

# Nonequilibrium Lattice Dynamics in photoexcited bismuth

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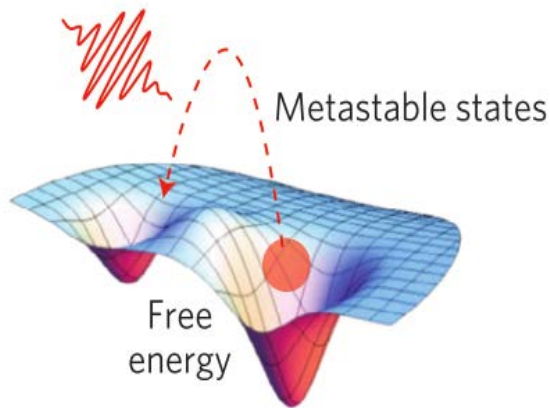
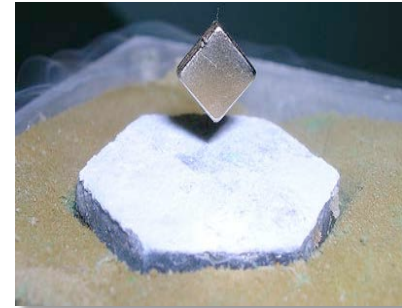
[dreis@stanford.edu](mailto:dreis@stanford.edu)



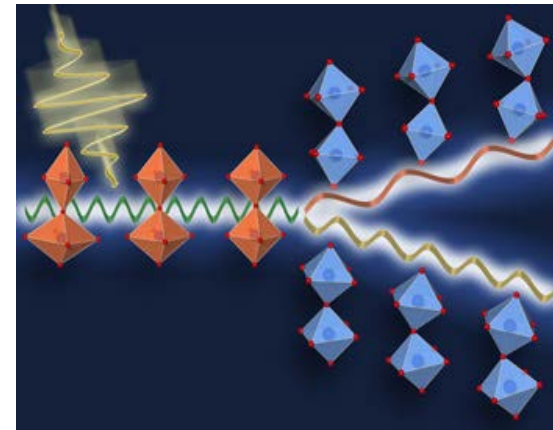
U.S. DEPARTMENT OF  
**ENERGY**

Office of  
Science

# Goal: understanding and controlling matter near and far from equilibrium



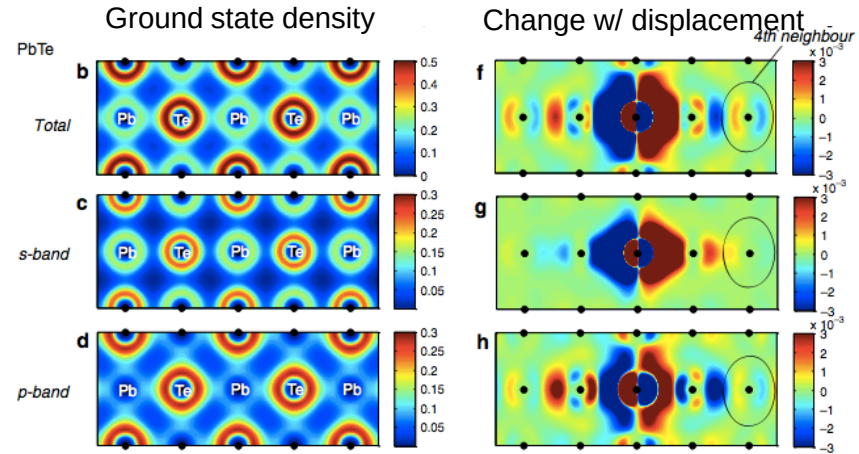
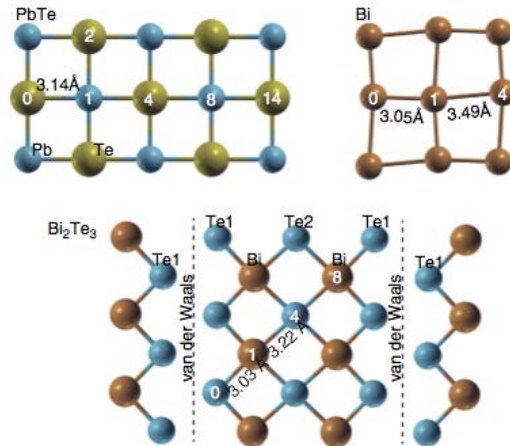
Basov (2018)



Andrea Cavalleri, MPD

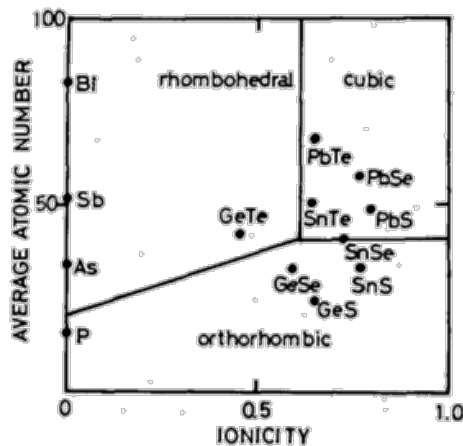
Requires new measurements,  
with combined time (energy) and momentum (spatial) resolution

# Lattice instabilities of Group V and IV-VI and related materials

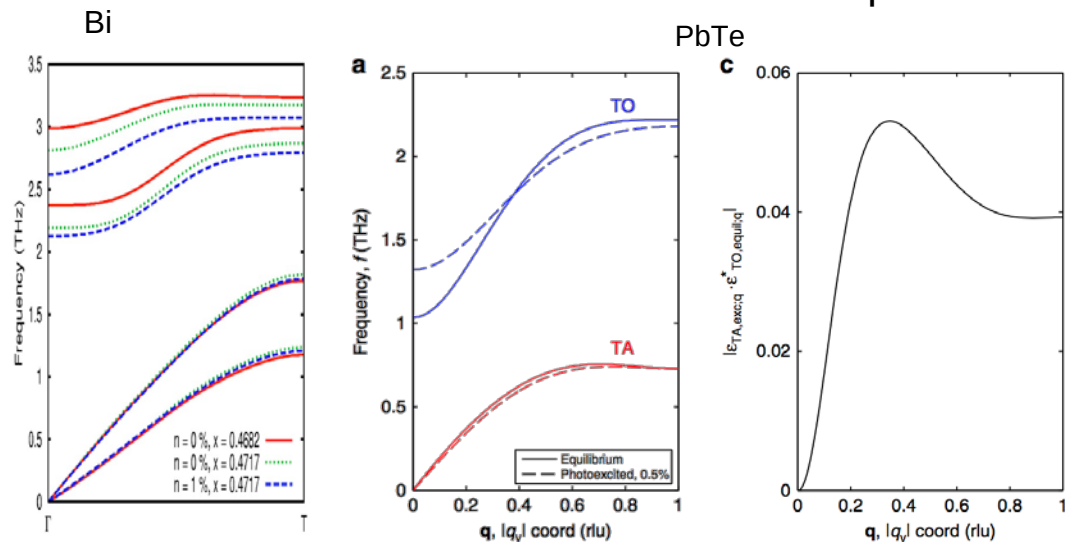


S. Lee et al., Nat. Comm. 2014

## Photo-excitation affects balance of e-ph



H Kawamura - Narrow Gap Semiconductors  
Physics and Applications, 1980

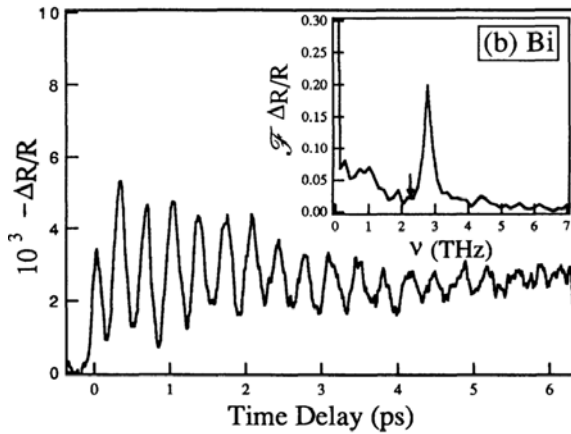


Murray et al. PRB 75 2007.

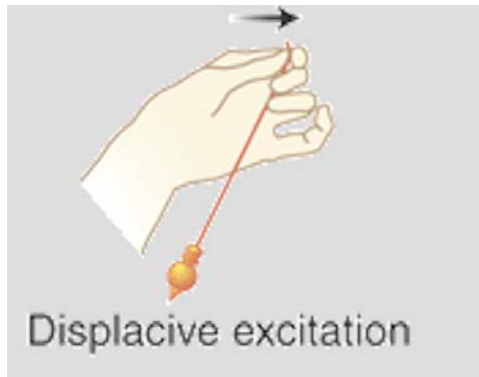
Jiang et al. Nat. Comm. 2016.

# “Displacive Excitation of Coherent Phonons”

$A_{1g}$ -mode optical  
generation/detection

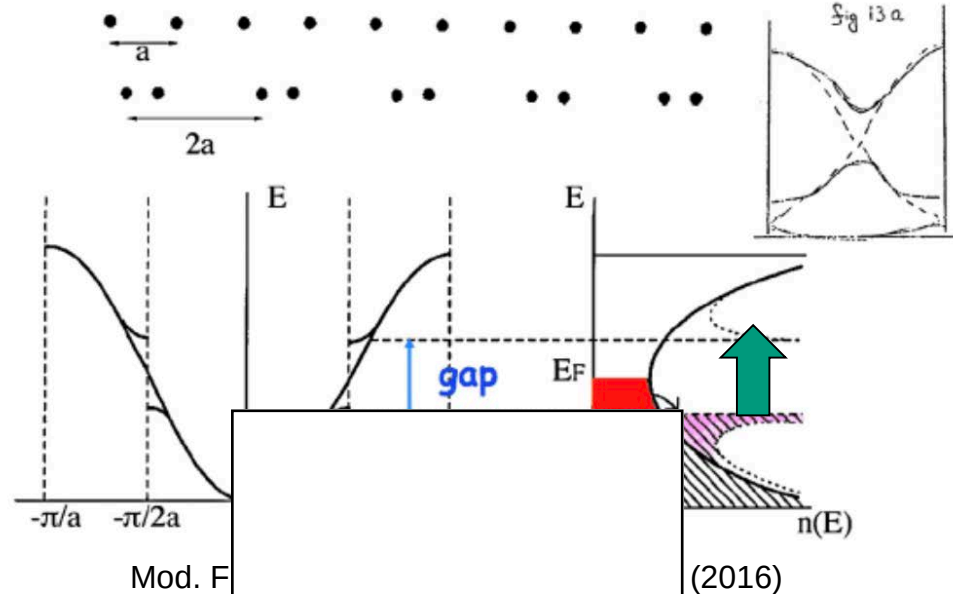


Zeiger et al., PRB 1992.



