



# Classical Simulation and Modeling to Advance Quantum Frontiers

## **Gokul Subramanian Ravi**

Postdoctoral Scholar, University of Chicago (- Aug '23)

Assistant Professor, University of Michigan (Sep '23 -)



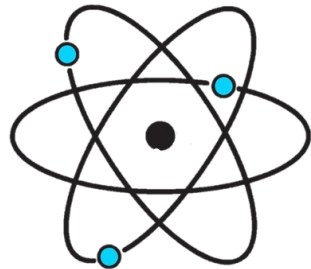
# Classical Simulation and Modeling to Advance Quantum Frontiers

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# What is quantum good for?

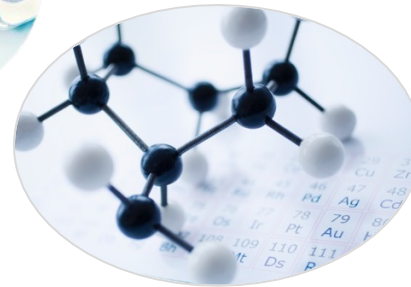


# What is quantum good for?

**Drug discovery**



**Industrial chemistry**



**Security**



**Optimization tasks**



**Finance**

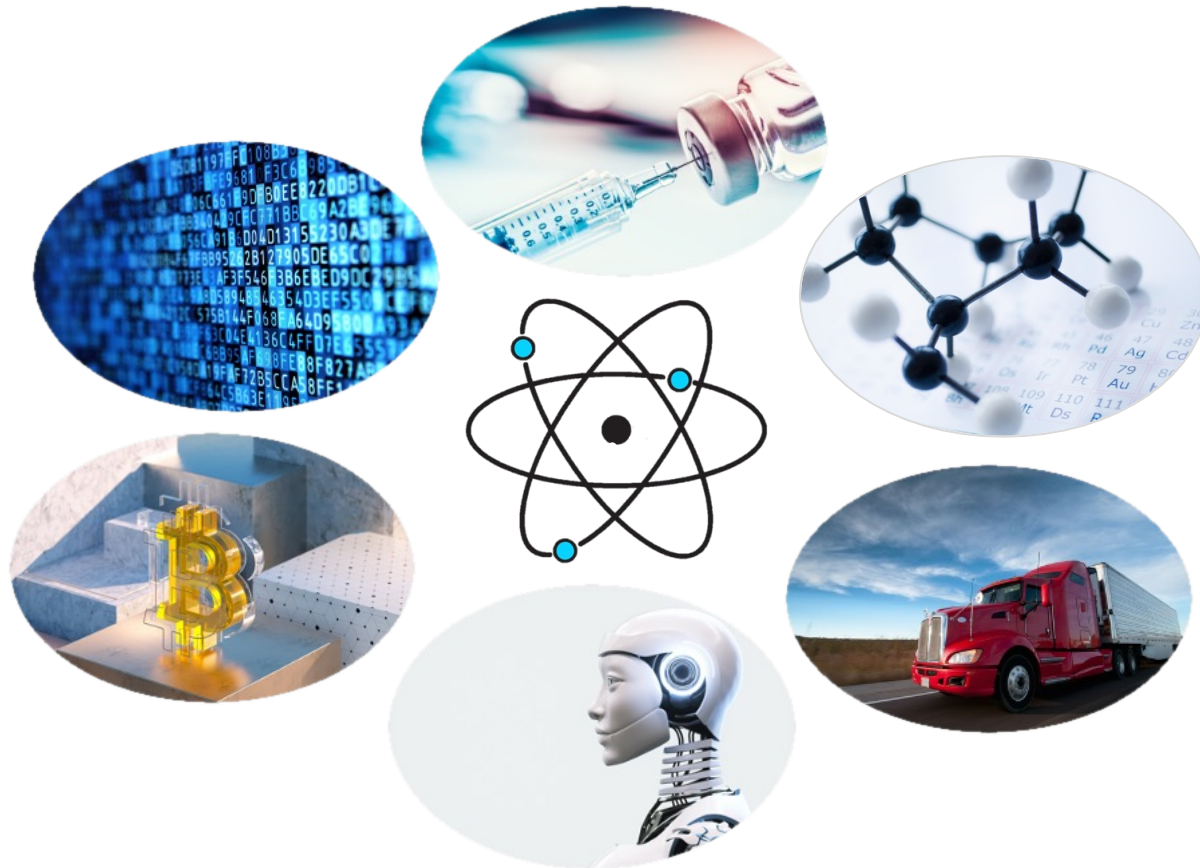


**Artificial Intelligence**

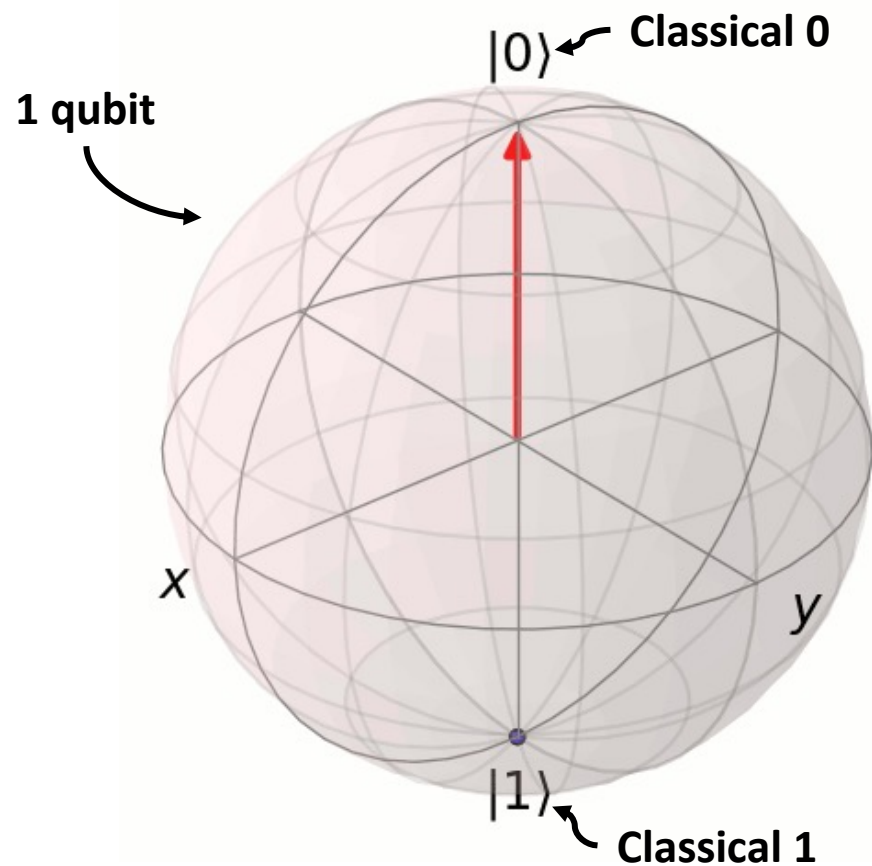




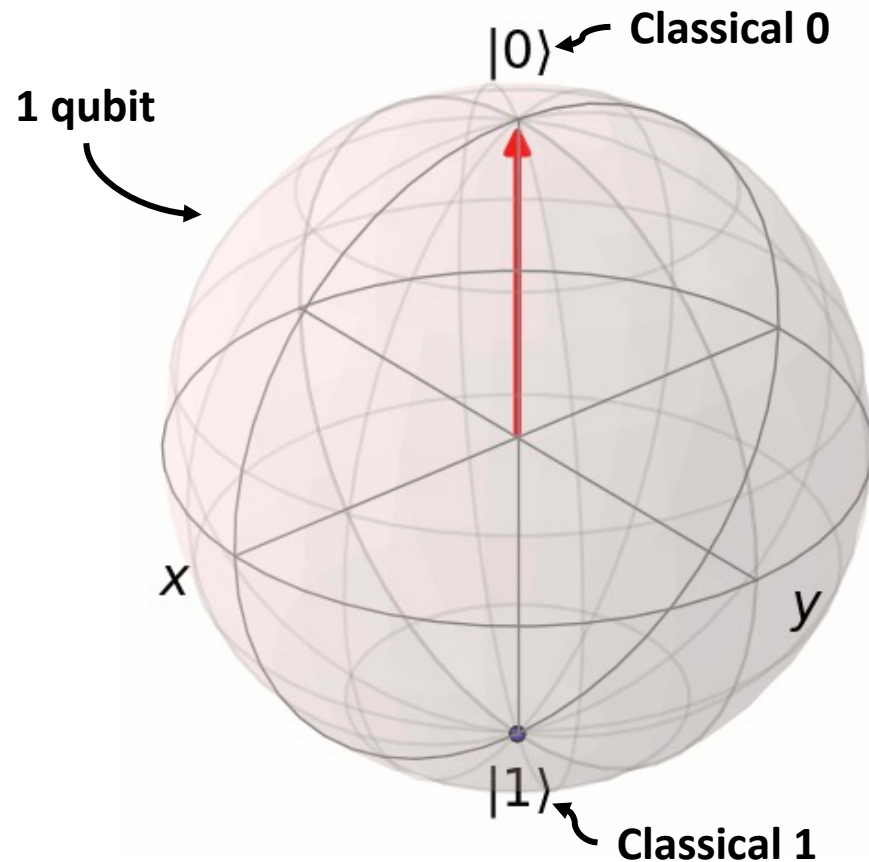
# What is quantum good for?



# How does quantum work?



# How does quantum work?



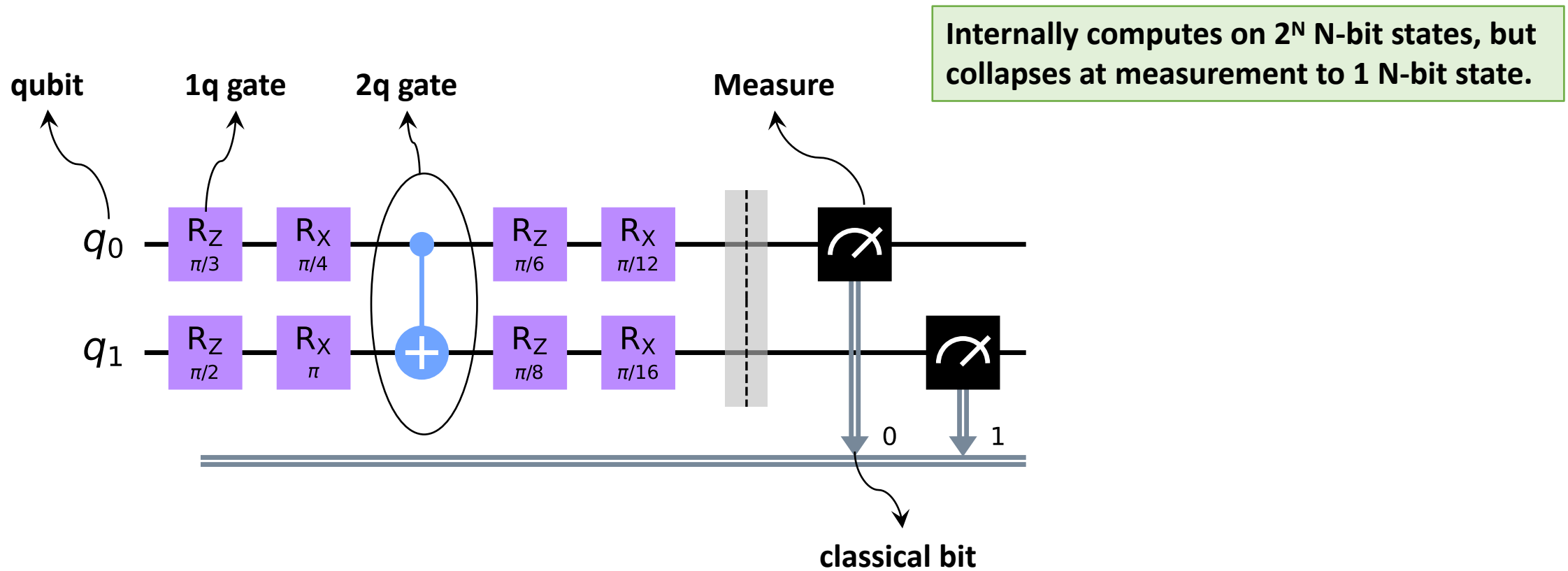
1 qubit → simultaneous  $2^1$  classical 1-bit states \*

N qubits → simultaneous  $2^N$  classical N-bit states \*

**Quantum Advantage**

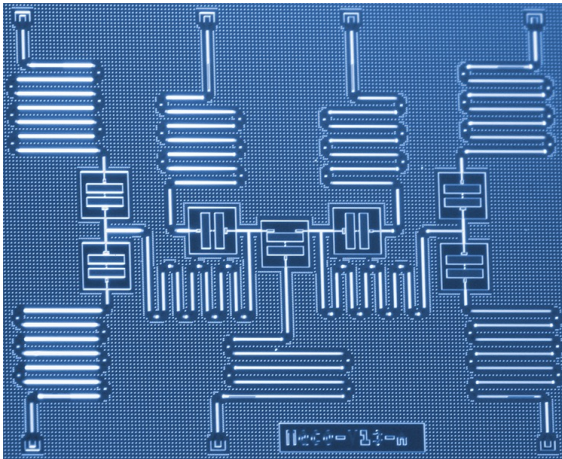
\* with some constraints

# How does quantum work?

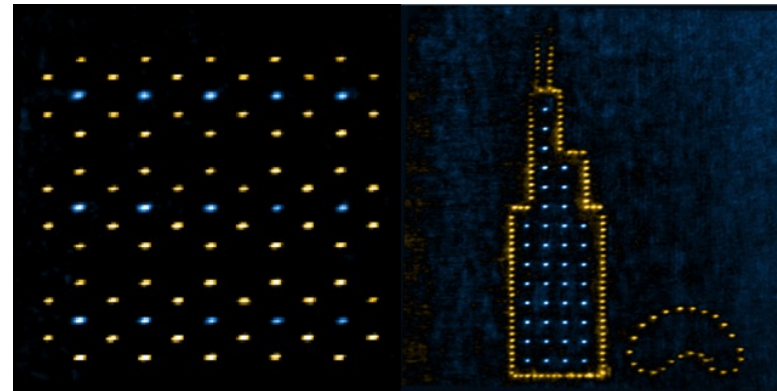


# NISQ era: Many promising but imperfect quantum technologies

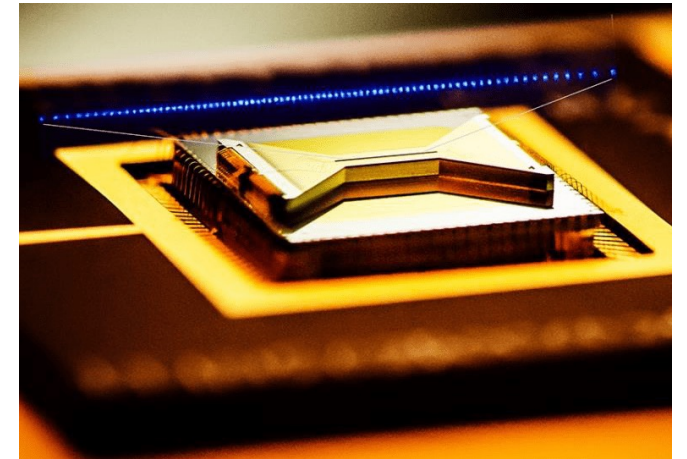
**NISQ: Noisy Intermediate Scale Quantum → Few qubits, poor quality**



**Superconducting**



**Neutral atom**

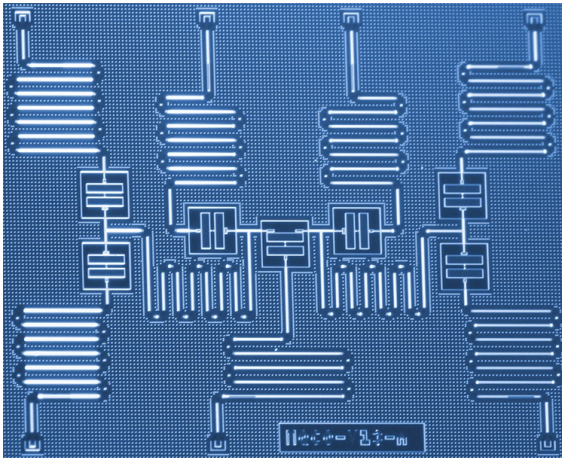


**Trapped Ion**

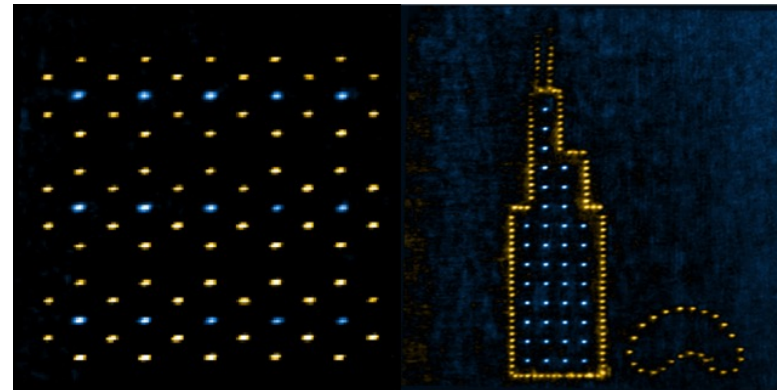


# NISQ era: Many promising but imperfect quantum technologies

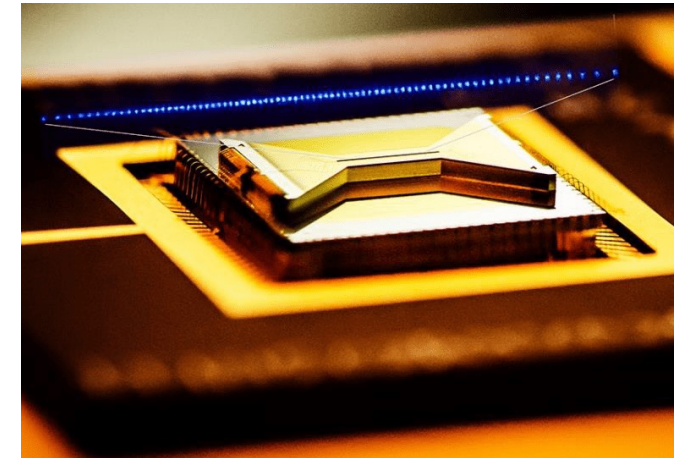
NISQ: Noisy Intermediate Scale Quantum → Few qubits, poor quality



**Superconducting**  
**Qubit Lifetime**  
**Gate Fidelity**

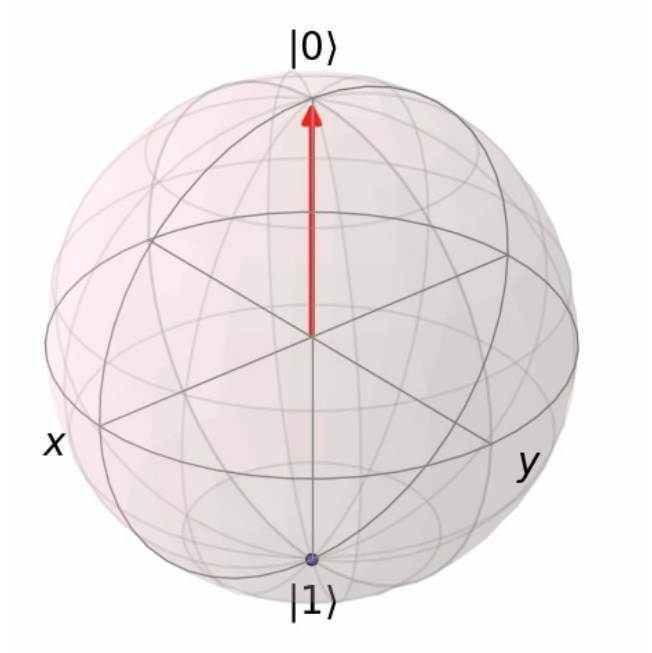
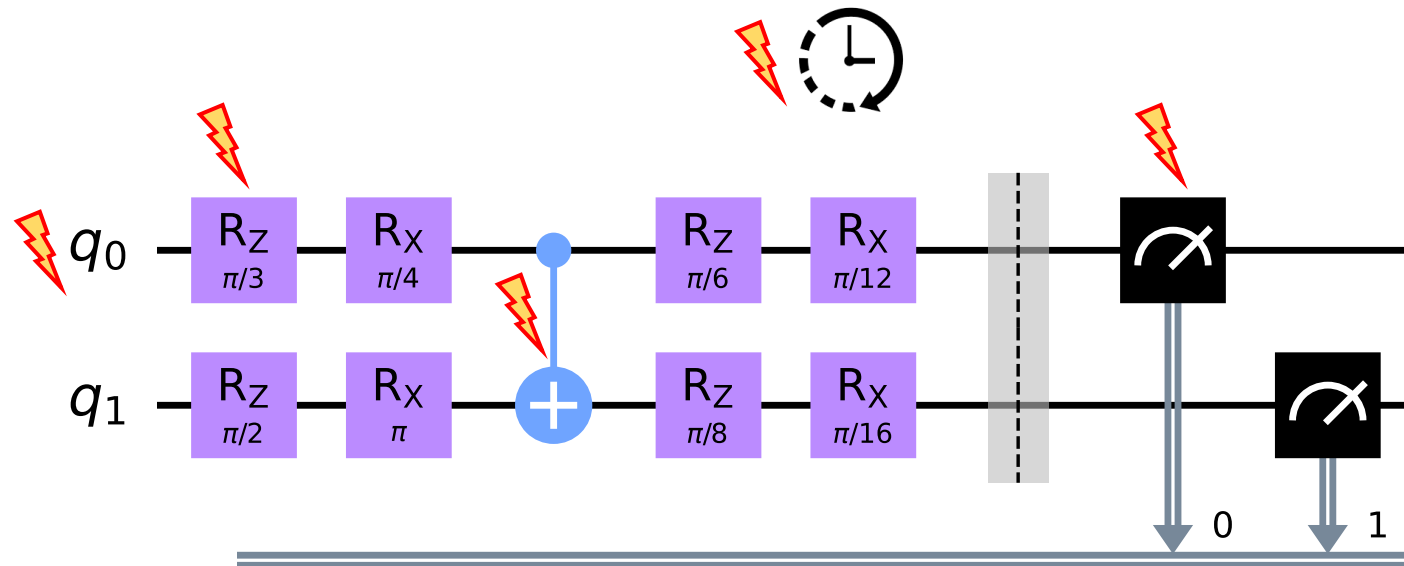


**Neutral atom**  
**Gate Fidelity**  
**Measurement**



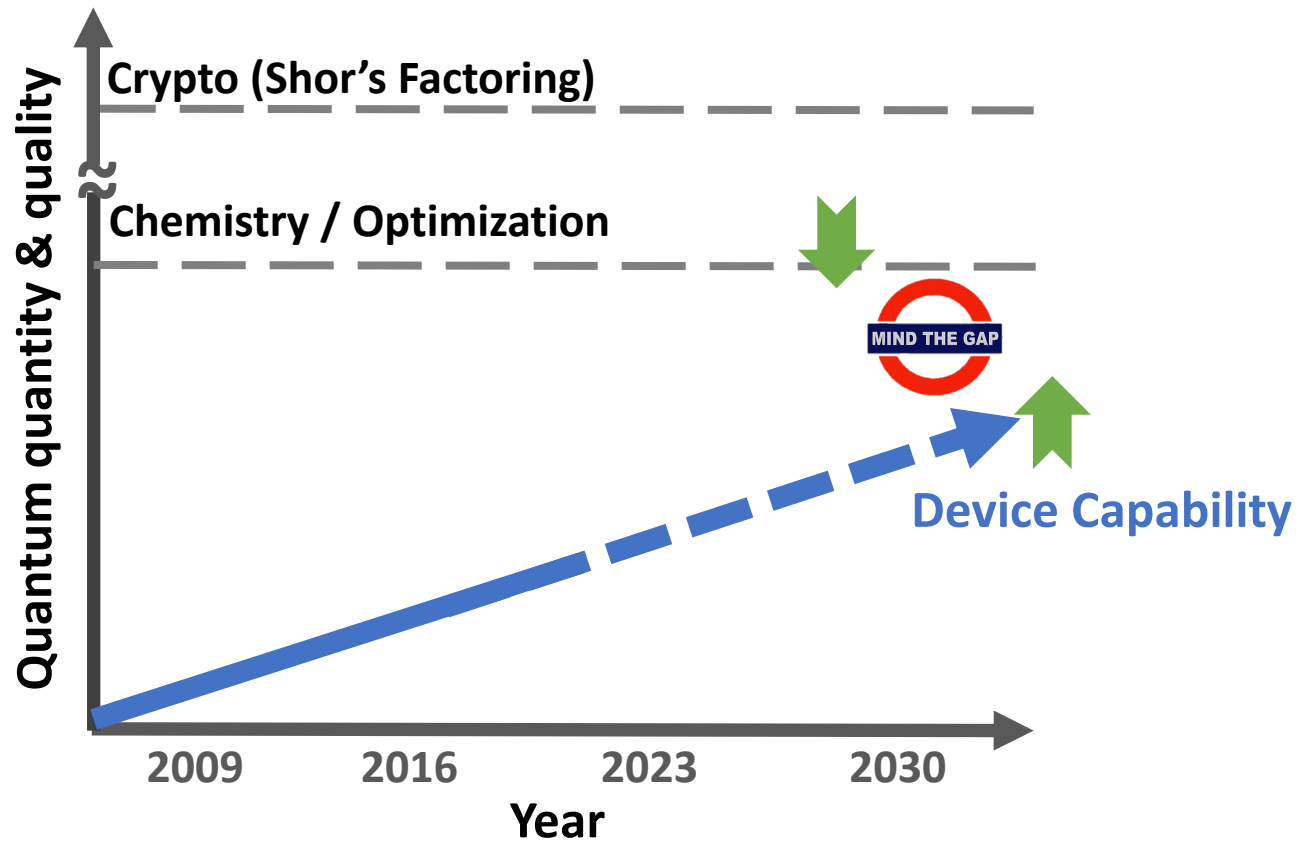
**Trapped Ion**  
**Scalability**  
**Gate Speed**

