

# Mapping sea-level change in time, space, and probability

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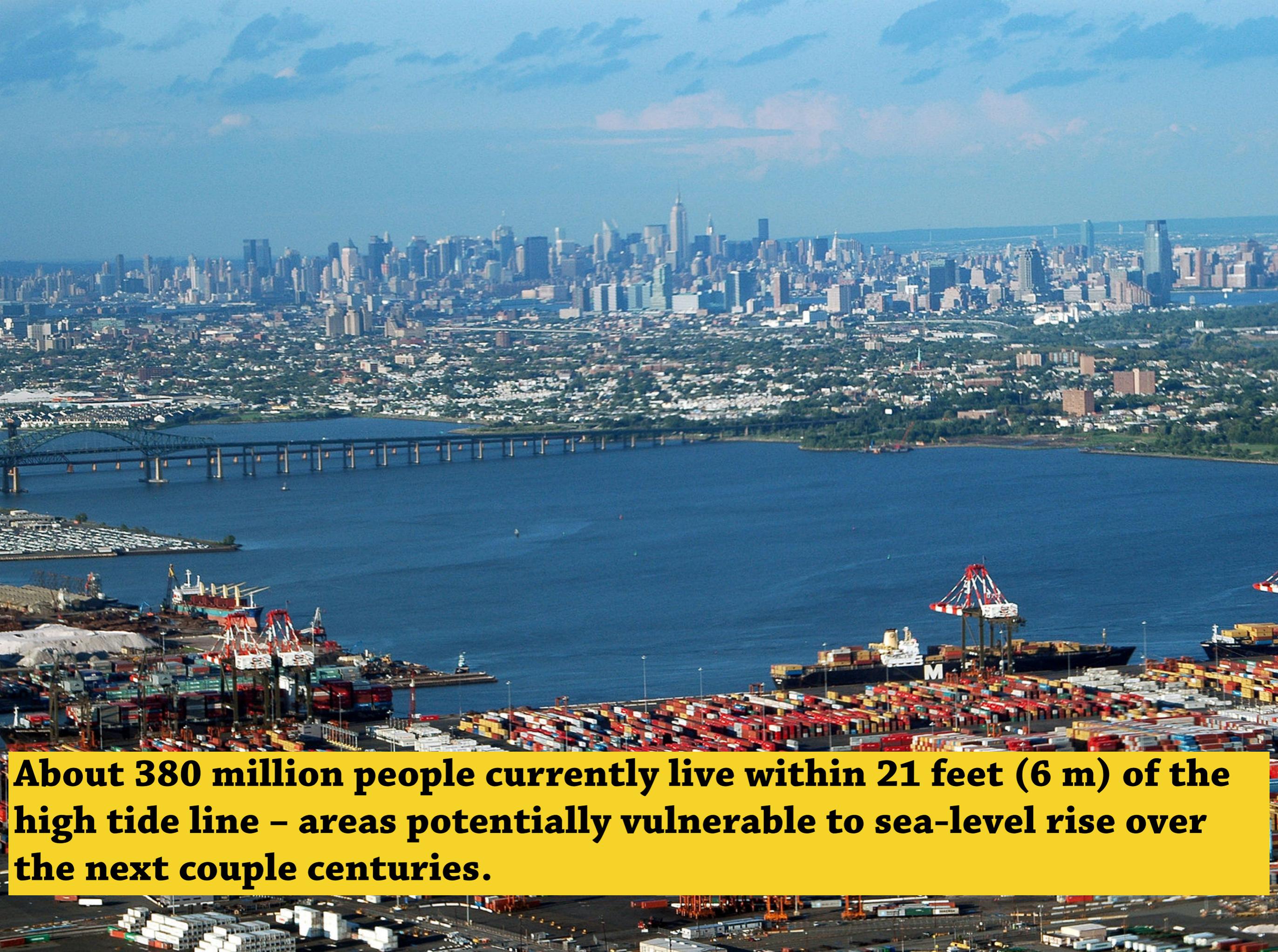
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Atmospheric Sciences



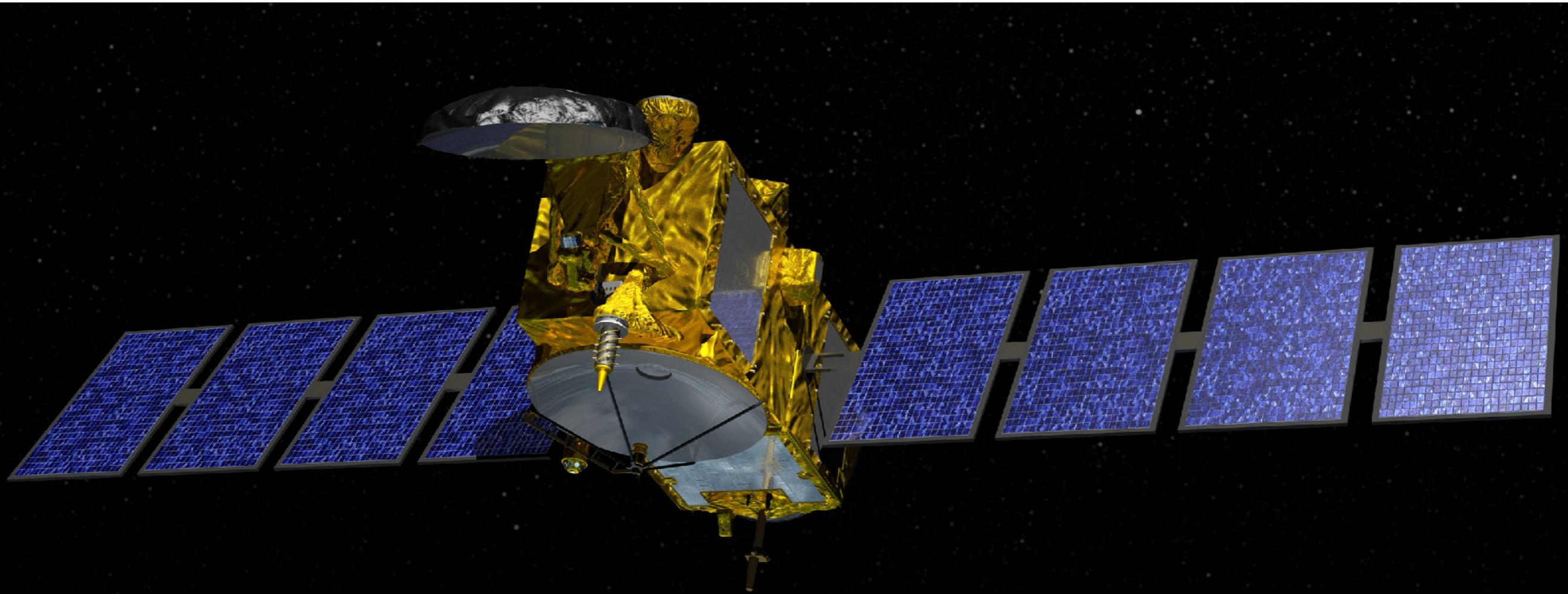
**New York Scientific Data Summit  
June 12, 2019**



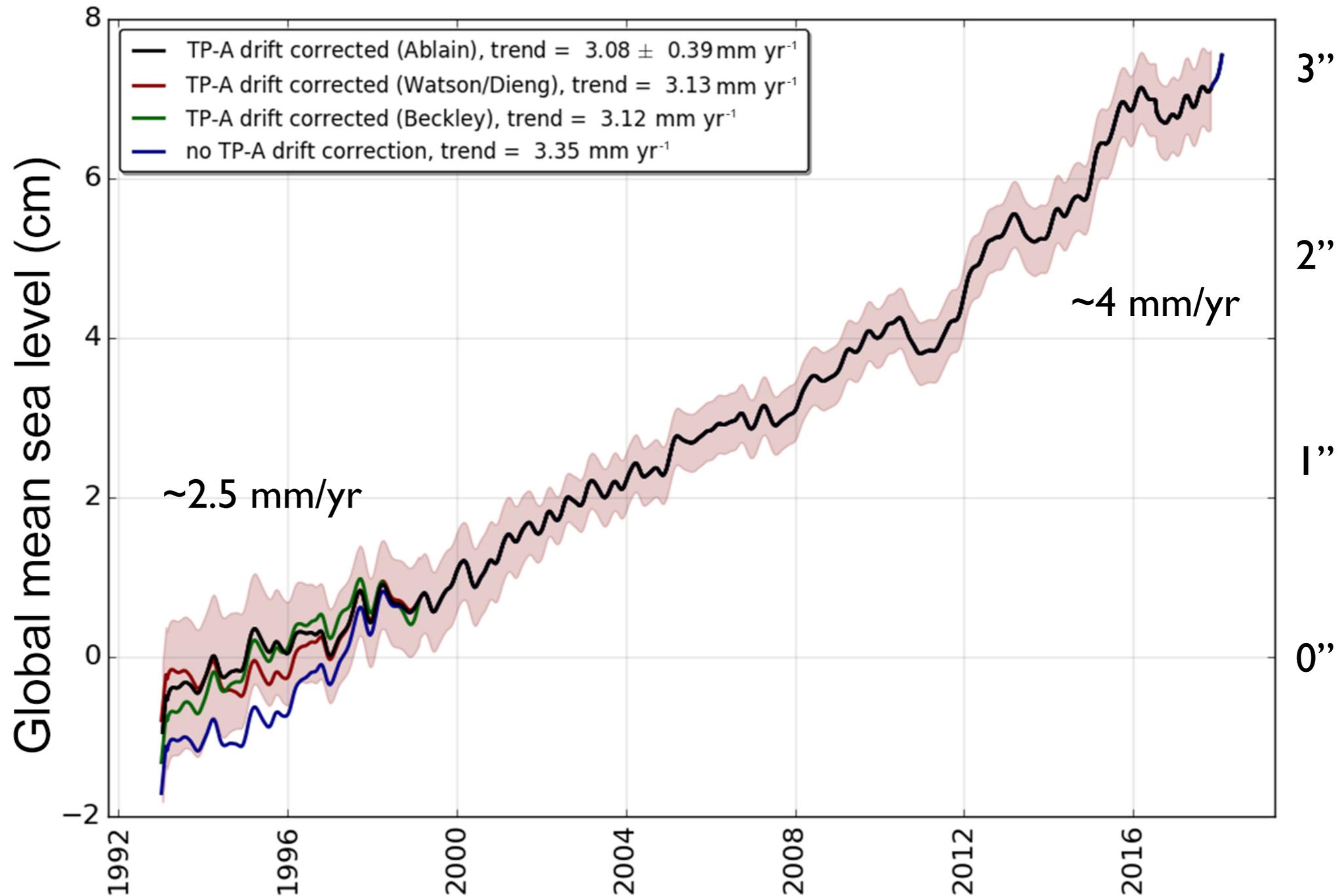


**About 380 million people currently live within 21 feet (6 m) of the high tide line – areas potentially vulnerable to sea-level rise over the next couple centuries.**