Modified from P. HUEY/SCIENCE

Oscillations about new equilibrium



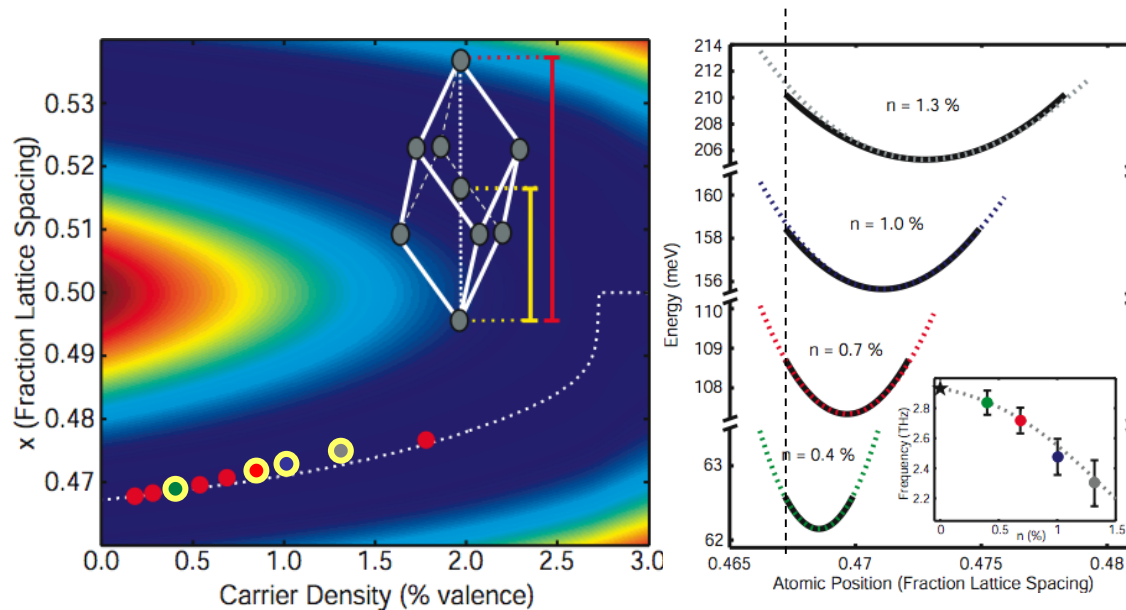
Mod. F

(2016)

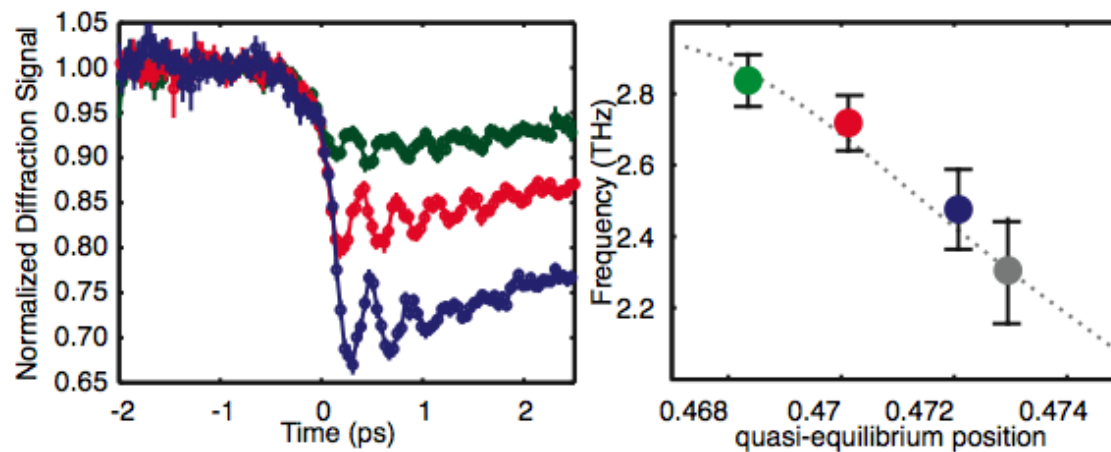
Peierls distortion



# Femtosecond diffraction ca. 2007

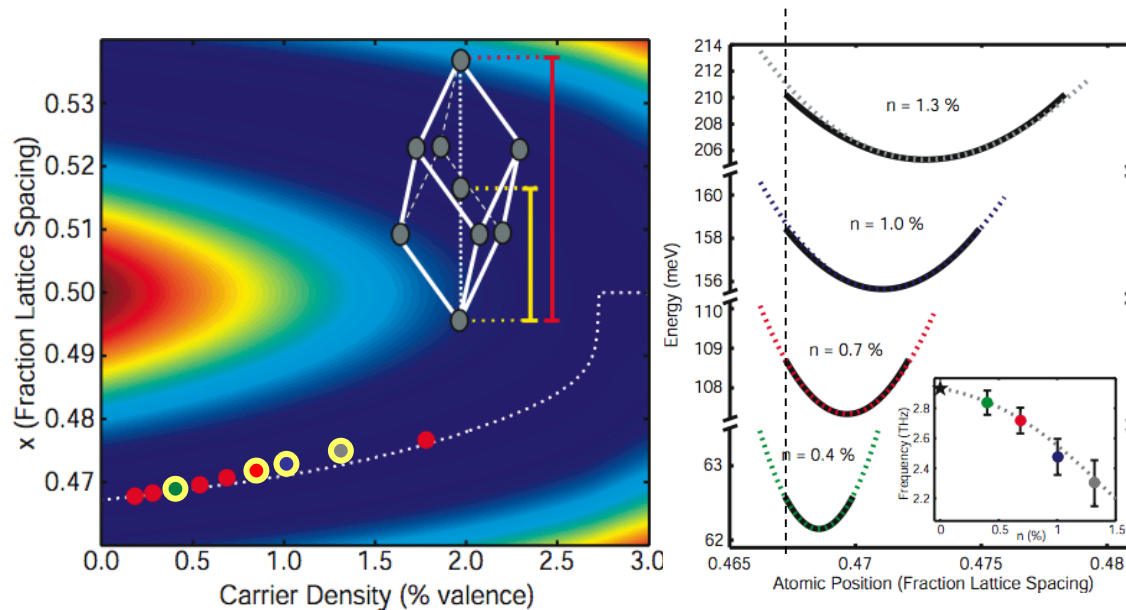


D. M. Fritz et al. Science 315, 2007.



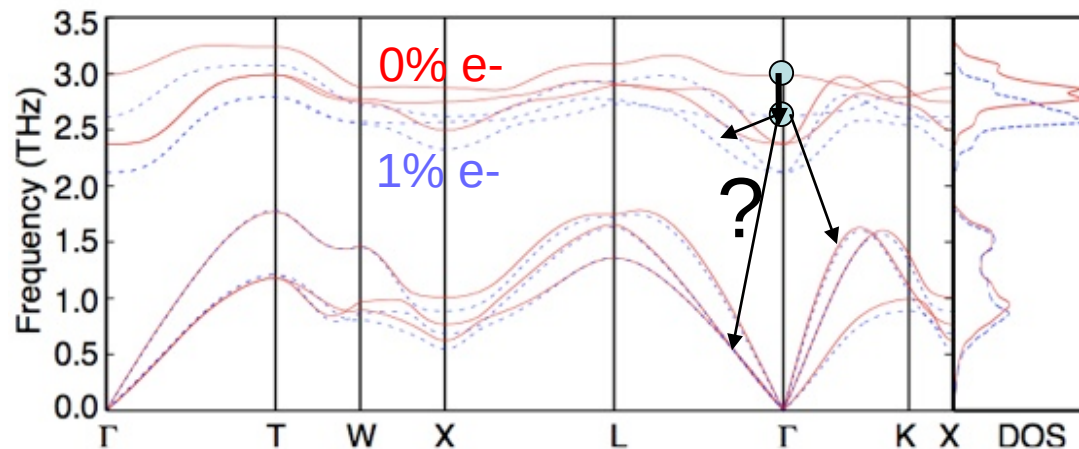
(SPPS)

# Femtosecond diffraction ca. 2007



D. M. Fritz et al. Science 315, 2007.

DFPT calculation



Murray et al. PRB 75 2007.

- Introduction to time-resolved (non-resonant) x-ray scattering (TRXS, FT-IXS)
- Measurement of Anharmonic decay constants ( $3^{\text{rd}}$  order forces)/channels in photo-excited bismuth
- Measurement of Nonequilibrium Dispersion/ Interatomic forces in photo-excited bismuth.

## Energy-resolved, time-integrated x-ray scattering (IXS)

$$I_s(\mathbf{Q}, \omega) \propto S(\mathbf{Q}, \omega) = \frac{1}{2\pi} \int S(\mathbf{Q}, \Delta t) e^{-i\omega\Delta t} d\Delta t$$
$$\propto \sum_j \left\langle (\mathbf{Q} \cdot \mathbf{u}_{jq})^2 \right\rangle \delta(\omega \pm \omega_{jq})$$

van Hove, Squires, ...

## Time-resolved, energy-integrated x-ray scattering (TRXS, FT-IXS)

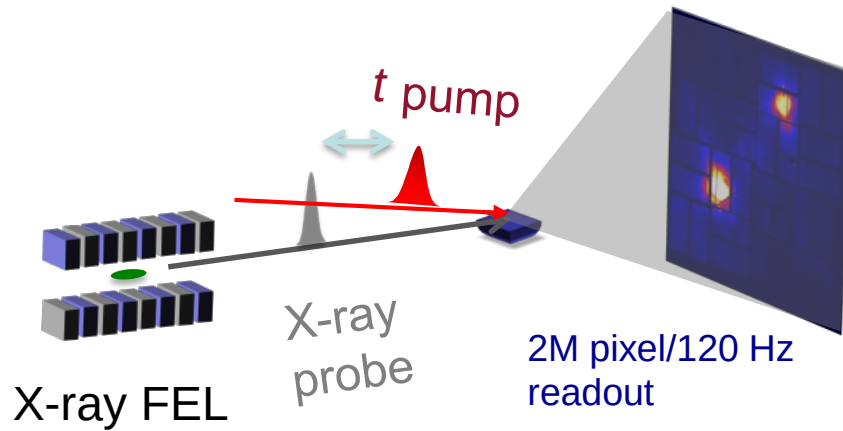
$$I_s(\mathbf{Q}, t) \propto S(\mathbf{Q}; t) \propto \sum_{jj'} \left\langle \mathbf{Q} \cdot \mathbf{u}_{jq}(t) \mathbf{u}_{\mathbf{q}j'}^*(t) \cdot \mathbf{Q} \right\rangle$$

$$\mathbf{q} = \mathbf{G} - \mathbf{Q}$$

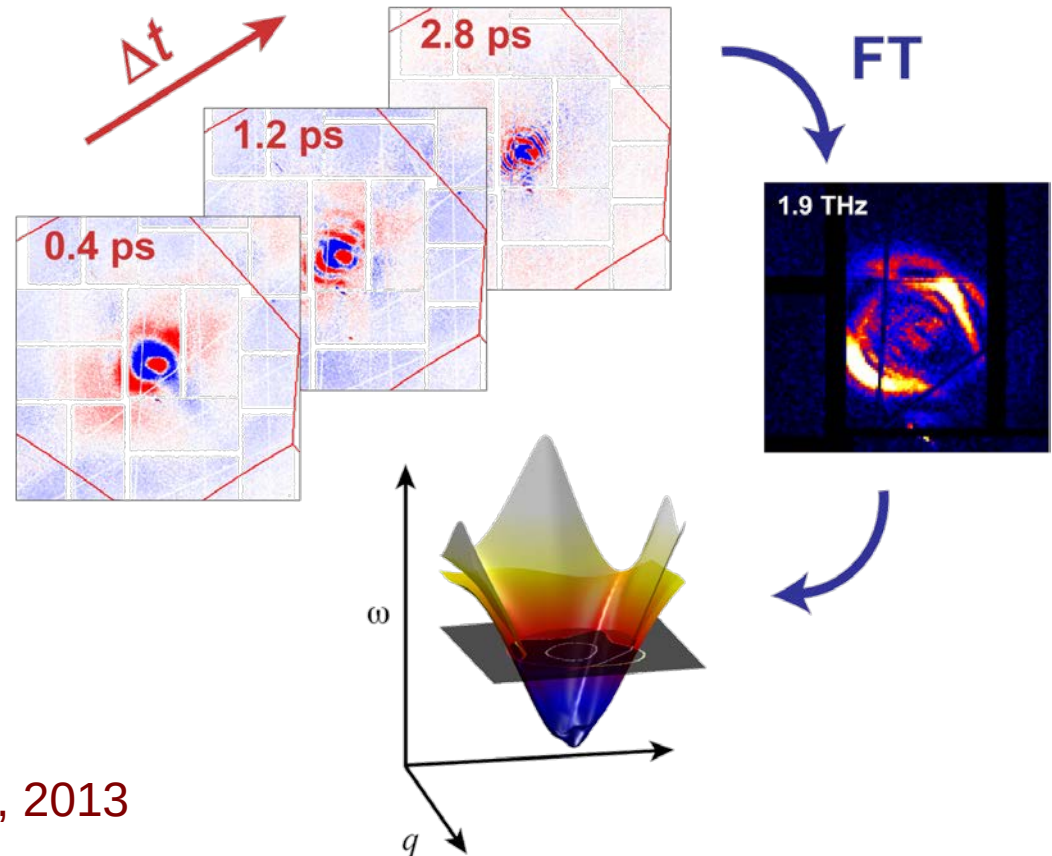
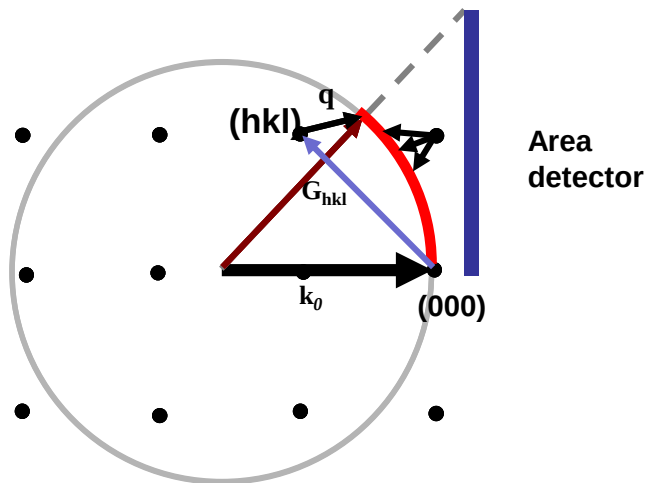
Trigo & DAR