# Noisy quantum circuits



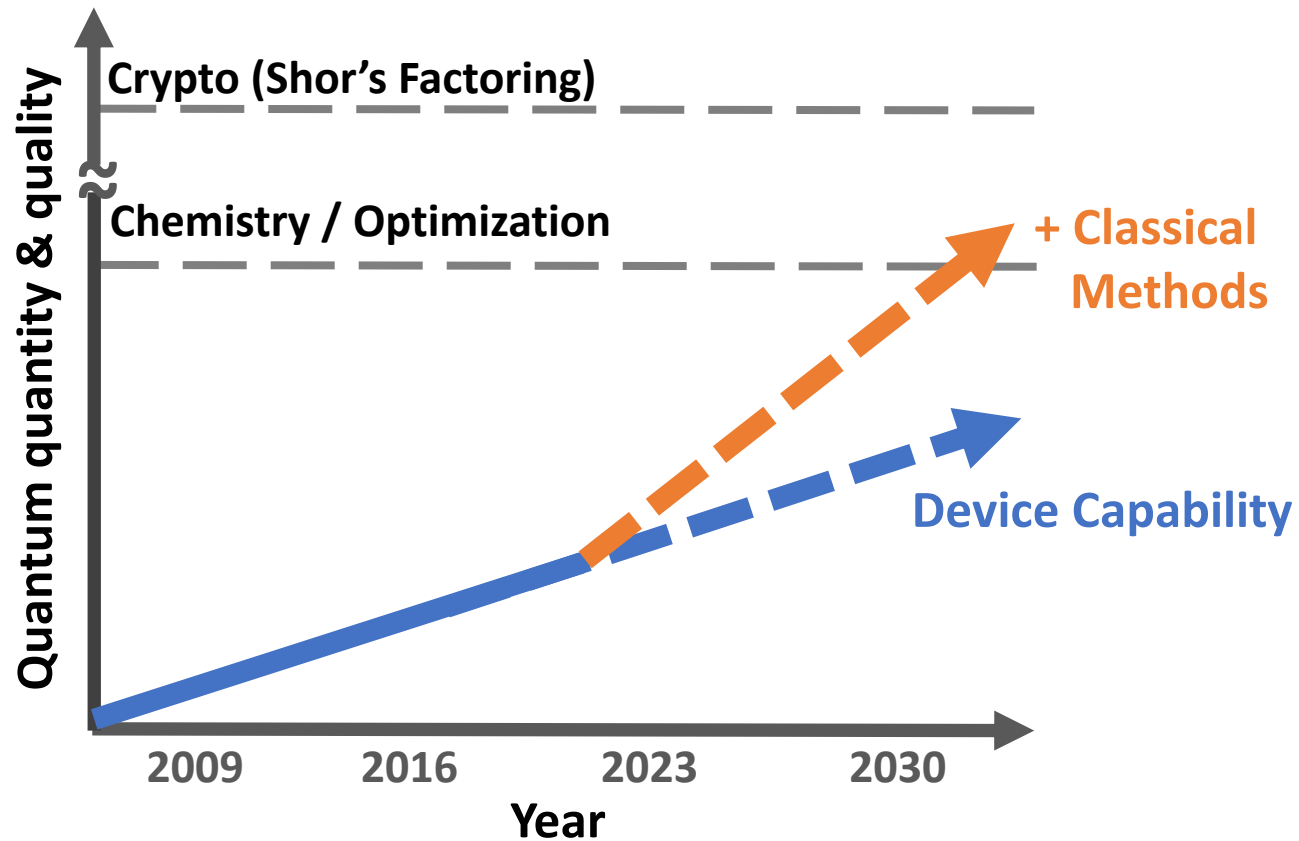
State prep error  
qubit decoherence,  
1Q/2Q gate errors,  
crosstalk errors,  
measurement errors

# Bridging the quantum gap: Reduced application requirements + better technology?

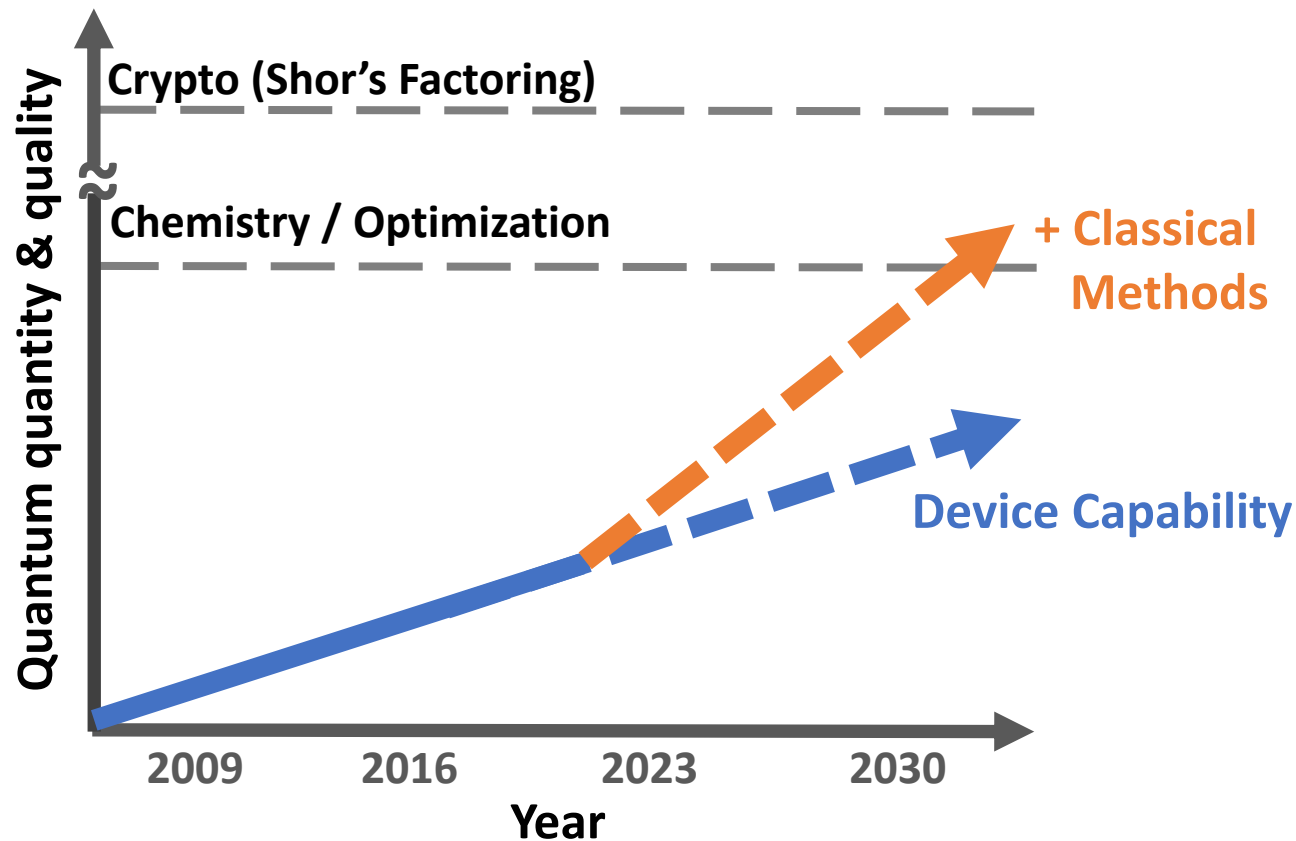




# Bridging the quantum gap: Classical computing approaches



# Bridging the quantum gap: Classical computing approaches

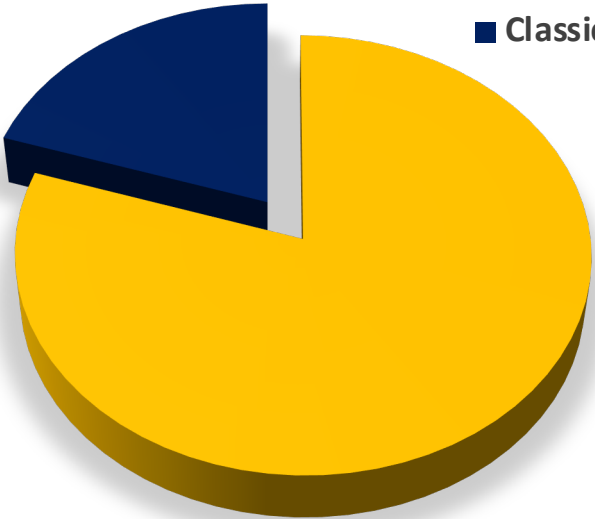


1. PL and Compilation
2. Computer Architecture
3. Classical simulation
4. High performance computing
5. Cryogenic hardware design
6. Noise modeling and Optimization
7. Multi-chip / distributed computing
8. Cloud resource modeling and management

# #1) Classical simulation to alleviate quantum challenges

Application fraction

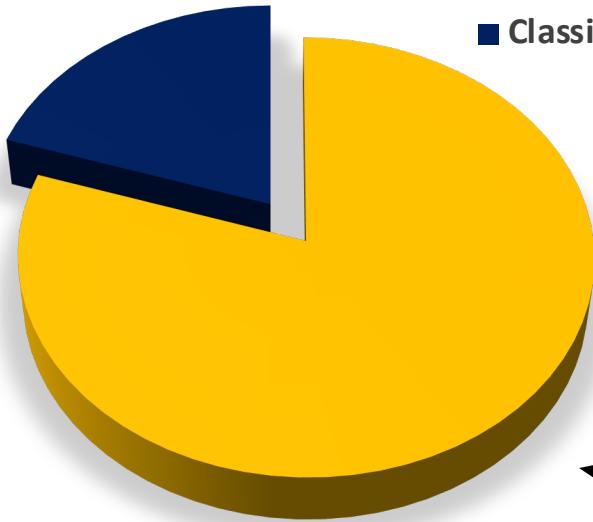
- Classically tractable
- Classically intractable



# #1) Classical simulation to alleviate quantum challenges

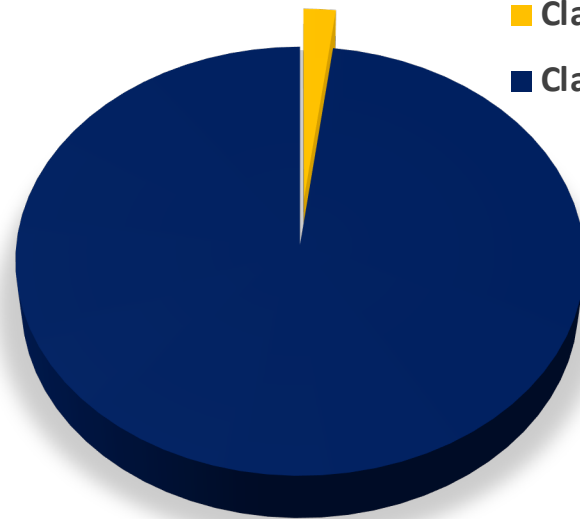
Application fraction

- Classically tractable
- Classically intractable



Classical runtime

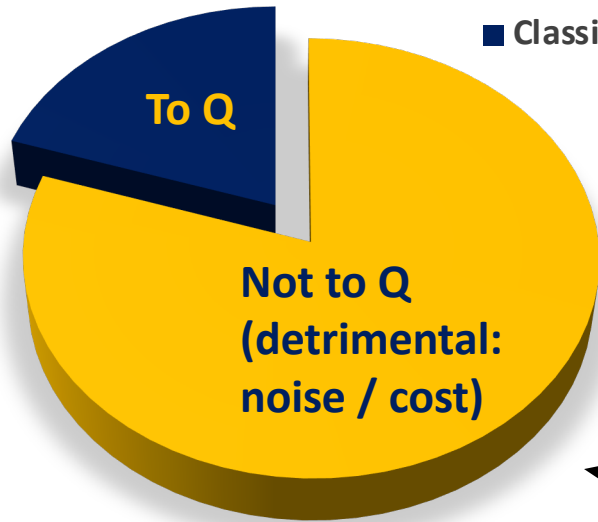
- Classically tractable
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# #1) Classical simulation to alleviate quantum challenges

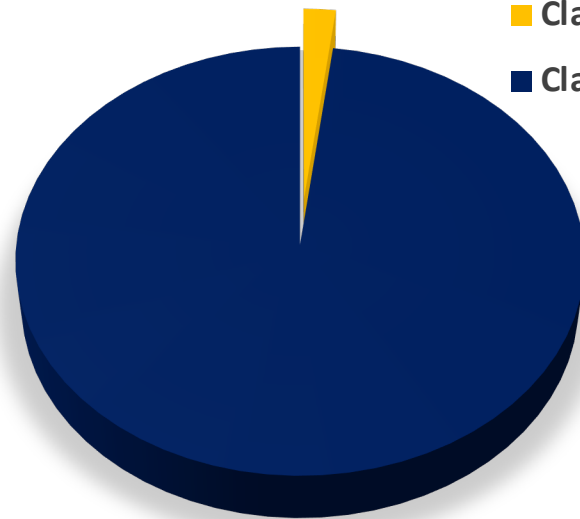
Application fraction

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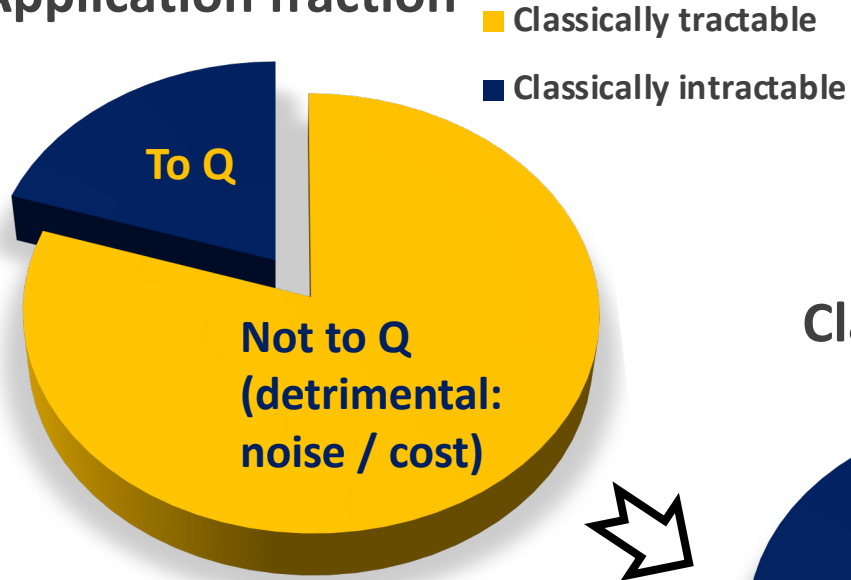
Classical runtime

- Classically tractable
- Classically intractable



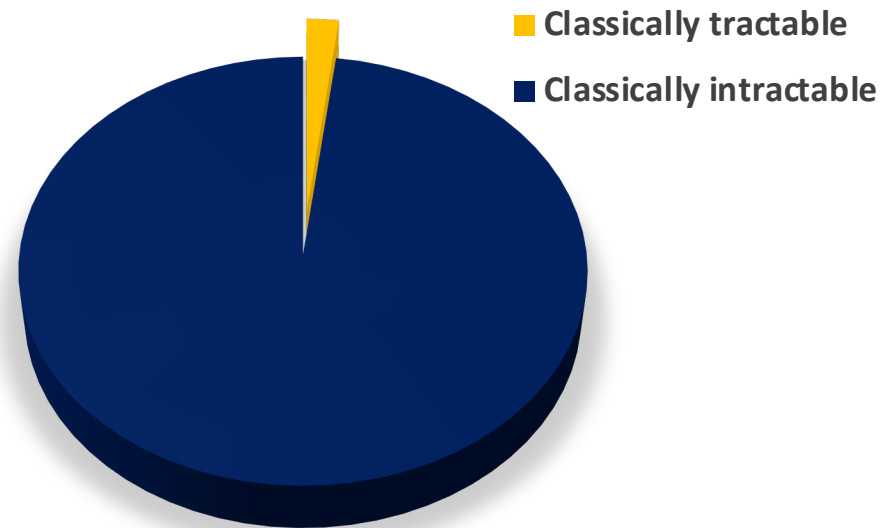
# #1) Classical simulation to alleviate quantum challenges

Application fraction



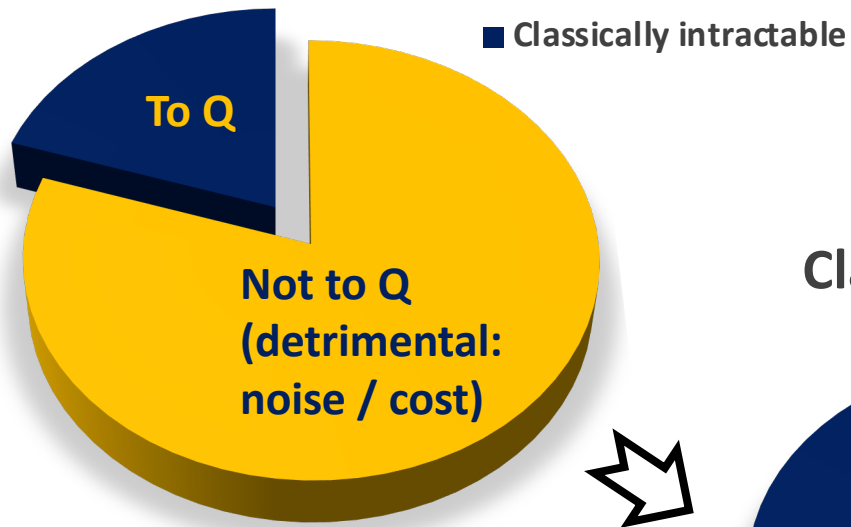
- *No clear separation between classical and quantum components.*
- *The classical tractability depends on the simulation platform.*

Classical runtime



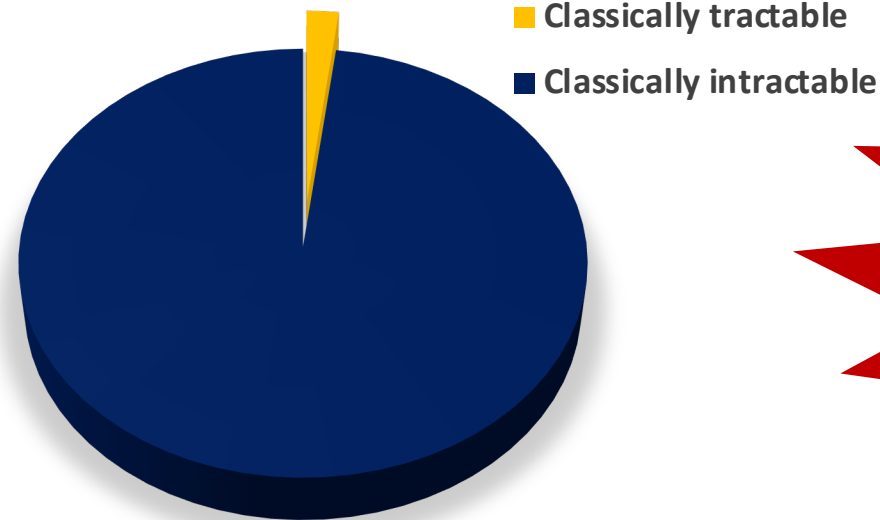
# CAFQA: A Classical Simulation Bootstrap for Variational Quantum Algorithms

Application fraction



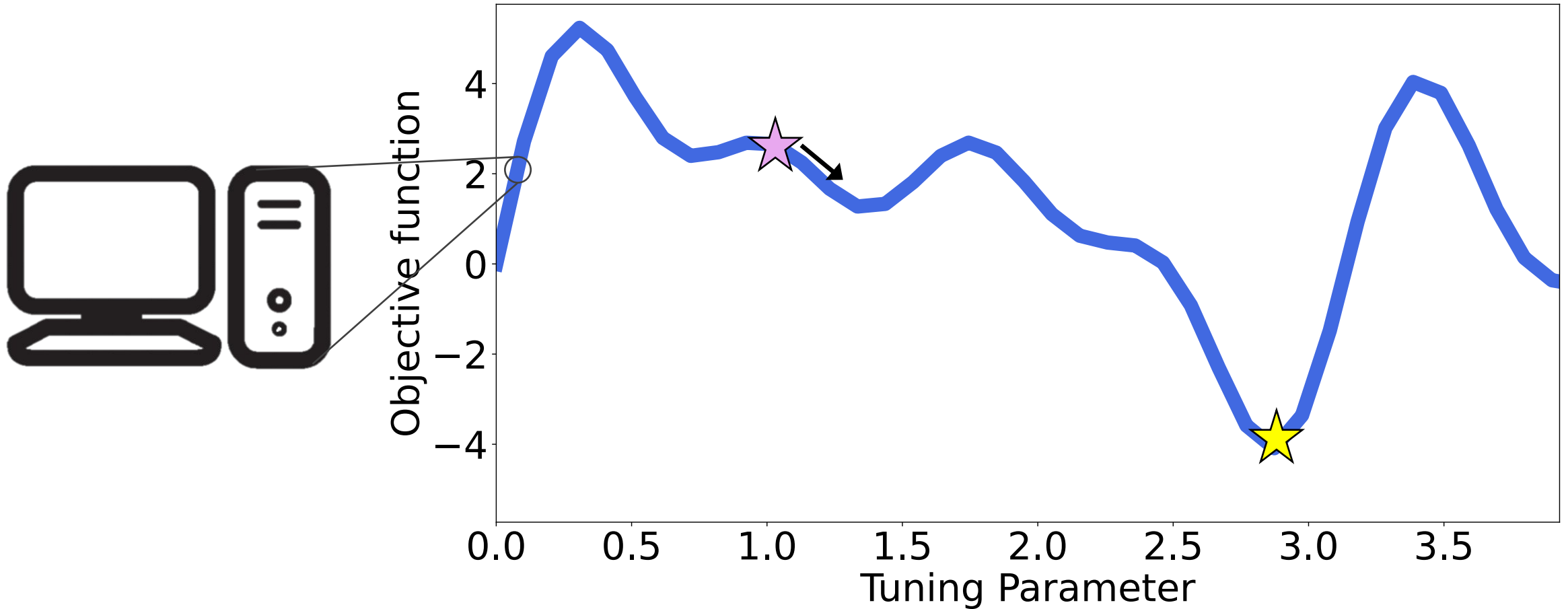
[Gokul Ravi](#), Pranav Gokhale, Yi Ding, William Kirby, Kaitlin Smith, Jonathan Baker, Peter Love, Hank Hoffmann, Kenneth Brown, Frederic Chong. **ASPLOS 2023 + QIP 2022**

Classical runtime



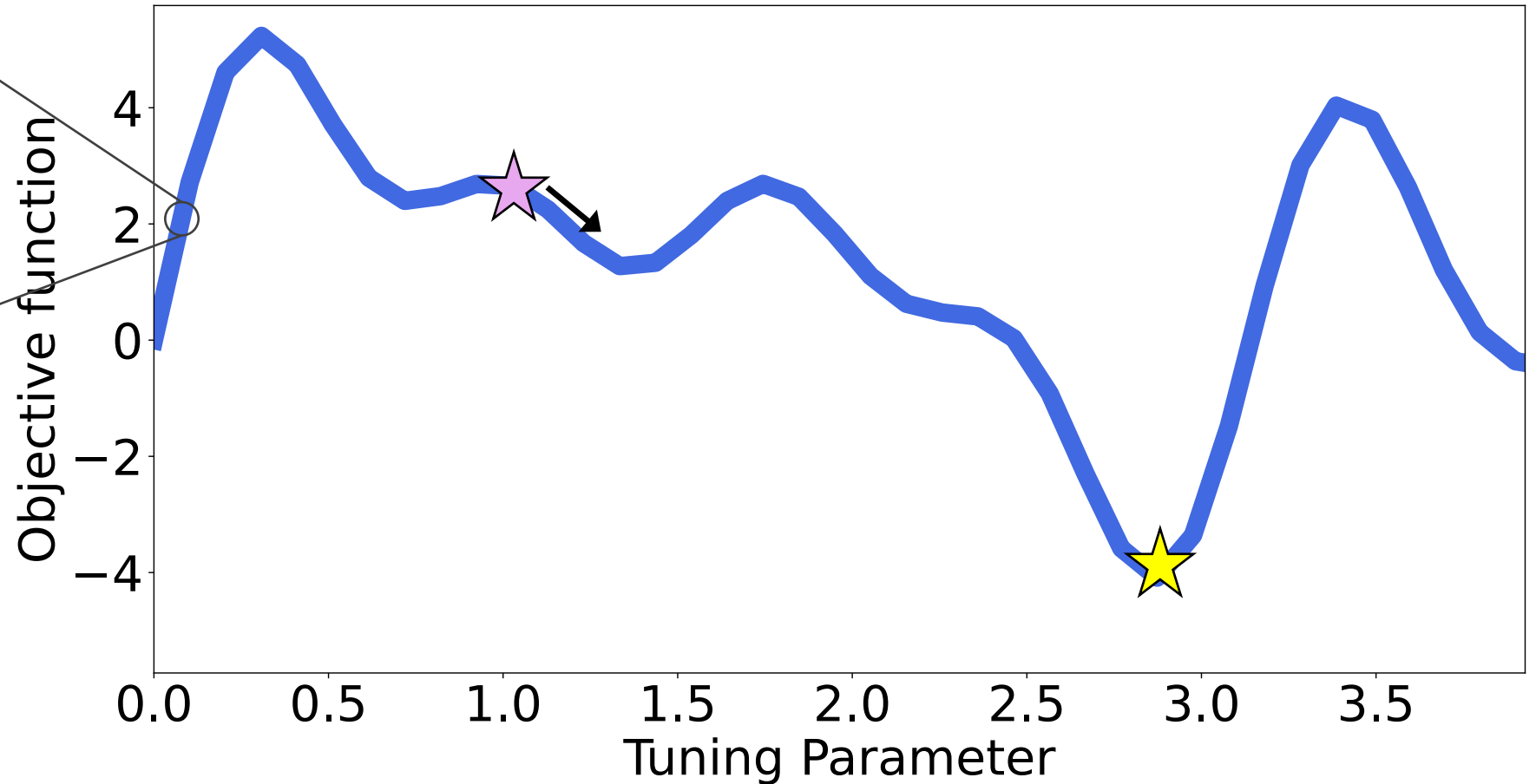
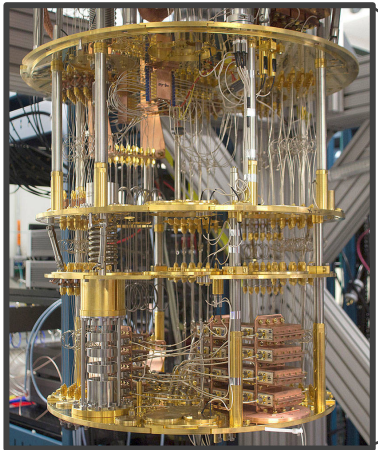
*Observed to recover 99+%  
of initialization accuracy  
lost in SOTA method!*

