Accelerated Materials Discovery

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Materials discovery involves small amounts of data: Uncertainties, Multicomponent, vast search space

Search for better Pb-free piezoelectrics



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Adaptive Learning for materials discovery



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Adaptive Learning for materials discovery



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Bayesian Global Optimization large scale computational tasks OR experiments





Design of Experiments (DOE)

Guide choice of experiments in an efficient manner

- Factors X1, ... Xk \rightarrow Y
- Designs

Randomized Complete Block Factorial: Full, Fractional, Composite : Box-Behnken Random Latin HyperCube

Mx **Optimal Design :** Find sample to optimize Y $\begin{aligned} \mathbf{y}_{i} &= \mathbf{f}_{\theta} \left(\mathbf{x}_{i} \right) \neq \mathbf{e}_{i} \\ \mathbf{y}_{i} &= \theta^{\mathsf{T}} \mathbf{x}_{i} \neq \mathbf{e}_{i} \end{aligned} \quad \begin{aligned} & \text{Var} \left(\theta \right) = \sigma^{2} \left(\mathbf{X}^{\mathsf{T}} \mathbf{X} \right)^{-1} \quad \text{Var} \left(\mathbf{y}_{i} \right) = \sigma^{2} \left(\mathbf{X}^{\mathsf{T}} \mathbf{X} \right)^{-1} \mathbf{x}_{i} \\ & \text{Optimal design Objective} \end{aligned}$ minimize trace $\{M_X^{-1}\}$ A-optimal minimize $\{\det M_X\}^{-\frac{1}{p}}$ D-optimal minimize max eigenvalue $\{M_X^{-1}\}$ Santner et al. ' 2003 E-optimal UNCLASSIFIED minimize max var { $\mathbf{f}(\mathbf{x})$ }, $\mathbf{x} \in R$ G-optimal Operated by Los Alamos National Security, LLC for NNSA minimize trace {MM_X⁻¹} I-optimal

Los Alamos Experimental design via Bayesian Optimization $(f(\mathbf{x}))$ \max $\mathbf{x} \in \mathcal{A} \subset \mathbb{R}^d$ Step 1: Estimate objective $y_i = f(\mathbf{x}_i) + \varepsilon_i$ $\mathcal{D}_{1:t} = \{\mathbf{x}_{1:t}, f(\mathbf{x}_{1:t})\}$ Data $\mu(\mathbf{x}_3) + \sigma(\mathbf{x}_3)$ $\mu(\mathbf{x}_3)$ $P(f|\mathcal{D}_{1:t}) \propto P(\mathcal{D}_{1:t}|f)P(f)$ $\mu(\mathbf{x}_1)$ $\mu(\mathbf{x}_2)$ $\mu(\mathbf{x}_2) - \sigma(\mathbf{x}_2)$ Gaussian $f(\mathbf{x}) \sim \mathcal{GP}(m(\mathbf{x}), k(\mathbf{x}, \mathbf{x}'))$ $\mu(\mathbf{x}_1) - \sigma(\mathbf{x}_1)$ process O'Hagan, 70 \mathbf{X}_1 \mathbf{X}_2 \mathbf{X}_{2} $P(f_{t+1}|\mathcal{D}_{1:t}, \mathbf{x}_{t+1}) = \mathcal{N}\left(\mu_t(\mathbf{x}_{t+1}), \sigma_t^2(\mathbf{x}_{t+1})\right)$ Posterior



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Step 2: Sample with utility function $\mathbf{x}_t = \operatorname{argmax}_{\mathbf{x}} u(\mathbf{x} | \mathcal{D}_{1:t-1})$

actual — predicted —

Choose next point to maximize uncertainty:



(150 data points, 3 in training set.)