# Fourier-Transform IXS



$$I_s(\mathbf{q}, t) \sim \sum_{jj'} \langle \mathbf{q} \cdot \mathbf{u}_{j\mathbf{q}}(t) \mathbf{u}_{j'\bar{\mathbf{q}}}^*(t) \cdot \mathbf{q} \rangle$$



Trigo et al. Nature Physics. 9, 790, 2013

Zhu et al., Phys. Rev. B, 92, 054303, 2015

# The Linear Coherent Light Source (LCLS) at SLAC

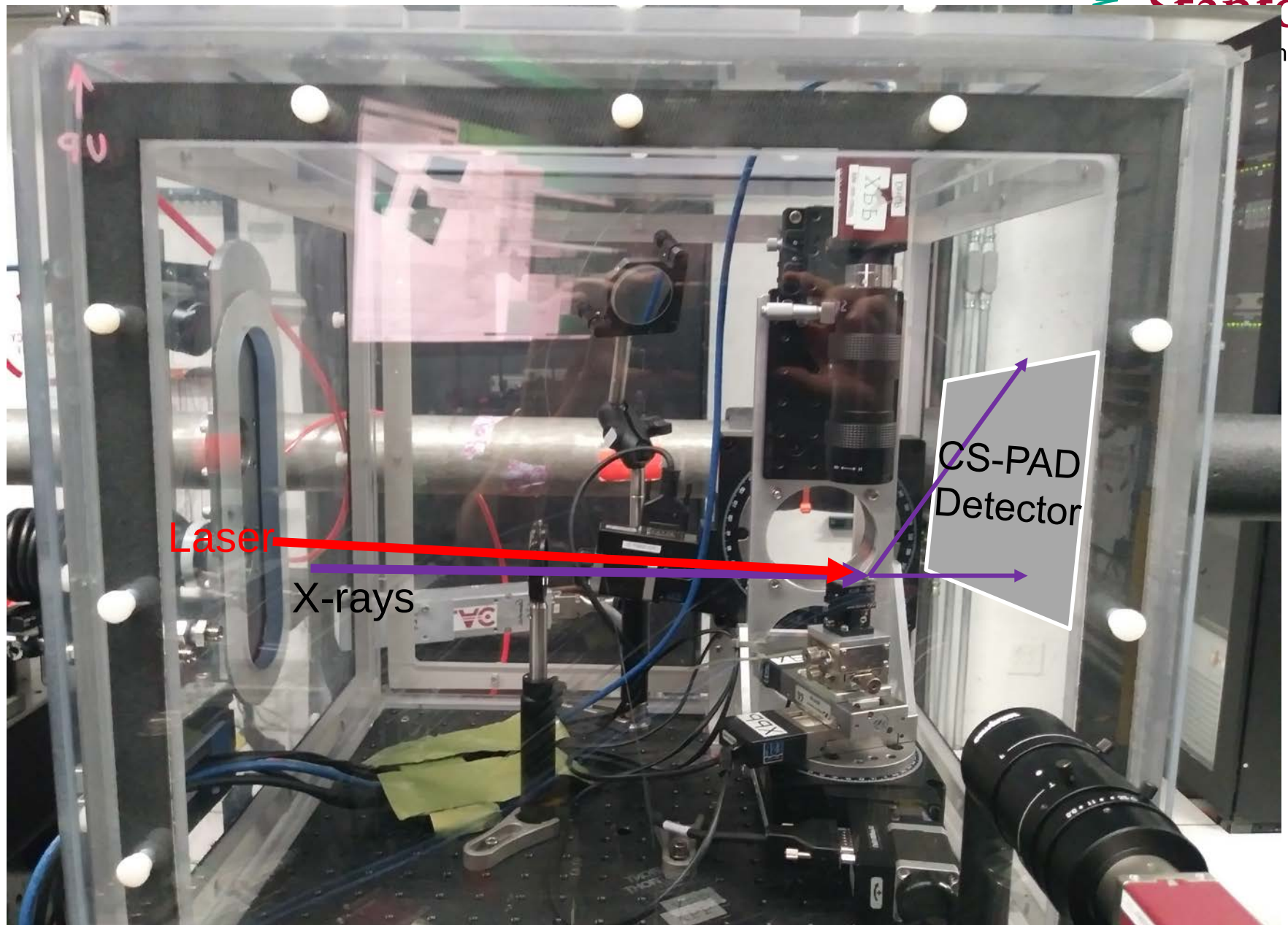




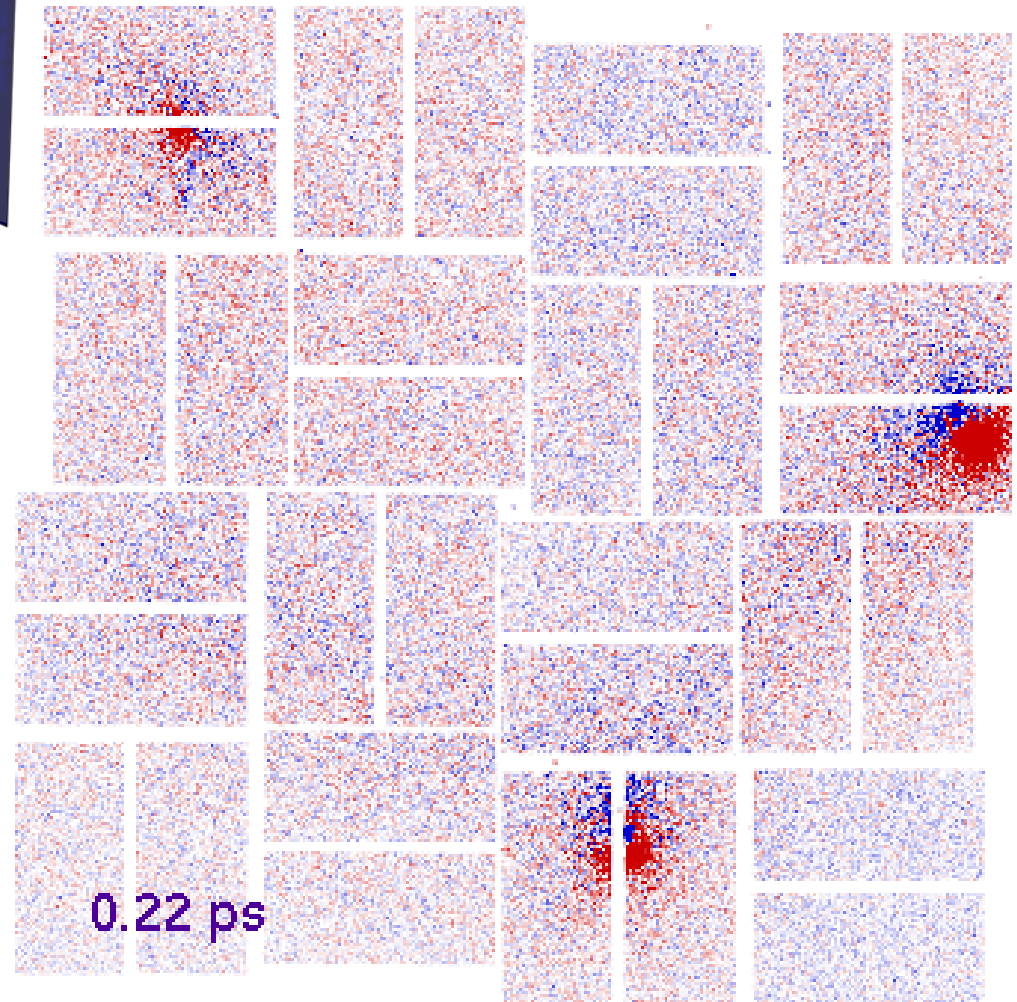
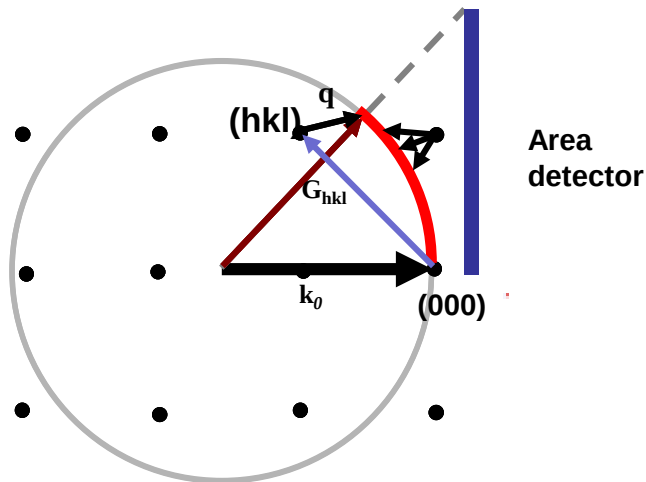
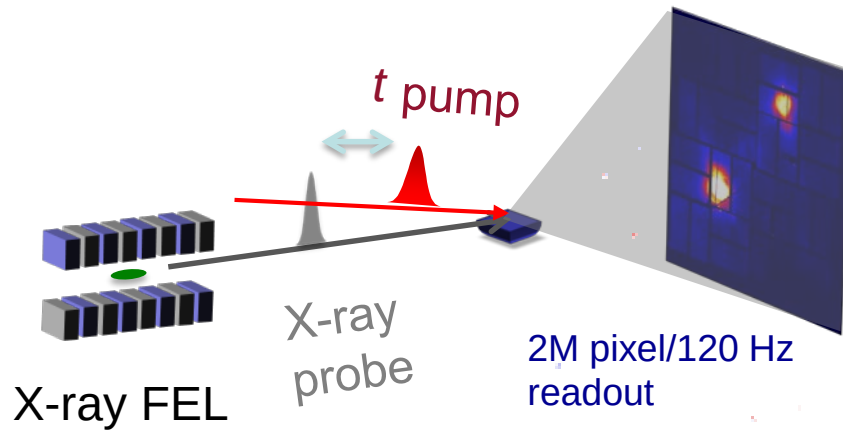
# The XPP instrument at LCLS



