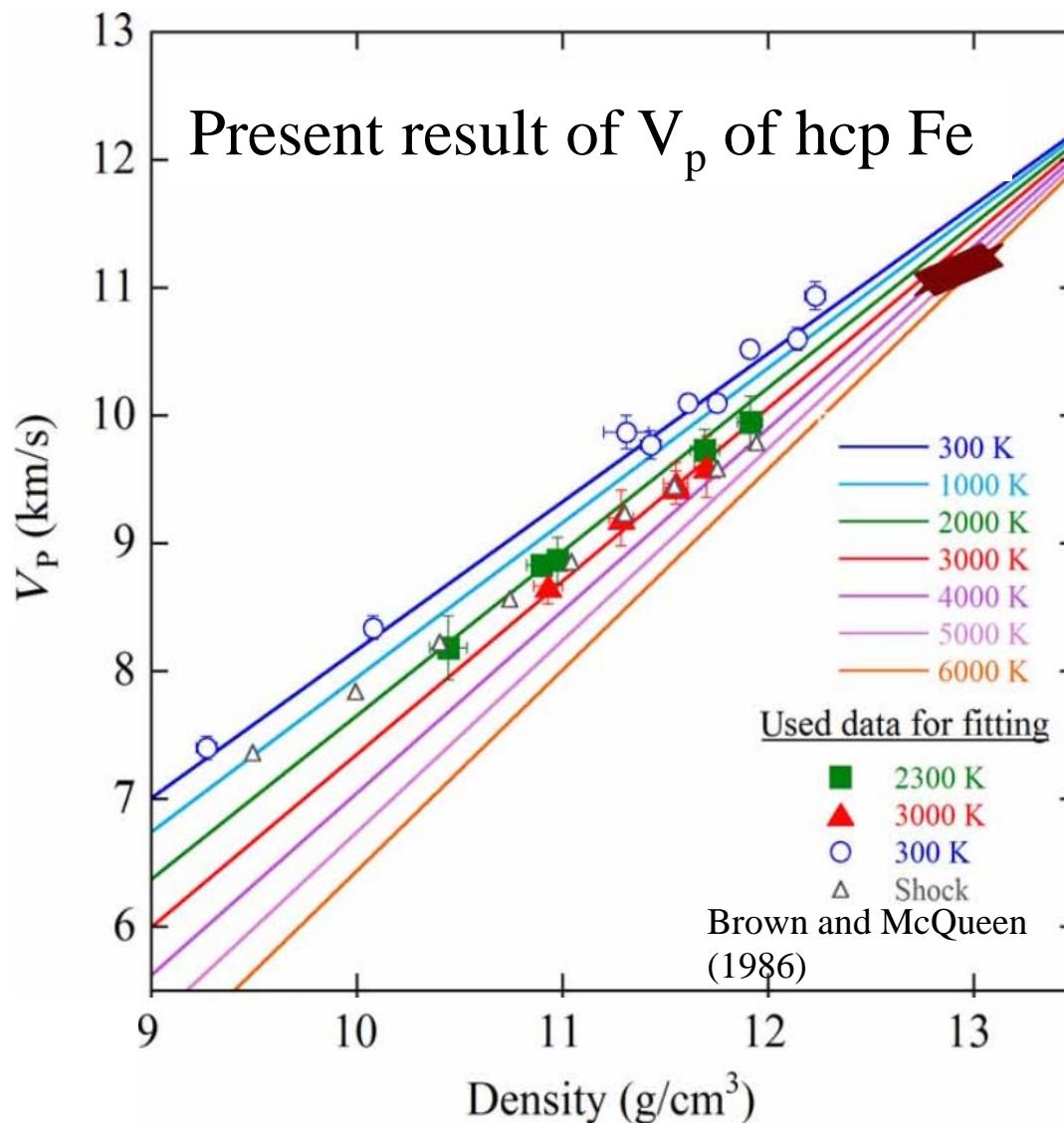
Sakamaki et al., (2016)  
hcp-Fe: ~163 GPa, ~3000 K