Choose next point to minimize uncertainty:







Utility functions: encoding decision criteria

- Expected Improvement → EGO (Kushner, Mockus, Jones)
- Expected Quantile Improvement (Picheny)
- Lower or Upp. Confidence Bounds (Cox and Johnson, Srinivas)
- Sequential Kriging Optimization (Huang)
- Knowledge Gradient (Powell, Frazier)
- Mean Objective Cost of Uncertainty (Yoon, Xian, Dougherty)
- Maximum Variance



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N_{train} = End 3

Results

N_{train} = sample 3

$$MAE = \frac{\sum_{i=1}^{n} |y_i - \mu|}{n}$$





Choose sample with largest "Expected Improvement": $x_i = \operatorname{argmax}_x [E(I(x))]$

Limiting cases:

Small σ $E \rightarrow \hat{y} - f_{max}$ Choose \hat{y} better than best-so-far f_{max} Large σ $E \rightarrow \sigma$ Exploitation (local, utilize model)Large σ $E \rightarrow \sigma$ Choose \hat{y} with largest uncertainty σ Large σ $E \rightarrow \sigma$ Choose \hat{y} with largest uncertainty σ Large σ $E \rightarrow \sigma$ Choose \hat{y} with largest uncertainty σ Large σ $E \rightarrow \sigma$ Exploration (global, improve model)





Mean Objective Cost of Uncertainty

Identify experiment expected to maximally reduce MOCU one step ahead

Assume cost function, $g(\theta; c)$

- heta Unknown parameters
- *c* characterizes an experiment e.g. material composition

If θ known, then the optimal material would be $c'_{\theta} = \arg \min g(\theta; c)$

If θ unknown, then the robust material is

be
$$c_{\theta} = \underset{c \in C}{\arg\min g(\theta; c)}$$

 $c'' = \underset{c \in C}{\arg\min E_{\theta}[g(\theta; c)]}$

Expected Loss in using
robust instead of optimal $MOCU = E_{\theta}[g(\theta; c'_{\theta}) - g(\theta; c'')]$ Property of optimal
material at state θ Property of optimal
material across all θ

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Dehghannasiri, R., Yoon, B-J., and E. R. Dougherty, "Optimal Experimental Design for Gene Regulatory Networks in the Presence of Uncertainty," *IEEE/ACM Transactions on Computational Biology and Bioinformatics*, 2016

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MOCU: Selection of next experiment

- Experiments C1, C2, C3, etc Outcomes: C_1, C_2, C_3
- Remaining after outcome c_i $MOCU = E_{\theta | Ci = c_i} [g(\theta; c'') - g(\theta; c'_{\theta})]$
 - Conditional distribution $f(\theta|Ci = c_i)$ Using Bayes, obtain $f(c|\theta)$

Expected remaining MOCU given that experiment c_i undertaken: $MOCU_i = E_{c_i} E_{\theta | Ci = c_i} [g(\theta; c'') - g(\theta; c'_{\theta})]$ $c_i^* = \underset{i \in 1,..n}{\operatorname{arg min}MOCU_i}$









Optimal experimental design for materials discovery

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Problem: Minimize energy dissipation by selecting optimal dopants in as few experiments as possible





Use physics based model as surrogate for objective:

$$g(h,\sigma,c;\mathbf{b}) = \max\left(\frac{1}{(b_1h+b_2\sigma+b_3h\sigma+b_4)c+b_5h+b_6\sigma+b_7h\sigma+b_8},0\right),$$



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Active learning loop





Comparison with several strategies





Optimize codes: LED structures for highest efficiencies at high currents





b

Compositi

Examples Use theory with data Experiments Strategy: Ti₅₀ Ni_{50-x-y-z} Cu_x Pd_y Fe_z gr. R. P. ADVANCED MATERIALS COMMUNICATION Total possibilities: 800,000 (22 known) Materials Discover 14 **Target: Minimize Thermal Hysteresis** Accelerated Discovery of Large Electrostrains in BaTiO₃-Phase diagrams Features Landau theory **Based Piezoelectrics Using Active Learning** Augment dataset Ti₅₀Ni $(Ba_{100-x-y}Ca_xSr_y)(Ti_{100-u-y}Zr_uSn_y)O_3$ Bayesian learning Cycle1 Cycle6 Predict new phase boundaries 60 Largest electrostrain Feedback from experiments: augmented dataset with 4 new alloys Perform experiments Electric field (kV/cm) Training data Trade-off % ZT-xBC1 strain - Exploitation Best in the training data 36 experiments # Iterations 14 with superior properties 30 Xue et al., Nature Comm., 2016 Yuan et al., Advanced Materials, 1702884 2018 Temperature (°C) Xue et al., PNAS, 2016