# Navigating a classical optimization contour

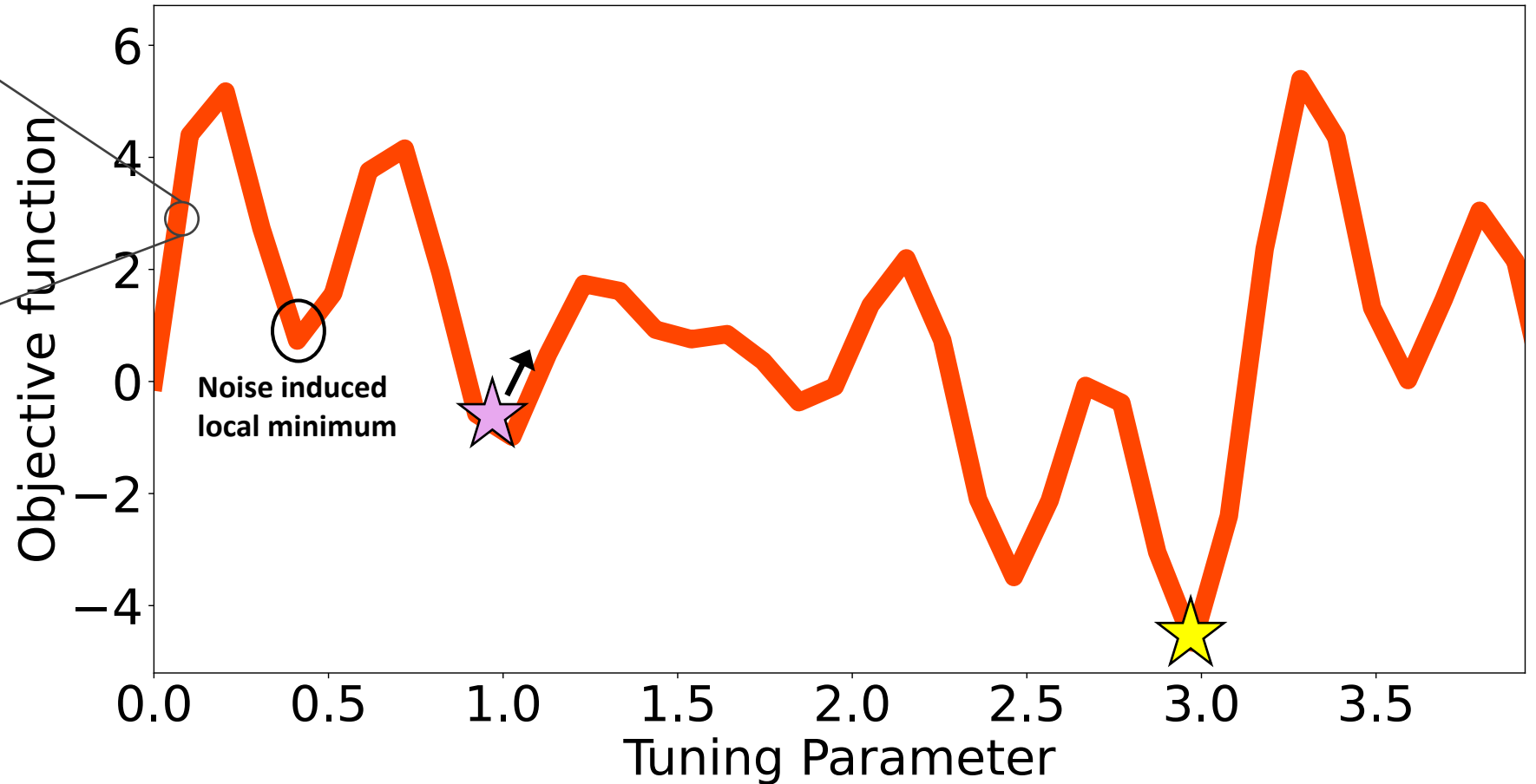
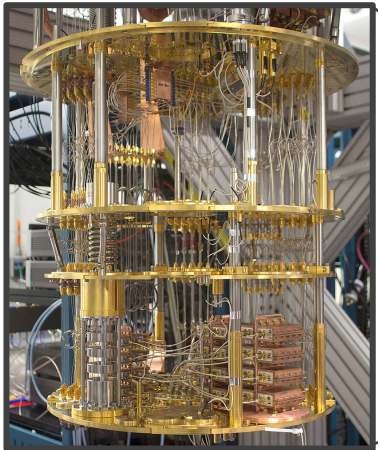




# Navigating an ideal Variational Quantum Algorithm contour

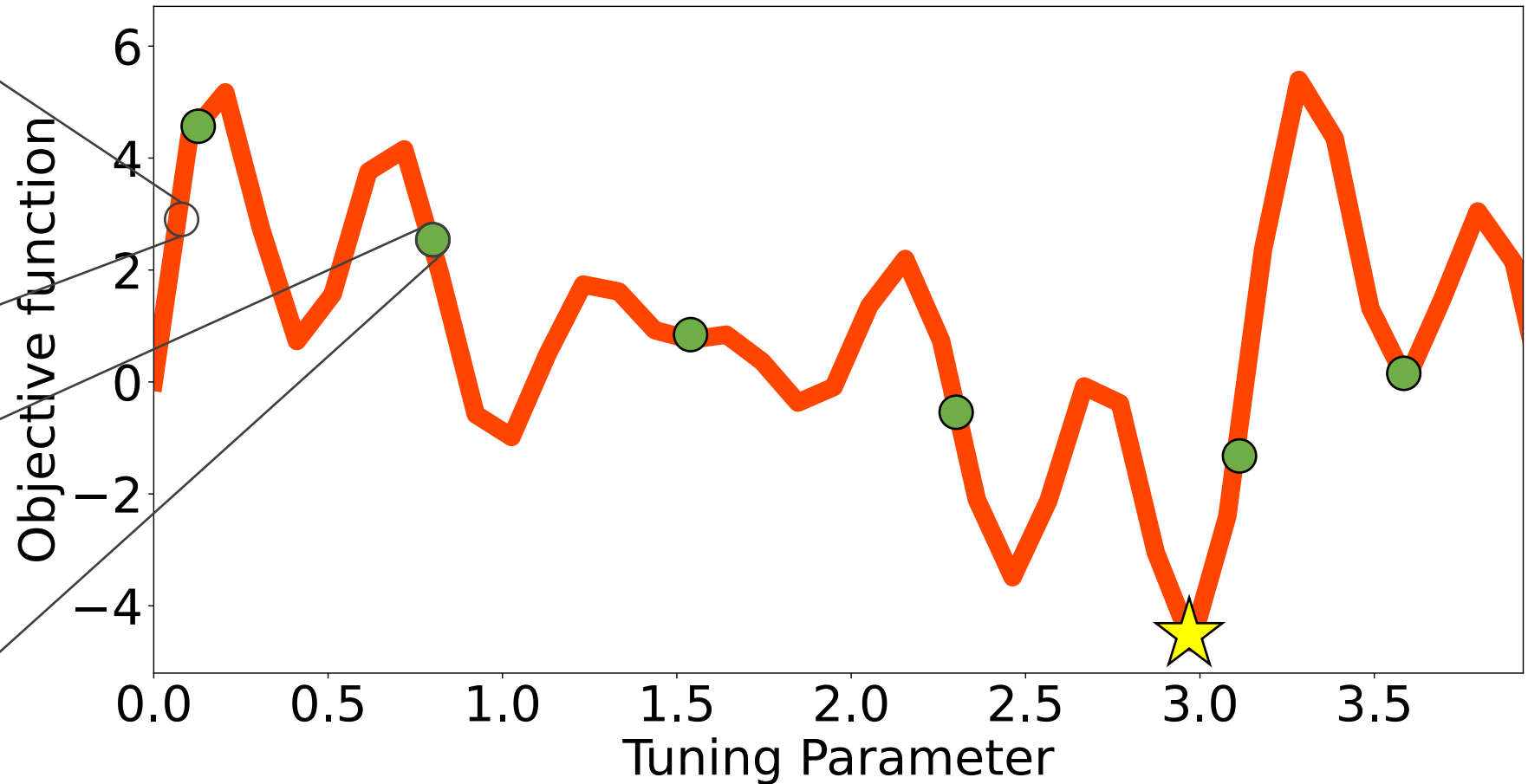
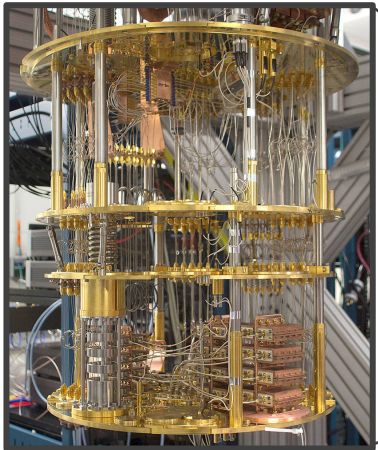


# Navigating a noisy Variational Quantum Algorithm contour



# CAFQA: Clifford Ansatz For Quantum Accuracy

CAFQA Insight #1: Portion of the quantum space is classically simulable (Clifford space).

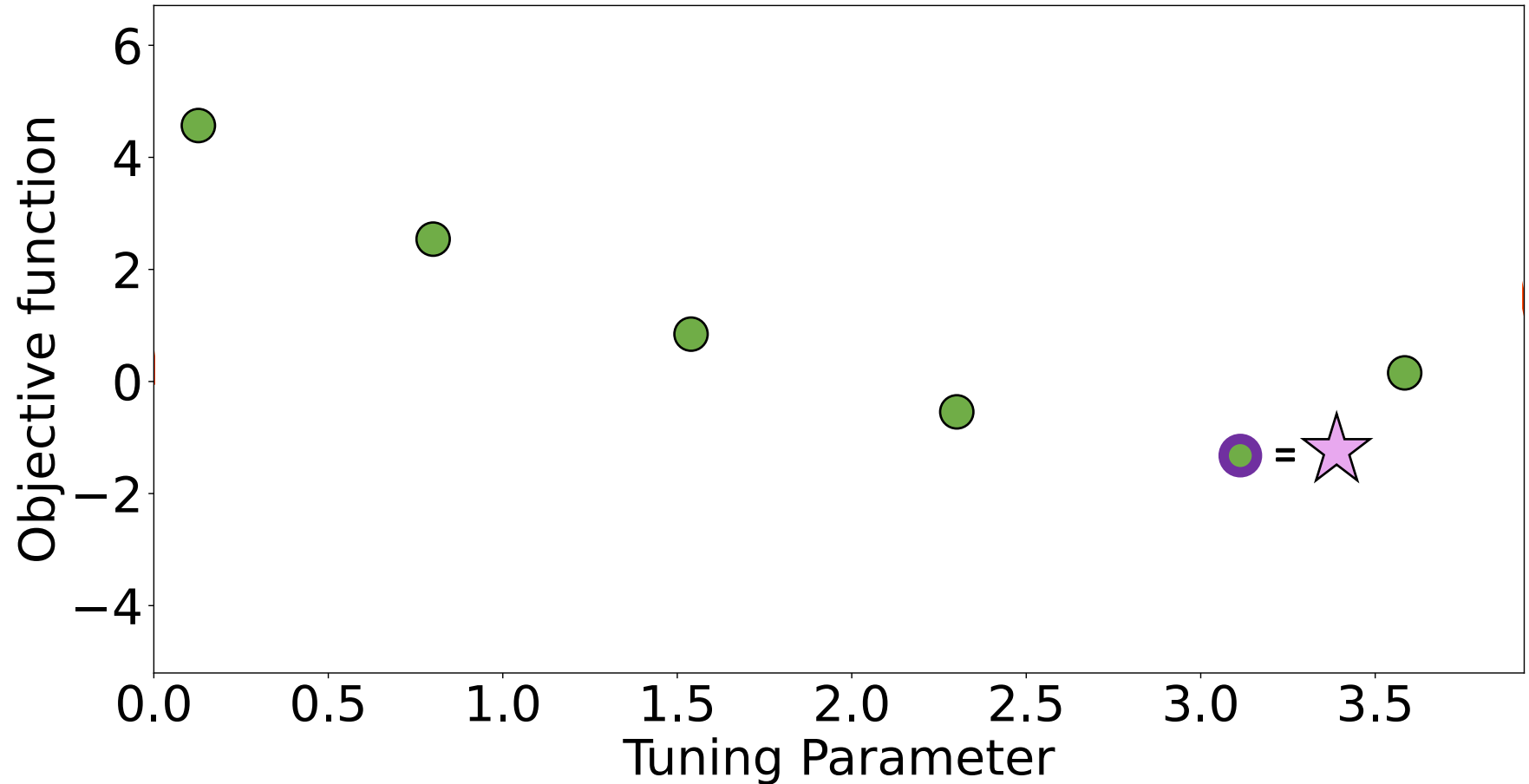


# CAFQA: Clifford Ansatz For Quantum Accuracy

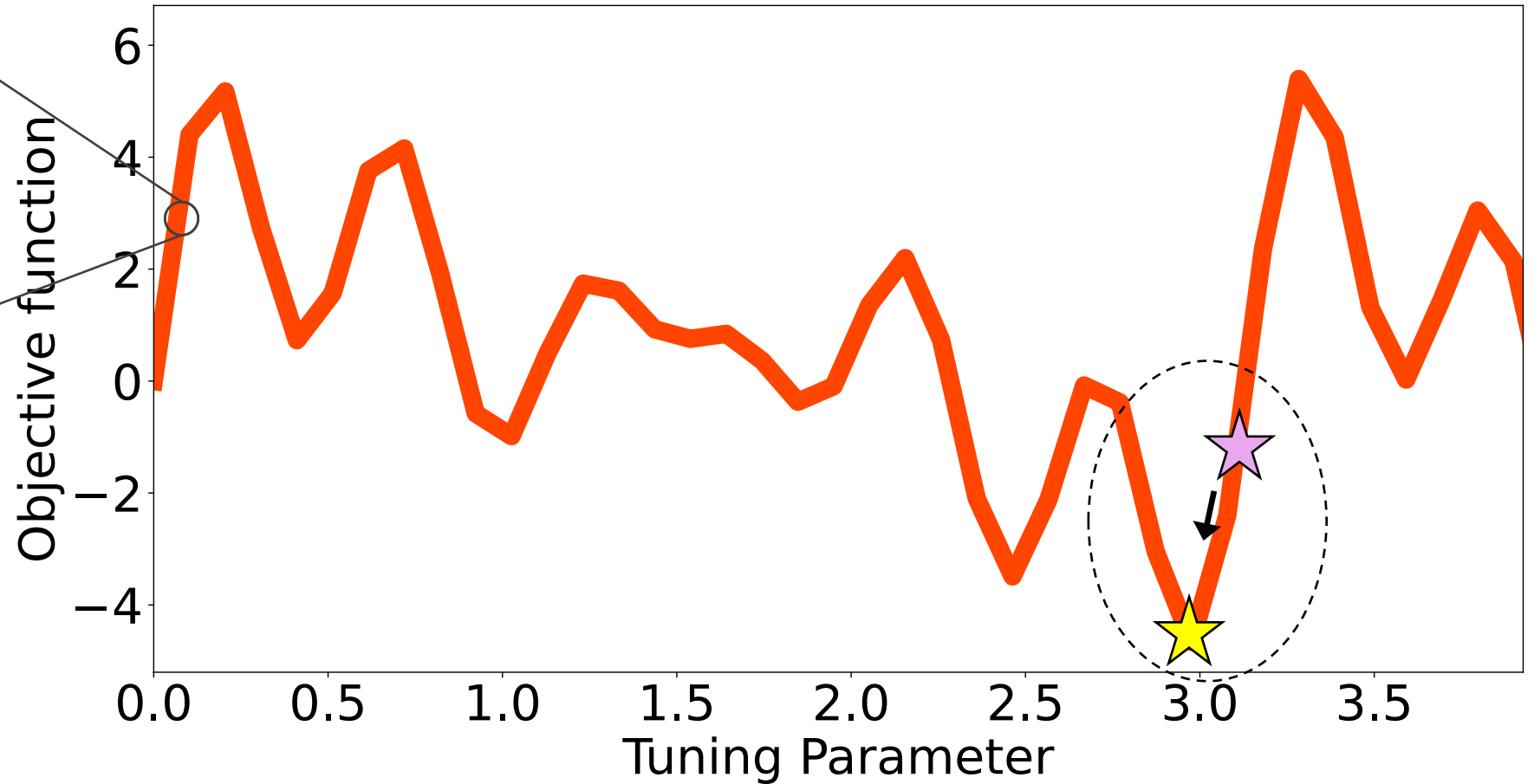
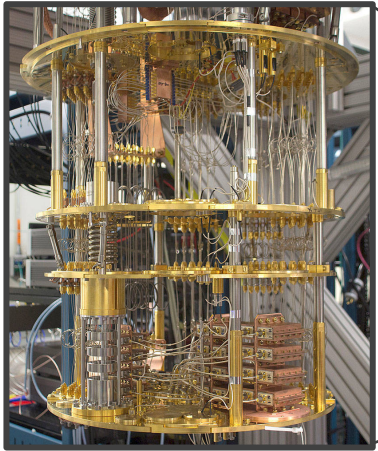
CAFQA Insight #2: Efficiently search the discrete space classically to find the lowest objective (w/ Bayesian Optimization).



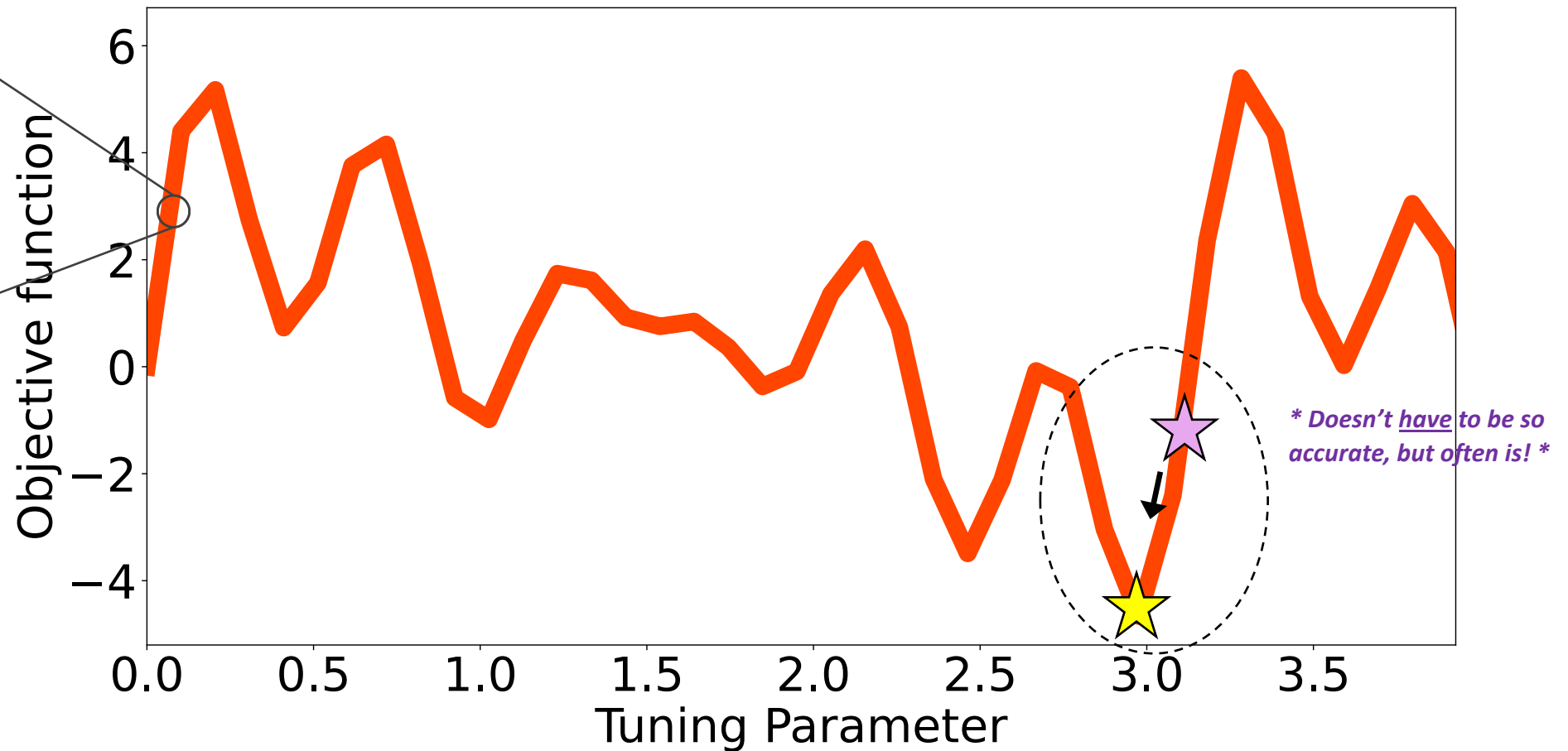
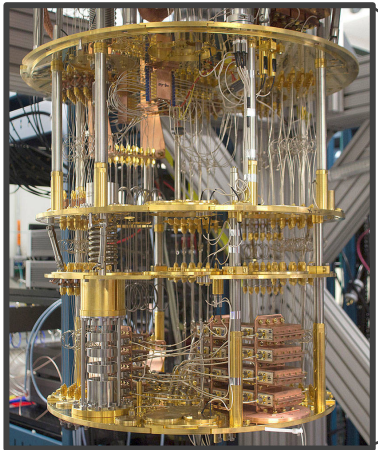
Bayesian Optimization



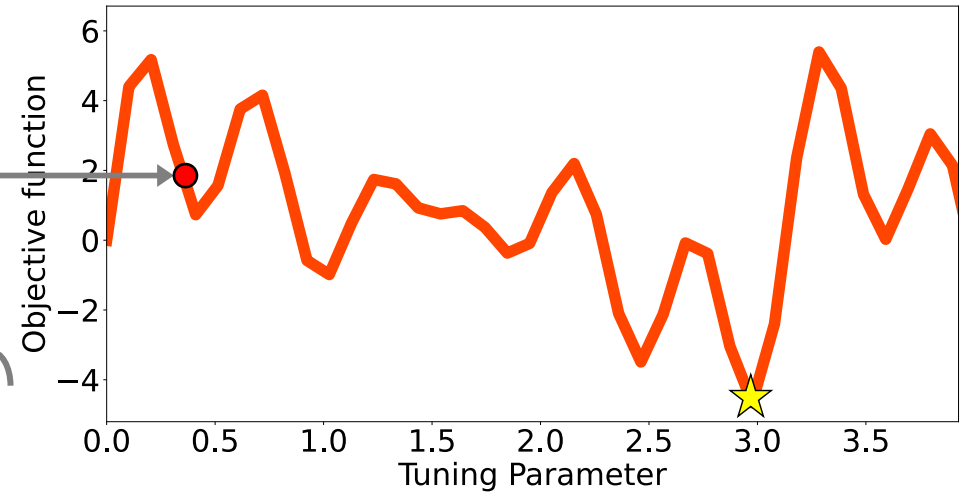
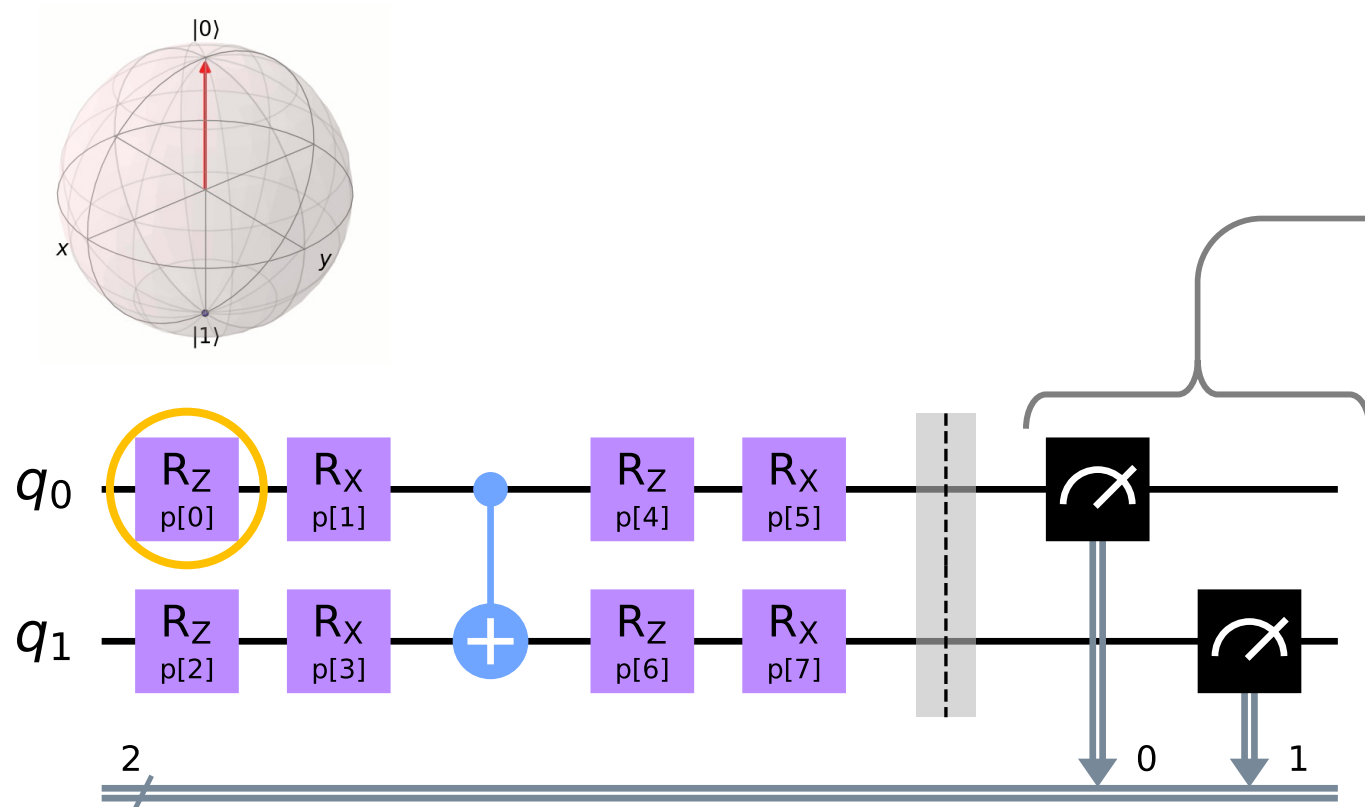
# CAFQA: Clifford Ansatz For Quantum Accuracy