Photo credit: Daniele Fanelli

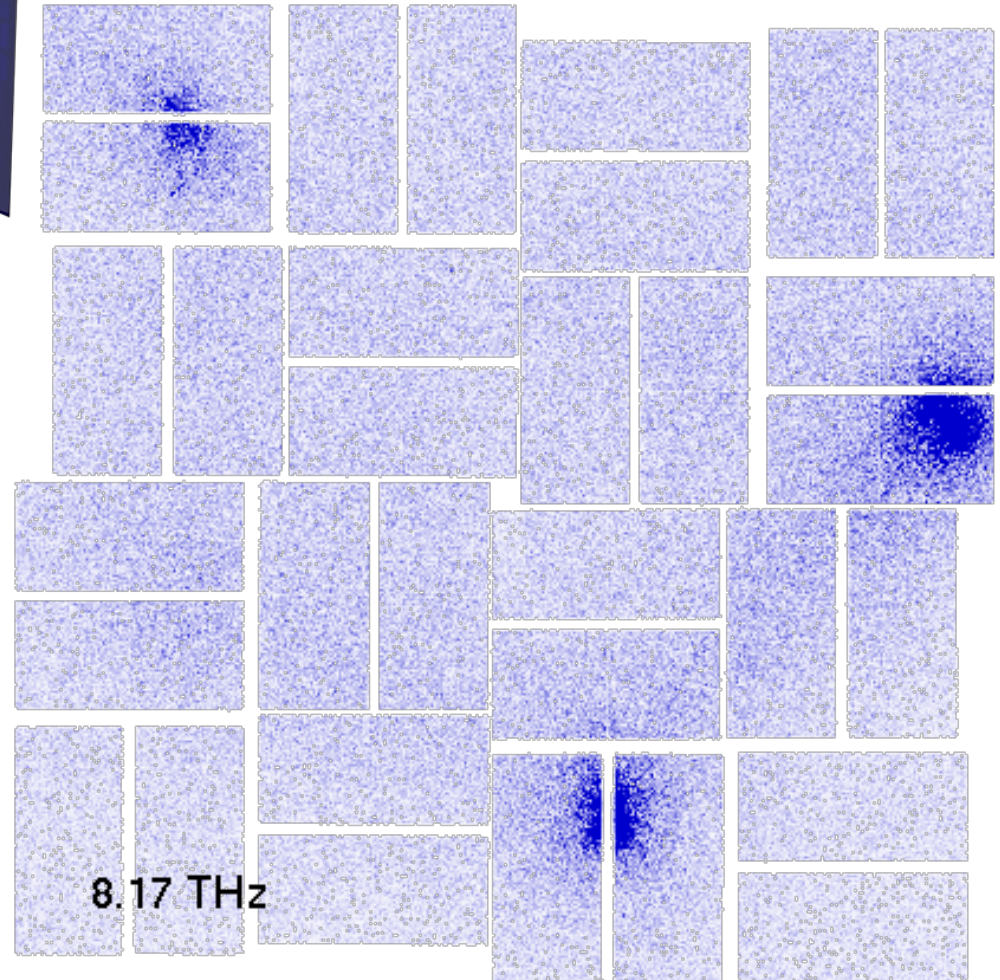
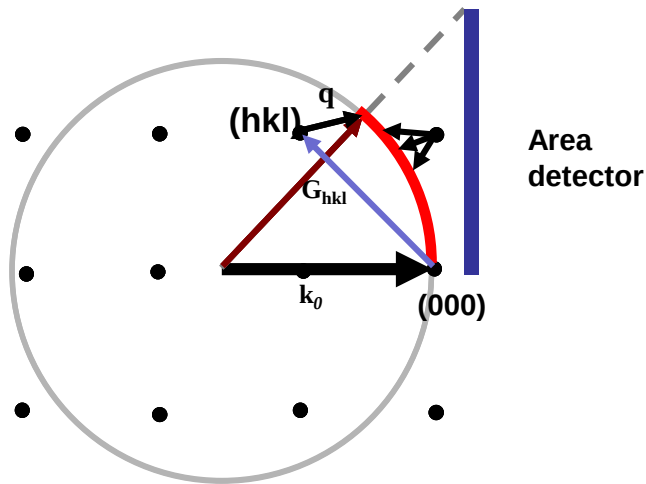
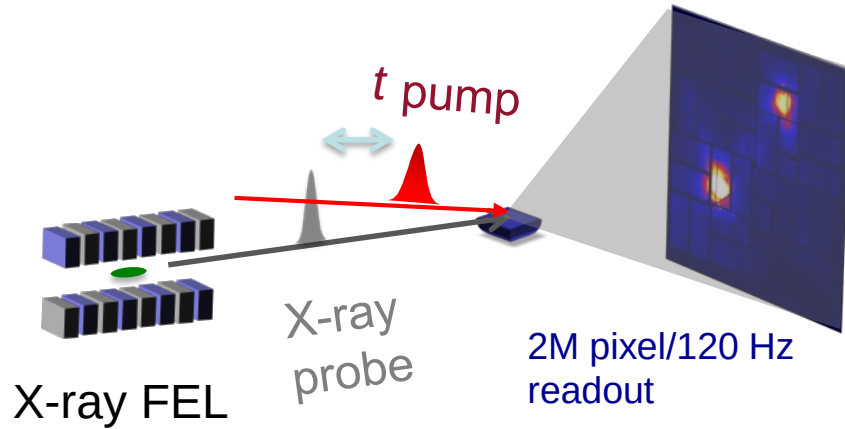


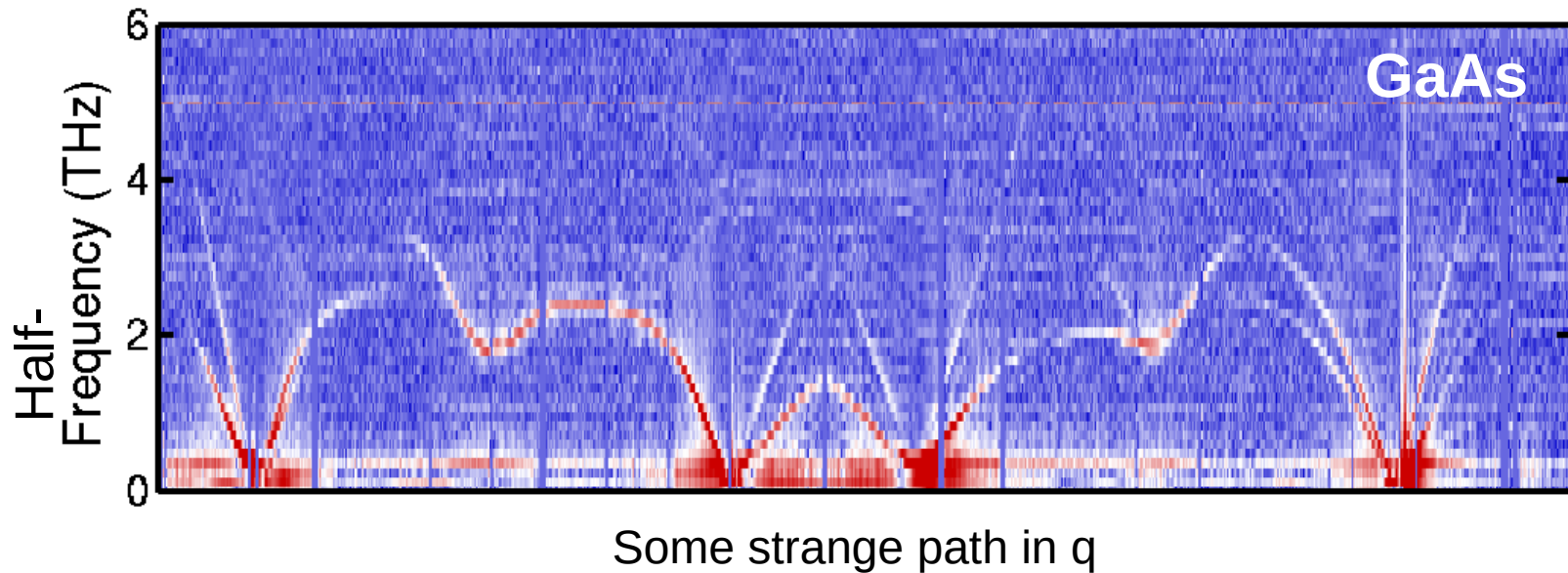
# Example, GaAs ~10fs pump/probe





# Example, GaAs ~10fs pump/probe





- Non-equilibrium measurement
- Efficient use of photons, broad band, no analyzer ( $\tau_p < 1/\omega$ )
- Resolution limited by maximum delay

# Mechanism?

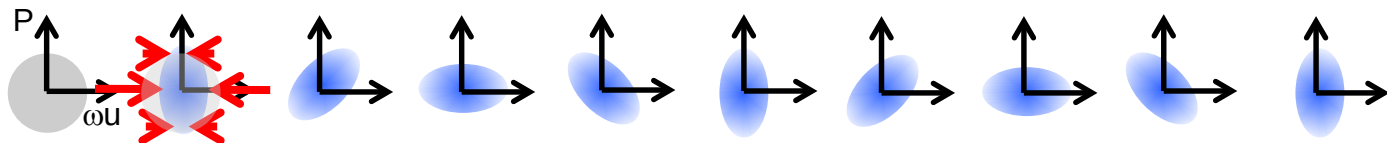
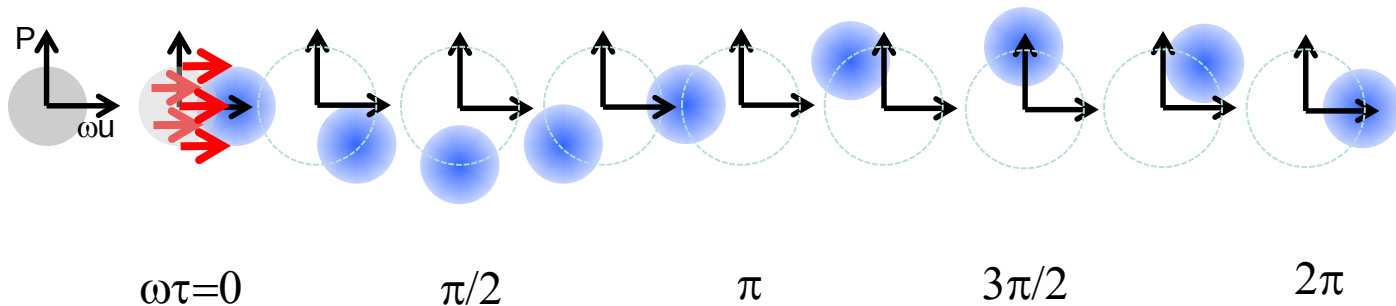
$$H' \propto I(t)u$$

1<sup>st</sup> order Raman

coherent state

$$\langle u \rangle \propto \cos \Omega t$$

$$\langle u \rangle^2 \propto \cos 2\Omega t$$



$$H' \propto I(t)u^2$$

2<sup>nd</sup> order Raman

squeezed state

$$\langle u \rangle = 0$$

$$\langle u^2 \rangle \propto \cos 2\Omega t$$

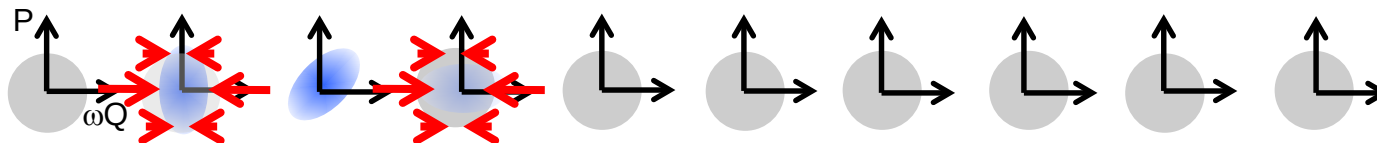
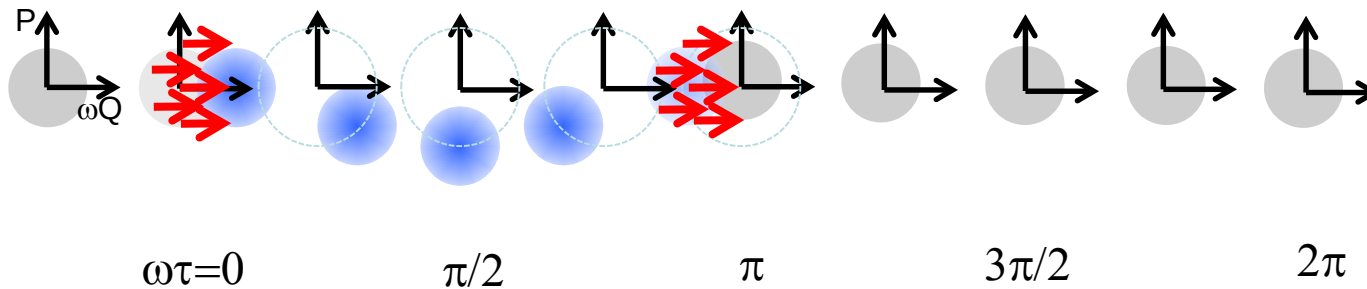
# Mechanism?