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Computations

Predict new materials

Multi- fidelity data

Ruddlesden-Popper Phases lower accuracy accuracy cheaper p-AlGaN comparable to GaN:Mg with fewer Applied Materials Density group theory informatics functional theory p-AlGaN expensive higher accuracy undoped Structural Energetic stability Chemical InGaN:Si criterion InGaN well criterion discovery expensive undoped n-GaN d Build BBU distortio Structural libraries Compute energies of structure (In)GaN barrier Bayesian analysis mode subspace Evaluate properties and descripto GaN:Si Recursive partitioning Enumerate maxima and minimal space Principal component analy a Contours: Number of HSE06 Bandgap Training Data Points (n_e) Sapphire Bandgap Training Data Points (n_c) 0.45 200 195 0.40 190 Quantum **APSYS** 140 185 0.35 130 180 Efficiencies code 175 P5 0.30 170 165 0.25 160 best LED 155 0.20 Number of PBE 150 of the 145 0.15 140 135 0.10 130 50 Active learning step 50 55 66 65 77 80 80 80 90 25 35 40 45 Leduc et al., Sci. Rep, 2016, APL 2017 $(n_c - n_e)$ Balachandran et al., Nature Comm., 2017 Pilania et al., Computational Materials Sci, 2017 os Alamos UNCLASSIFIED 2016 Materials for the Future NATIONAL LABORATORY

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Accelerate codes

Example: Find NiTi alloy with lowest hysteresis



Search space of multicomponent alloy ~800K 22 training samples (.003%) with measured ΔT

$$x \le 20\%, y \le 5\%, z \le 20\%$$

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$$50 - x - y - z \ge 30\%$$



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 Image: Image:

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Knowledge:

- Transition temperatures influenced by valence electron concentration
- Hysteresis influenced by atomic size
- Relative stability influenced by changes in electron number

Features:

Valence electron number Radii: metallic, Clementi, Zunger Electronegativity Pettifor Chemical scale



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Cycle1



Adaptive Design for Alloy Discovery



Feedback from experiments: augmented dataset with 4 new alloys

Xue et al., Nature Comm., 2016



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Experiments



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Material Performance for Synthesized Alloy



TABLE I | Five new best alloys, which were found in iterations 6 and 7, amongst 14 with the lowest ΔT . From a total of 9 iterations, which resulted in 36 new alloys, 14 had a ΔT smaller than 3.15 K, the lowest in the original training set of 22. Transformation temperature is given by the endothermic peak in the DSC curve.

Iterati	ons Composition	$\Delta T (K)$	Transformation temperature (K)
6	${ m Ti}_{50.0}{ m Ni}_{46.8}{ m Cu}_{0.9}{ m Fe}_{2.0}{ m Pd}_{0.3}$	2.64	289.95
6	${ m Ti}_{50.0}{ m Ni}_{44.2}{ m Cu}_{1.9}{ m Fe}_{3.8}{ m Pd}_{0.1}$	2.53	243.43
6	Ti _{50.0} Ni _{46.7} Cu _{0.8} Fe _{2.3} Pd _{0.2}	1.84	281.77
7	${ m Ti}_{50.0}{ m Ni}_{48.1}{ m Cu}_{0.2}{ m Fe}_{1.5}{ m Pd}_{0.2}$	2.09	301.86
7	$\rm Ti_{50.0}Ni_{46.5}Cu_{1.1}Fe_{2.2}Pd_{0.2}$	2.32	283.79

How good does the model have to be ?