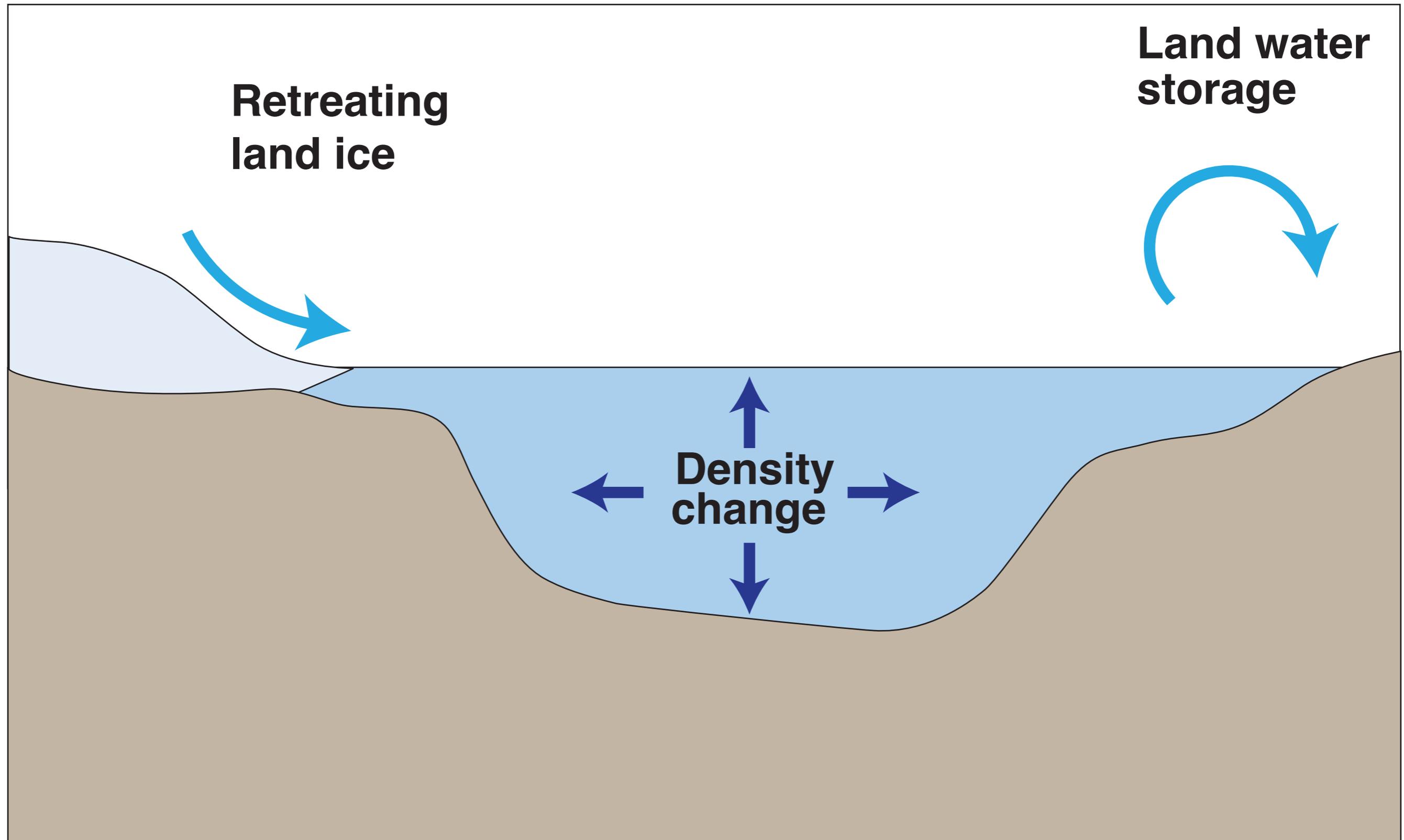
Since the early 1990s, scientists have measured changes in the height of the sea surface using satellite-borne radars.