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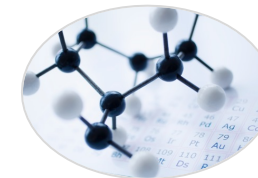
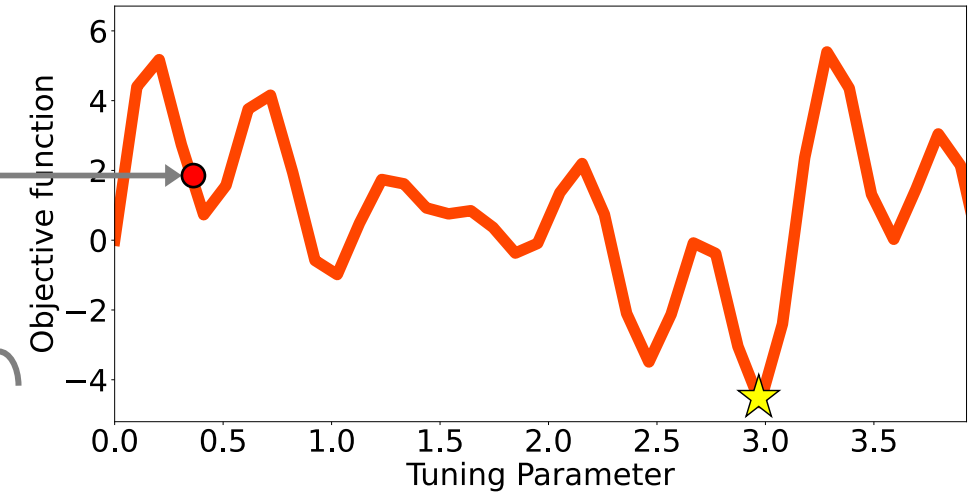
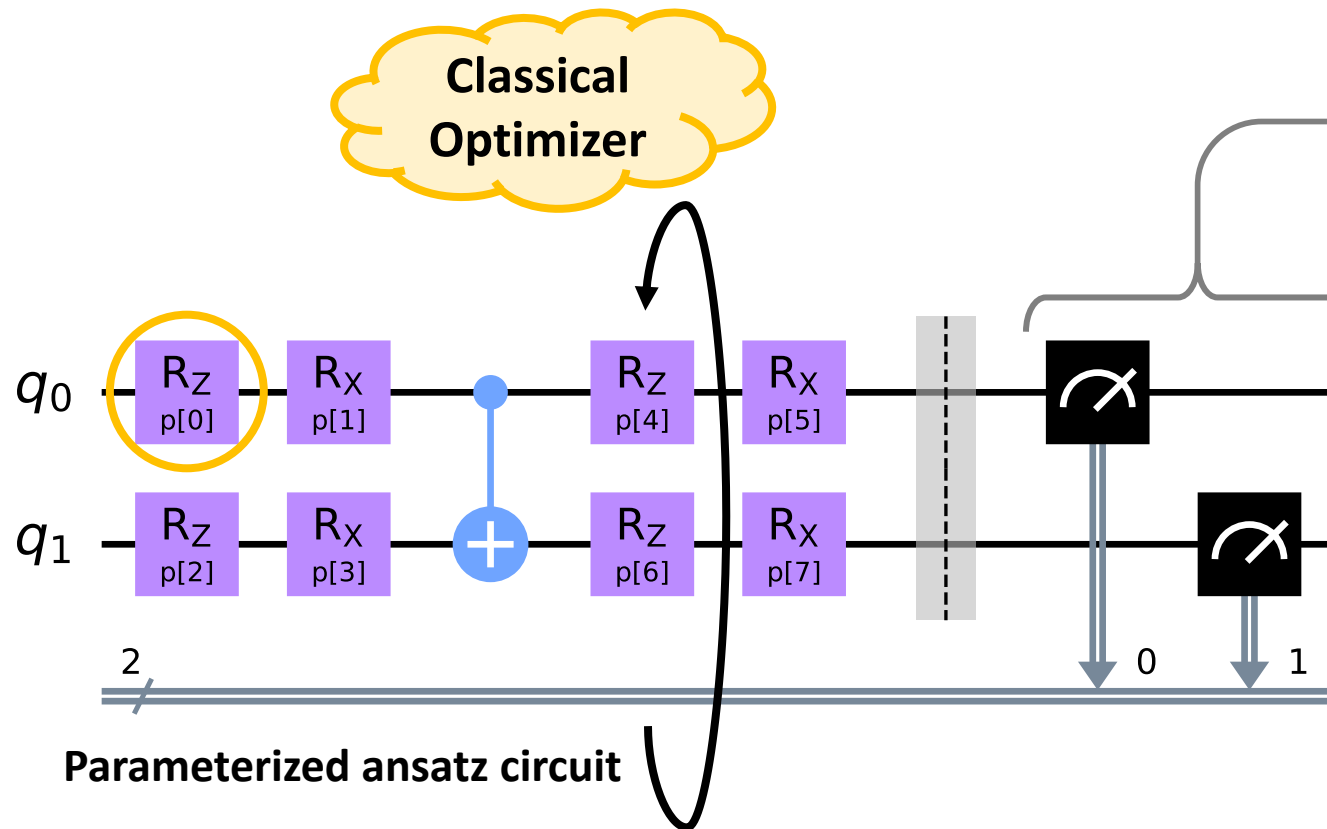
# How VQA works



Parameterized ansatz circuit

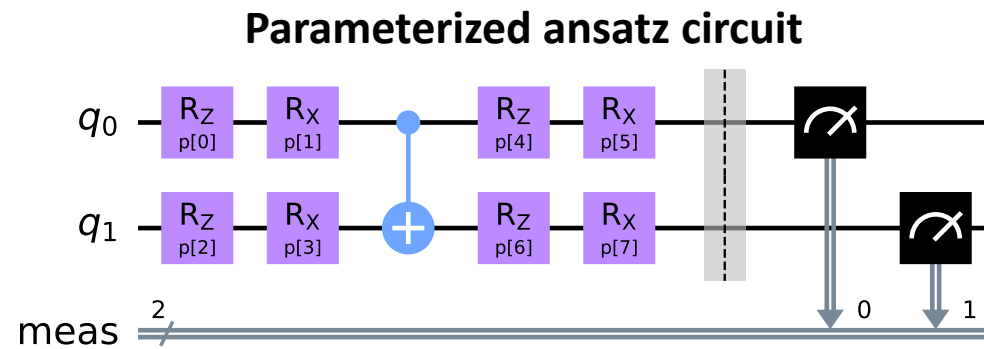


# How VQA works



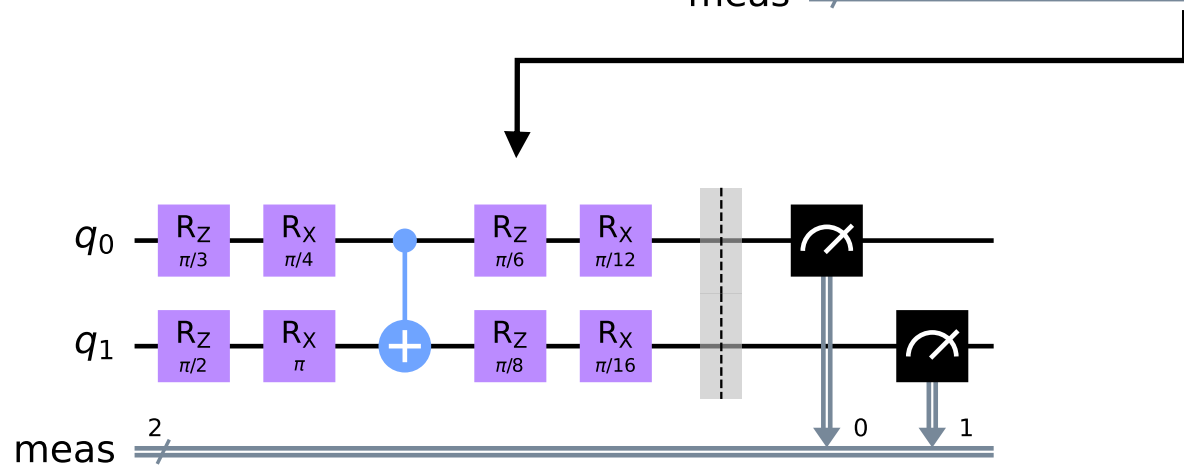
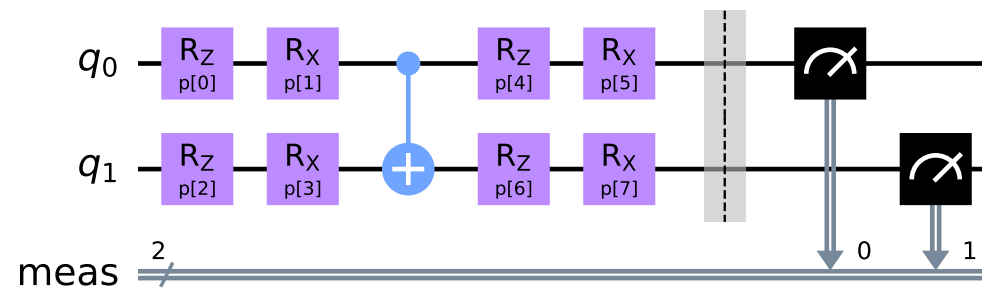


# Classical simulability of Clifford quantum circuits



# Classical simulability of Clifford quantum circuits

Parameterized ansatz circuit



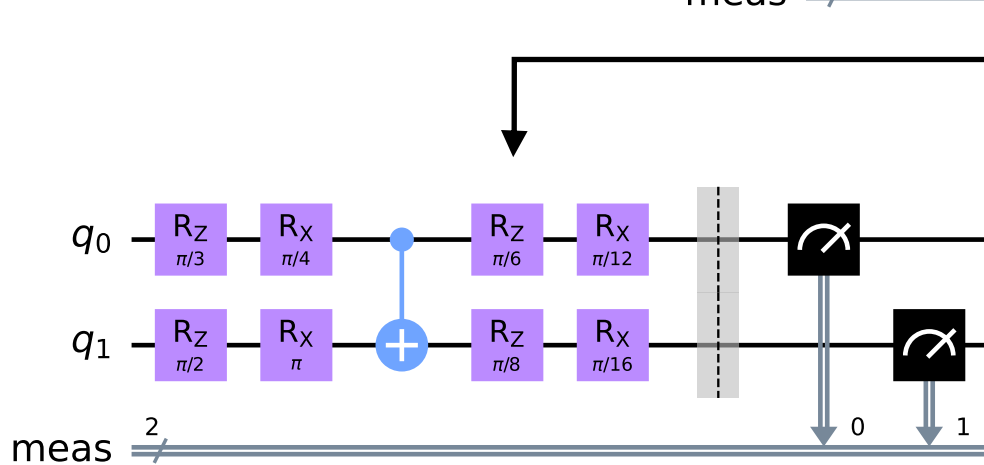
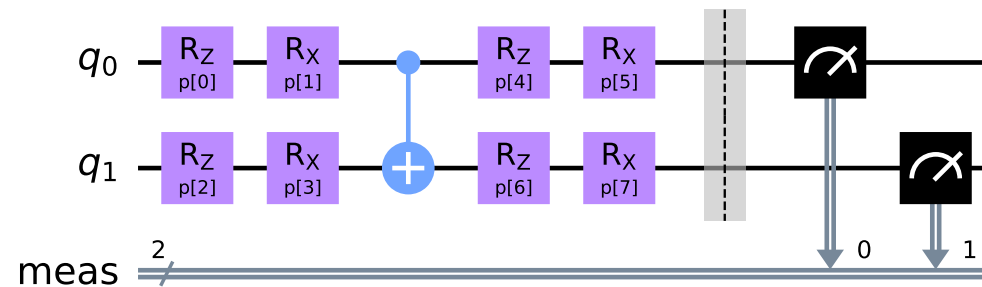
A classically intractable general circuit

Continuous angles =  $[0, 2 * \pi]$

# Classical simulability of Clifford quantum circuits

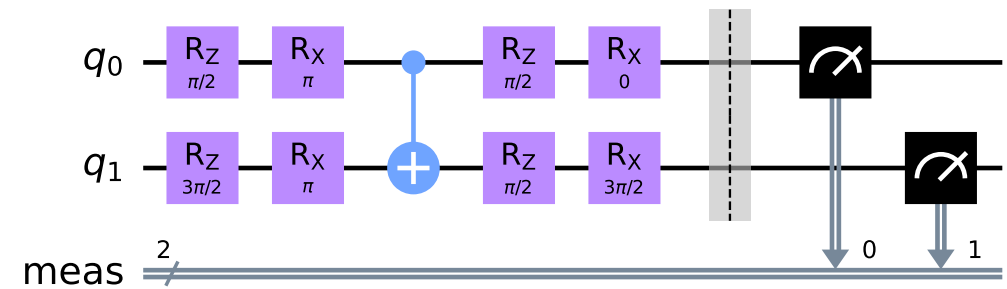
**Gottesman–Knill theorem [‘98] - A QC circuit can be classically simulated efficiently if: (a) it has only Clifford gates, (b) classical qubit prep and measurement.**

Parameterized ansatz circuit



**A classically intractable general circuit**

**Continuous angles =  $[0, 2 \cdot \pi]$**

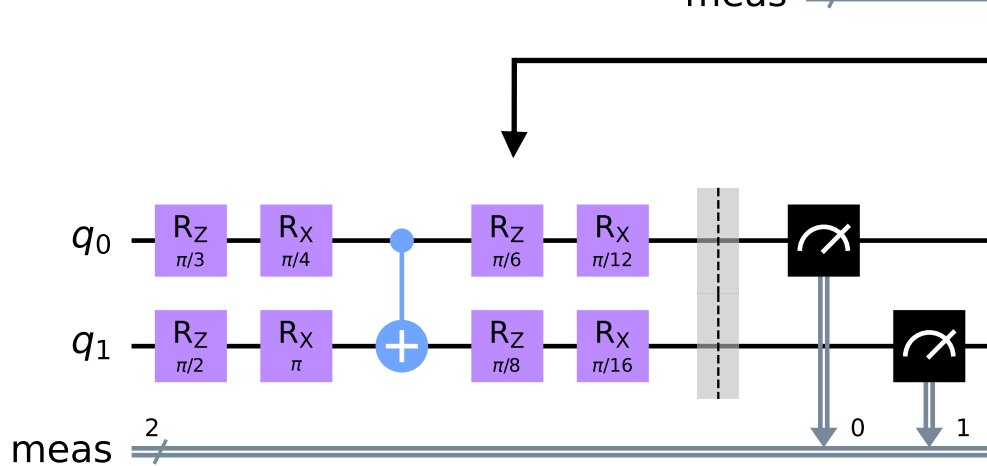
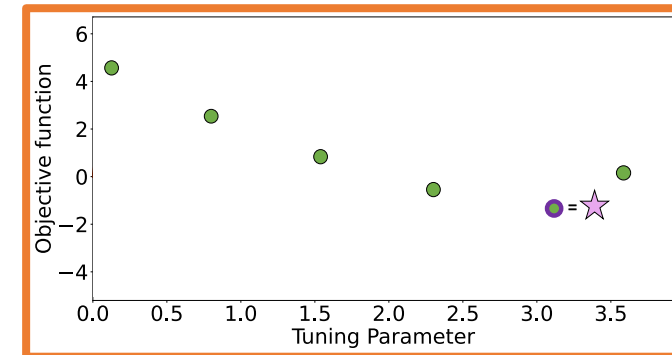
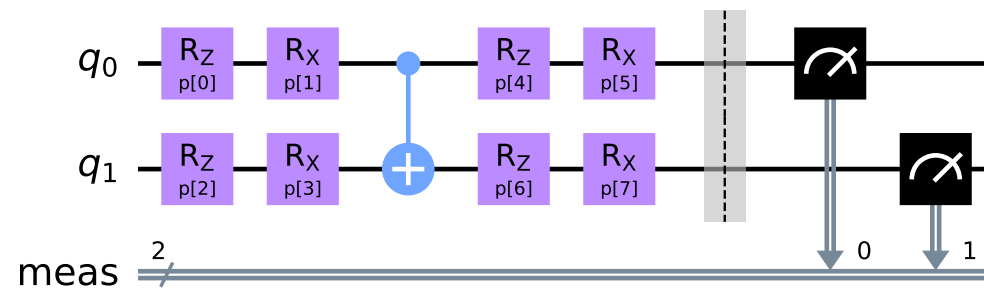


**A classically simulable Clifford circuit**

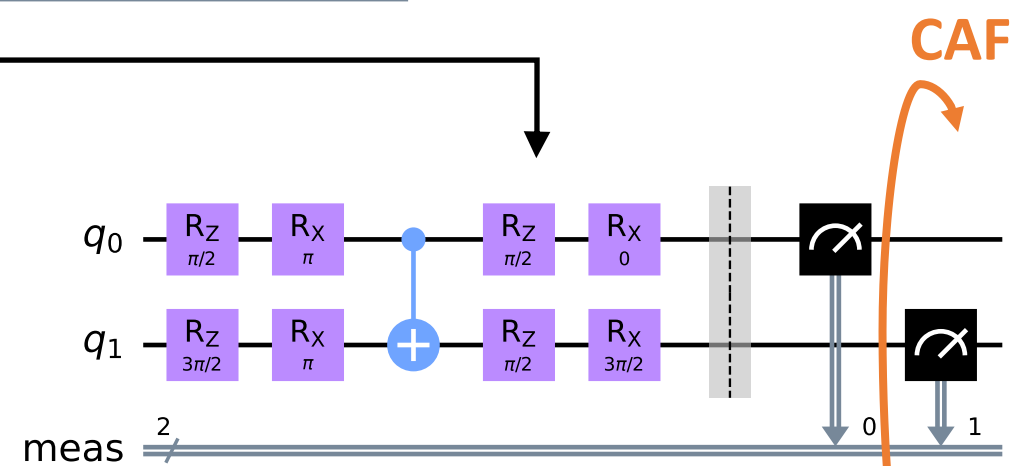
**Discrete angles =  $\{0, \pi/2, \pi, 3 \cdot \pi/2\}$**

# Classical simulability of Clifford quantum circuits

Parameterized ansatz circuit



A classically intractable general circuit  
Continuous angles =  $[0, 2\pi]$

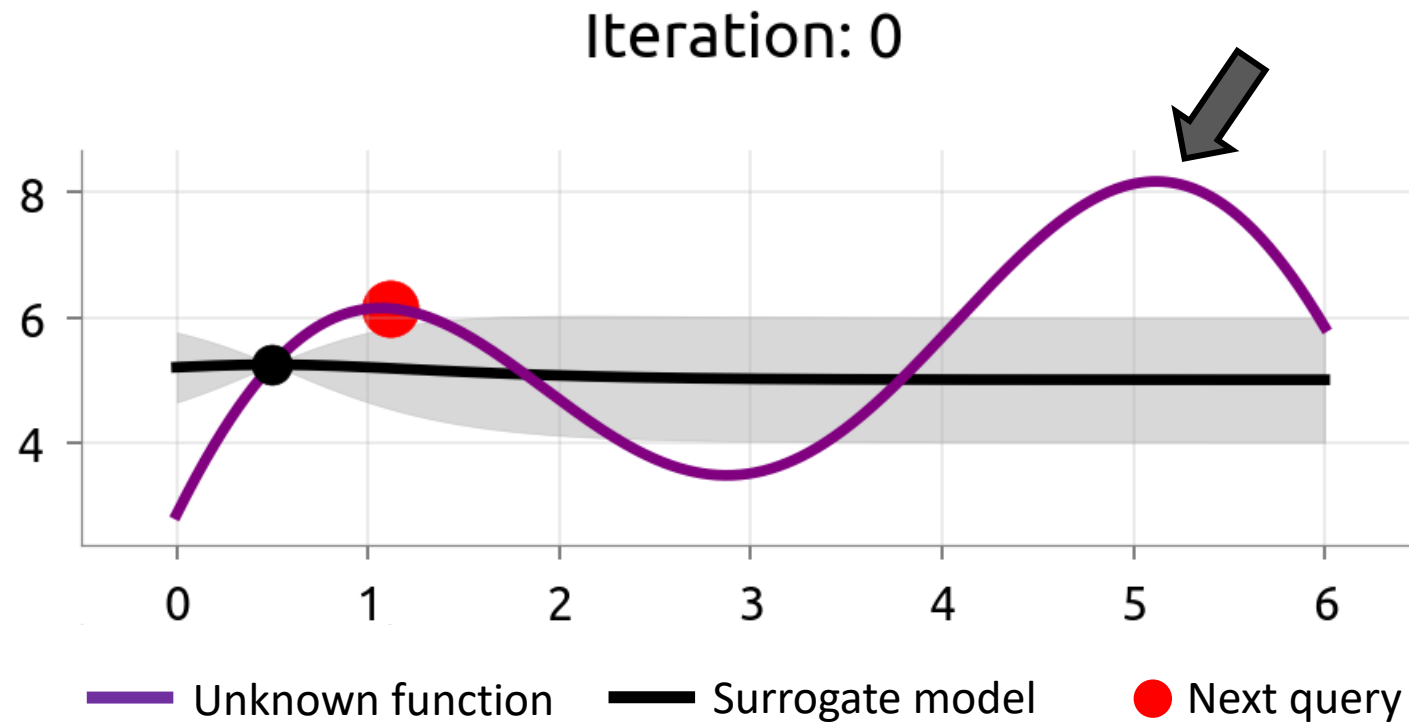


A classically simulable Clifford circuit  
Discrete angles =  $\{0, \pi/2, \pi, 3\pi/2\}$

CAFQA

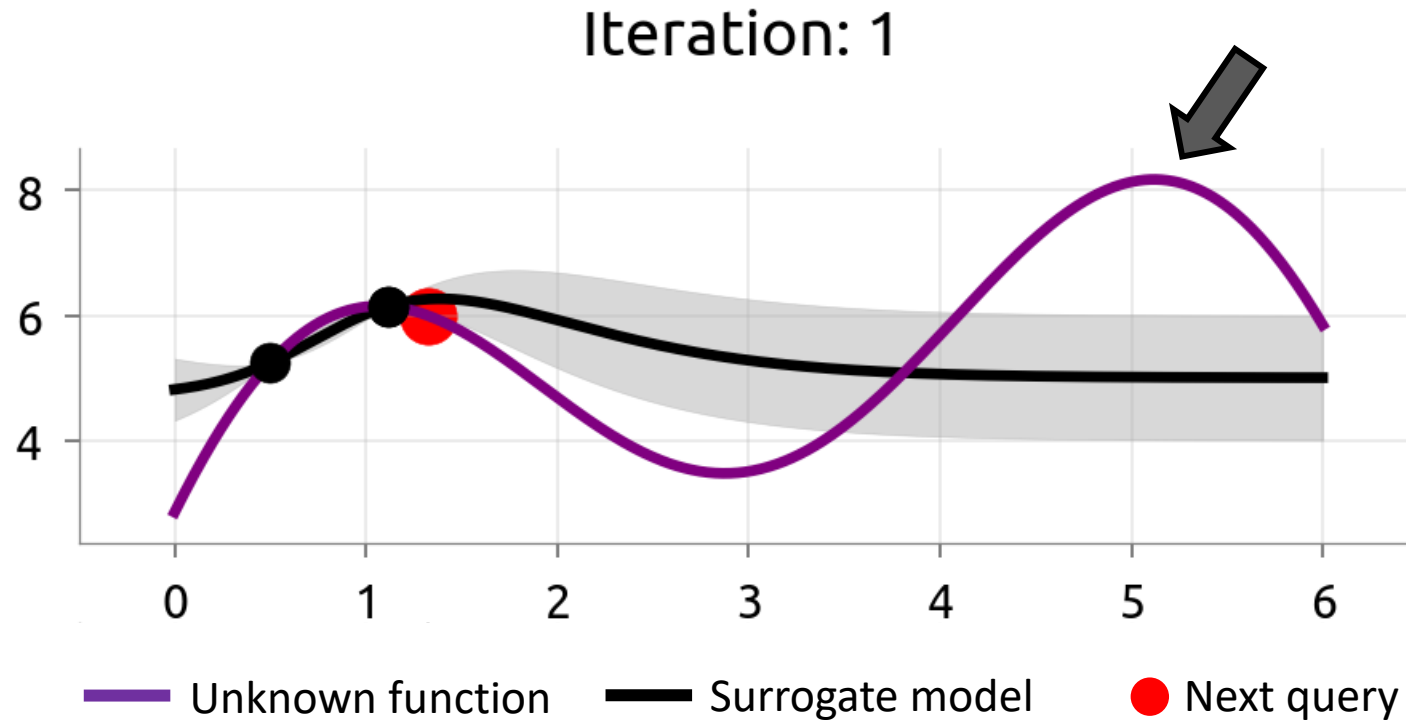


# Finding the optimal Clifford point: Bayesian Optimization



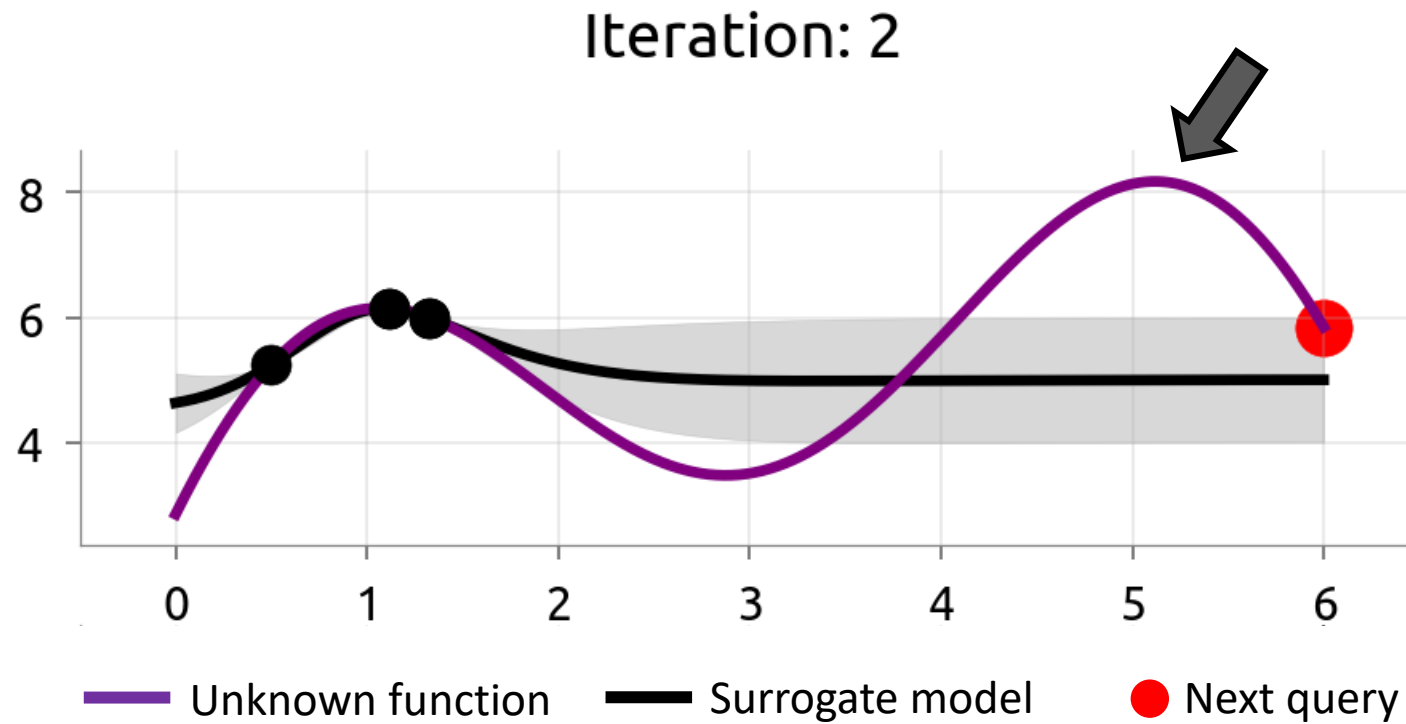
<https://distill.pub/2020/bayesian-optimization/>