$$H' \propto I(t)u$$

1<sup>st</sup> order Raman

coherent state

$$\nu = (2n + 1) \frac{1}{2\Delta t}$$



$$H' \propto I(t)u^2$$

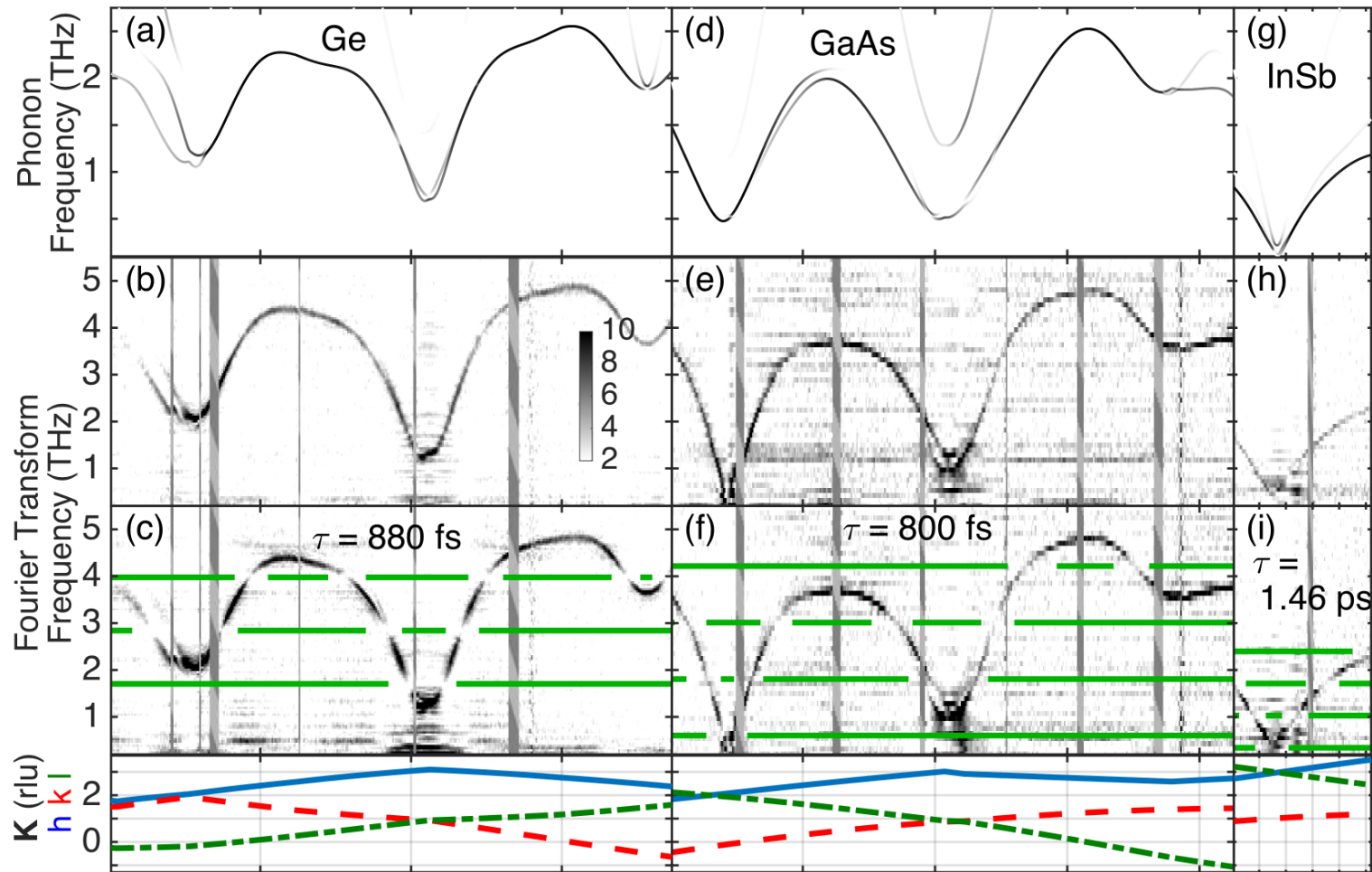
2<sup>nd</sup> order Raman

squeezed state

$$\nu = (2n + 1) \frac{1}{4\Delta t}$$



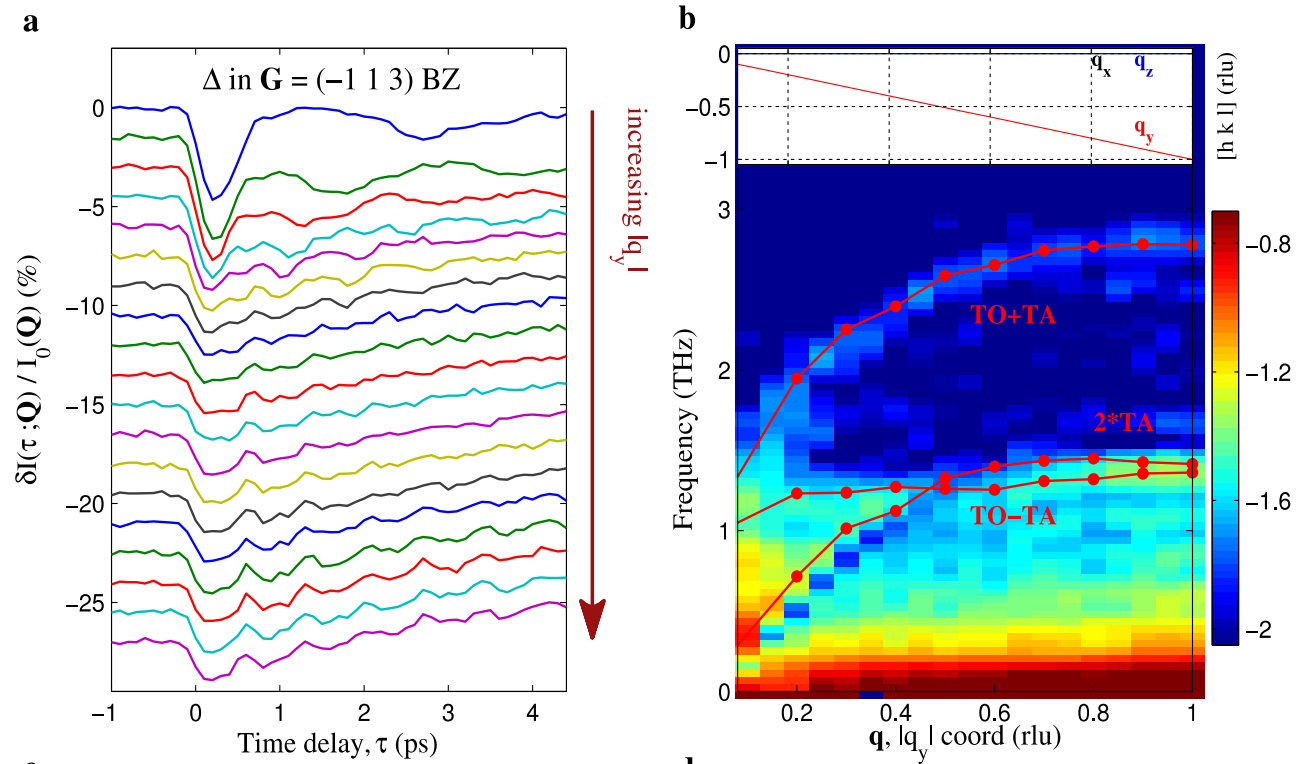
# For perfect crystals, squeezing...



# Stabilization of paraelectric phase in PbTe with photo-excitation

Transverse two-phonon  
Spectra along bonding  
direction ( $\Gamma$ -X )

overtone ( $2\omega_{TA}$ ) &  
combination ( $\omega_{TO} \pm \omega_{TA}$ )

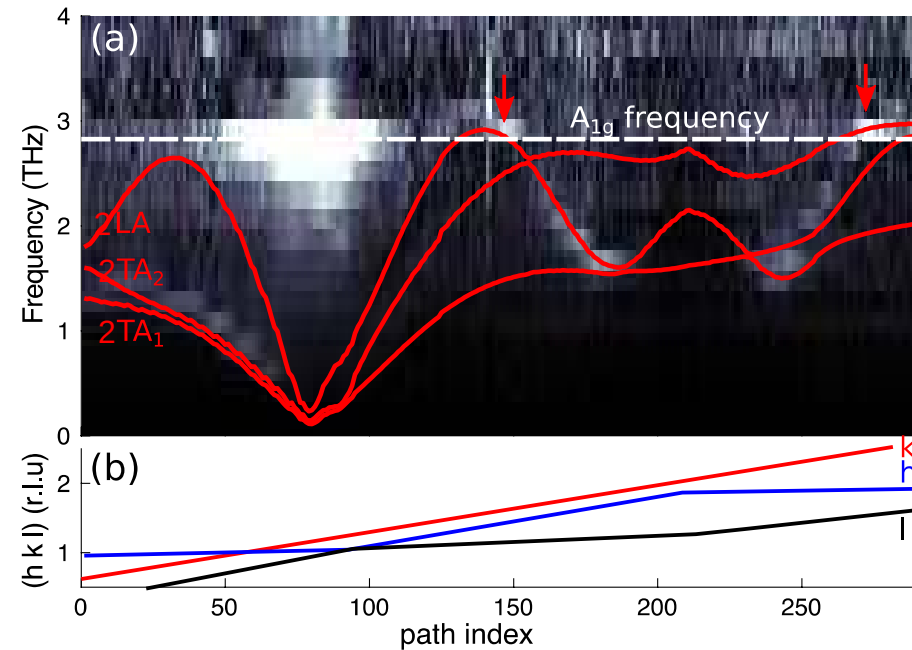
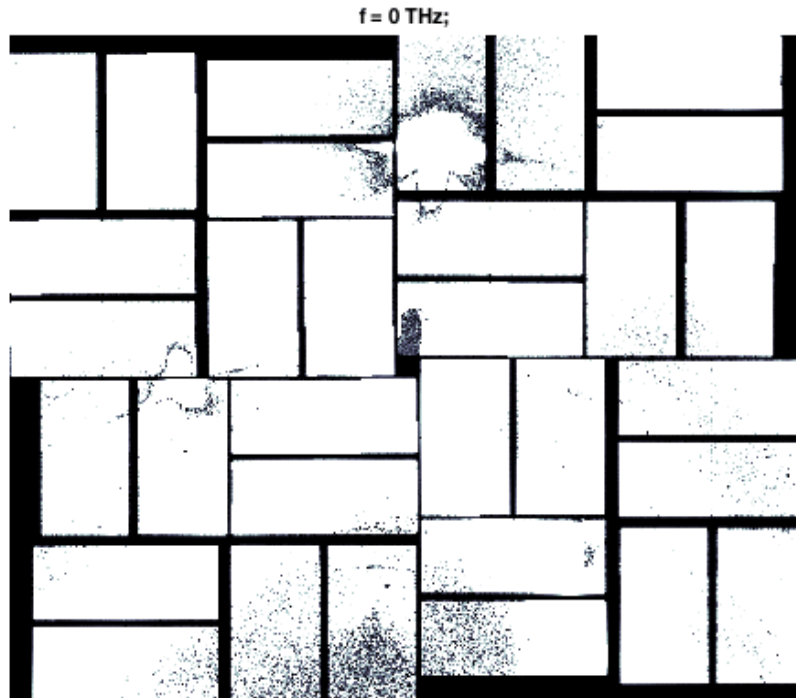


Consistent with reduction of long-range interactions and  
Peierls-like electron-lattice instability