# Satellite altimetry shows us that global average sea level is rising at an accelerating rate.

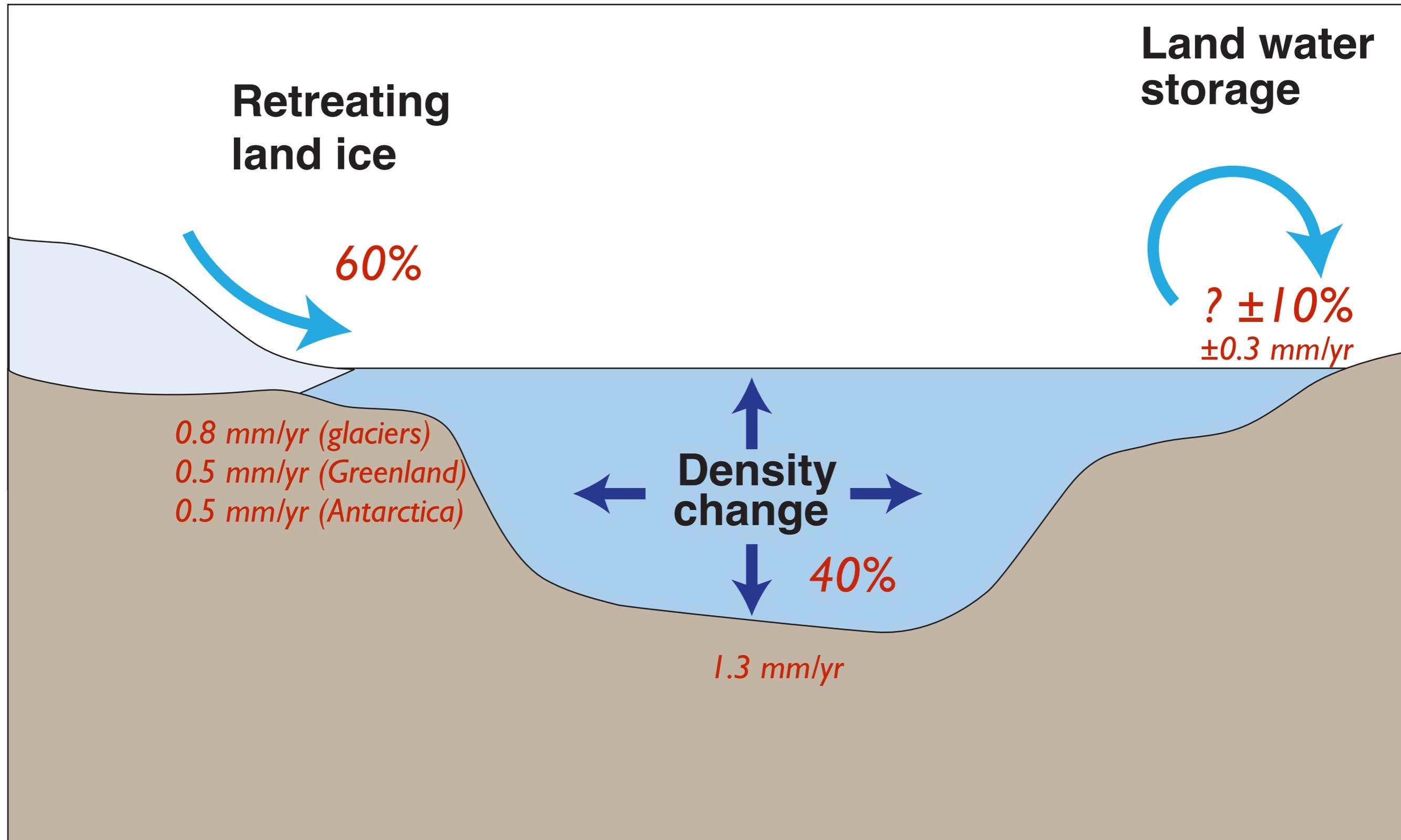


# Sources of global mean sea-level change

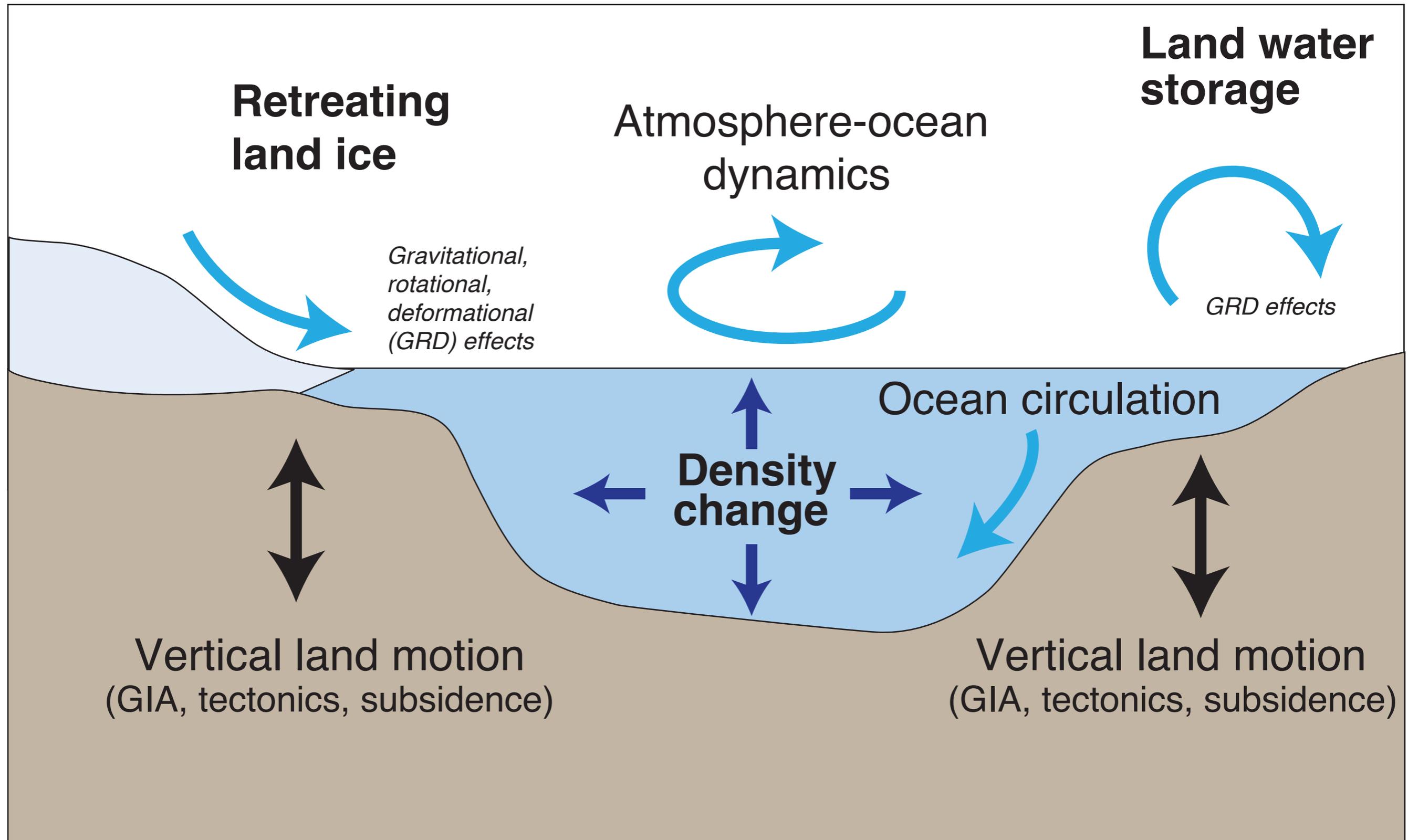


# Sources of global mean sea-level change

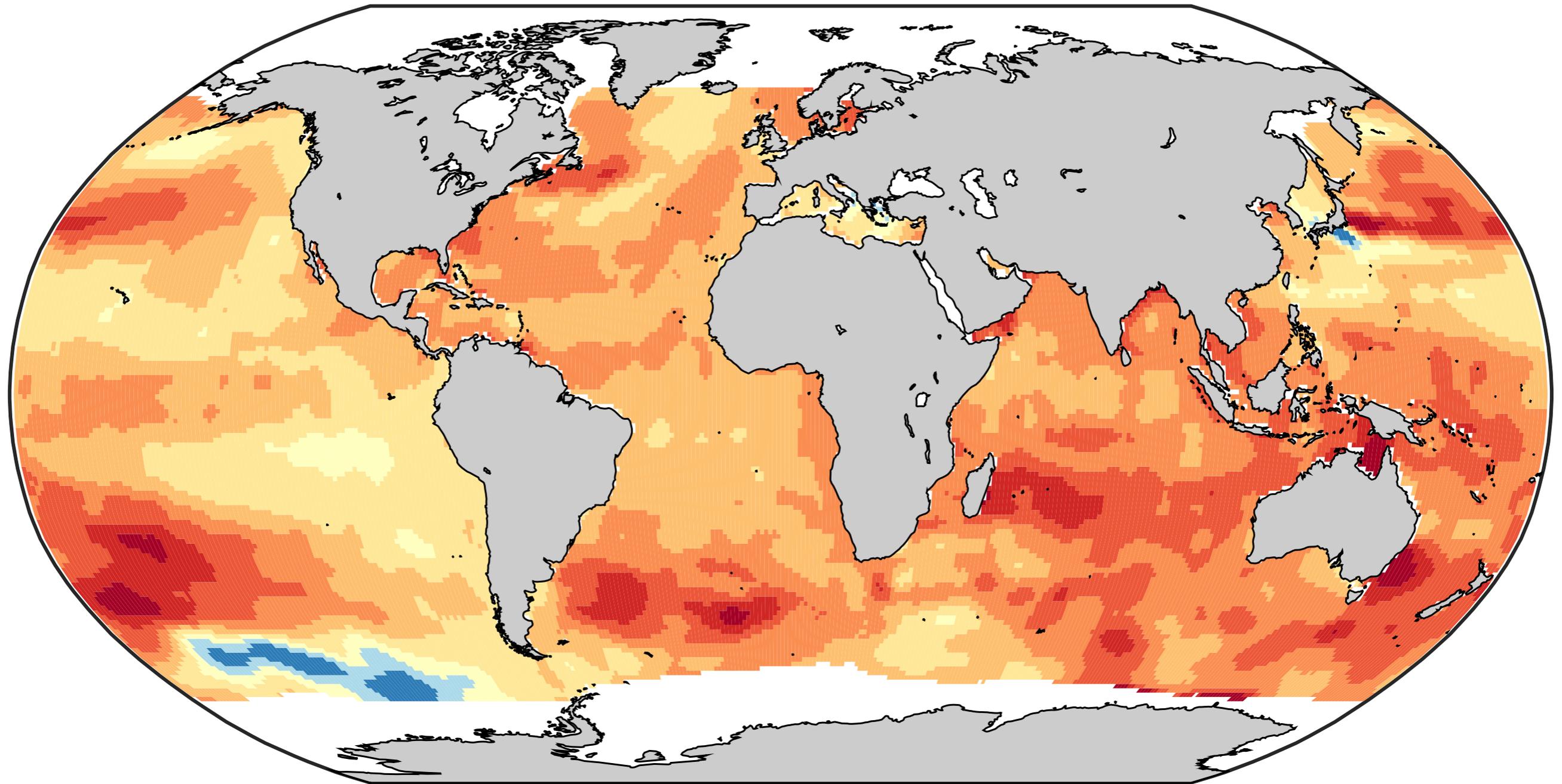
Contributions over 1993–2017 out of  $3.1 \pm 0.4$  mm/yr (1.2"/decade) total



# The story becomes more complex when you look at specific places!



# Change in sea-surface height, 1993-2018



-2      -1      0      1      2      3      4      5      6      7  
mm/yr

## In short:

- Sea-level rise is a complex, spatiotemporally varying process of considerable societal importance.
- Reconstructions of past sea-level change provide a crucial baseline for understanding current changes, and producing these reconstructions requires fusing data from multiple different sources with different error structures, sparsity, and process-sensitivity.
- Local sea-level rise projections are a key input to coastal risk management, and require synthesizing many different lines of evidence. In some cases, alternative approaches to estimating different processes highlight areas of deep uncertainty.
- We are working to produce flexible, scalable, open-source tools to facilitate both these tasks.

# 1. Reconstructing past sea-level changes before the satellite era

*Reconstructions of past sea-level change provide a crucial baseline for understanding current changes, and producing these reconstructions requires fusing data from multiple different sources with different error structures, sparsity, and process-sensitivity.*

# For further reading: review by Erica Ashe

Quaternary Science Reviews 204 (2019) 58–77

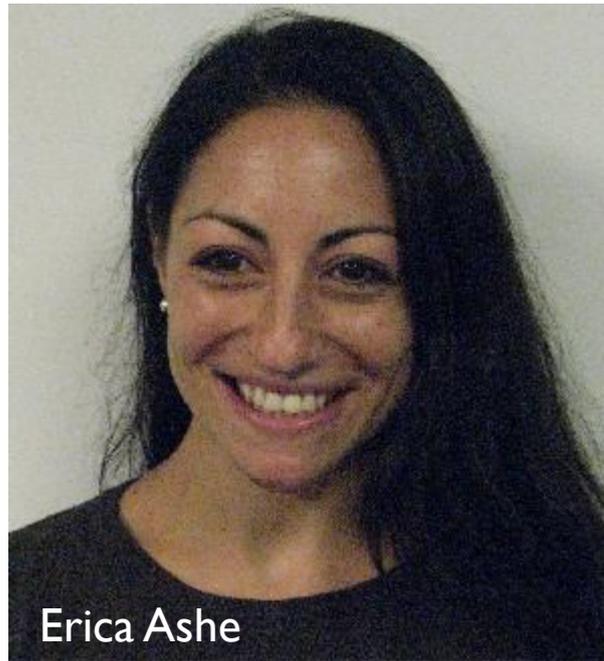


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## Quaternary Science Reviews

journal homepage: [www.elsevier.com/locate/quascirev](http://www.elsevier.com/locate/quascirev)



Erica Ashe

### Statistical modeling of rates and trends in Holocene relative sea level

Erica L. Ashe<sup>a, b, c, \*</sup>, Niamh Cahill<sup>d</sup>, Carling Hay<sup>e</sup>, Nicole S. Khan<sup>f</sup>, Andrew Kemp<sup>g</sup>,  
Simon E. Engelhart<sup>h</sup>, Benjamin P. Horton<sup>f, i, j</sup>, Andrew C. Parnell<sup>d, k</sup>, Robert E. Kopp<sup>b, c</sup>

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<sup>d</sup> School of Mathematics and Statistics, Maynooth University, Kildare, Ireland

<sup>e</sup> Department of Earth and Environmental Sciences, Boston College, Chestnut Hill, MA, United States

<sup>f</sup> Asian School of the Environment, Nanyang Technological University, Singapore

<sup>g</sup> Department of Earth and Ocean Sciences, Tufts University, Medford, MA, United States

<sup>h</sup> Department of Geosciences, University of Rhode Island, Kingston, RI, United States

<sup>i</sup> Earth Observatory of Singapore, Nanyang Technological University, Singapore

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<sup>k</sup> Hamilton Institute, Insight Centre for Data Analytics, Maynooth University, Kildare, Ireland



## Basic concepts: Hierarchical modeling

A hierarchical statistical model separates into different levels, distinguishing (for example) between uncertainty arising at the observation level and uncertainty arising at the process level.