# Finding the optimal Clifford point: Bayesian Optimization



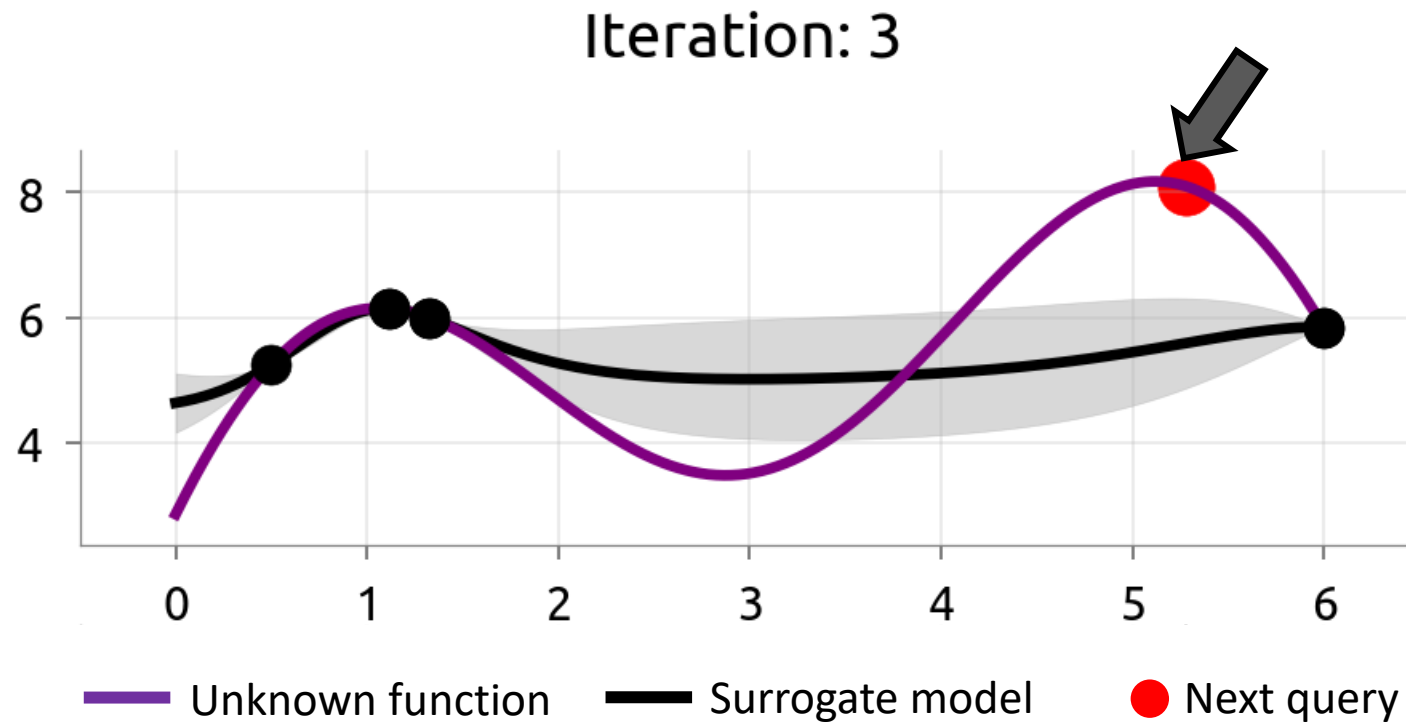
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# Finding the optimal Clifford point: Bayesian Optimization



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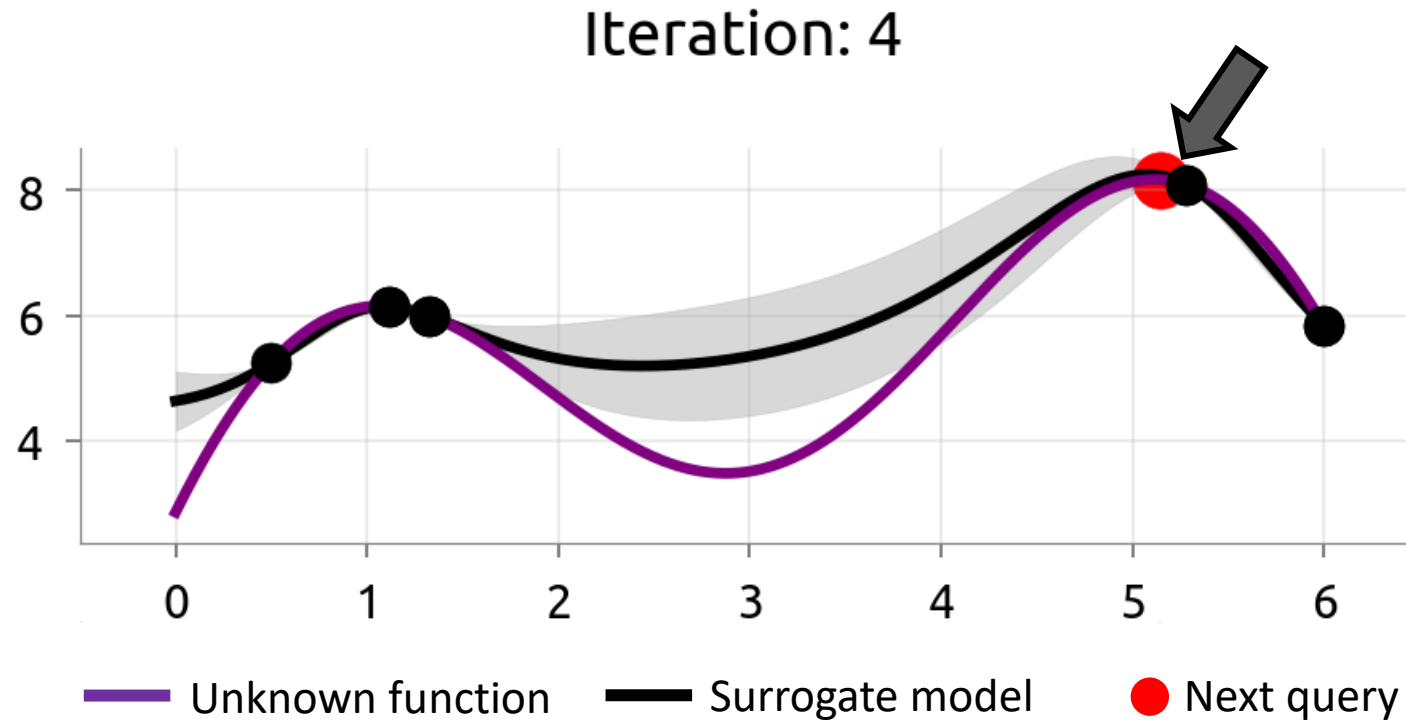
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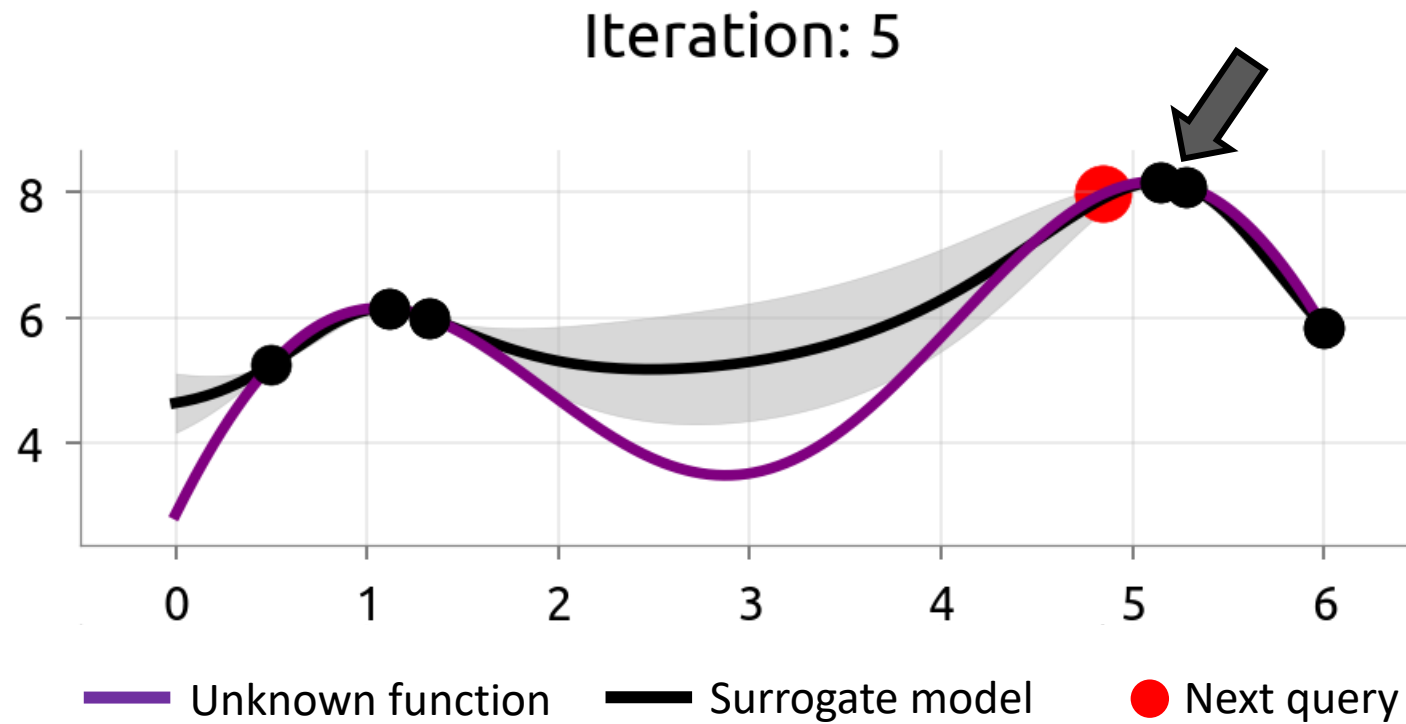


# Finding the optimal Clifford point: Bayesian Optimization



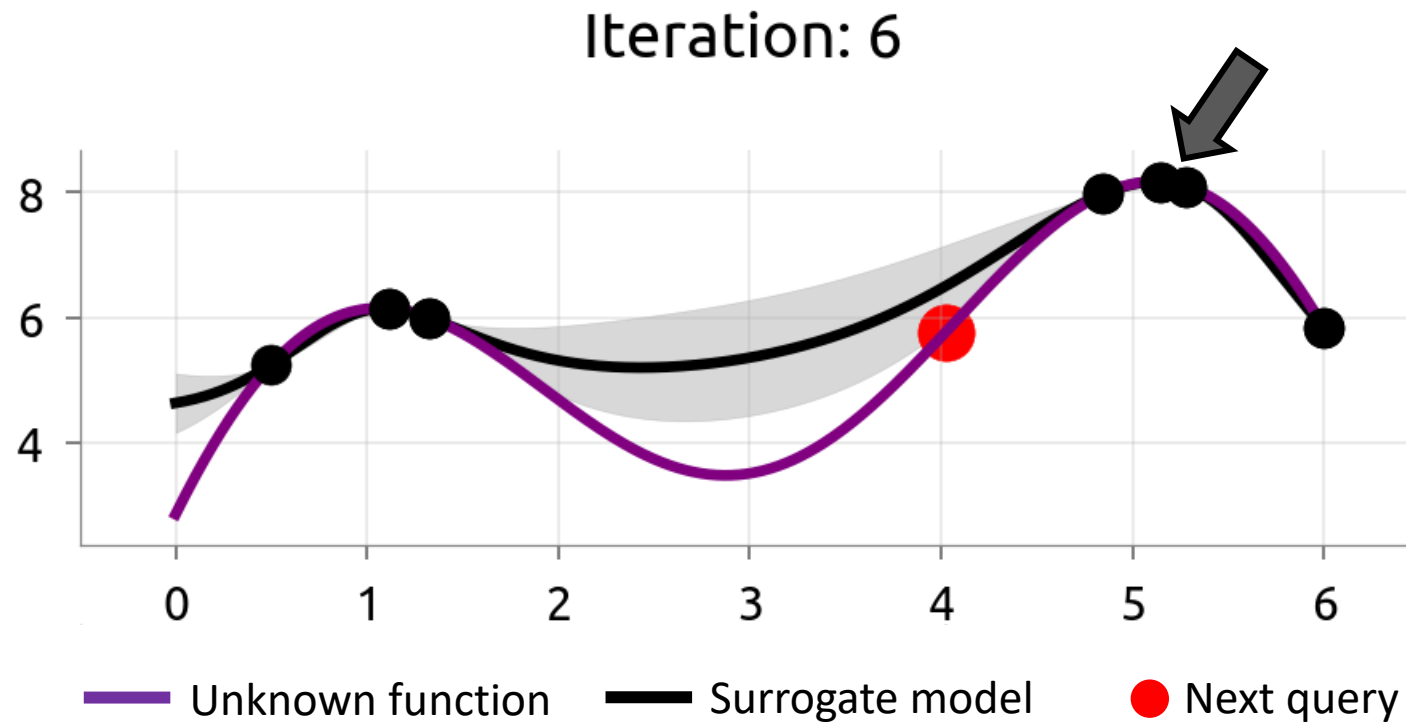
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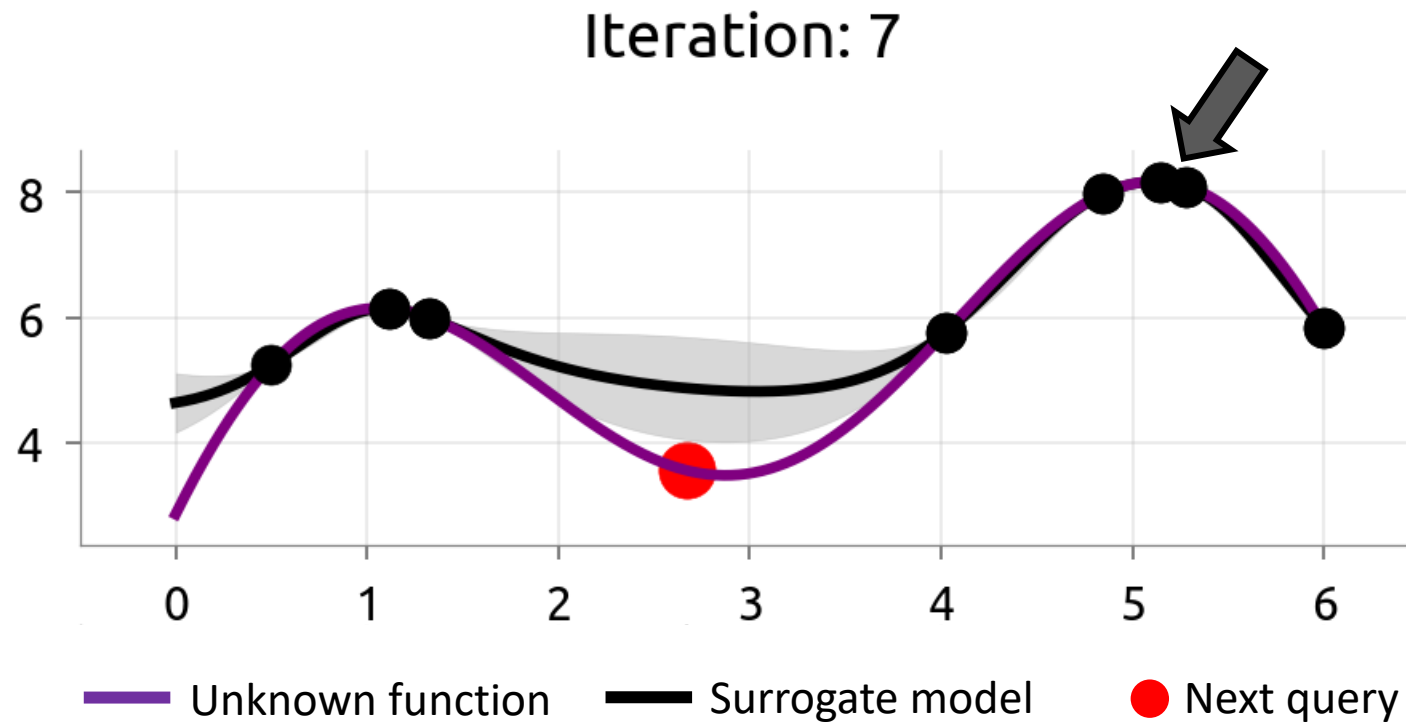
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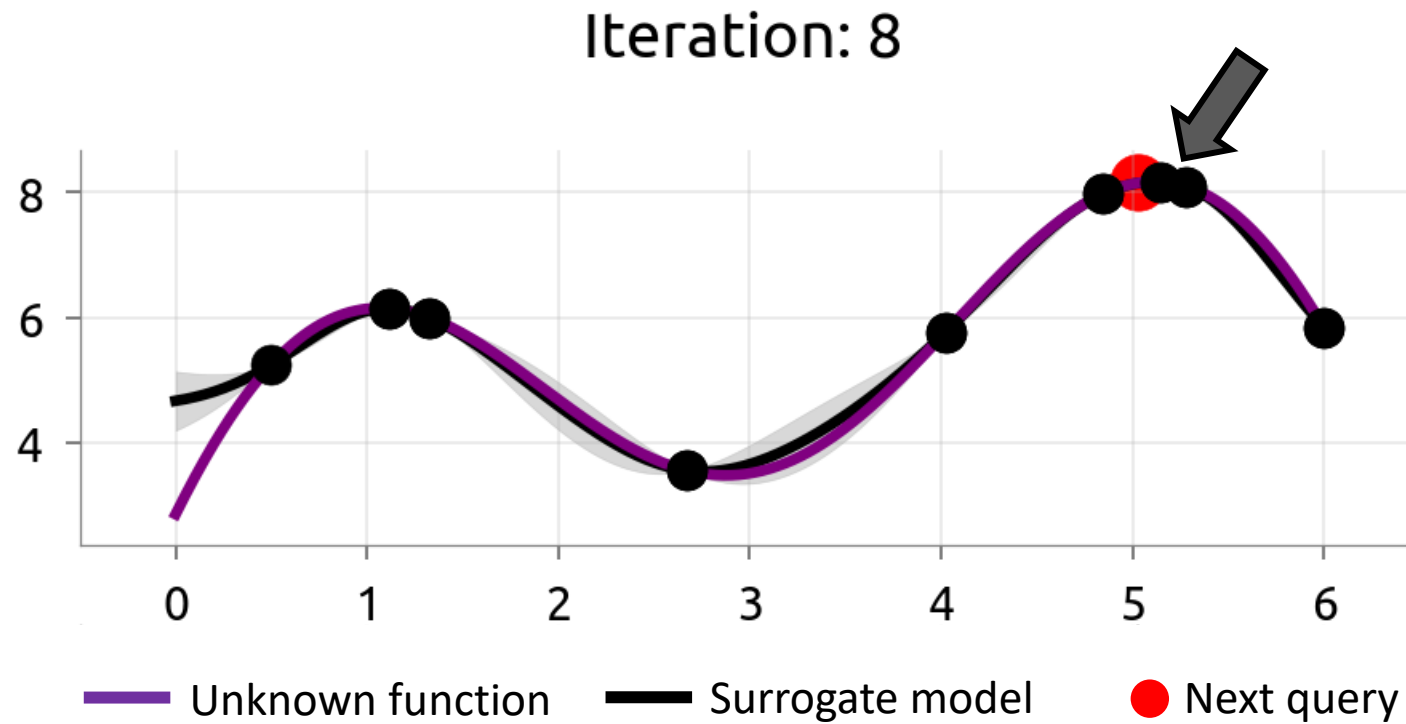
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# Finding the optimal Clifford point: Bayesian Optimization



<https://distill.pub/2020/bayesian-optimization/>

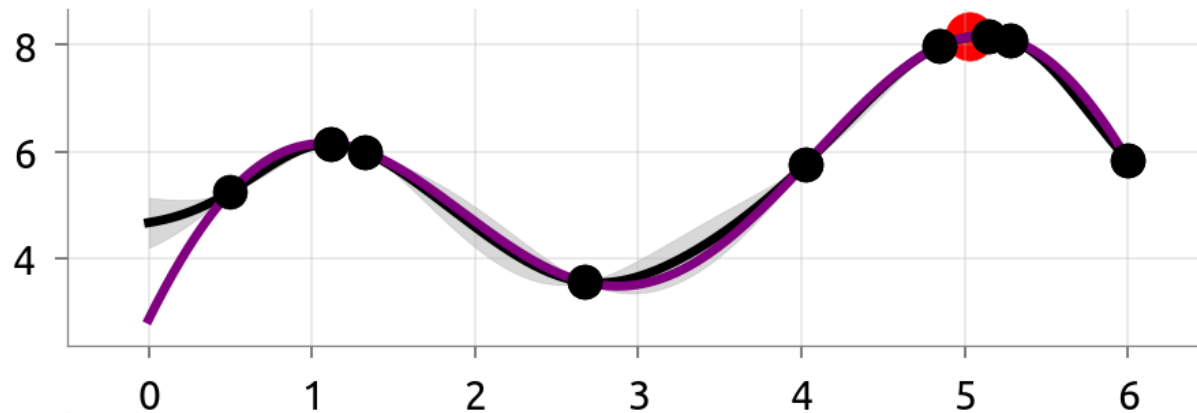
# Finding the optimal Clifford point: Bayesian Optimization



<https://distill.pub/2020/bayesian-optimization/>

# Finding the optimal Clifford point: Bayesian Optimization

Iteration: 8

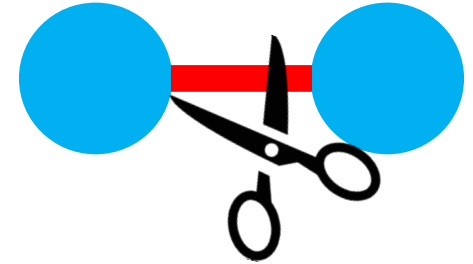


***HyperMapper [Nardi 2019]: A Practical Design Space Exploration Framework.***

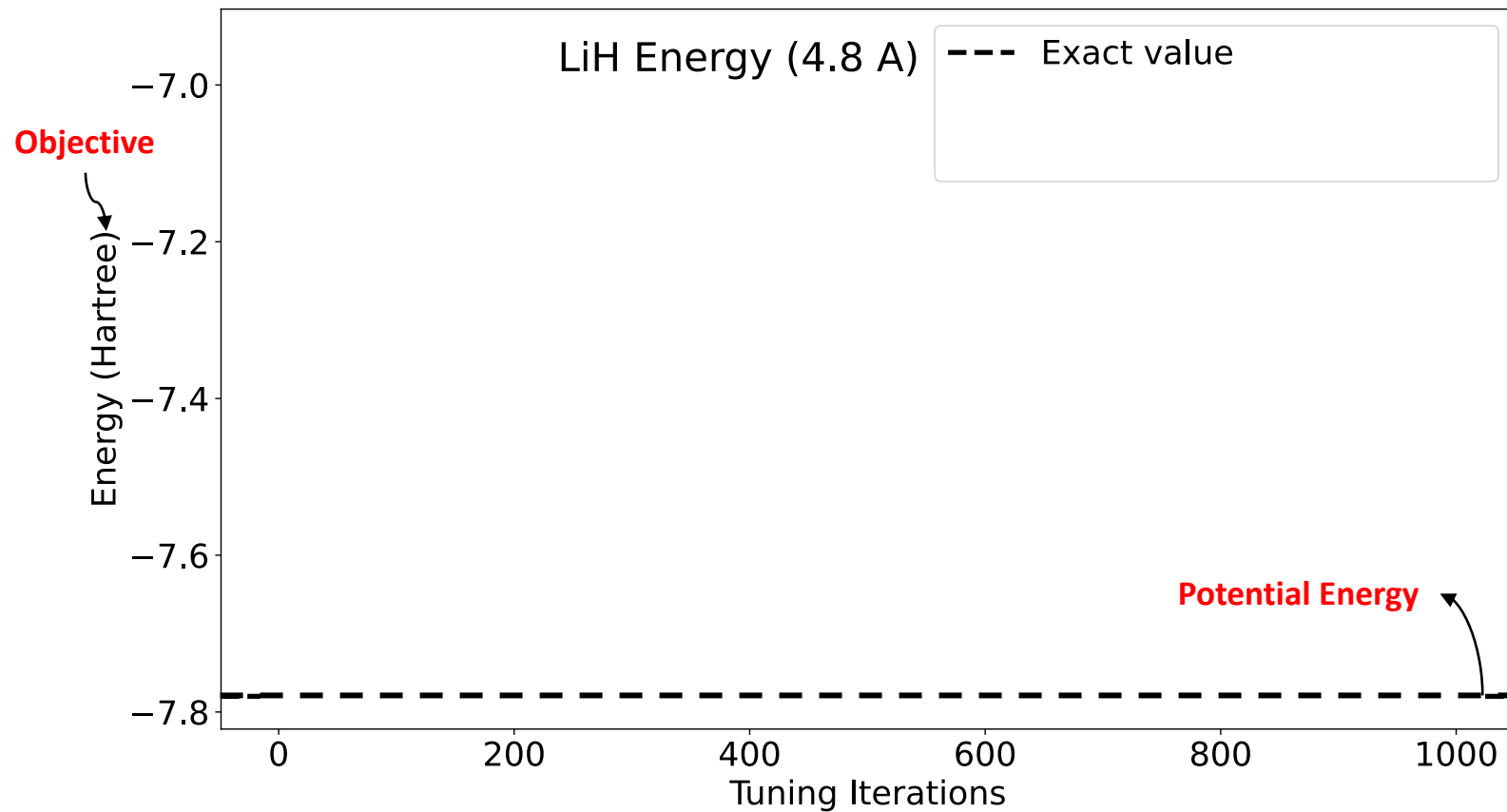
- (1) Random forests surrogate model (discrete search space).**
- (2) Semi-greedy acquisition function.**