# TR-diffuse scattering from photo-ex. Bi



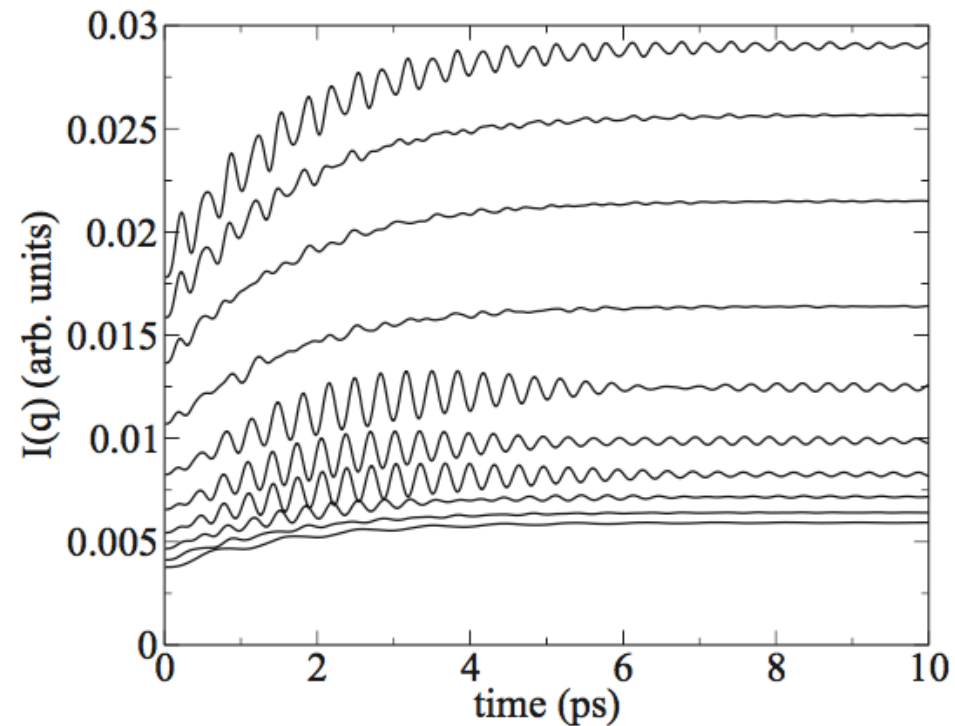
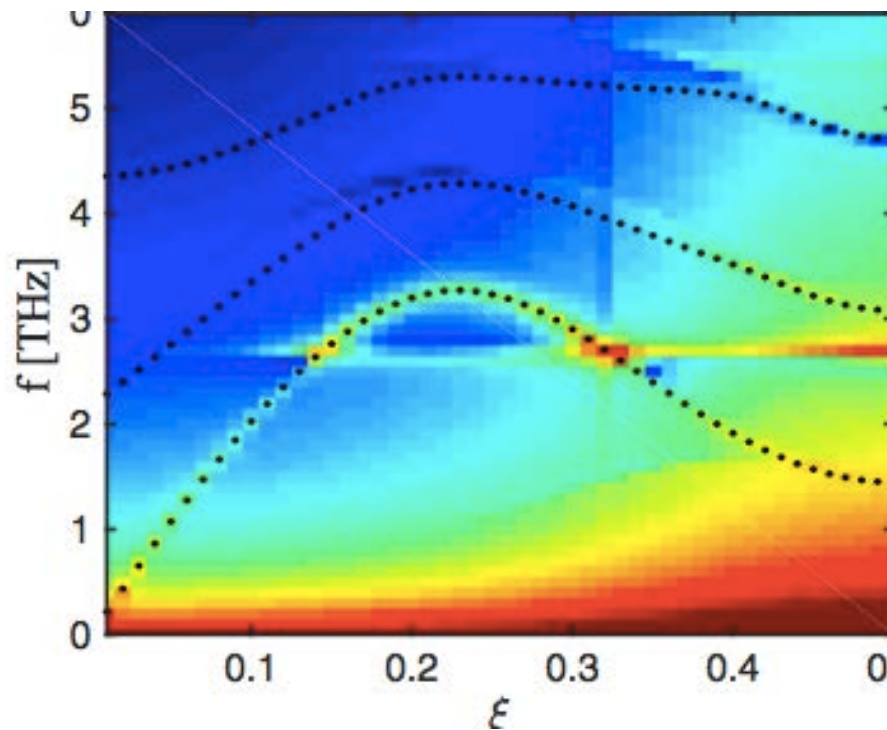
# FT-IXS spectra for Bi



Teitlebaum, Trigo, Henighan et al.  
PRL 121, 125901 (2018).



# Predictions for $A_{1g}$ decay in Bi



# Anharmonic decay of coherent phonon (parametric resonance)

$$H = \underbrace{\frac{1}{2} (P_0^2 + \Omega^2 u_0^2)}_{\text{Single phonon}} + \frac{1}{2N} \sum_q \underbrace{(P_q^2 + \omega_q^2 (1 + \underbrace{2g_q u_0}_{\tilde{\omega}_q^2(u_0)}) u_q^2)}_{\text{Continuum of anharmonic phonons}}$$

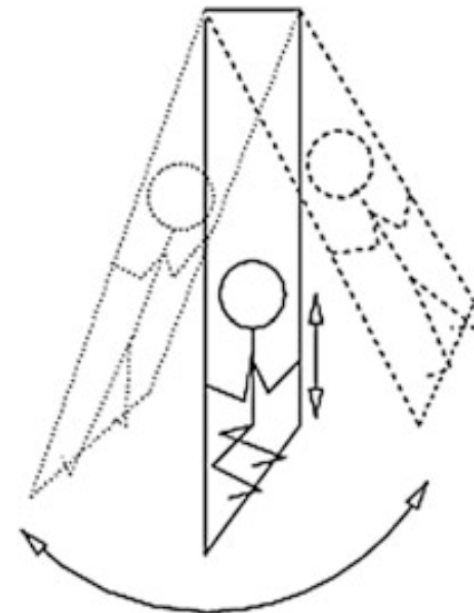
Coherent phonon:

$$\langle u_0 \rangle = A(1 - \cos(\Omega t)e^{-i\gamma_0 t}) \rightarrow \tilde{\omega}_q(u_0) = \tilde{\omega}_q(t)$$

Squeezed phonons:

$$\langle u_q^2 \rangle \sim g_q A \omega_q / \gamma_q \left( e^{-\frac{\gamma_0 t}{2}} - e^{-\gamma_q t} \right) \sin \Omega t$$

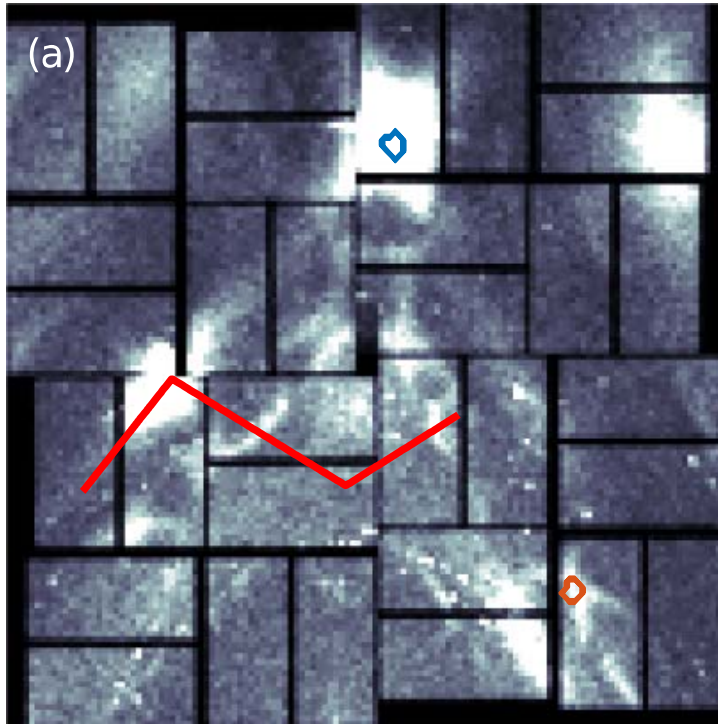
(on resonance)



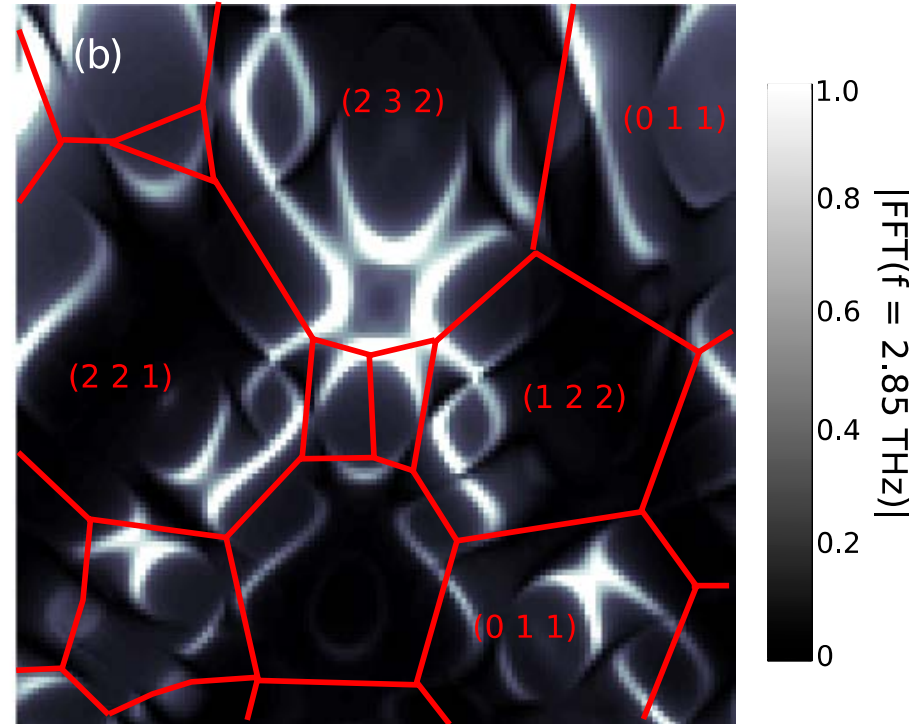
A. Champneys, Encyclopedia of Complexity and Systems Science

# Image of downconverted phonons

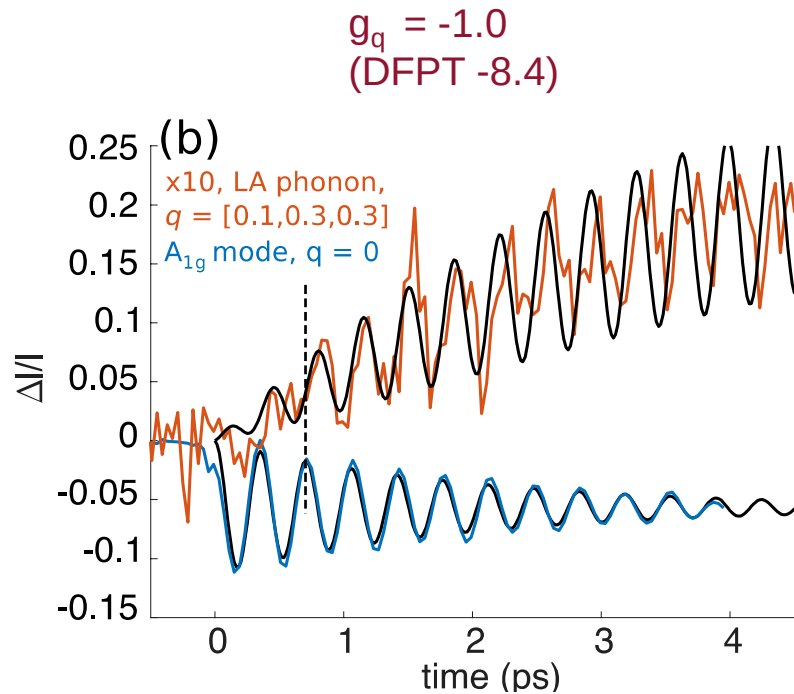
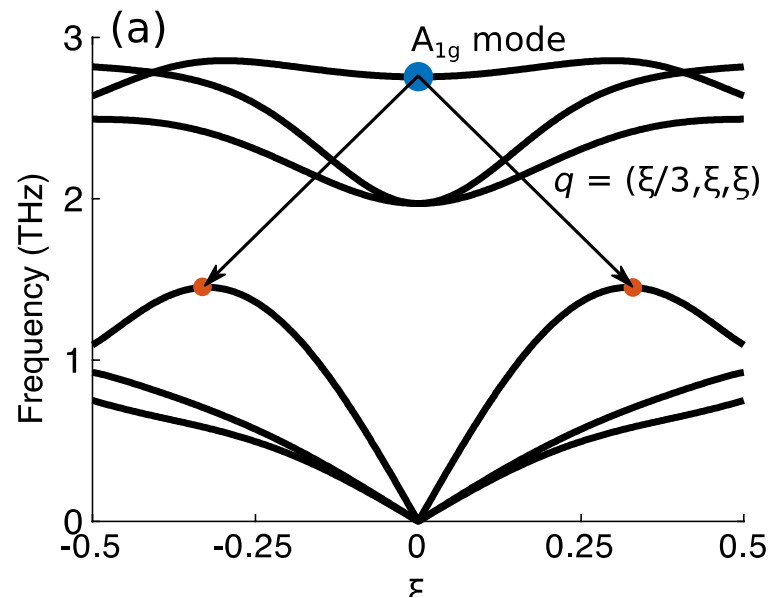
- Measured FT-IXS @  $\omega_{A1g}$