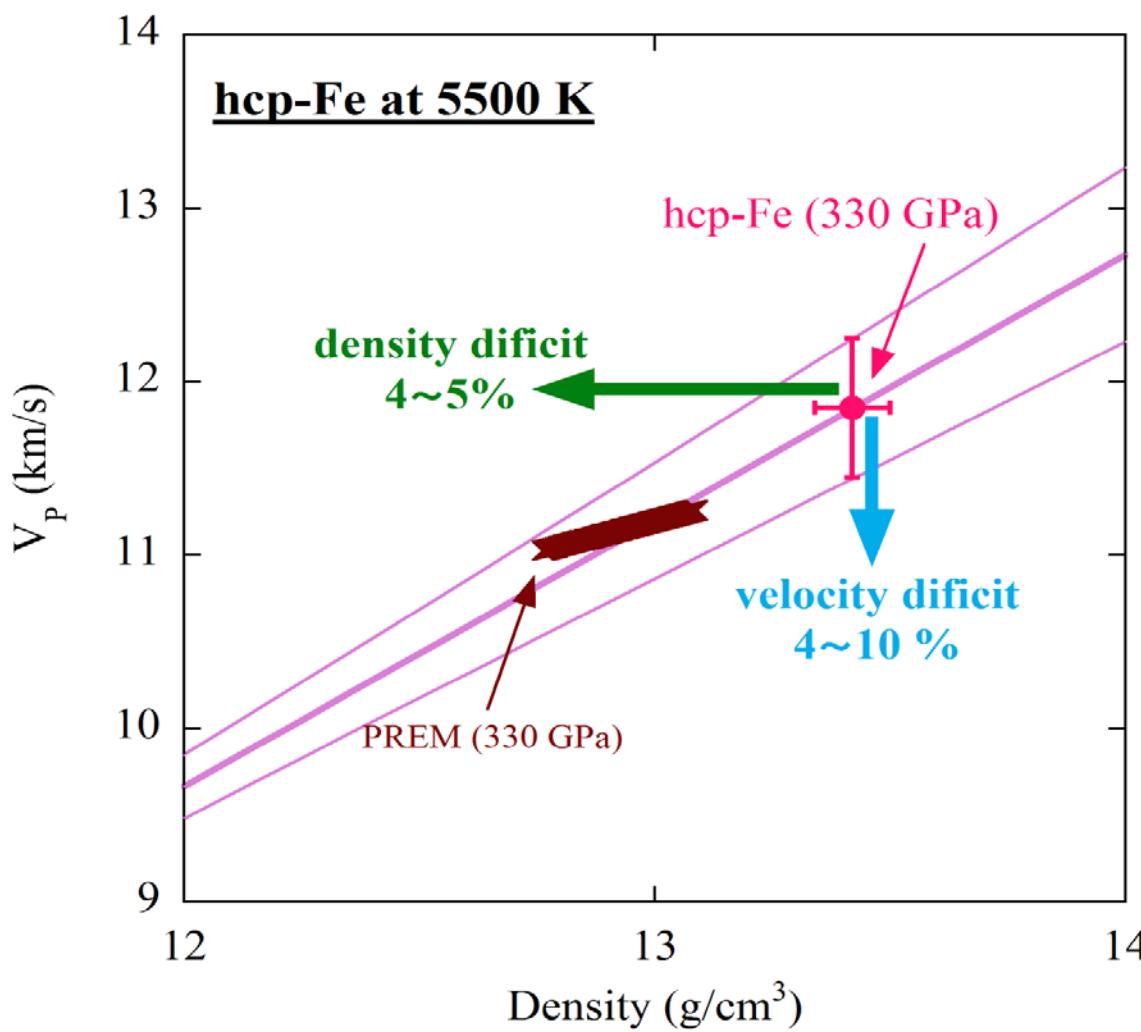


The dispersion curve was fitted by a sine function for determining V<sub>p</sub>

$$E[\text{meV}] = 4.192 \times 10^{-4} \text{ } V_p[\text{m/s}]^p Q_{\text{MAX}}[\text{nm}^{-1}] \sin\left(\frac{\pi}{2} \frac{Q[\text{nm}^{-1}]}{Q_{\text{MAX}}[\text{nm}^{-1}]}\right)$$

Isothermal  $\rho$ - $V_p$  fitting lines for **hcp-Fe** are expressed as  
 $V_p$  (km/s) = [1.160 $\rho$ (g/cm<sup>3</sup>) - 3.43] + [7.2 × 10<sup>-5</sup> × (T(K) - 300)  
× ( $\rho$  (g/cm<sup>3</sup>) - 14.2)]