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Piezoelectrics



Applications

- EST.1943 -

	Pi	ezoelectric Appli	cations	
	Automotive Spark Ignition Fuel Atomization Knock Sensors Tire Pressure Safety/Security Alarms Sound Systems Motion sensor Elow level sensor	Commercial Hydrophones Fans Production sensors Counters Security Robotics/Toys Game machine Massaging	Industrial Ultrasonic Cleaning Ultrasonic Welding Ultrasonic Machining Flaw Detection Pneumatic Valves Computers Ink Jet Printers	
4	Consumer Goods Telephone Ringers Speakers Humidifier Atomizers Smoke Detectors Automatic Lighting Security Systems Jewelry Cleaners	Medical Fetal Heart Monitors Blood Flow Diagnosis Flow Meters/Controls Insulin Pumps Vaporizors / Nebulizers Ultrasonic Surgery Ultrasonic Imaging	Disk Drive Keyboards Aerospace/ Defense Sonar Hydrophones Ring Laser Gyros	
LOS Alar				LDRD



Search for BaTiO3 based solid solutions with relatively large electrostrains





Figure of merit and target



Experiments - fabrication



Experimental Comparison of design strategies : Search for BaTiO3-based large electrostrains

MaRIE





Relative Figure of Merit





Comparing outcome to predictions





Comparison of BCT-BZT based piezoelectrics





Example: Importance of knowledge

Accelerated search for BaTiO₃-based piezoelectrics with vertical morphotropic phase boundary using Bayesian learning

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Approach





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NIS

Learning from theory + data

$x(Ba_1-mCa_m)TiO_3-Ba(Zr_nTi_1-n)O_3$

18%< m < 50%: 15% < n < 30%

(1200 phase diagrams)

•Features:

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 Order parameters: Polarization, Strain $\Delta V = V_T - V_R \quad U_T, U_R$

$$t_{f} = \frac{R_{A}^{\mathsf{T}} + R_{o}}{R_{B}^{\mathsf{R}} + R_{o}} \qquad r_{eff_{nucl}} = \frac{A_{enc_{T}}}{B_{enc_{R}}} \qquad r_{elec_{neg}} = \frac{A_{en_{T}}}{B_{en_{R}}}$$

Training data: 19 phase diagrams

$$\tau = f(\tau_{c}, a_{2}, a_{6}, .., p_{R}, p_{T})$$

Prior distribution subject to constraints









Data



Predictions/ synthesis from model + data



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Best in the training data: $Ba(Zr_{0.2}Ti_{0.8})O_3 - (Ba_{0.7}Ca_{0.3})TiO_3$

New Prediction: $Ba(Zr_{0.3}Ti_{0.7})O_3 - (Ba_{0.5}Ca_{0.5})TiO_3$



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Xue et al., PNAS, 2016





- No free lunch theorem ! (Wolpert, 98)
- Integrate physics models
- Guiding principles for different classes of problems (materials, ..)



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What Problem are we Trying to Solve?

- Plastics—synthetic polymers made from petrochemicals—have revolutionized our society.
- However, plastics are over-engineered for durability, and plastic pollution is now a scourge on our planet.
- We propose to help solve this problem with an *innovative process* to discover, design, and develop new biopolymers with improved functionalities, balancing durability with faster degradability in the environment.
- Use biology as a template for new chemistries.



The Plastic Lifecycle. Top: <u>Past</u>: Cradle to Grave. Plastic from petroleum is used for most packaging, but ends up in landfills or in the environment. Bottom: <u>Future</u>: Cradle to Cradle. Algae can be used to produce bio-based plastics. Along with improved recycling methods (e.g. P&G's Head & Shoulders shampoo bottle made from pelletized beach plastic) biodegradable compostable bioplastic can be broken down into basic molecules that can be captured and re-used as nutrients in agriculture.

APPROACH





- A model or recipe that will predict the synthesis conditions/chemistries to make **polymers with targeted performance** from the biology or chemistry routes with given confidence levels.
- A general approach that allows for efficient exploration of vast chemical spaces and synthesis conditions using ML to guide chemistry and/or biology based synthesis routes
- Novel, degradable biopolymers (with a favorable combination of other properties, e.g., breathability, durability, mechanical strength) synthesized via the proposed biosynthesis route