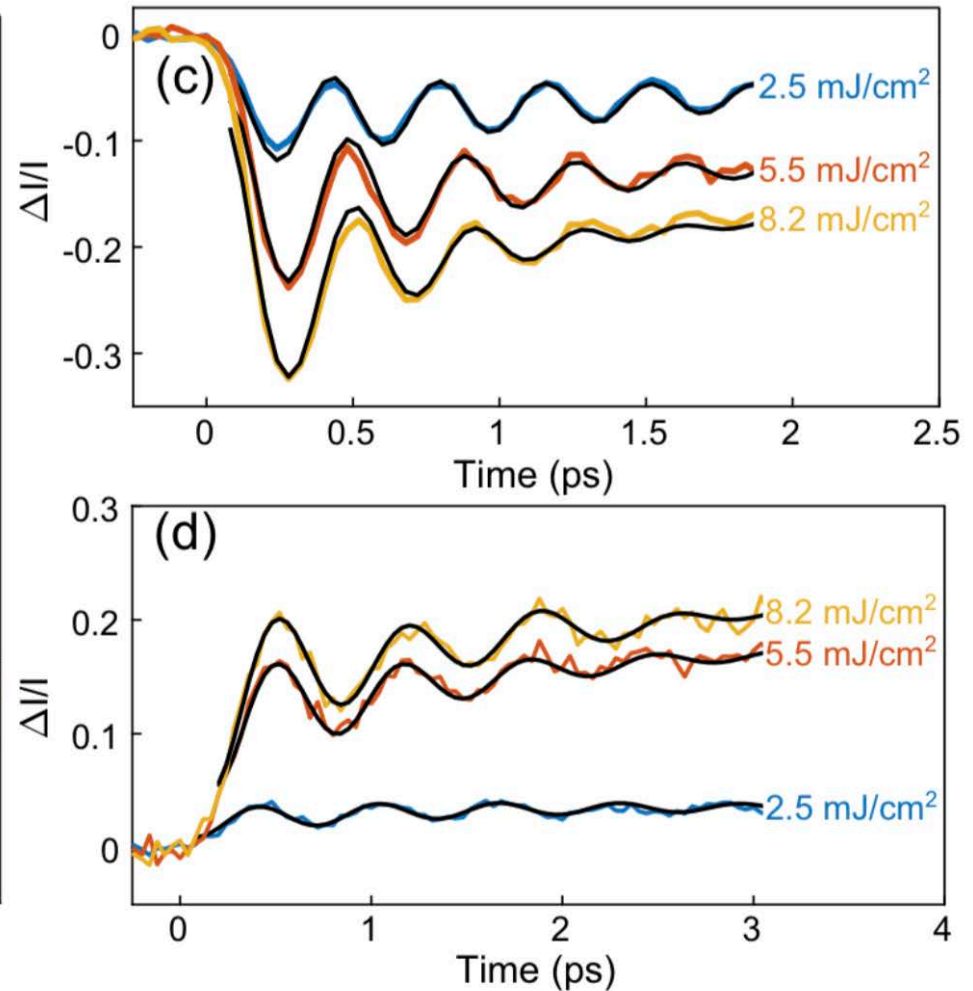
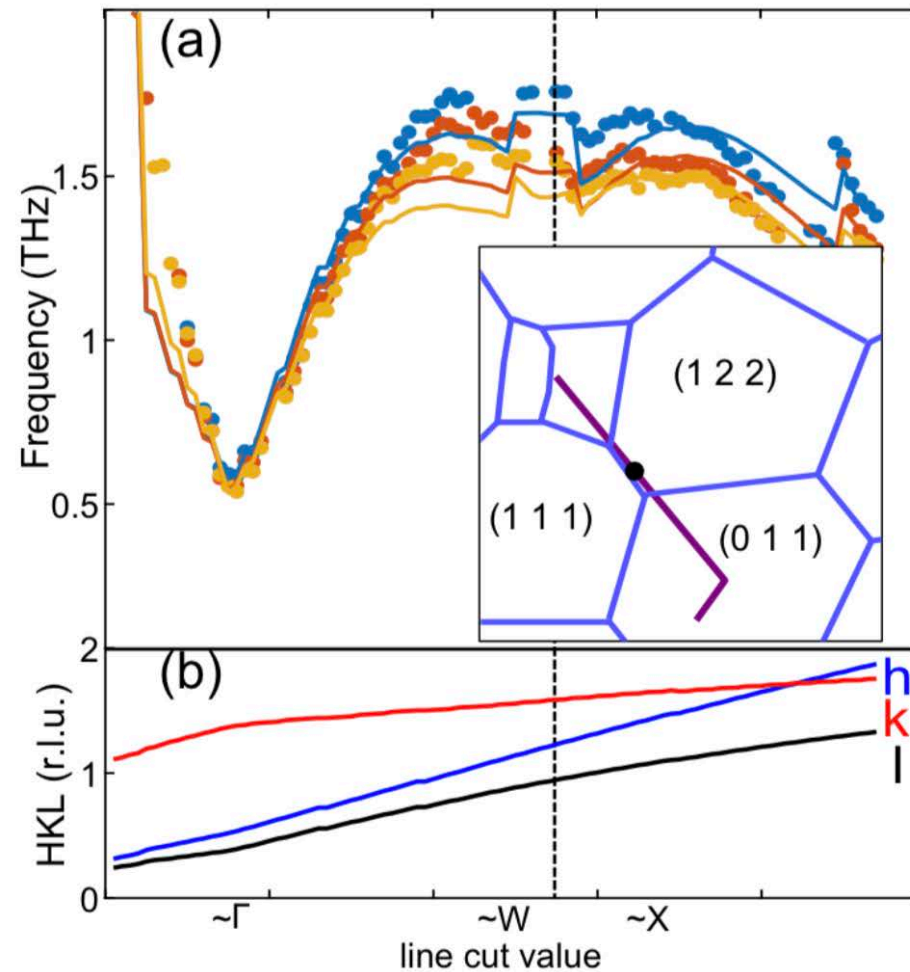
- Prediction with uniform coupling



# Measurement of q-dependent coupling constants



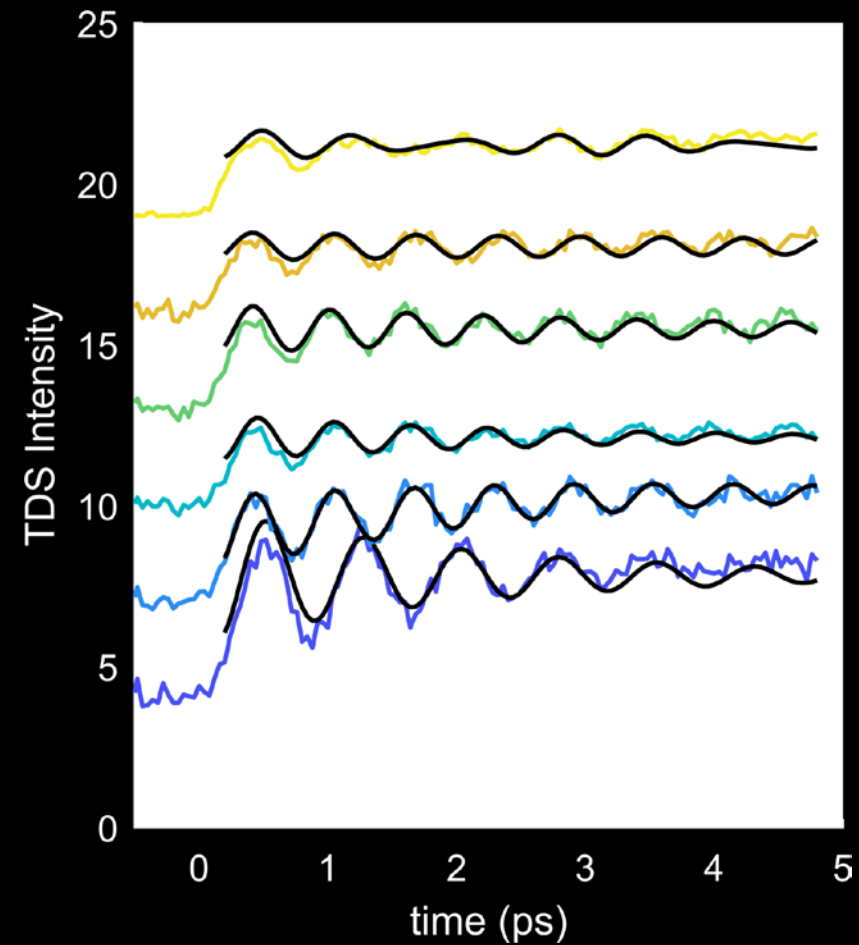
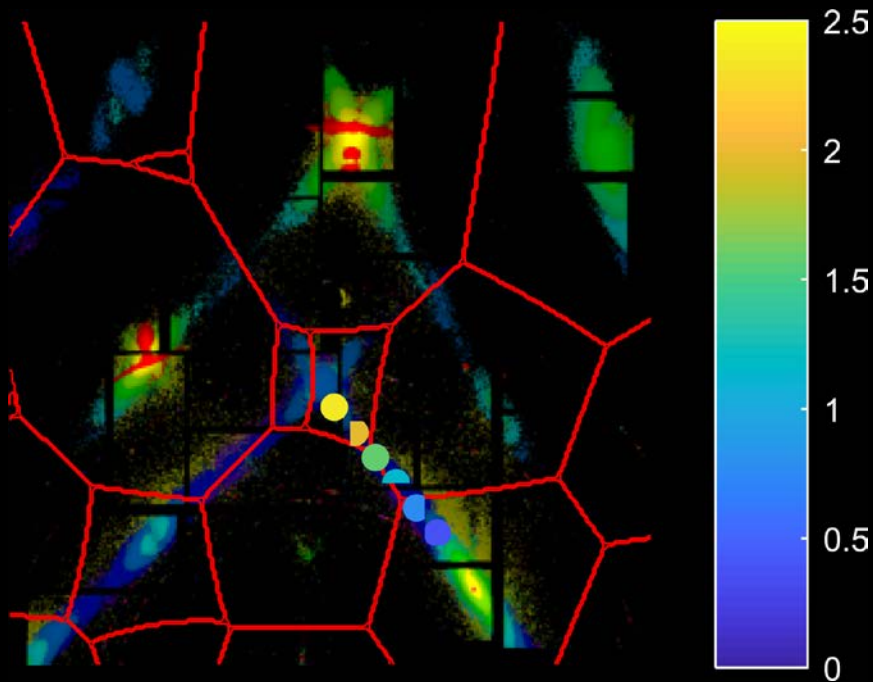
# Fluence dependence of excited-state dispersion bismuth