# Quantitative benefits for chemistry applications

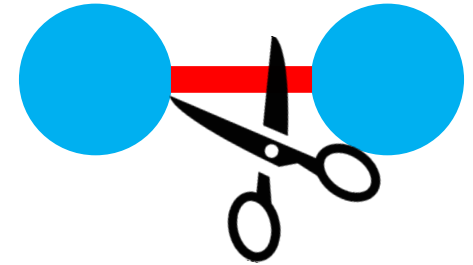
Potential Energy



# Quantitative benefits for chemistry applications

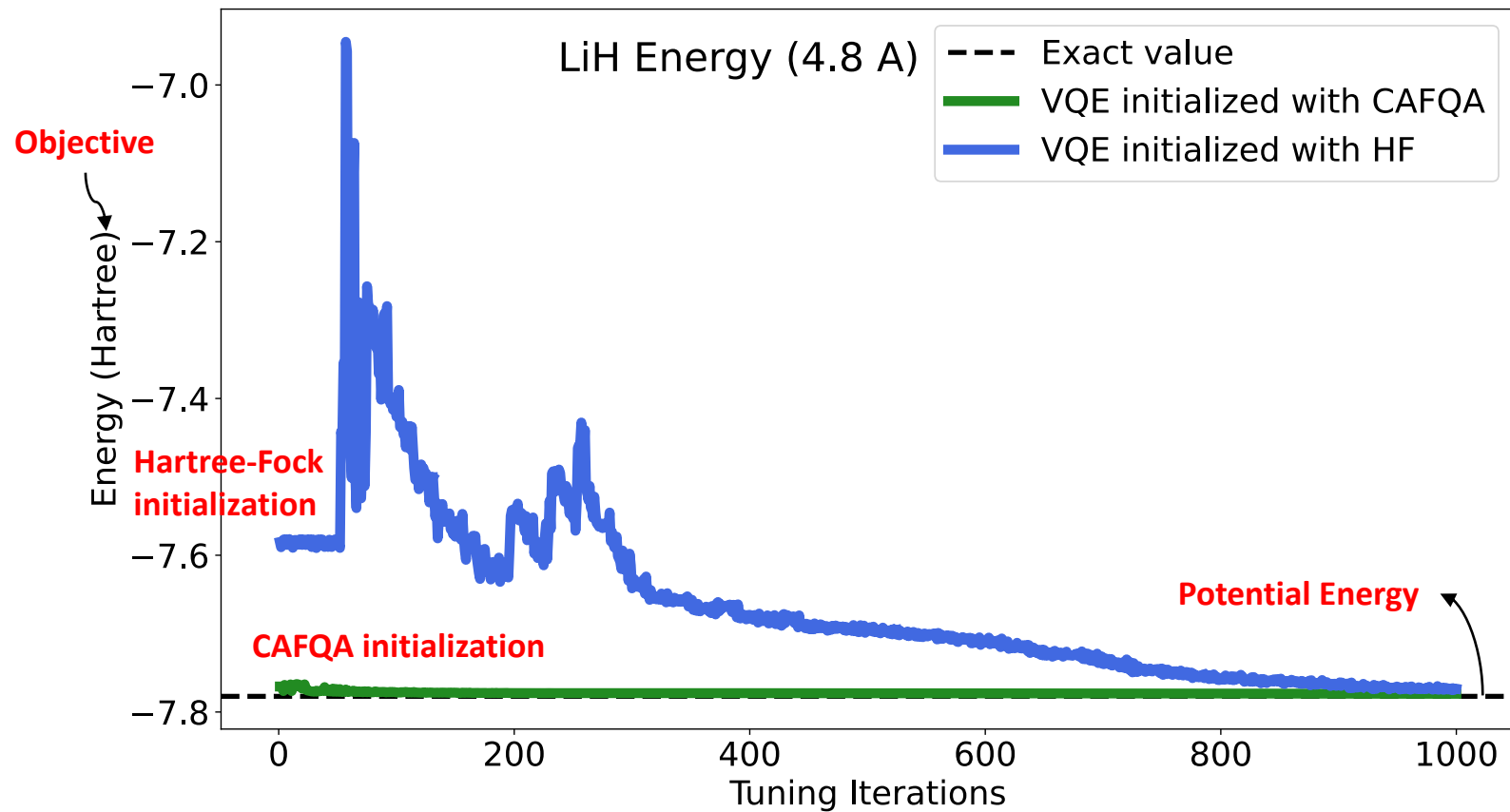


Potential Energy

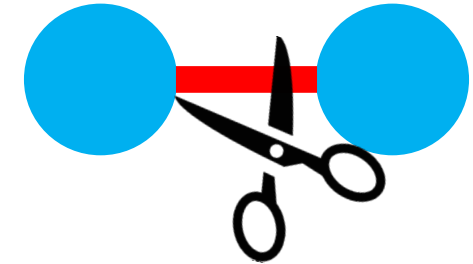




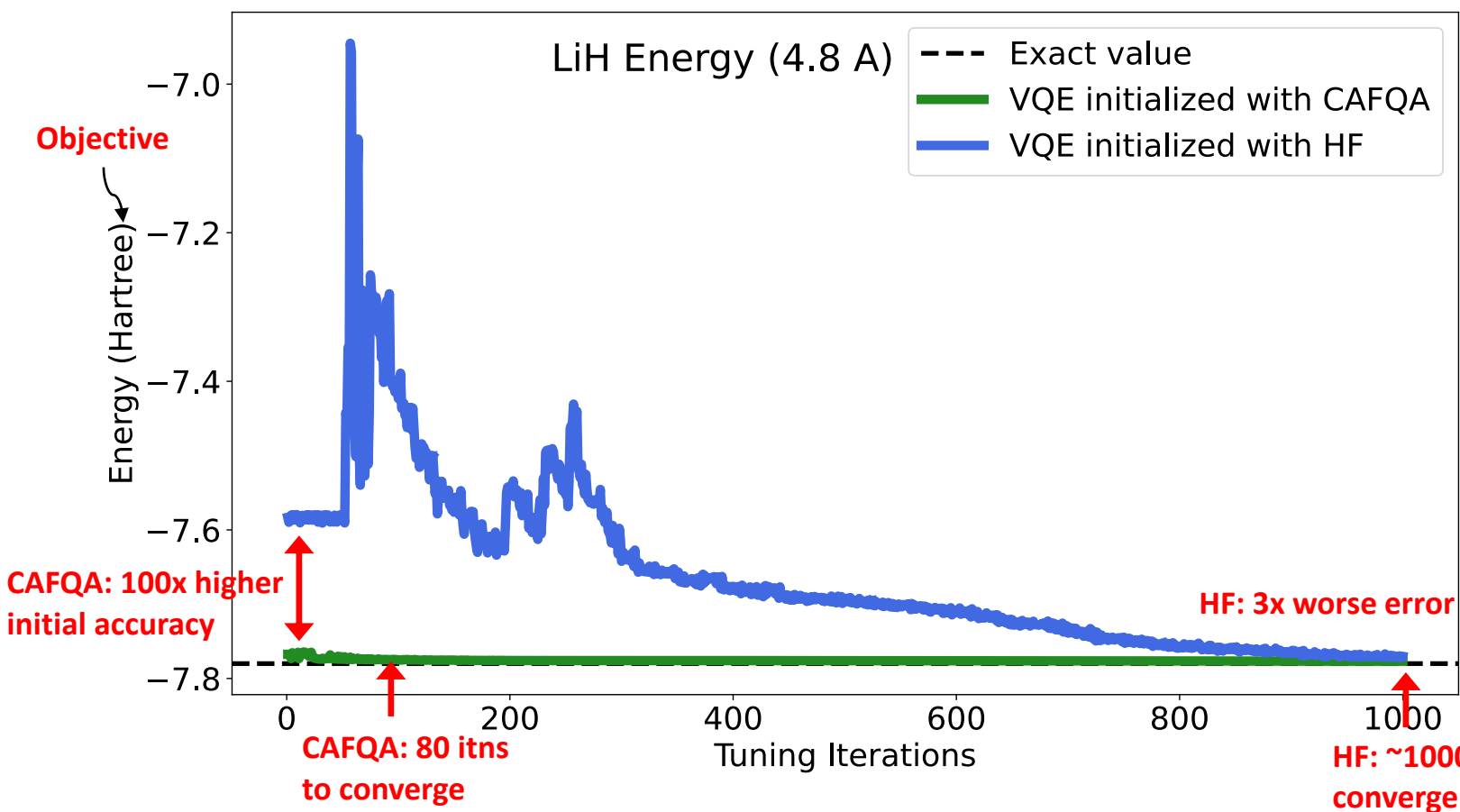
# Quantitative benefits for chemistry applications



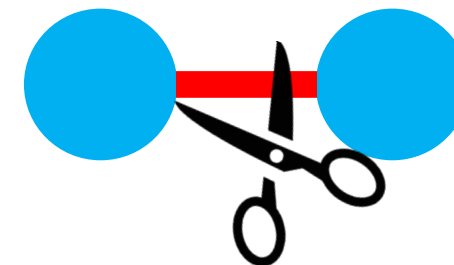
Potential Energy



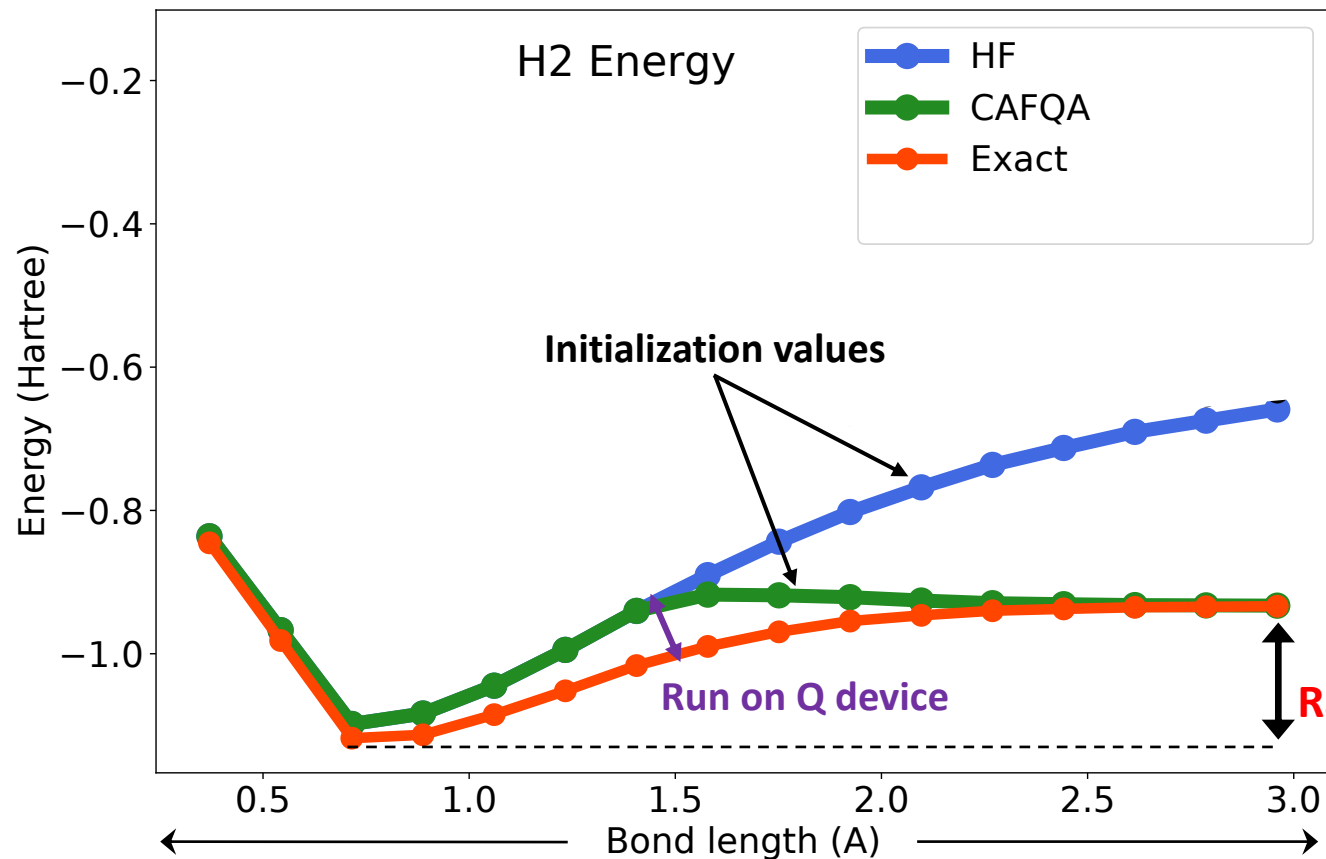
# Quantitative benefits for chemistry applications



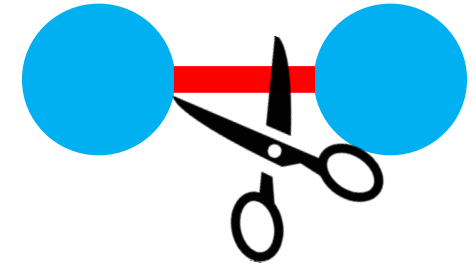
Potential Energy



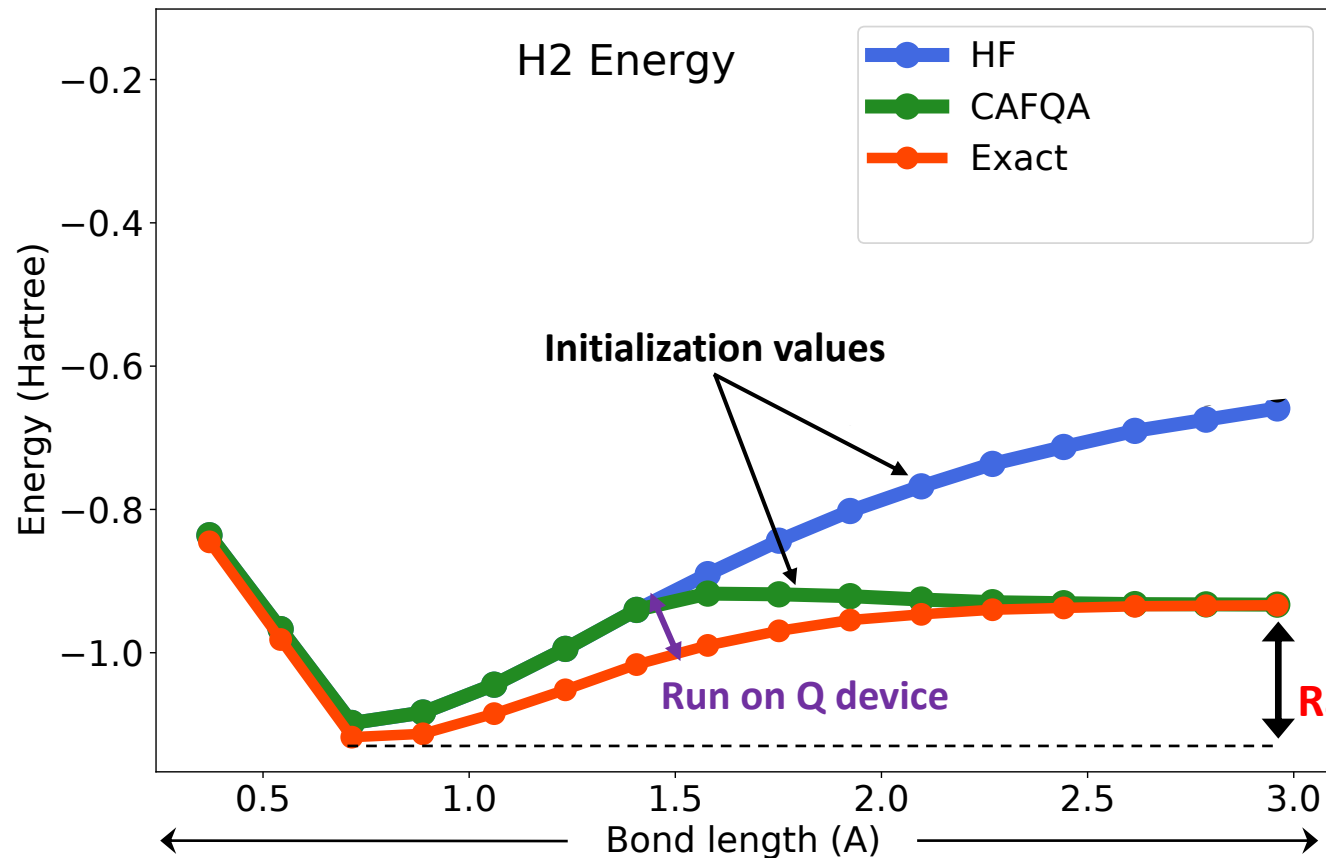
# Quantitative benefits for chemistry applications



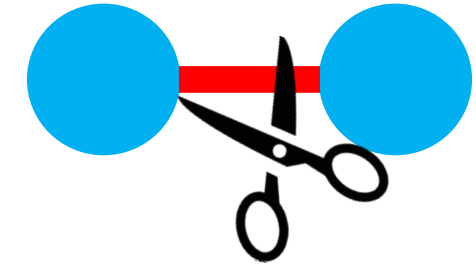
Potential Energy



# Quantitative benefits for chemistry applications



Potential Energy

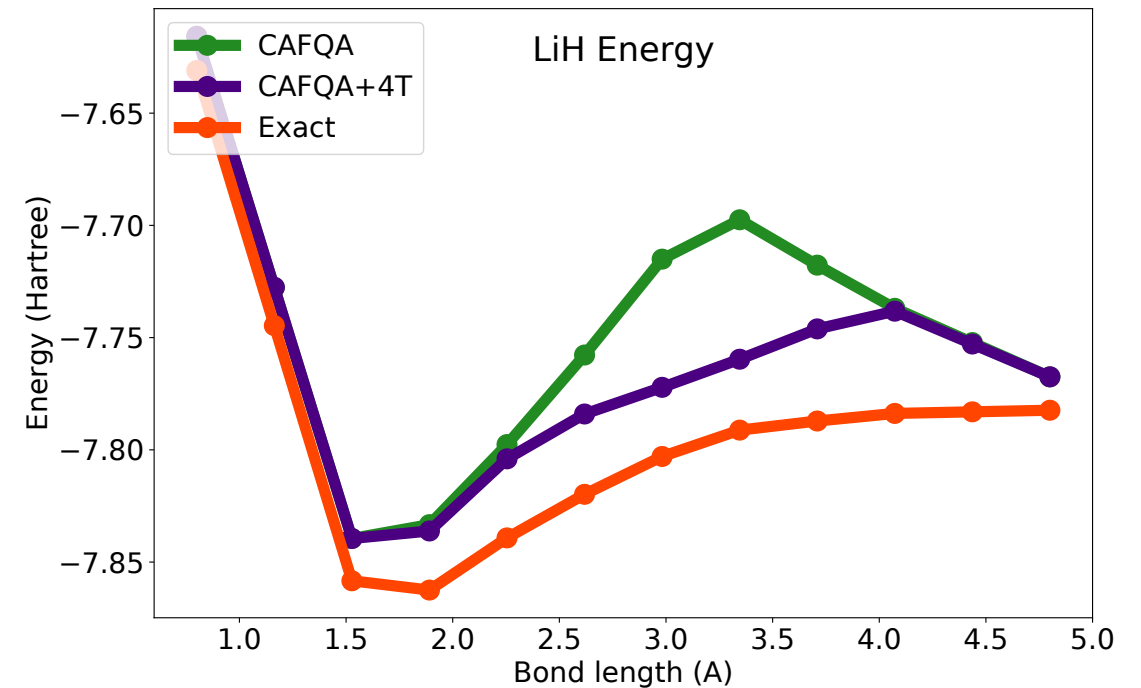
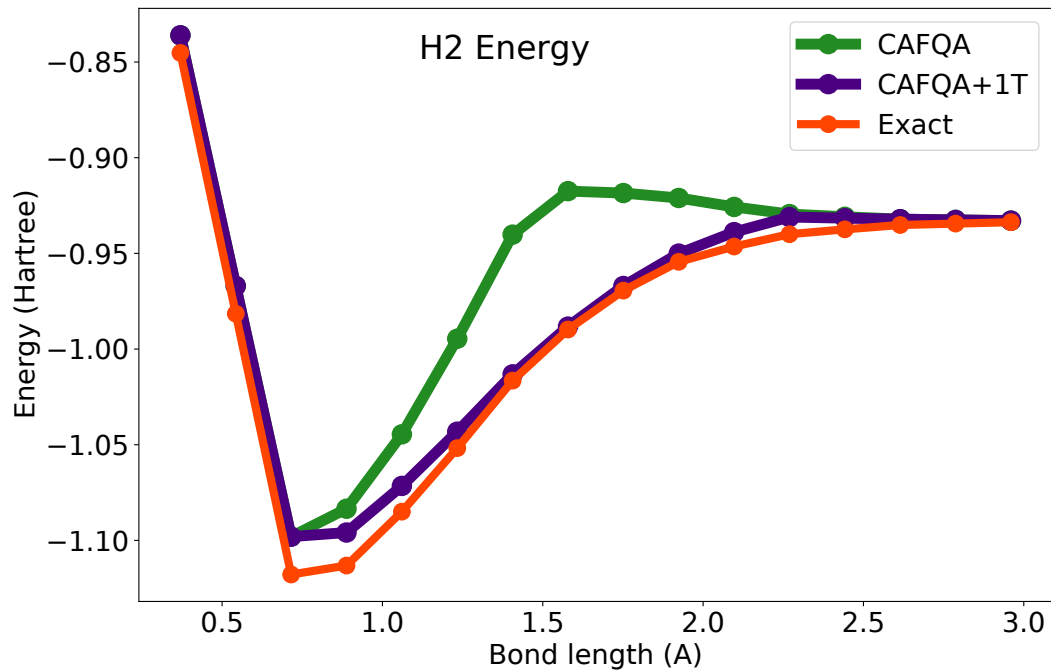


1. CAFQA achieves 99% mean initialization accuracy (systems up to 34 qubits).
2. Recovers up to 99.99% of Hartree-Fock inaccuracy (57x mean).
3. BO takes ~2000 iterations (mean), 1 hour to a week in wall-clock time.