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For example, at the process level:

$$\mathbf{f}(\mathbf{x}, t) = g(t) + \mathbf{f}_{\text{GRD}}(\mathbf{x}, t) + \mathbf{f}_{\text{DSL}}(\mathbf{x}, t) + \mathbf{f}_{\text{VLM}}(\mathbf{x}, t)$$

And at the data level:

$$y_i = f(\mathbf{x}_i, \hat{t}_i + \delta) + \epsilon$$

# 1.1. Sea-level change over the instrumental period

# Tide gauges

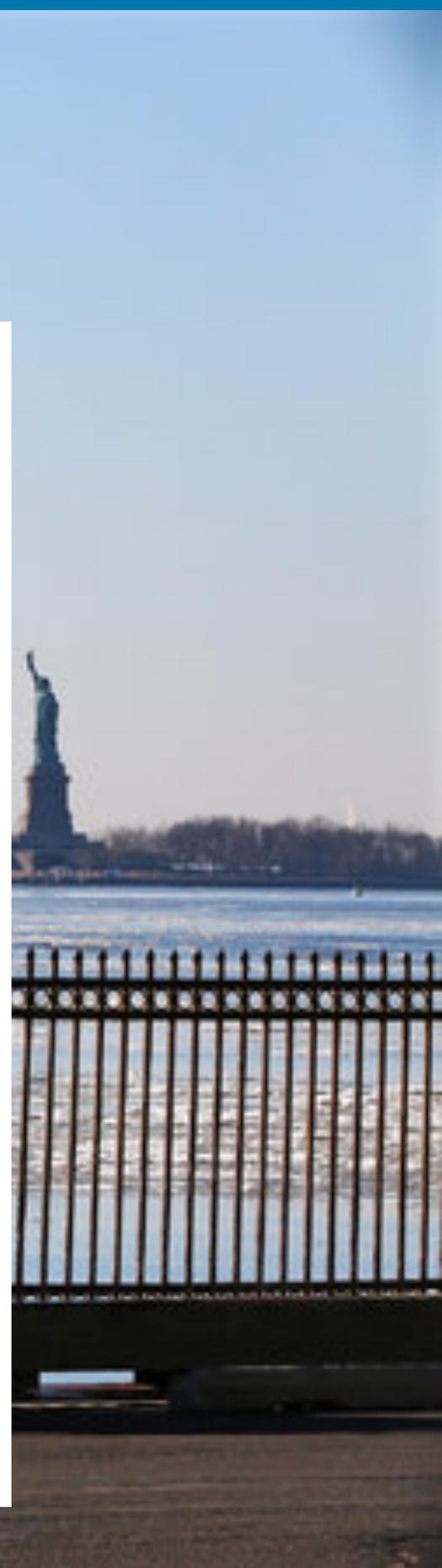
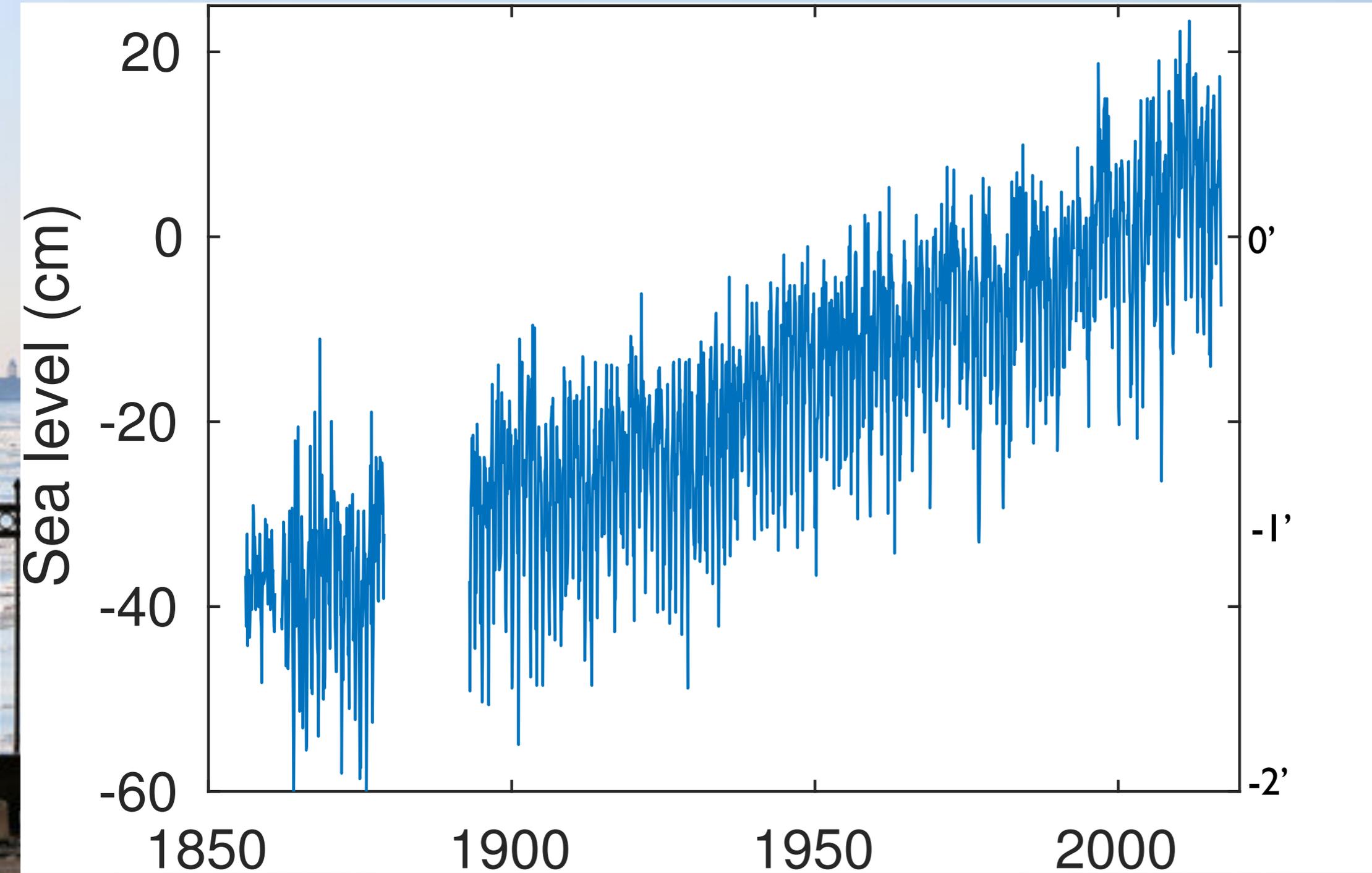
Battery Tide Gauge, New York City



# Tide gauges

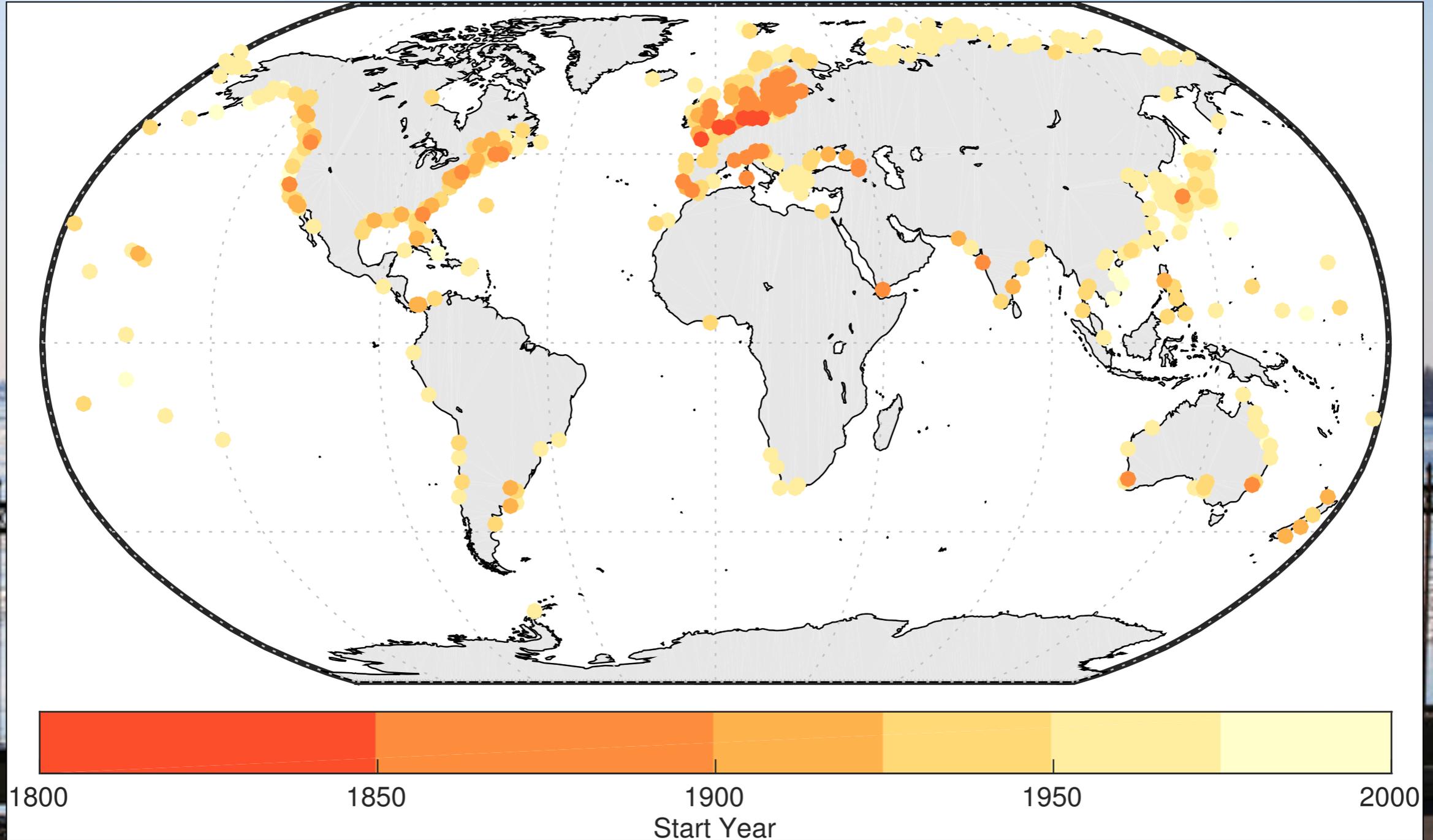
Battery Tide Gauge, New York City

(monthly mean sea-level relative to 1991-2009)