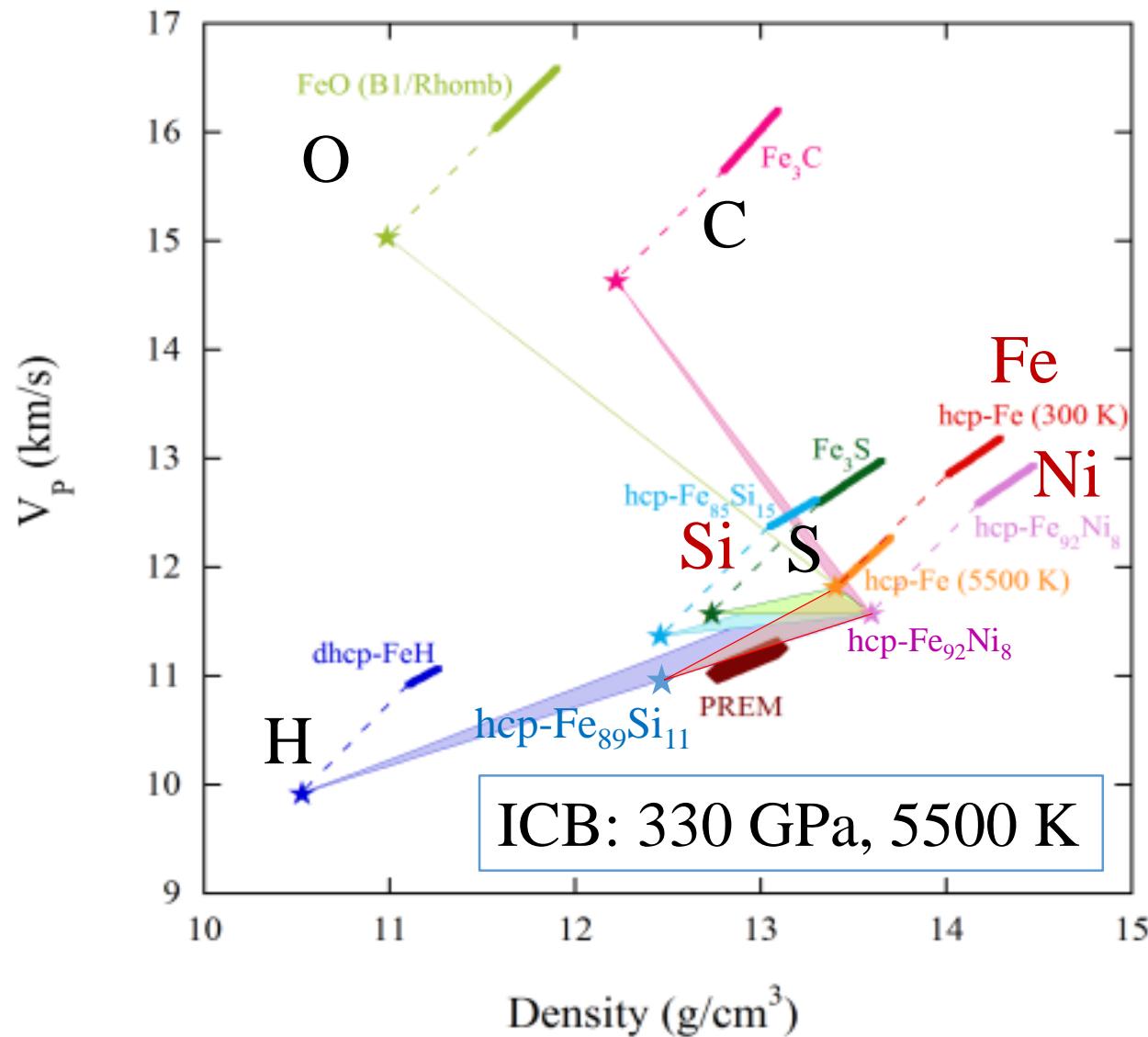


Effect of light elements:

**Inner core:  $V_p, Vs$  of hcp-Fe >  $V_p, Vs$  of PREM inner core.**

**Outer core:  $V_p$  of liquid hcp-Fe <  $V_p$  of PREM outer core.**

# The effect of light elements on Birch's law of hcp-Fe



# Two topics

- Sound velocity of iron and its alloy compounds and the Earth's core
- **Sound velocity at multi-Megabar pressure and the primary pressure scale**

# BL43XU Higher pressure: P>200 GPa

## IXS Optics [Baron et al., 2016]

- Si (9 9 9) reflection: 2.8 meV resolution at 17.793 keV:
- Multilayer Kirkpatrick-Baez (KB) mirror pair:  
**5 × 5 μm** beam size
- **Soller screen** [Baron, 2019]: to reduce scattering backgrounds from the diamond and to improve the signal to noise ratio

**XRD:** Flat panel area detector

# BL43XU Optics: Baron et al. (2000)

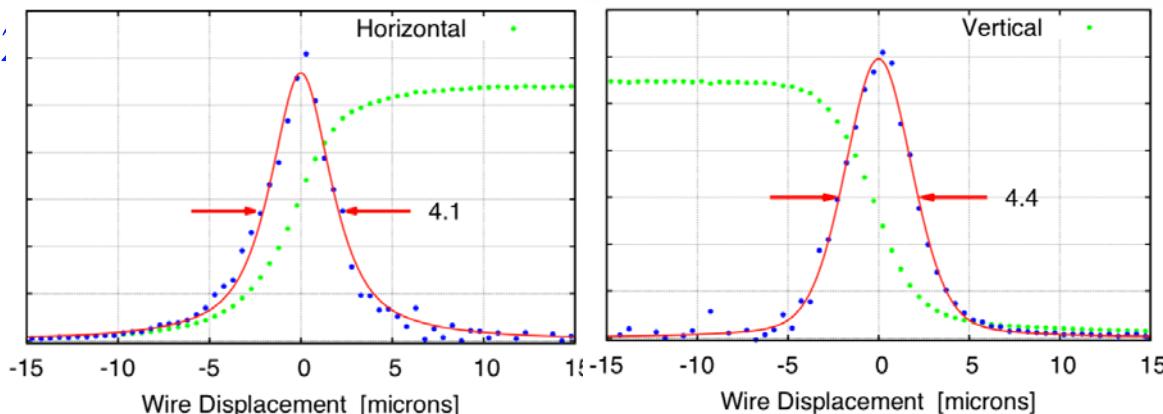
IXS with Diamond Anvil Cells (DACs) @  $P > 200$  GPa

**Focus Size:  $5 \times 5 \mu\text{m}^2$**

(FWHM):

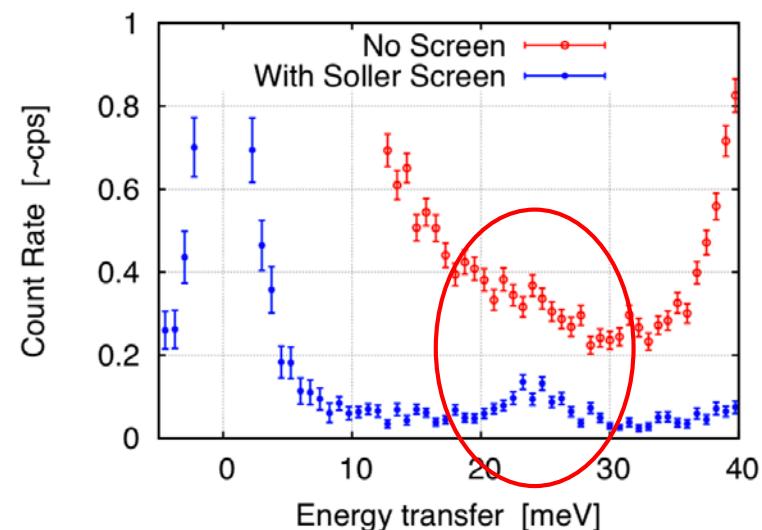
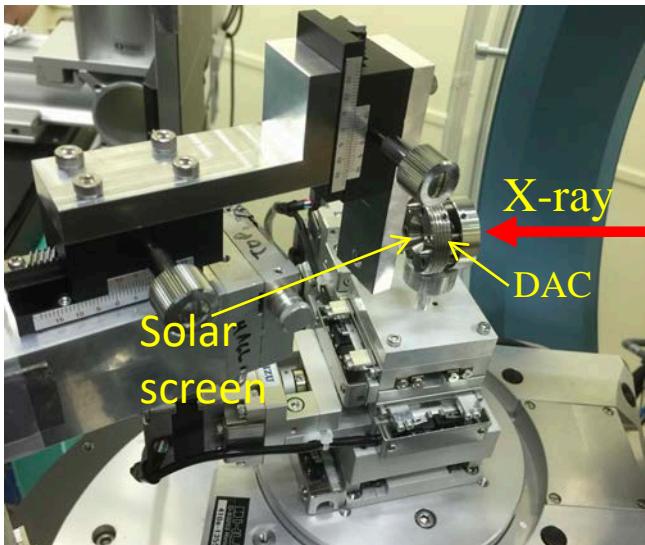
Elliptical KB (Multilayer)