# CAFQA 2.0: Reducing the constants and tackling new applications.

- Bare-metal Hamiltonian expectation compute on Cliffords: 10x speedup.
- Genetic Algorithm – inefficient but much faster: 10x speedup.
- Parallelization of GA population: 10-100x speedup.
- 100-qubit *physics spin models*:
  - CAFQA 1.0: NA vs. CAFQA 2.0: 1 hour
- Cr2 molecule (34 qubits, 30k terms):
  - CAFQA 1.0: 1+ week vs. CAFQA 2.0: 10 hours (and order of magnitude higher accuracy)
- Exploiting Clifford symmetry in designing the ansatz: ??? speedup

# CAFQA-ish: Classical sim to the compute limit



**Systematically push to max classical limit**  
**What is the classical limit?: Laptop vs Desktop vs Supercomputer**  
**Interesting optimization problems**

# Working with classical simulators

**Build new theory-inspired simulators, accelerate with application-tailoring, software, hardware optimizations, integrate with SOTA classical/AI tools**

## CAFQA: A classical simulation bootstrap for variational quantum algorithms

Gokul Subramanian Ravi\*  
University of Chicago

Pranav Gokhale  
Super.tech (a division of ColdQuanta)

Yi Ding  
MIT

William M. Kirby  
Tufts University

Kaitlin N. Smith  
University of Chicago

Jonathan M. Baker  
University of Chicago

Peter J. Love  
Tufts University

Henry Hoffmann  
University of Chicago

Kenneth R. Brown  
Duke University

Frederic T. Chong  
University of Chicago  
Super.tech (a division of ColdQuanta)

## Simulating quantum circuit expectation values by Clifford perturbation theory

Tomislav Begušić, Krasa Hejazi, and Garnet Kin-Lic Chan

Division of Chemistry and Chemical Engineering, California Institute of Technology, Pasadena, California 91125,

## Efficient tensor network simulation of IBM's Eagle kicked Ising experiment

Joseph Tindall,<sup>1</sup> Matthew Fishman,<sup>1</sup> E. Miles Stoudenmire,<sup>1</sup> and Dries Sels<sup>1,2</sup>

<sup>1</sup>Center for Computational Quantum Physics,  
Flatiron Institute, New York, New York 10010, USA

<sup>2</sup>Center for Quantum Phenomena, Department of Physics,  
New York University, 726 Broadway, New York, NY, 10003, USA

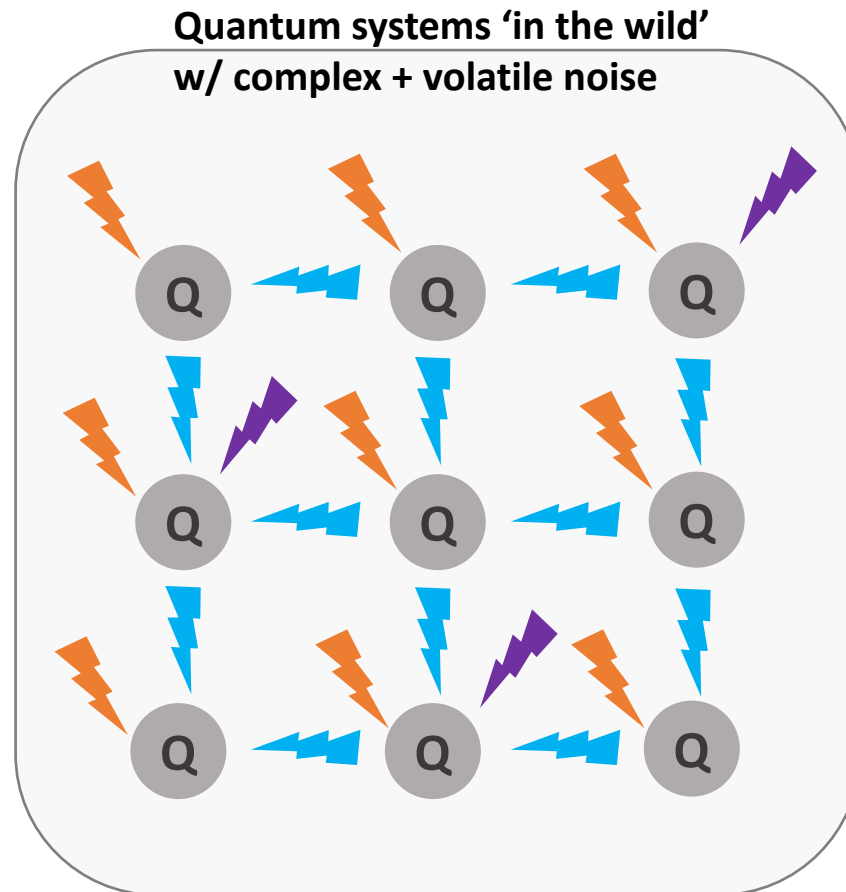
## #2) Adaptive noise mitigation through modeling and optimization



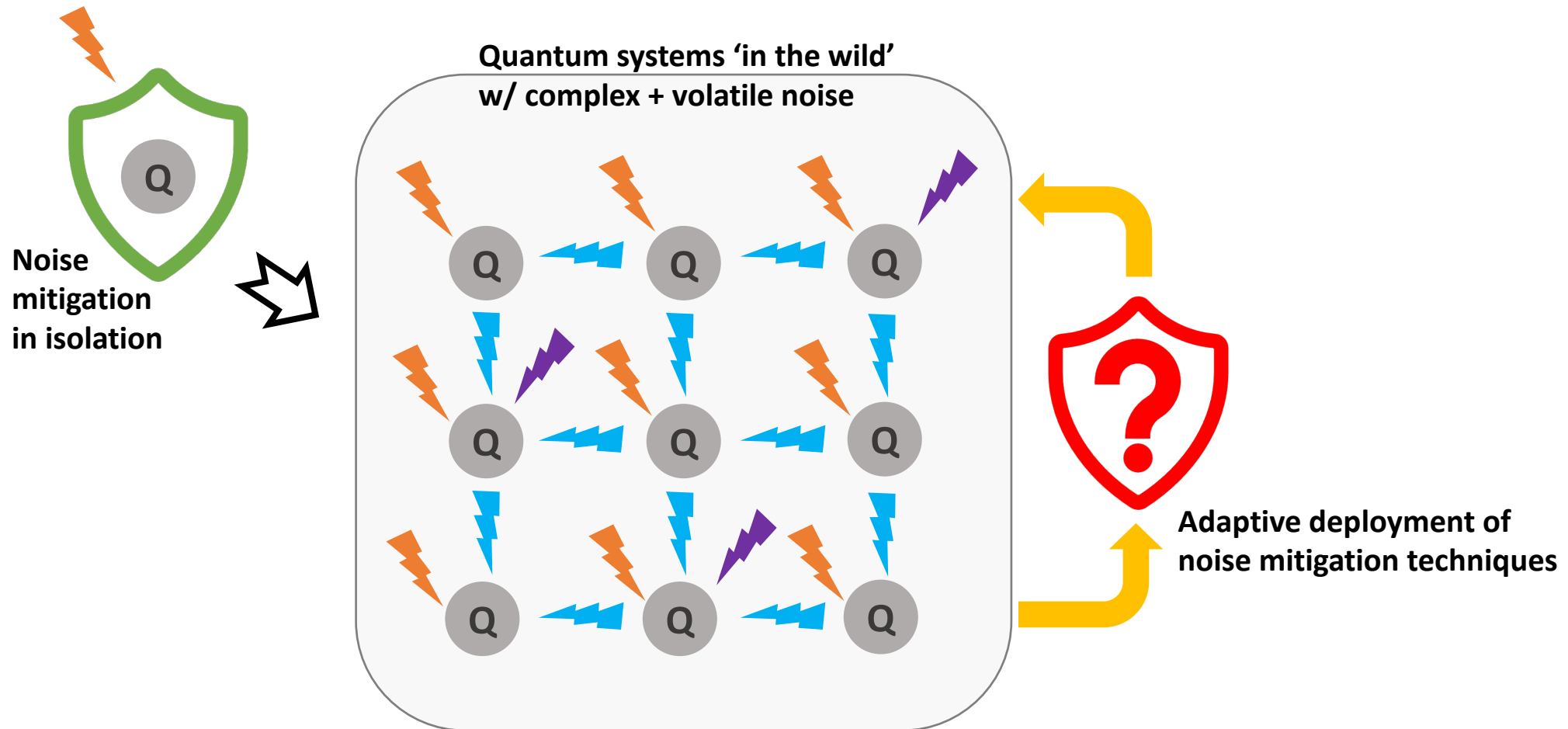
Noise  
mitigation  
in isolation



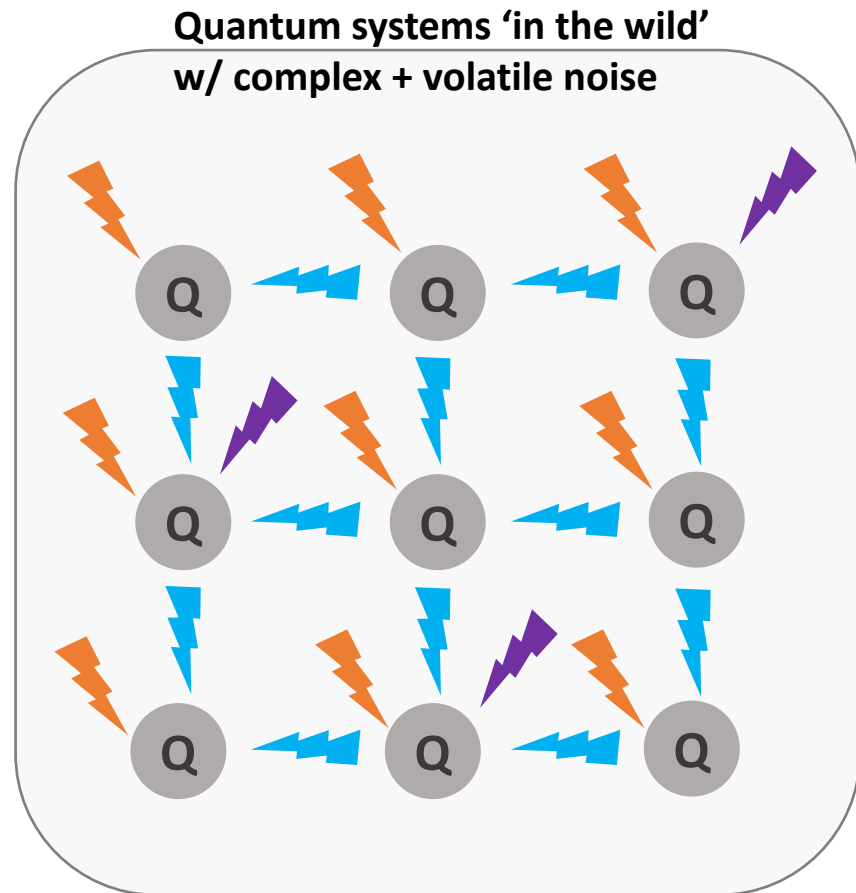
## #2) Adaptive noise mitigation through modeling and optimization



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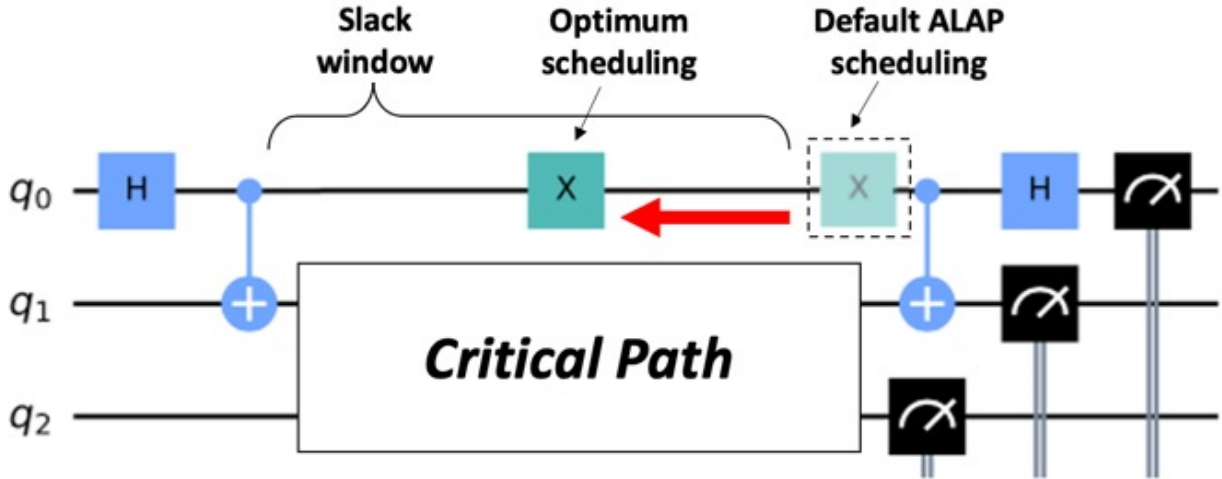


- *Noise models are important.*
- *Noise models are hard / will not suffice.*

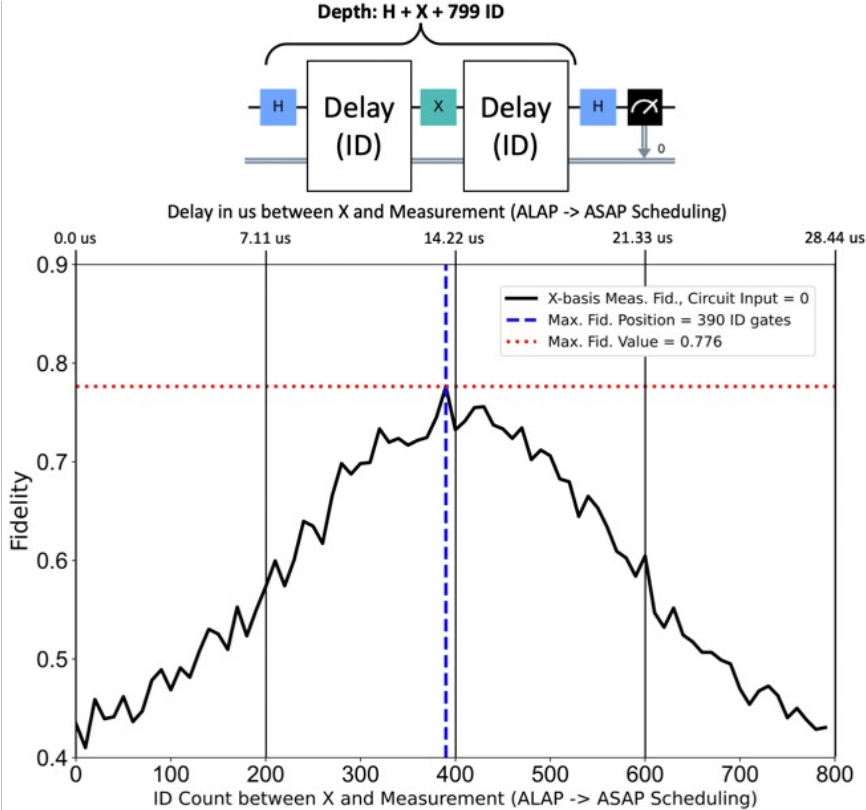


# Gate scheduling and insertion for noise mitigation

Error Mitigation in Quantum Computers through Instruction Scheduling. Smith, Ravi, et al. ACM TQC. 2022

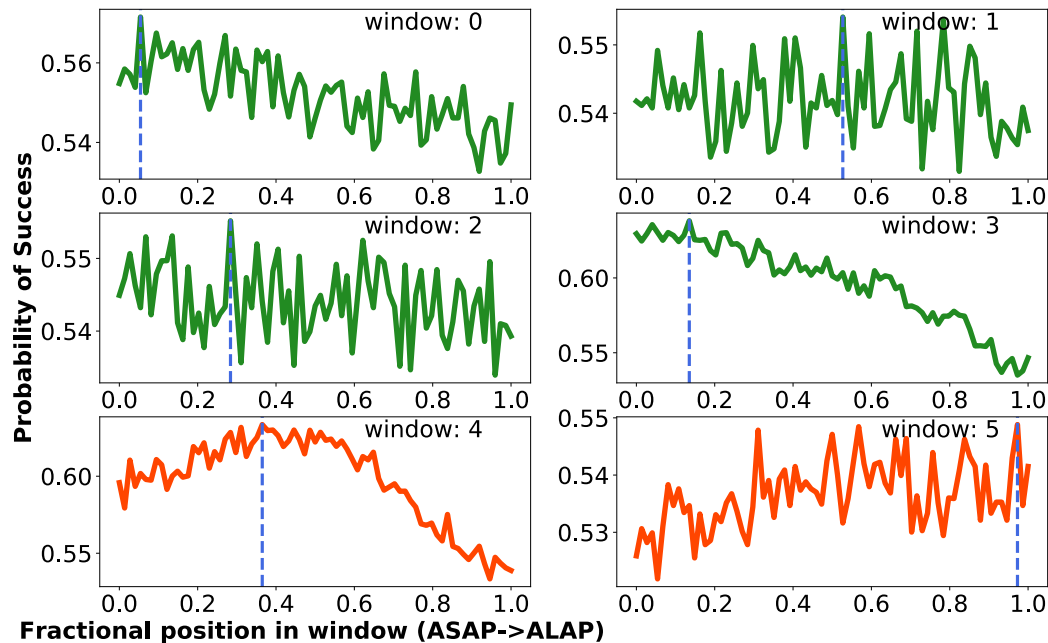


Noise modeling is critical to study new error mitigation techniques!

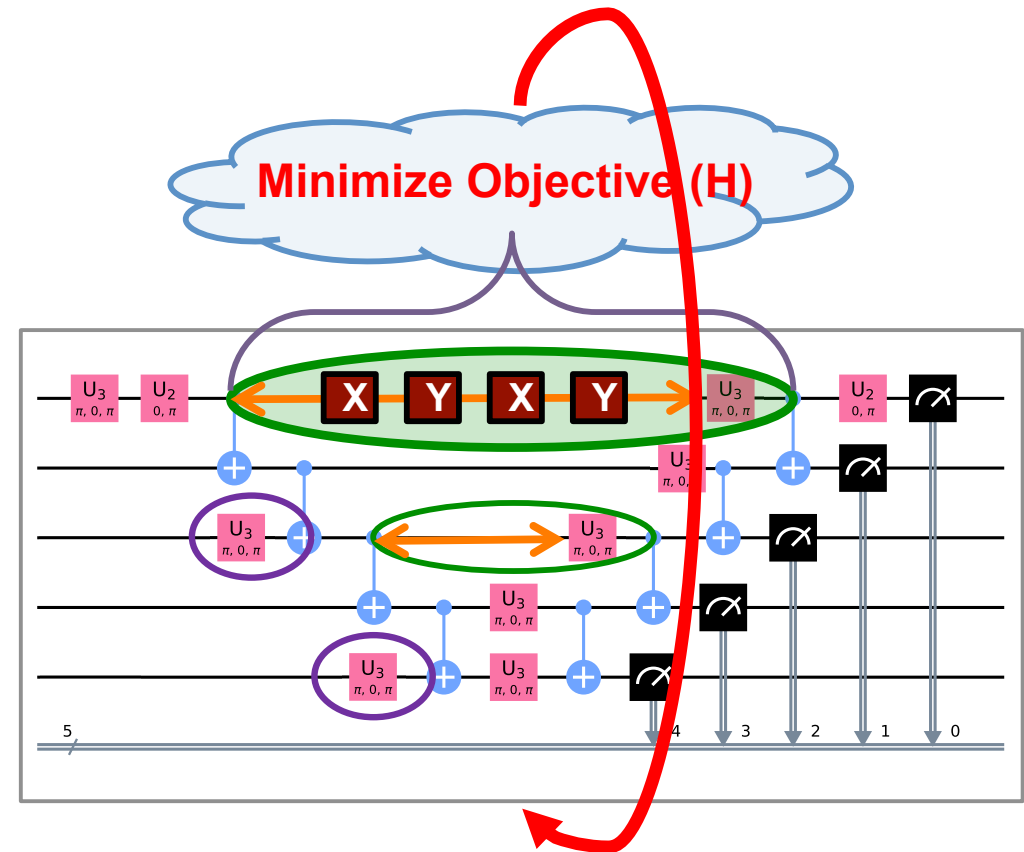


# Optimizing VQA noise mitigation 'in the loop'

VAQEM: A Variational Approach to Quantum Error Mitigation. [Ravi et al.](#), HPCA '22



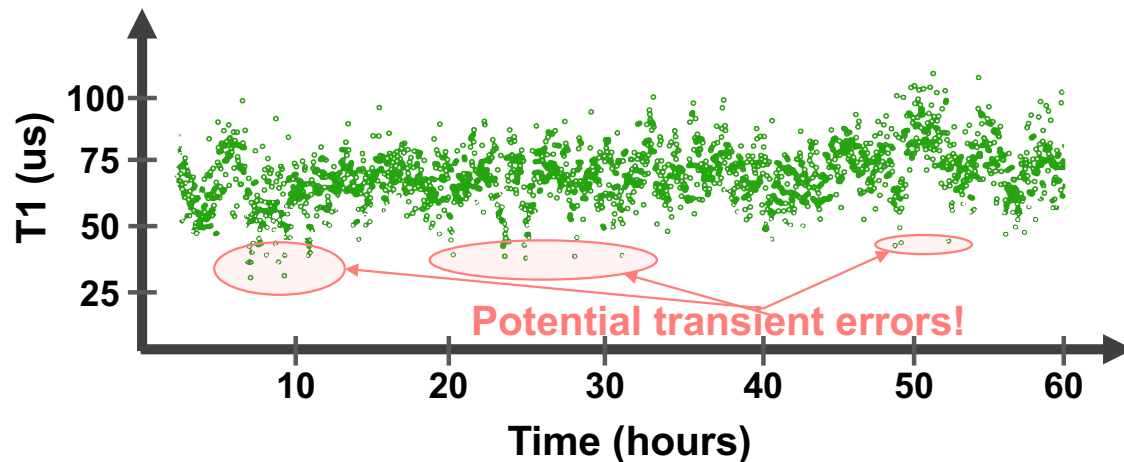
Gate scheduling / DD seq. insertion



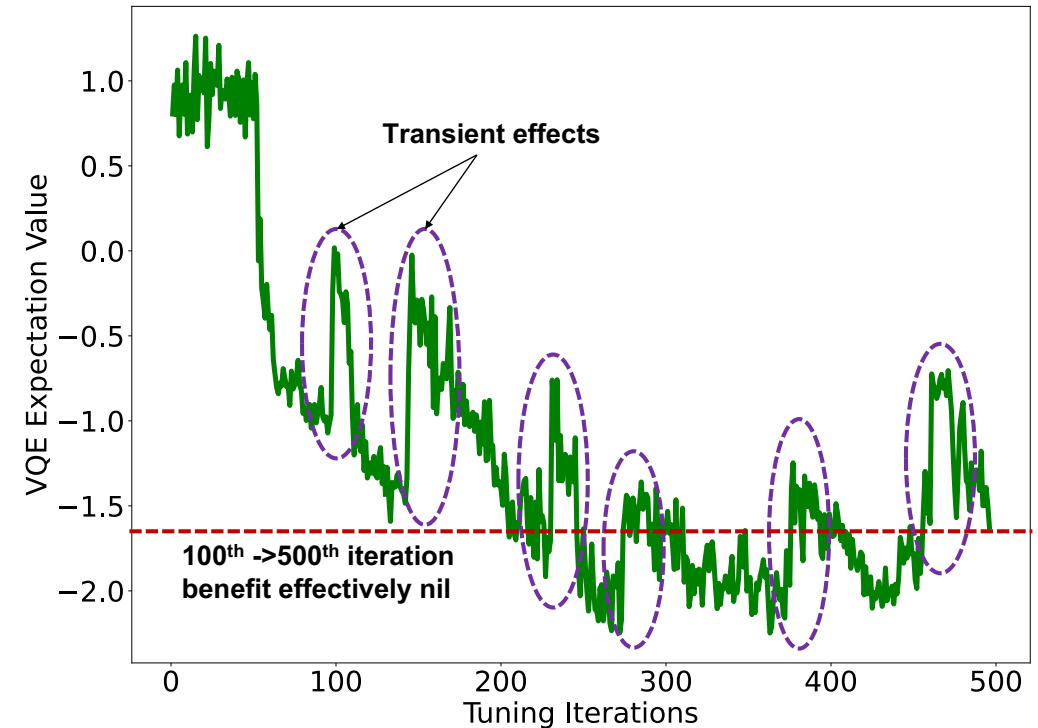
**Noise models don't capture complex interactions but can help strategize and reduce search space for dynamic optimization schemes!**

# Mitigating transient noise effects in VQA

QISMET: Navigating the Dynamic Noise Landscape of Variational Quantum Algorithms. [Ravi et al.](#), ASPLOS '23

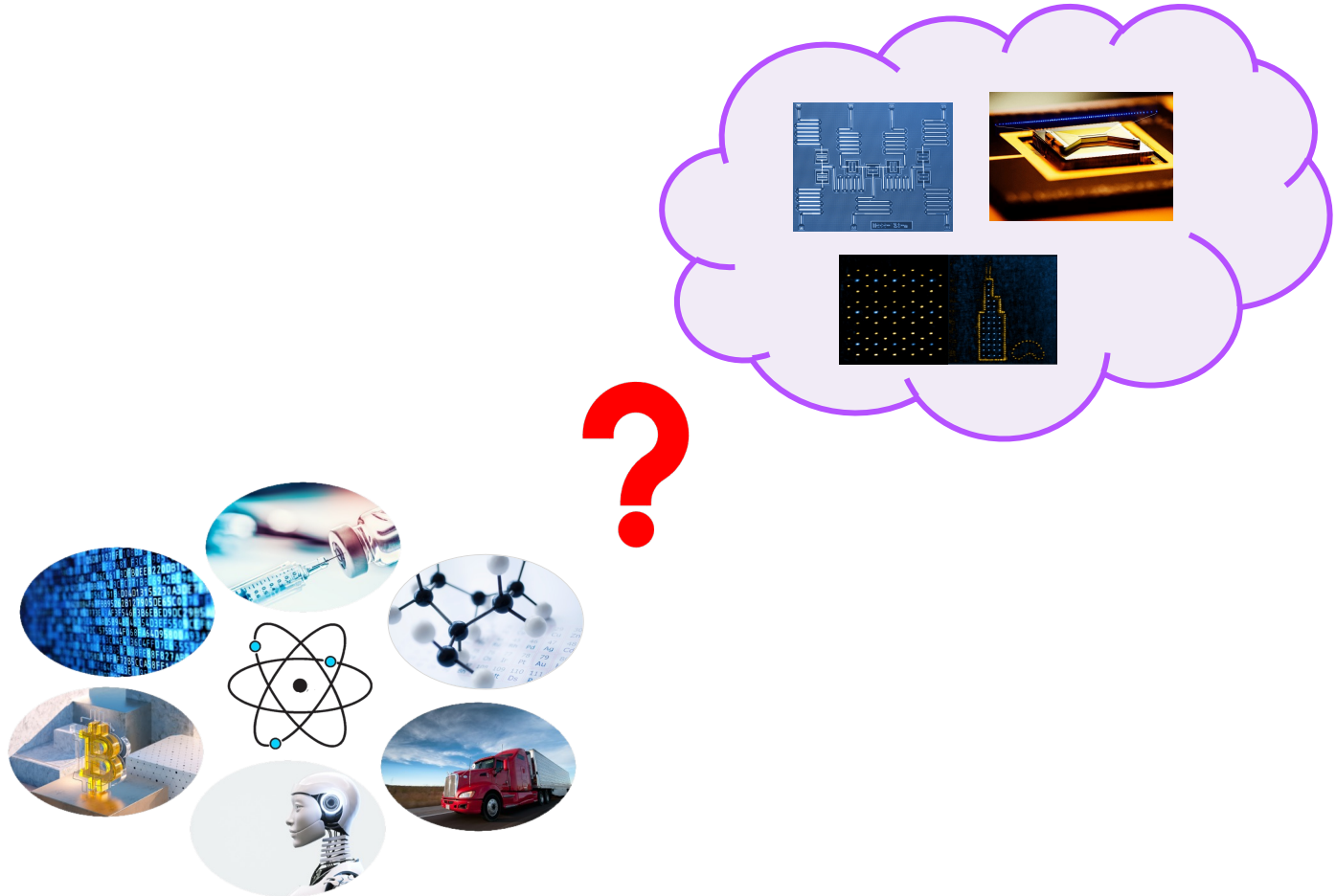


JJ Burnett, et al. Decoherence benchmarking of superconducting qubits. NPJ Quantum 2019