# Tide gauges

Start year of tide-gauge records



# Tide gauges

## Global statistical model

### LETTER

doi:10.1038/nature14093

## Probabilistic reanalysis of twentieth-century sea-level rise

Carling C. Hay<sup>1,2</sup>, Eric Morrow<sup>1,2</sup>, Robert E. Kopp<sup>2,3</sup> & Jerry X. Mitrovica<sup>1</sup>



Jerry Mitrovica  
Carling Hay  
Eric Morrow

# Tide gauges

## Global statistical model

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$$\text{RSL}(\mathbf{x}, t) = \text{Uniform}(t) + \sum_j \text{fingerprint}_j(\mathbf{x}) \text{Ice}_j(t) + \text{DSL}(\mathbf{x}, t) + \text{GIA}(\mathbf{x}, t)$$

$$\text{TG}_i(t) = \text{RSL}(\mathbf{x}_i, t) + \text{Noise}(\mathbf{x}, t)$$

Jerry Mitrovica  
Carling Hay  
Eric Morrow



# Tide gauges

## Global statistical model

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Jerry Mitrovica  
Carling Hay  
Eric Morrow

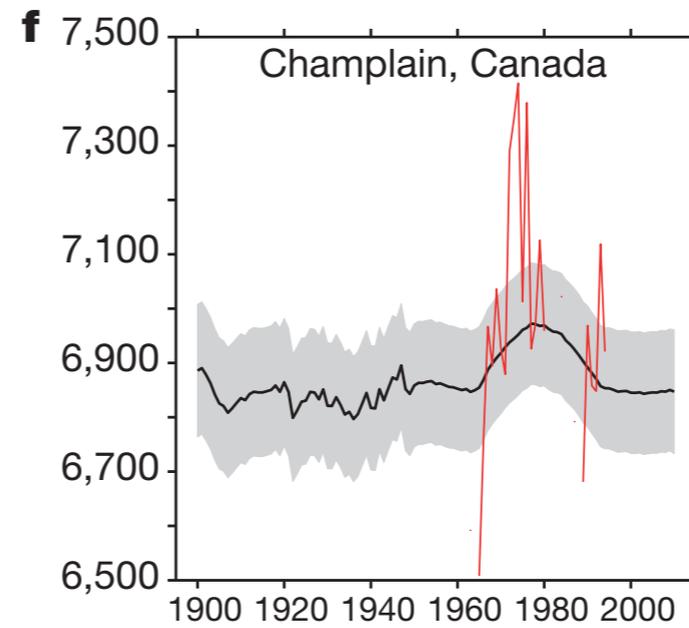
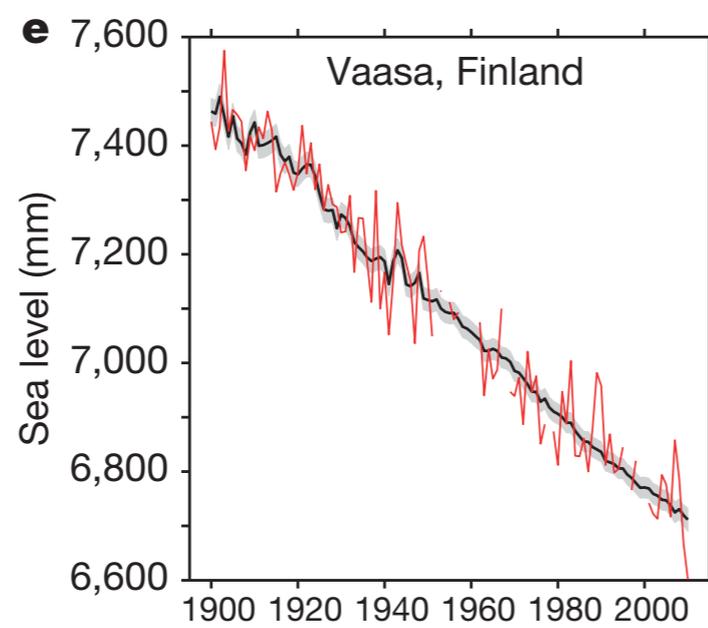
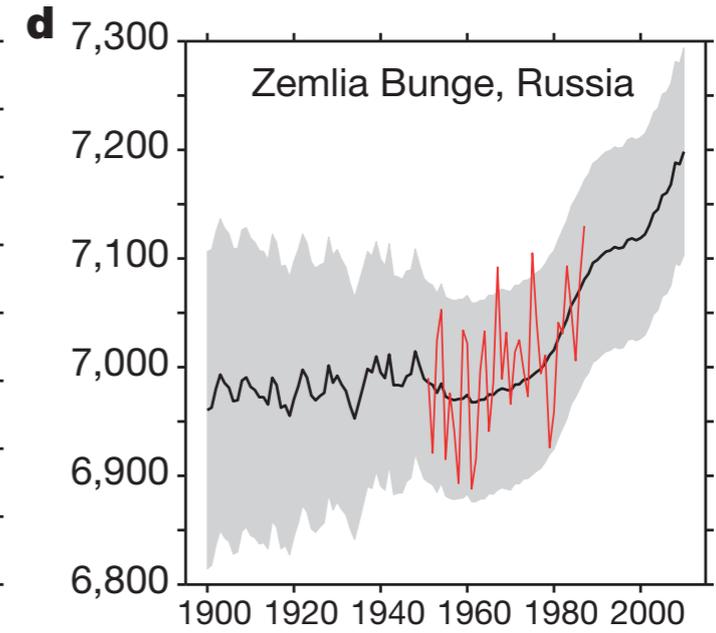
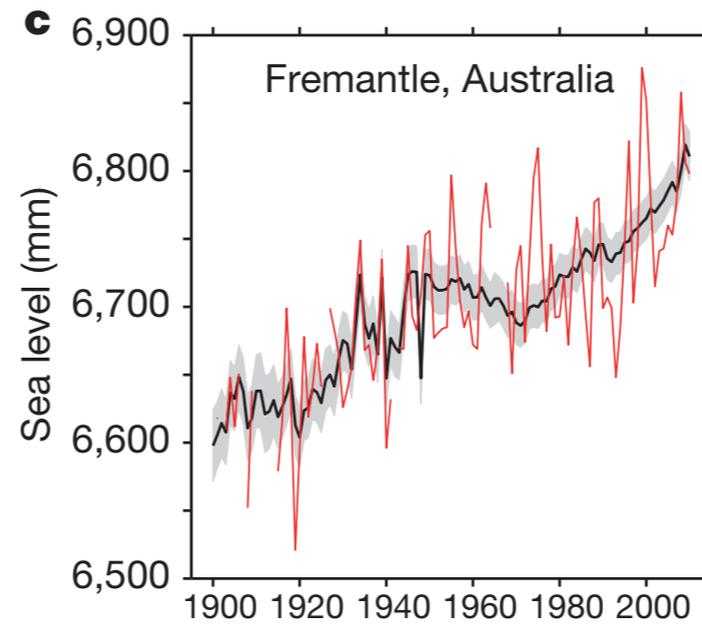
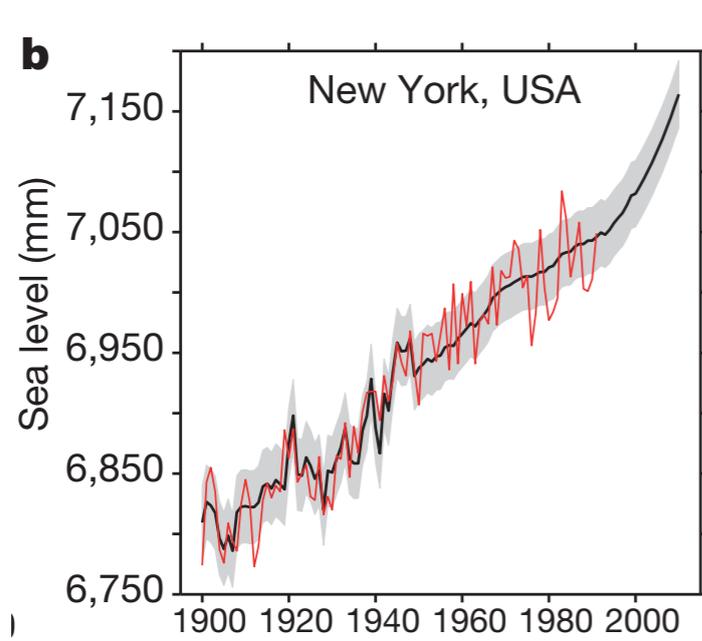


Two computational approaches:

1. State-space model (Kalman smoother)
2. Gaussian process regression

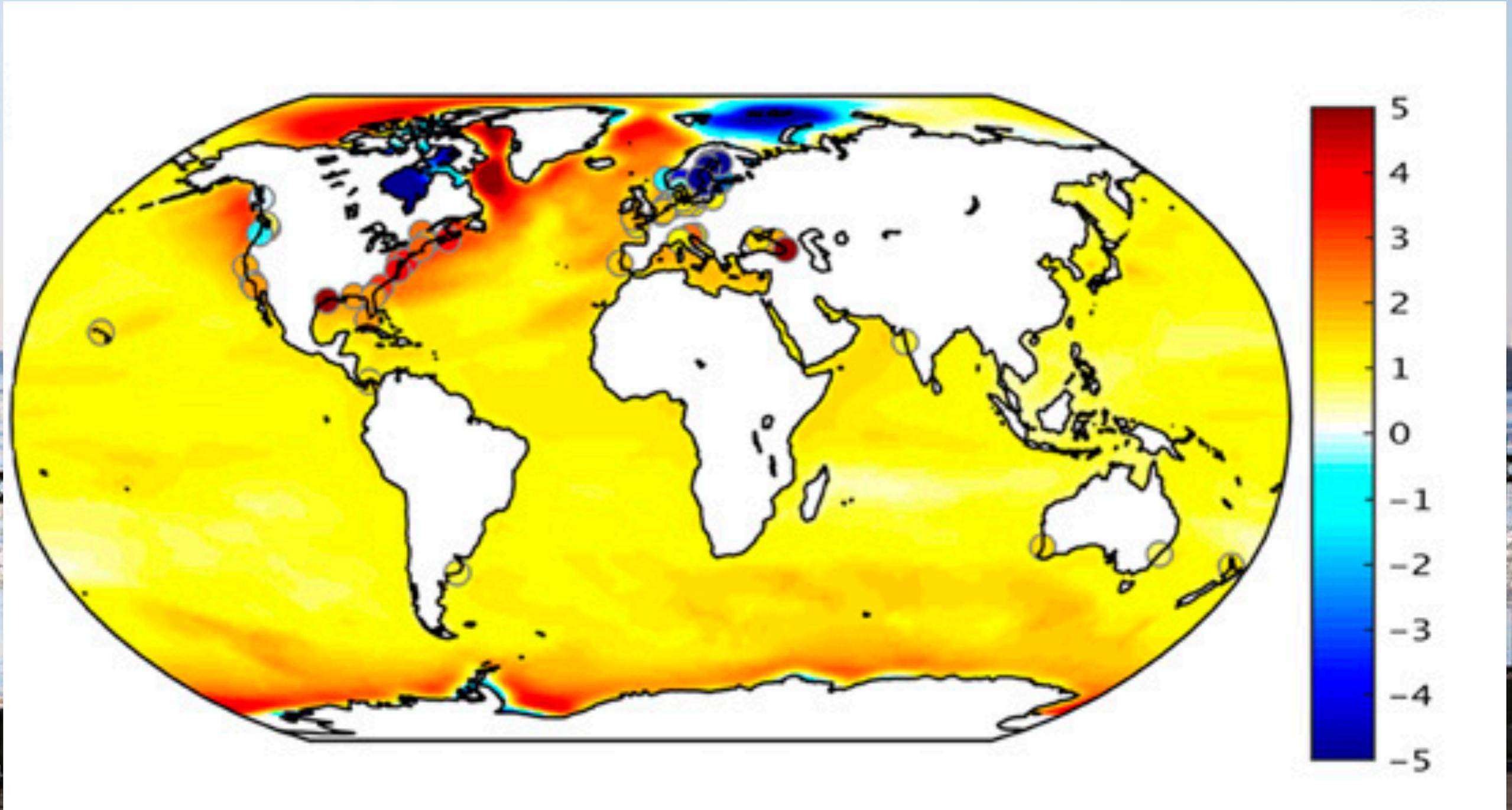
# Tide gauges

Model fits the data!



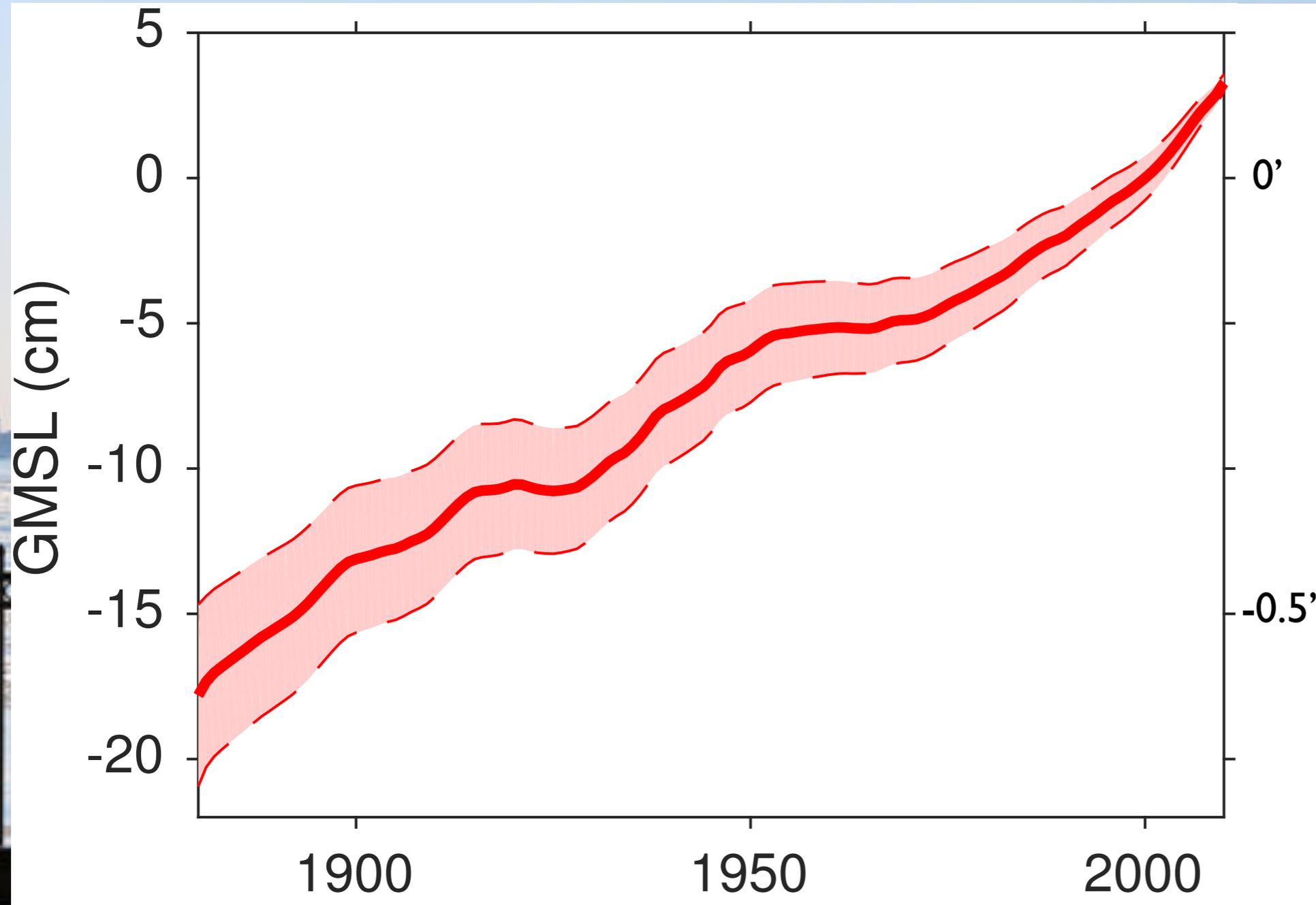
# Tide gauges

Rate of relative sea-level rise, 1901-1990 (mm/yr)