for 17.8 keV



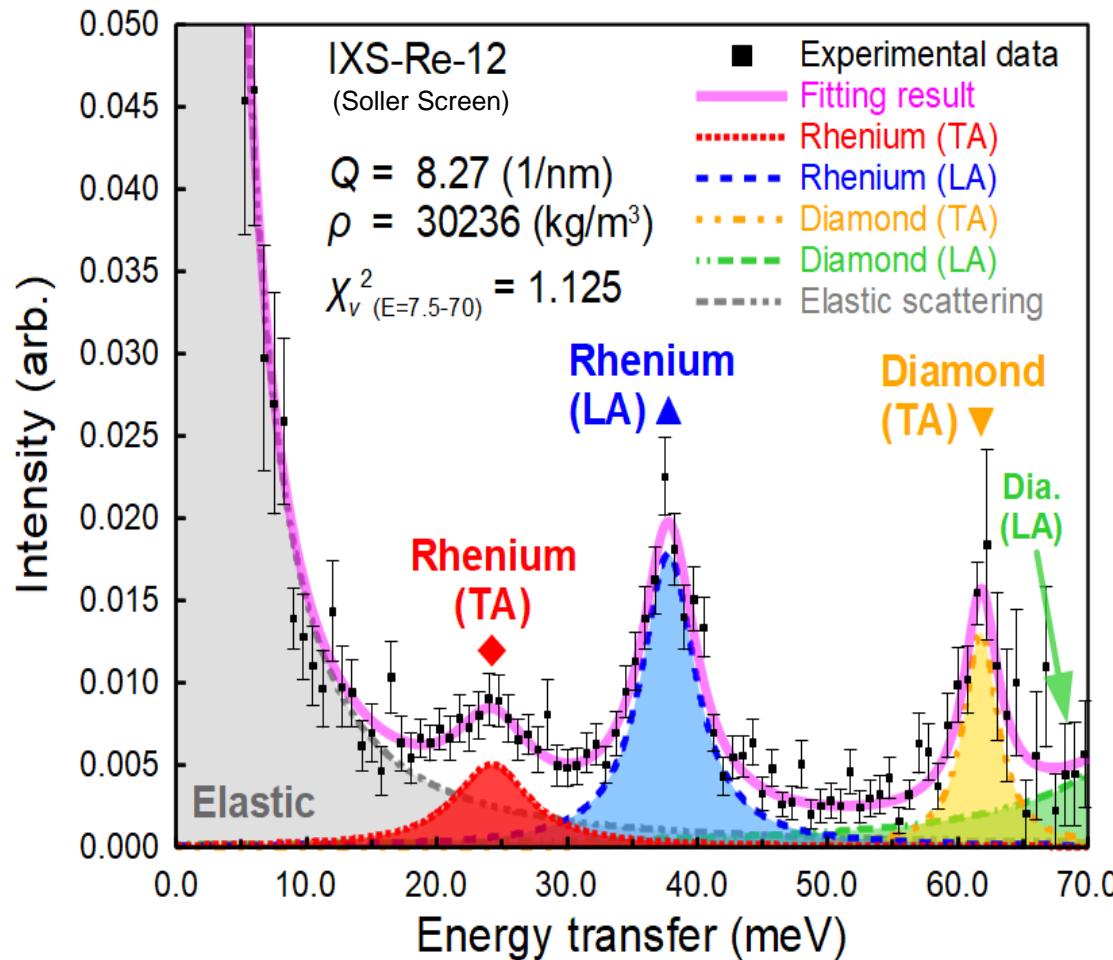
## Soller Screen

HP DAC work limited by **background from diamonds** (or Be gasket) ie: parasitic scattering from within a few mm of the sample