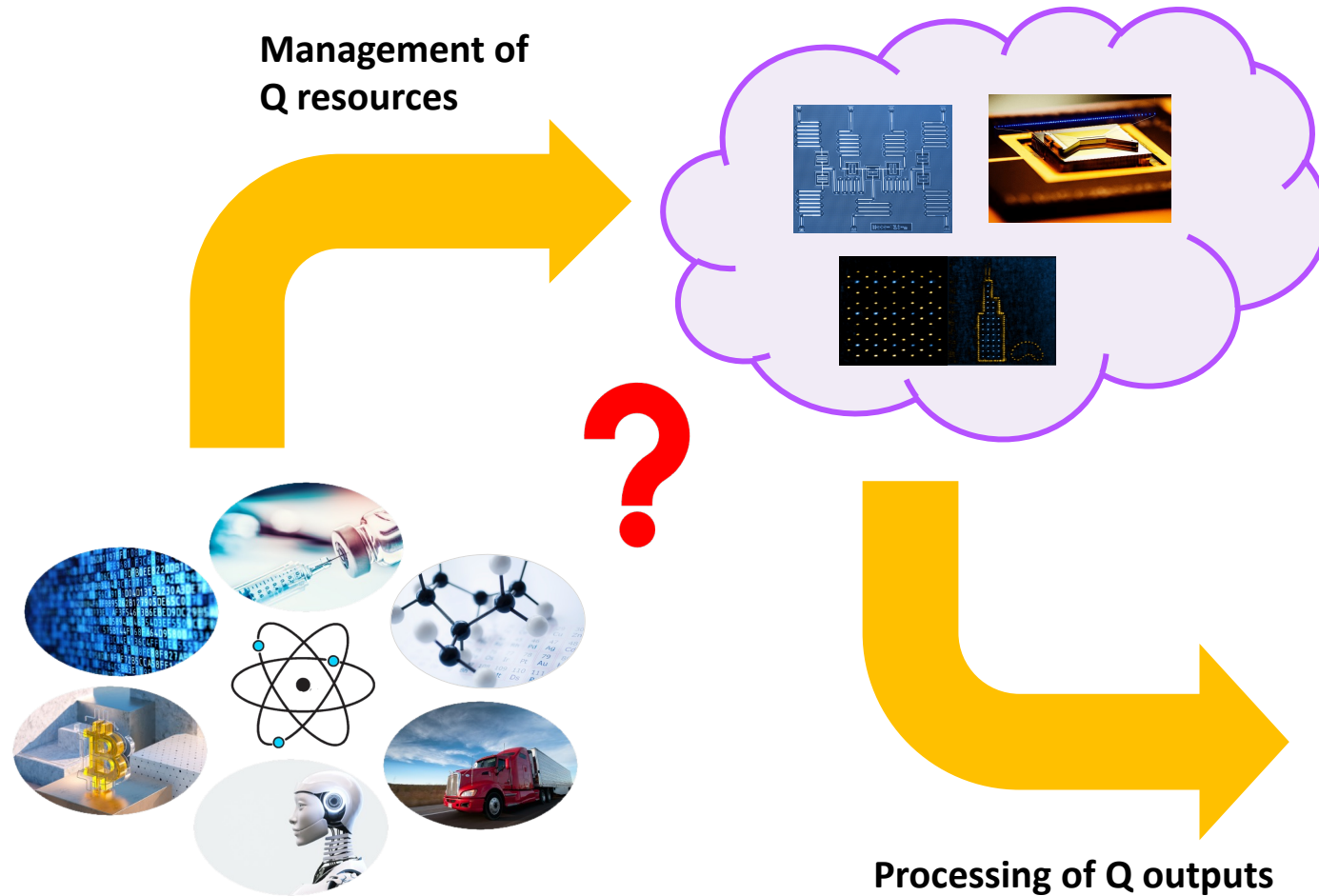


**Noise models are poor for transient noise but profiling can help learn thresholds for dynamic optimization schemes!**

# #3) Resource modeling in the cloud



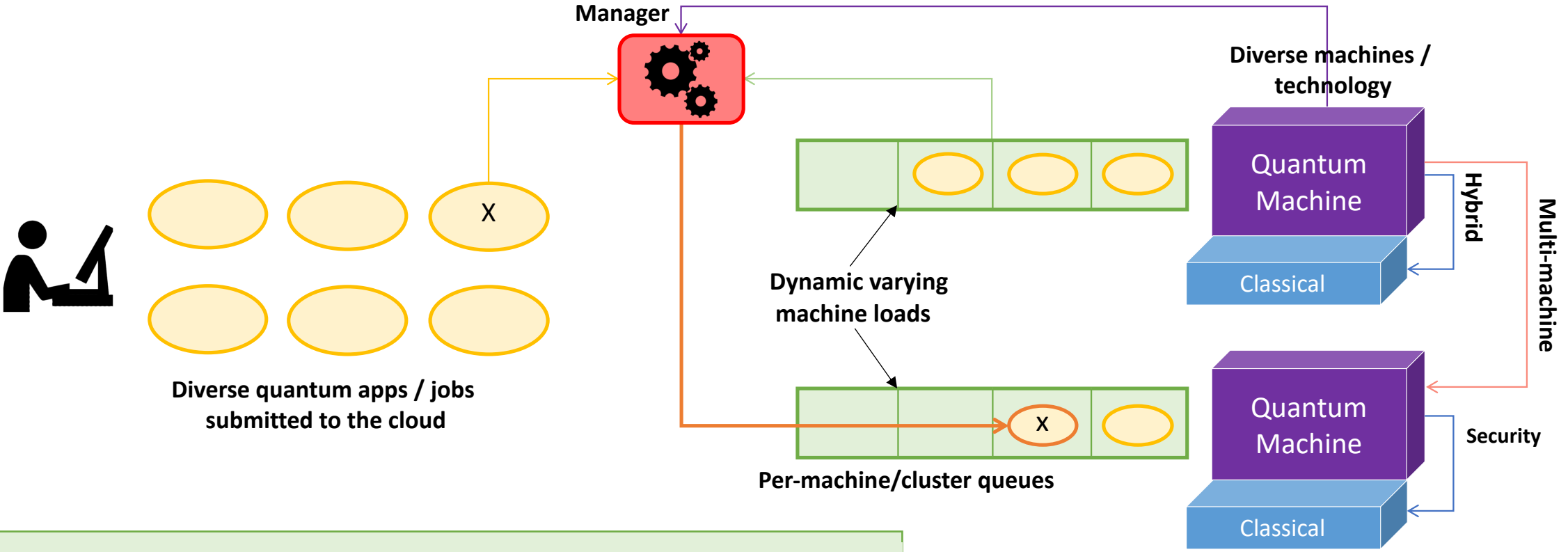
# #3) Resource modeling in the cloud





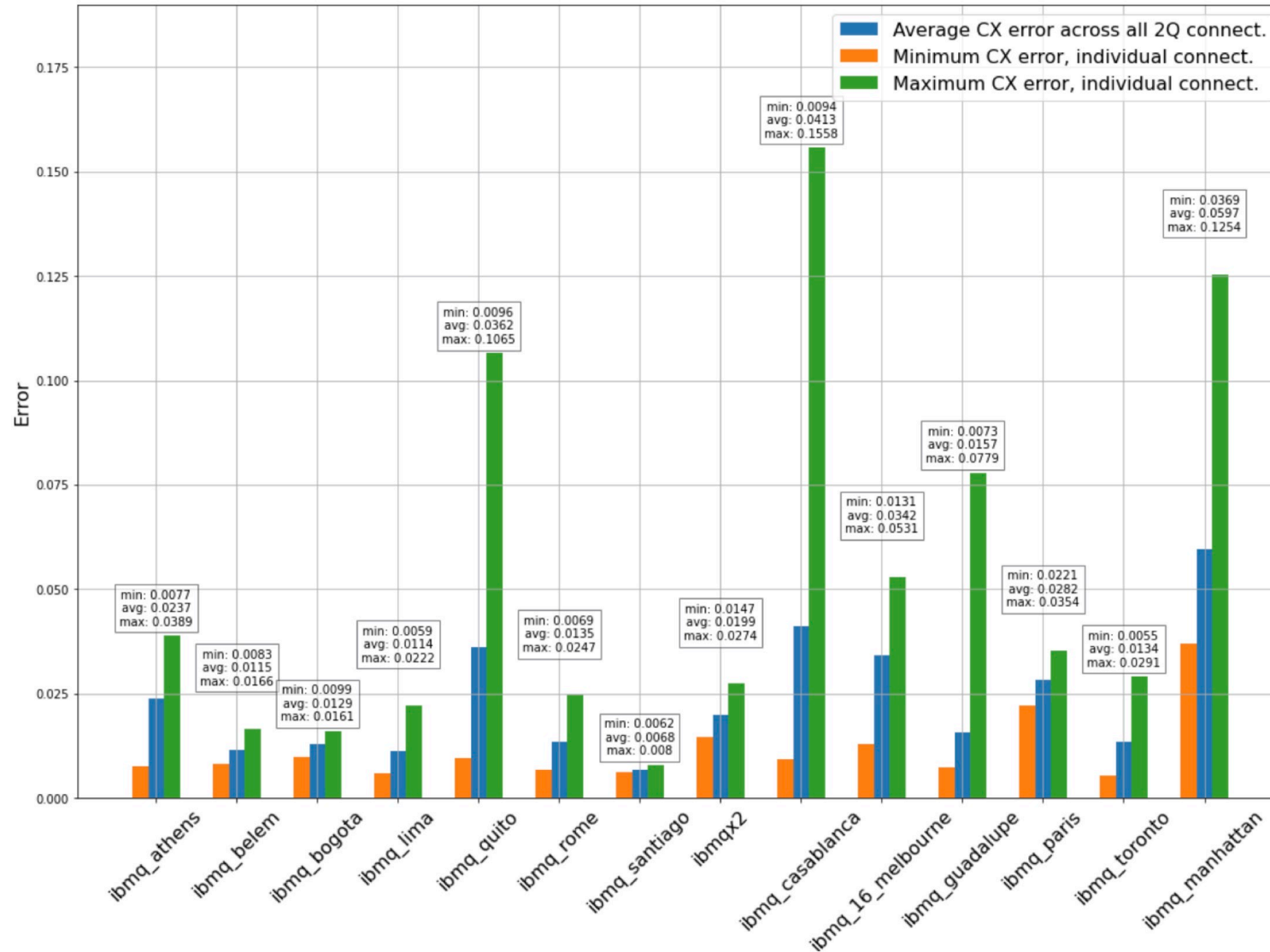
# Managing cloud resources

Best Q machines for app? Best hybrid systems for app? Throughput vs fidelity? FT + NISQ? QOS guarantees?

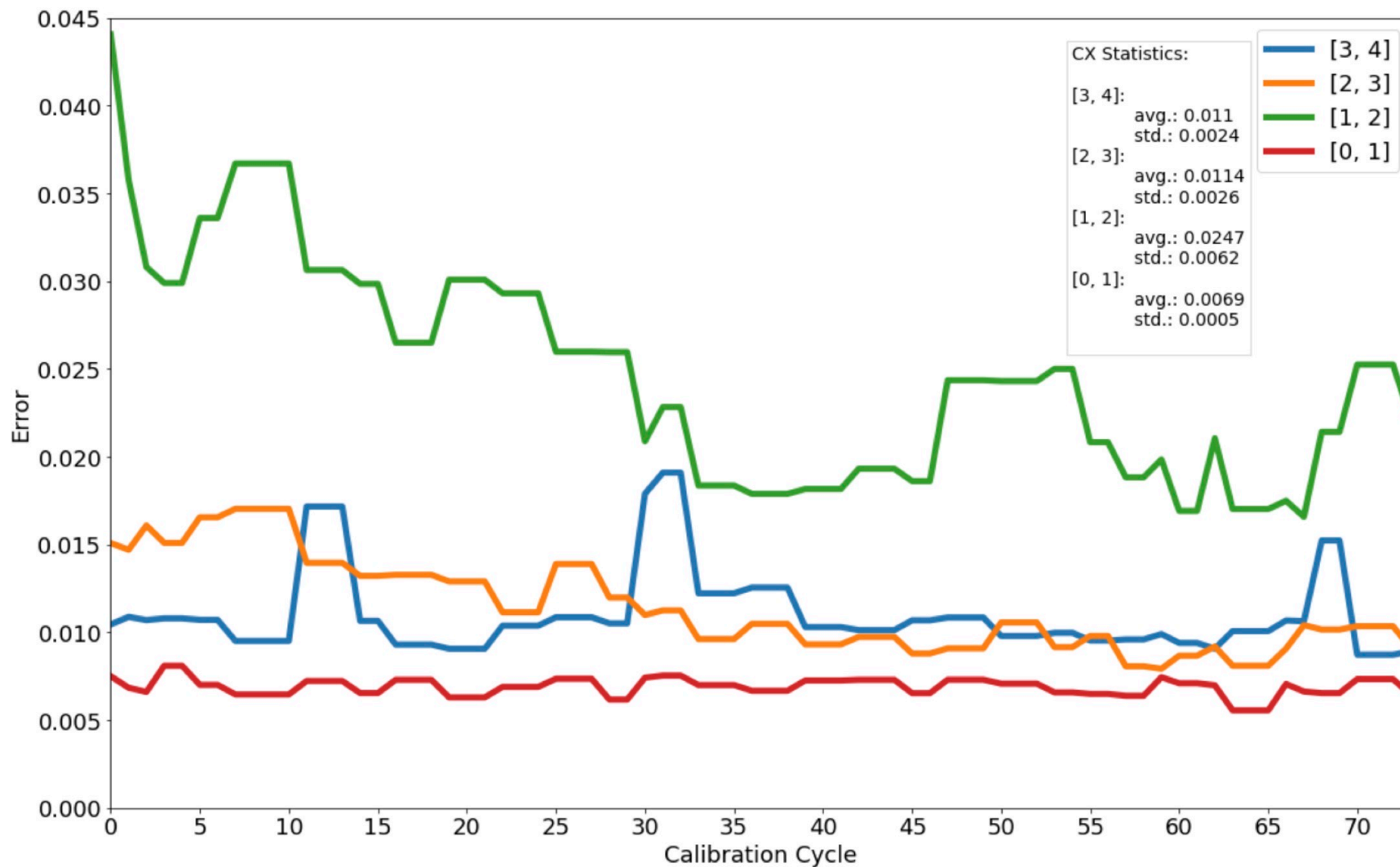


Quancorde: Boosting fidelity with Quantum Canary Ordered Diverse Ensembles. [Ravi et al., ICRC '22](#) + Patent filed  
 Adaptive job and resource management for the growing quantum cloud. [Ravi et al., QCE '21](#) + Patent filed  
 Quantum Computing in the Cloud: Analyzing job and machine characteristics. [Ravi et al., IISWC '21](#)

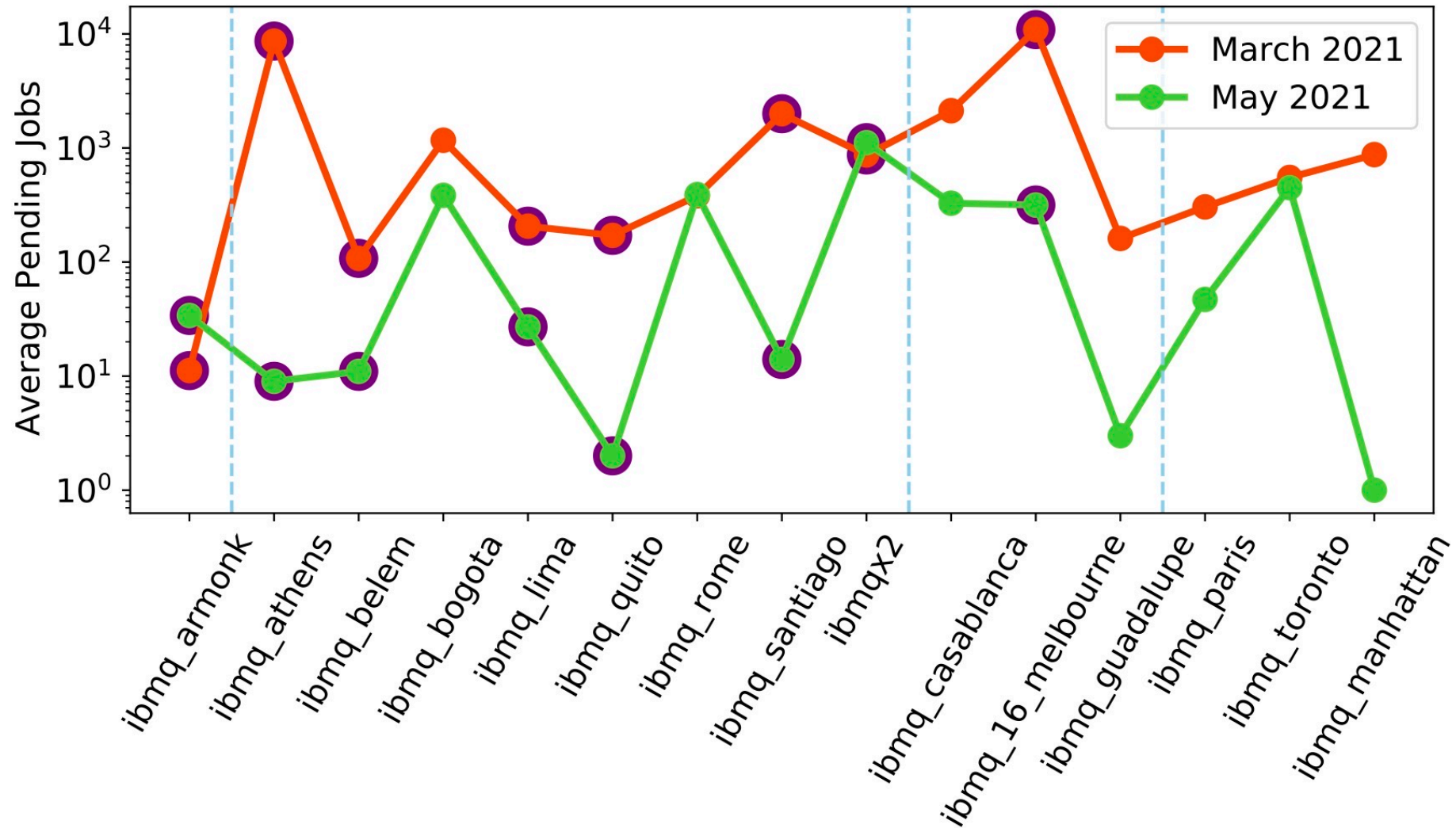
# Quantum Cloud: Error diversity (Spatial)



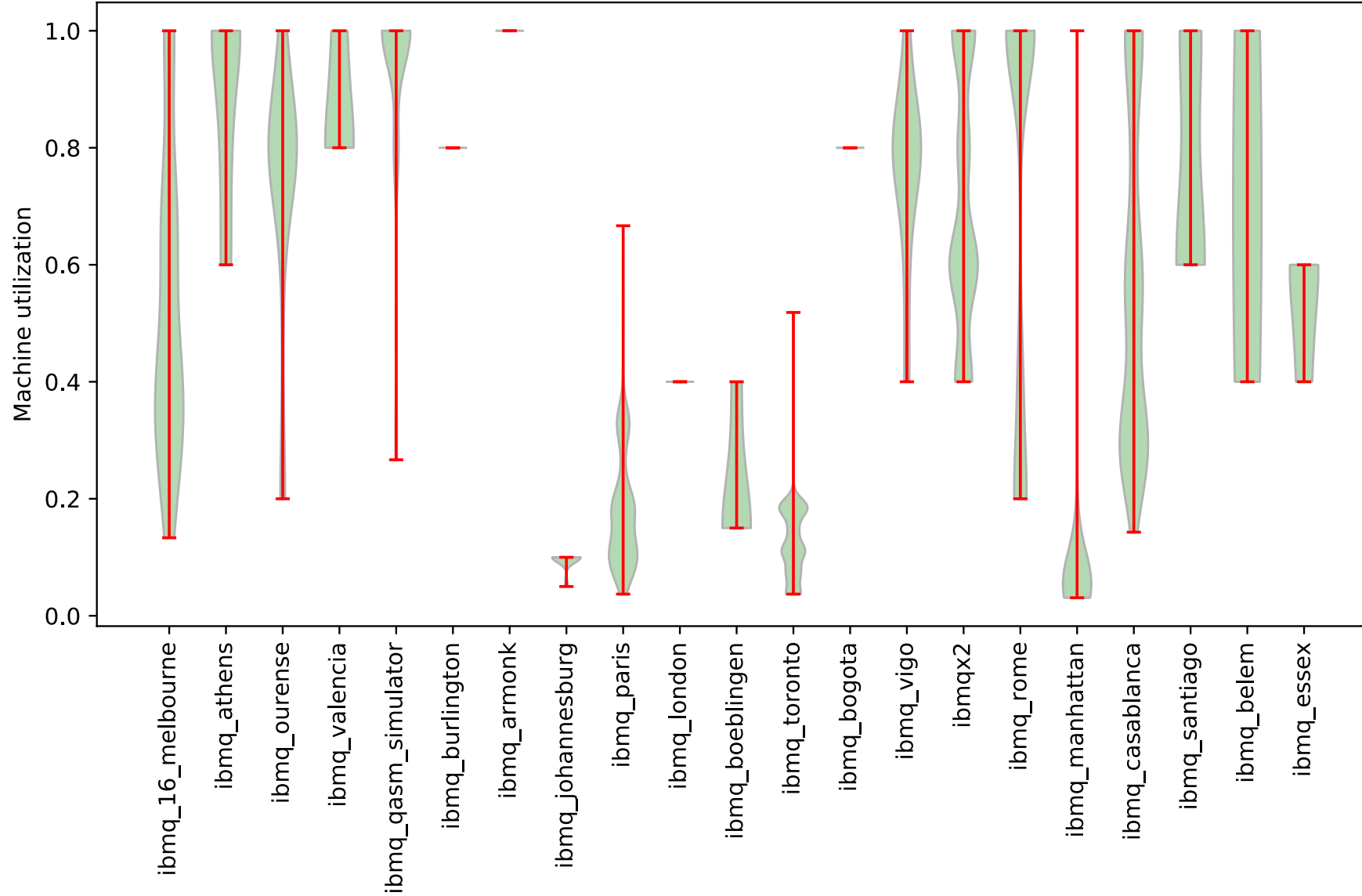
# Quantum Cloud: Error diversity (Temporal)



# Quantum Cloud: Machine loads and wait times



# Quantum Cloud: Machine utilization





# Bonus: Cryogenic chip design

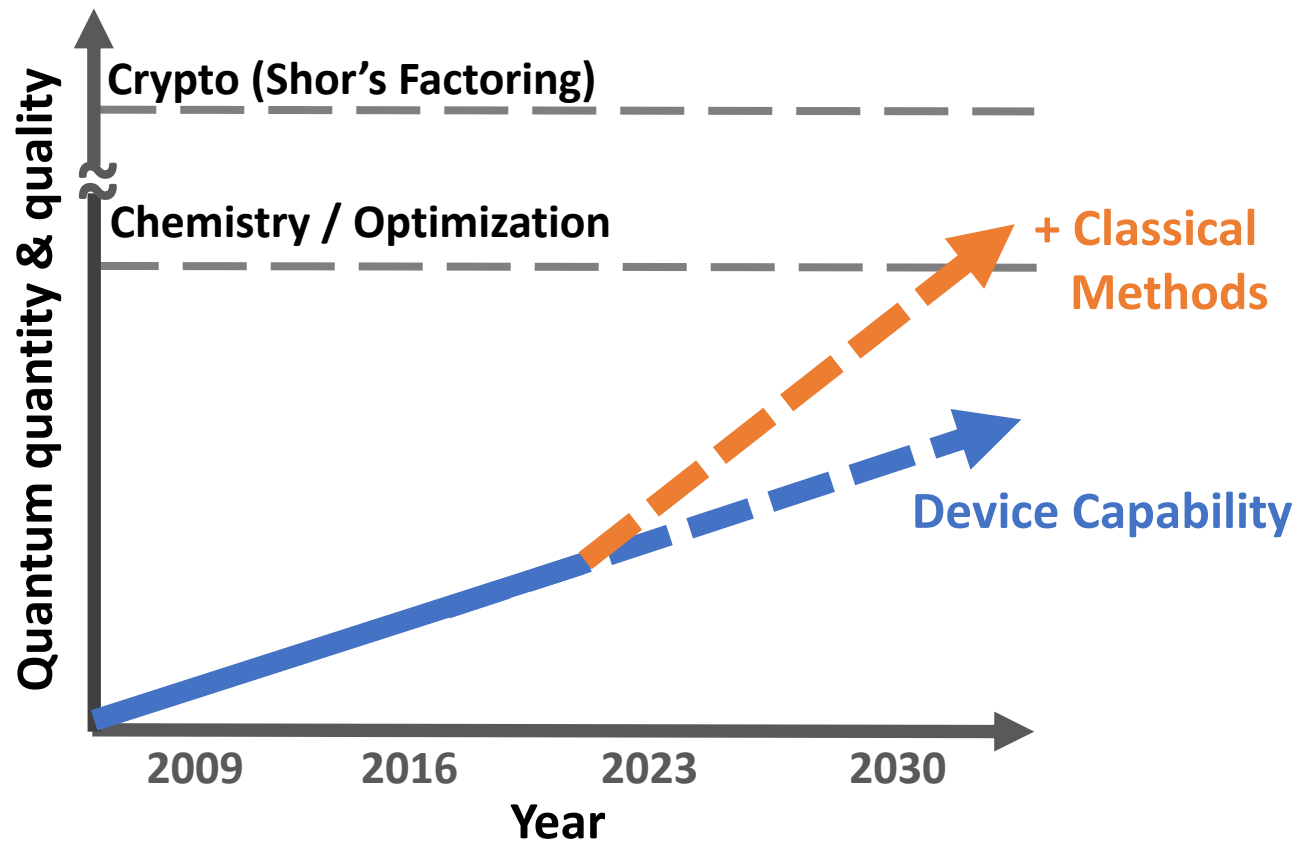
## IBM scientists cool down the world's largest quantum-ready cryogenic concept system

Project Goldeneye pushes the limits of low-temperature refrigeration while laying the groundwork for the quantum industry's ability to scale to larger experiments.

<https://research.ibm.com/blog/goldeneye-cryogenic-concept-system>



# Bridging the quantum gap: Classical computing approaches



1. PL and Compilation
2. Computer Architecture
3. Classical simulation
4. High performance computing
5. Cryogenic hardware design
6. Noise modeling and Optimization
7. Multi-chip / distributed computing
8. Cloud resource modeling and management



*applied sciences*



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## Current Developments in Quantum Hybrid Systems

### Guest Editors

Prof. Dr. Frederic Chong, Dr. Gokul Subramanian Ravi



### Deadline

20 November 2023

# Special Issue

[mdpi.com/si/173742](https://mdpi.com/si/173742)

Invitation to submit 68



Thank you!  
gsravi@umich.edu

Project	Arxiv	Software
CAFQA	<a href="https://arxiv.org/abs/2202.12924">arXiv:2202.12924</a>	<a href="https://github.com/rgokulsm/CAFQA">github.com/rgokulsm/CAFQA</a>
VAQEM	<a href="https://arxiv.org/abs/2112.05821">arXiv:2112.05821</a>	<a href="https://github.com/rgokulsm/VAQEM">github.com/rgokulsm/VAQEM</a>
QISMET	<a href="https://arxiv.org/abs/2209.12280">arXiv:2209.12280</a>	Coming Soon
VarSaw	<a href="https://arxiv.org/abs/2306.06027">arXiv:2306.06027</a>	<a href="https://github.com/siddharthdangwal/VarSaw">https://github.com/siddharthdangwal/VarSaw</a>
QCloud	<a href="https://arxiv.org/abs/2203.13121">arXiv:2203.13121</a>	<a href="https://github.com/rgokulsm/QuantumQueue">https://github.com/rgokulsm/QuantumQueue</a>