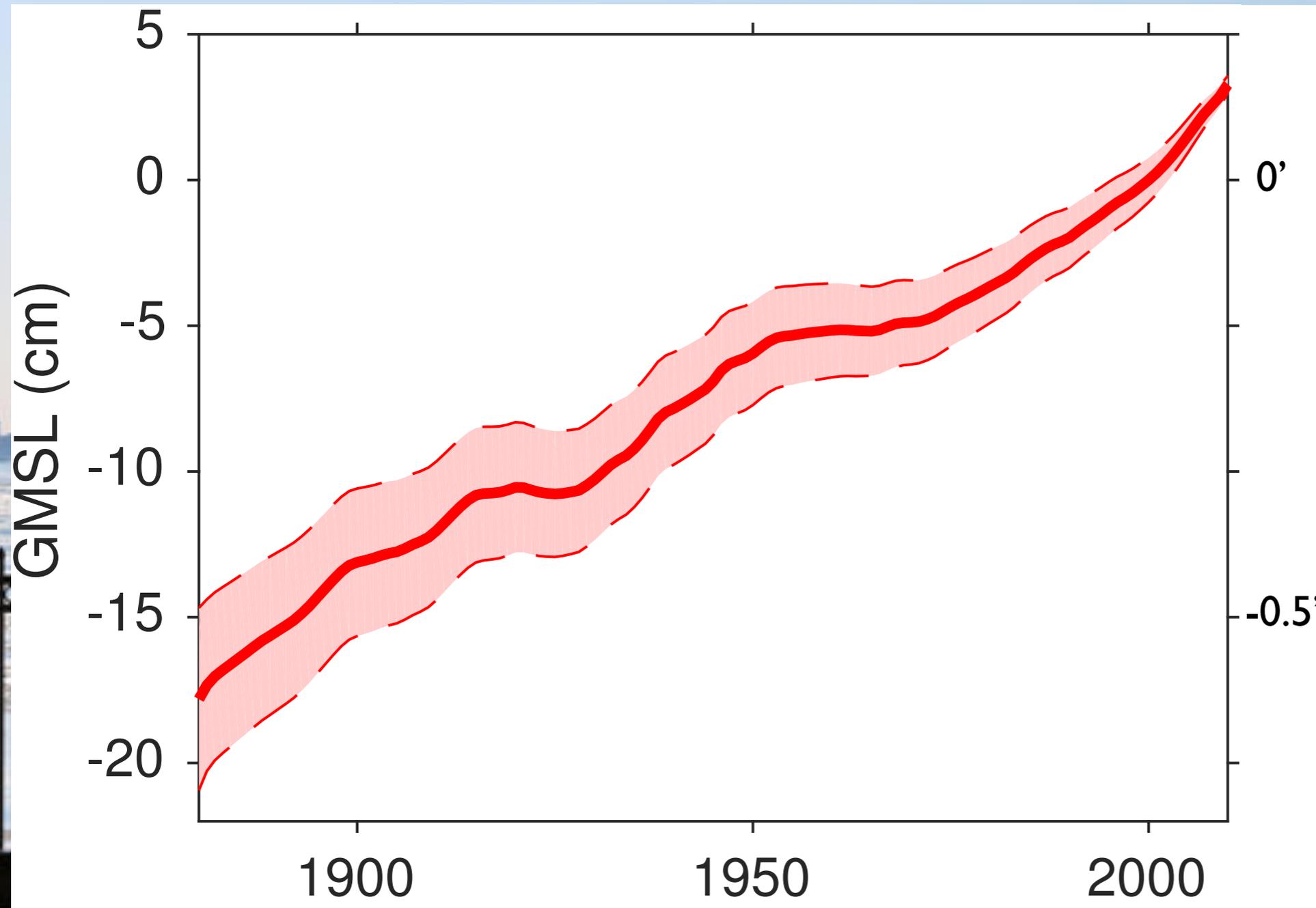
# Tide gauges

Global mean sea level



# Tide gauges

Global mean sea level



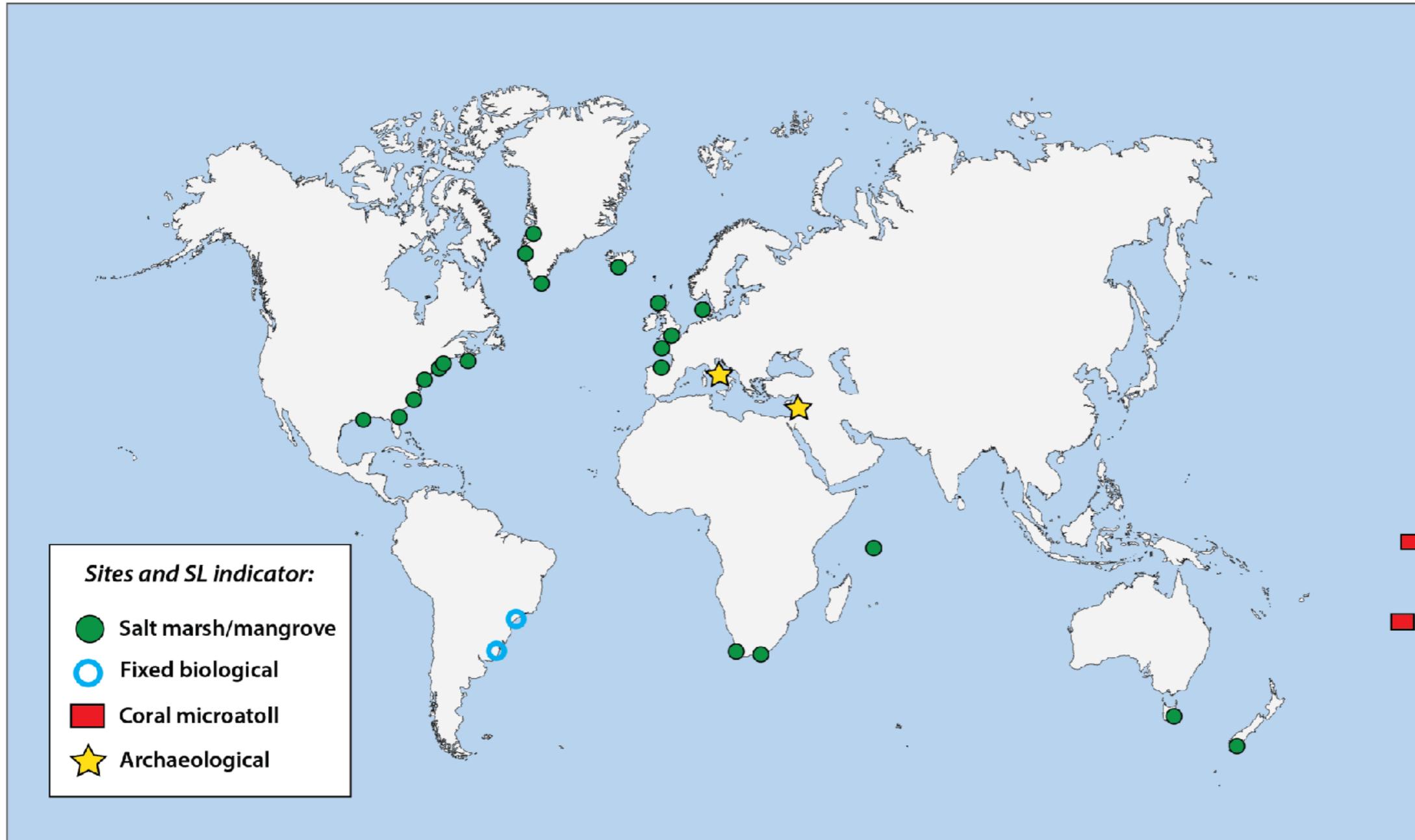
From 1901-1990, global mean sea level rose at  $\sim 1.2 \pm 0.2$  mm/yr ( $\sim 0.5''$ /decade). From 1993-2010, it rose  $\sim 2.5$ x faster.

## 1.2. Sea-level change over the last three thousand years

# Extending the record back with geology



# Common Era sea-level database



# Common Era sea-level model

[github.com/bobkopp/CESL-STEHM-GP](https://github.com/bobkopp/CESL-STEHM-GP)

bobkopp / CESL-STEHM-GP

Unwatch 1

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Code

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Spatio-Temporal Empirical Hierarchical Modeling of sea-level data with Gaussian Processes

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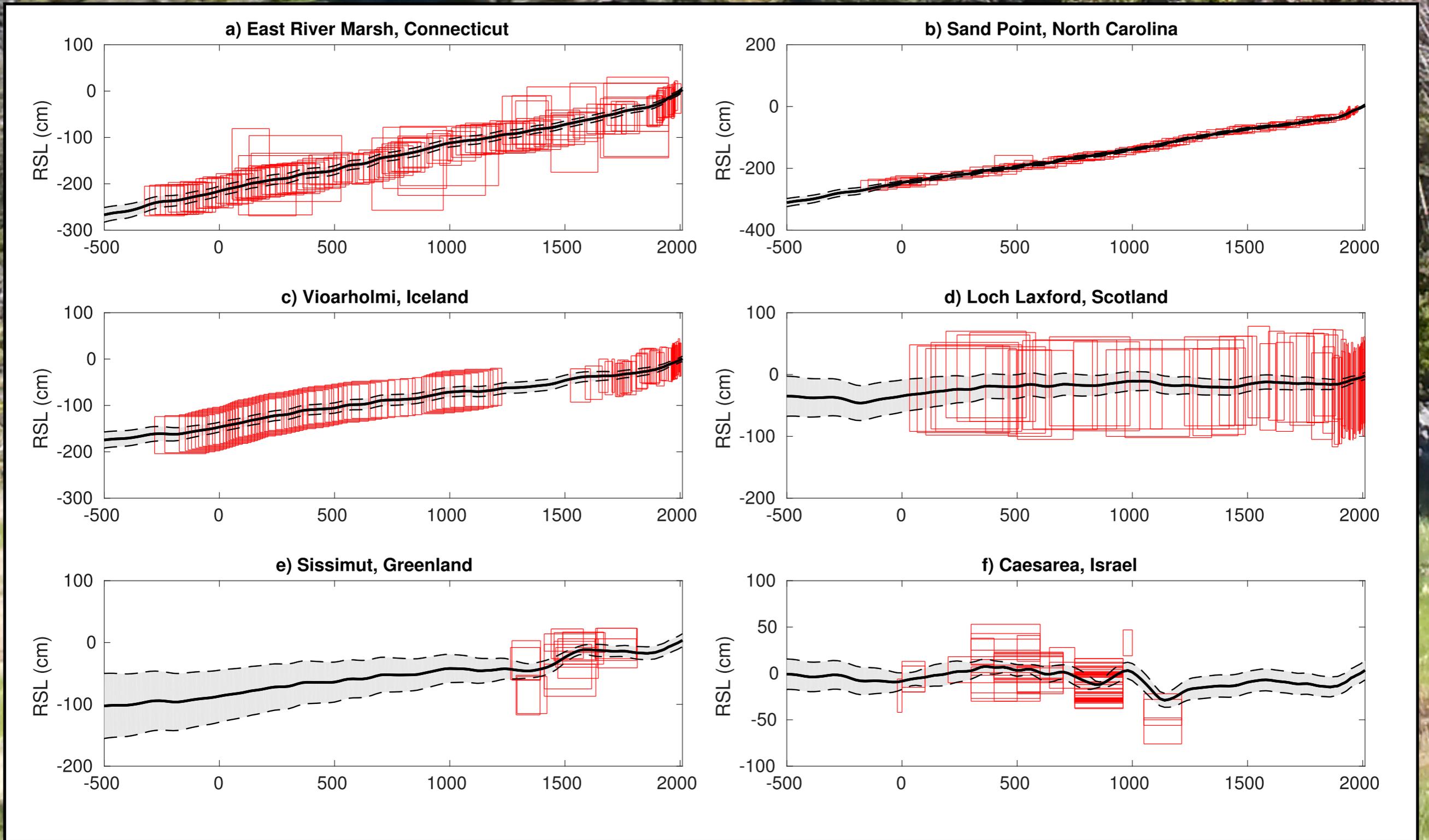
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$$\text{RSL}(\mathbf{x}, t) = \text{Global}(t) + \text{Linear}(\mathbf{x})(t - t_0) + \text{Regional}(\mathbf{x}, t)$$