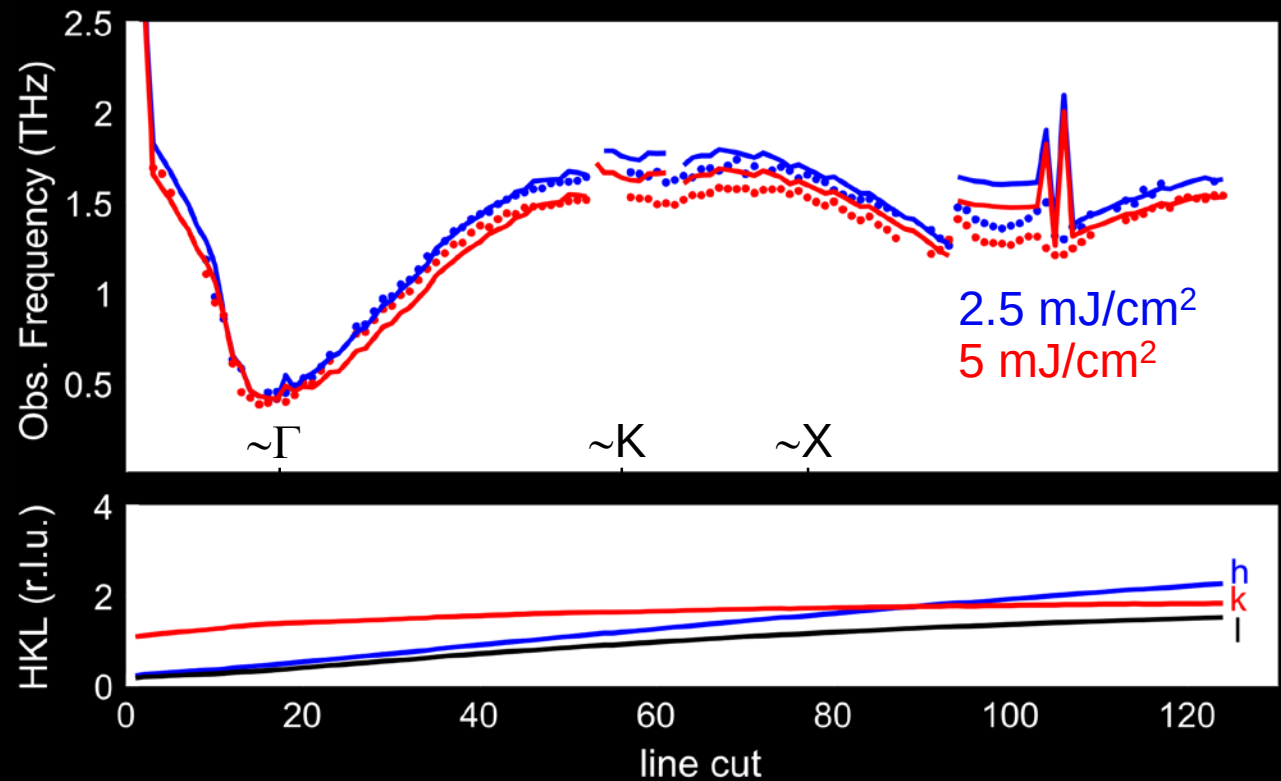
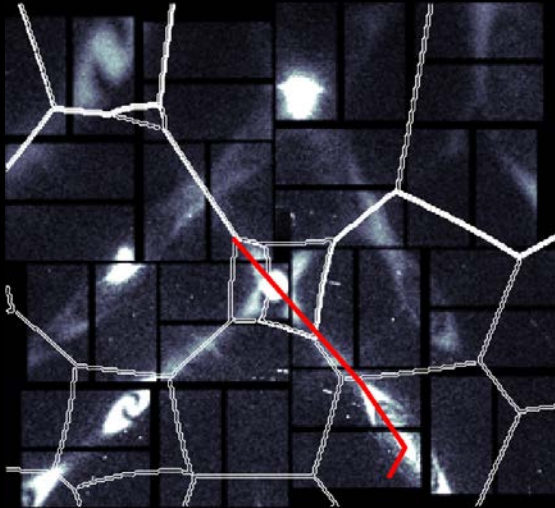
# Extraction of excited-state forces: determine frequencies from FT-IXS

**Dominant frequency**

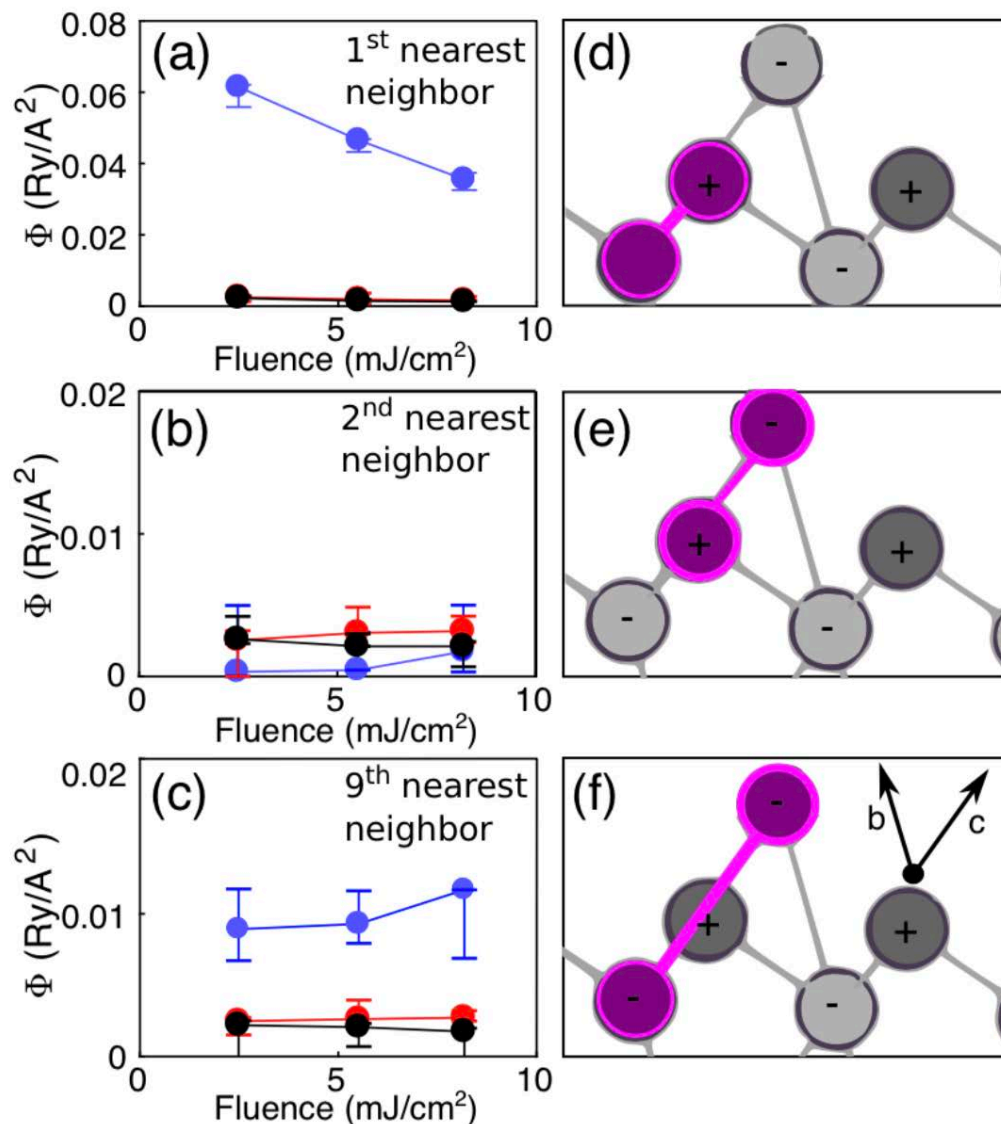


# ...Fit modified dispersion to IF-model

$f = 1.45 \text{ THz}$



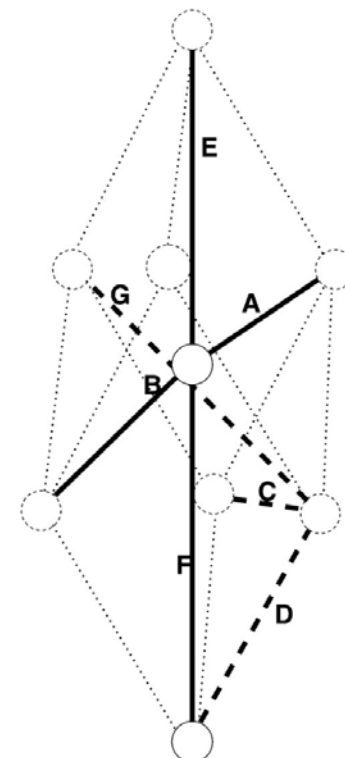
# Excited-state interatomic forces of Bi



A: 1nn

B: 2nn

G: 9nn

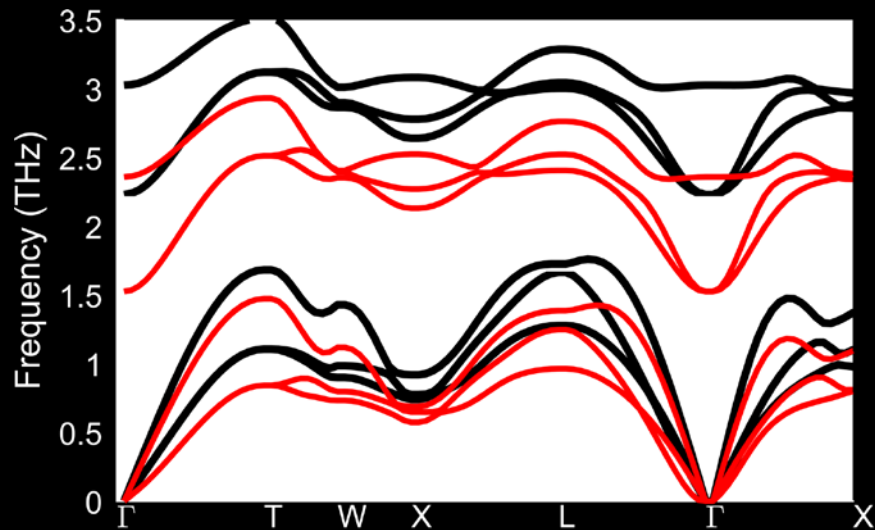


Theory (Ha/bohr)

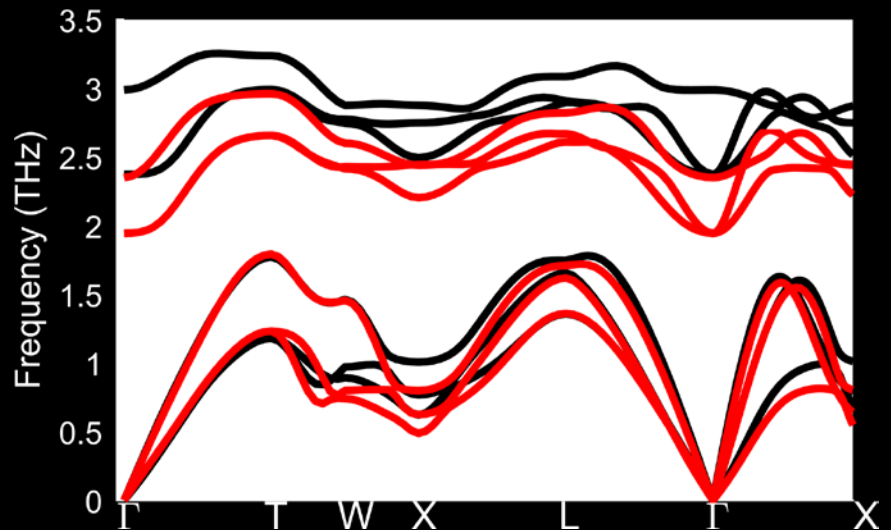
| Pair | NN     | IFC Trace |         | Distance |         |
|------|--------|-----------|---------|----------|---------|
|      |        | $n=0\%$   | $n=1\%$ | $n=0\%$  | $n=1\%$ |
| A    | First  | -33.23    | -27.74  | 5.766    | 5.807   |
| B    | Second | -0.88     | -0.52   | 6.604    | 6.552   |
| C    | Third  | -0.67     | -0.86   | 8.544    | 8.544   |
| D    | Fourth | -0.30     | -0.50   | 8.873    | 8.873   |
| E    | Sixth  | -0.26     | -0.16   | 10.360   | 10.439  |
| F    | Eighth | -0.43     | -0.26   | 11.766   | 11.687  |
| G    | Ninth  | -4.16     | -4.40   | 12.318   | 12.318  |

# Comparison with DFT calculations

Experimental (Reconstruction)



DPFT Calculations\*



\*ED Murray et al, PRB, (2007)

# Acknowledgments

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**Tom Henighan**, **Mason Jiang**, Mike Kozina, Crystal Bray, Jian Chen

LCLS: **D. Zhu**, M. Chollet, T. Sato

**S. Fahy**, S. O'Mahony, **I. Savic (Cork)**, **E. Murray** (Imperial), Olivier Delaire (Duke)  
C. Uher, T.P. Bailey (Michigan)