# Shear/Transverse (TA) Modes of Rhenium

(1) Good signal to noise (Soller screen) and (2) Simple setup (**no pressure medium**) make it possible to unambiguously **identify** the transverse modes of Re



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P~210 GPa  
and 300 K

# Primary Pressure Scale

Relate the density of a material (MgO, Gold, Re, etc) to P (at well-defined T)

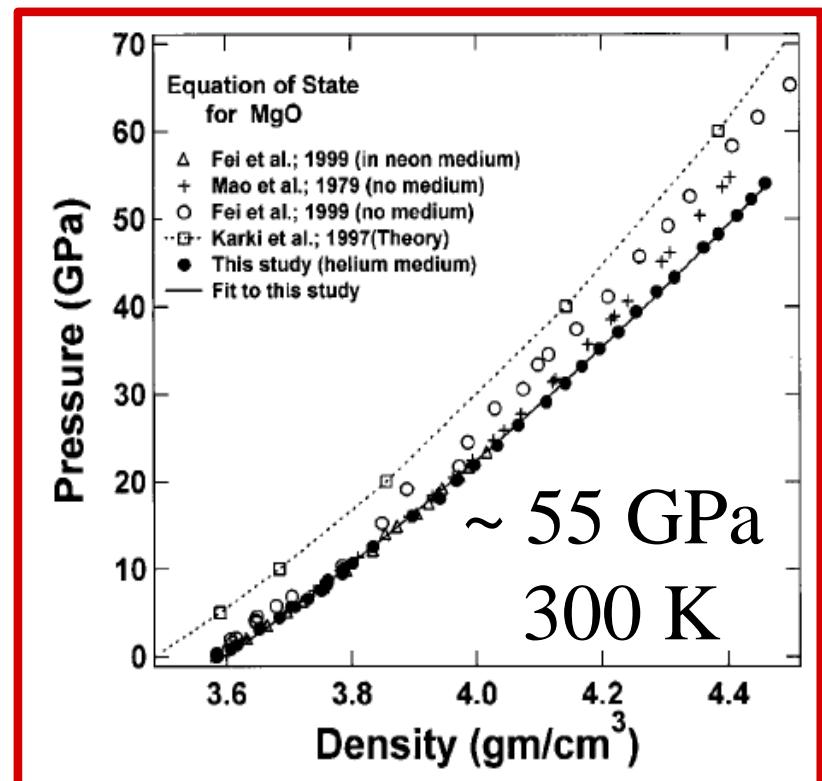
**Primary pressure scale:  $\rho$  (density),  $V_p$  and  $V_s$**

## MgO Primary Scale

Brillouin Scattering with  
a High Pressure Cell

gets both  $V_p$  and  $V_s$  at  
300 K (Density from  
separate x-ray works)

$\sim 55$  GPa at 300 K



Zha, Mao & Hemley, PNAS 2000 25

# Primary Pressure Scale

$$v_p = \sqrt{\frac{K_S + (4/3)G}{\rho}} \quad v_s = \sqrt{\frac{G}{\rho}}$$

$$K T_{(PT)} = \frac{K_{S(PT)}}{1 + [\alpha_{V(T)} \times \gamma_{(PT)} \times T]}$$

$$K T_{(PT)} = \rho_{(PT)} \left( \frac{\delta P}{\delta \rho} \right)_T$$

Integration of  $\left( \frac{\delta P}{\delta \rho} \right)_T$  provides a primary pressure scale

Primary  
Pressure Scale

$$P_{(\rho_T)} = \int_{\rho_{(0T)}}^{\rho_{(PT)}} \frac{K T_{(PT)}}{\rho_{(PT)}} \delta \rho$$

# Summary

We determined  $V_p$  of iron, and iron-light element (Si, S, O, H...) alloys using IXS to the Earth's core conditions

We proposed the Re primary pressure scale using  $V_p$ ,  $V_s$ , and  $\rho$  of Re measured by IXS to 210 GPa.

Thank you for your attention!