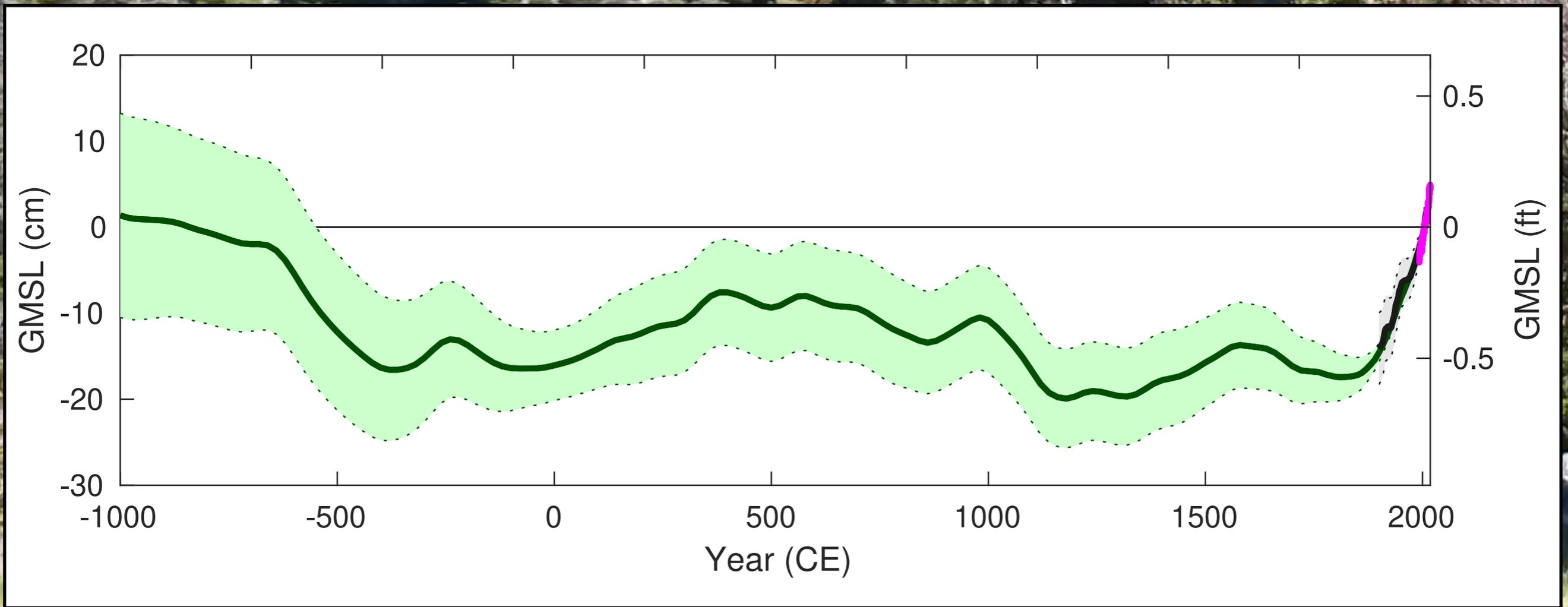
$$\text{Proxy}(\mathbf{x}, \hat{t}_i) = \text{RSL}(\mathbf{x}, t_i) + \text{Noise}_i$$

$$\hat{t}_i = t_i + \text{AgeNoise}_i$$

# Common Era sea-level model fits the data!

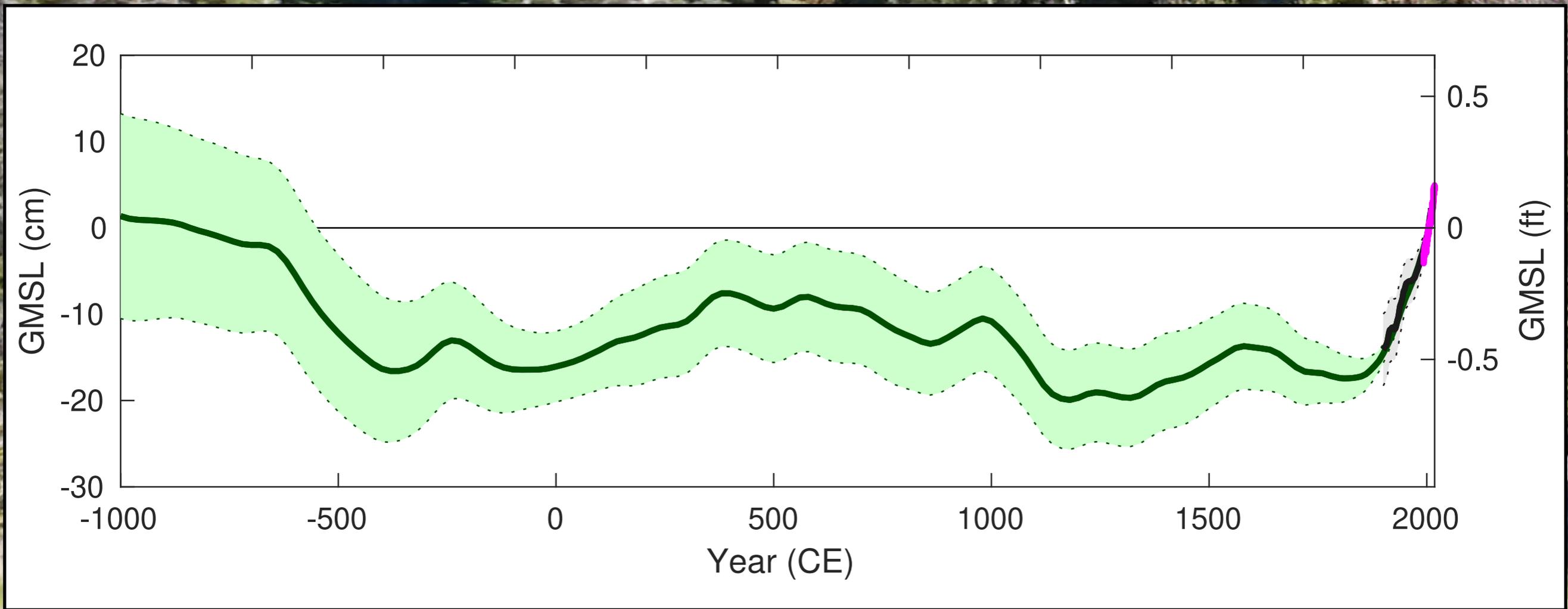


# Common Era global sea level



Kopp et al. (2016); Kemp et al. (2018); instrumental data from Hay et al. (2015) and Nerem et al. (2018)

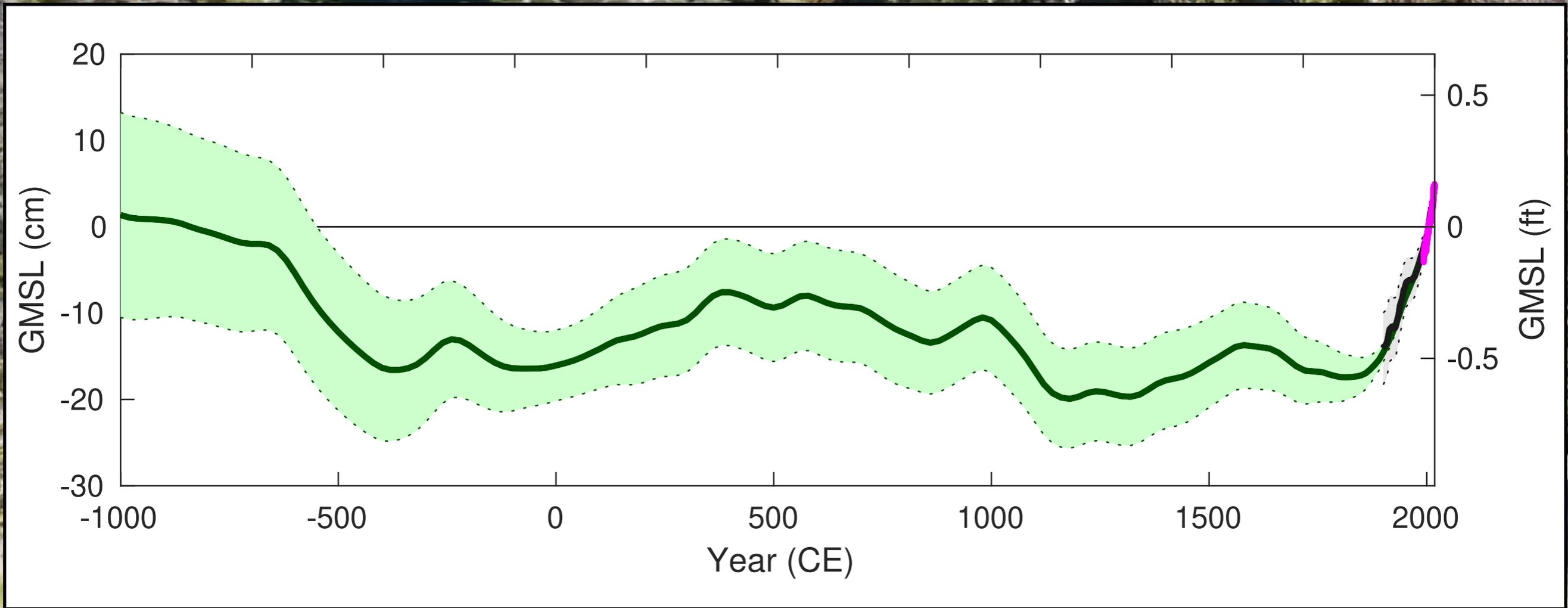
# Common Era global sea level



**Barack Obama** ✓  
@BarackObama

We're seeing the fastest rise in sea-levels in nearly 3,000 years:  
[ofa.bo/j9qS](https://ofa.bo/j9qS) #ActOnClimate

# Common Era global sea level



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We're seeing the fastest rise in sea-levels in nearly 3,000 years:  
[ofa.bo/j9qS](https://ofa.bo/j9qS) #ActOnClimate

20th century global mean sea-level rise of  $1.4 \pm 0.2$  mm/yr (6"/century) was *virtually certain* ( $P > 99\%$ ) faster than any century since at least 1000 BCE

## 2. Projections of future changes

*Local sea-level rise projections are a key input to coastal risk management, and require synthesizing many different lines of evidence. In some cases, alternative approaches to estimating different processes highlight areas of deep uncertainty.*

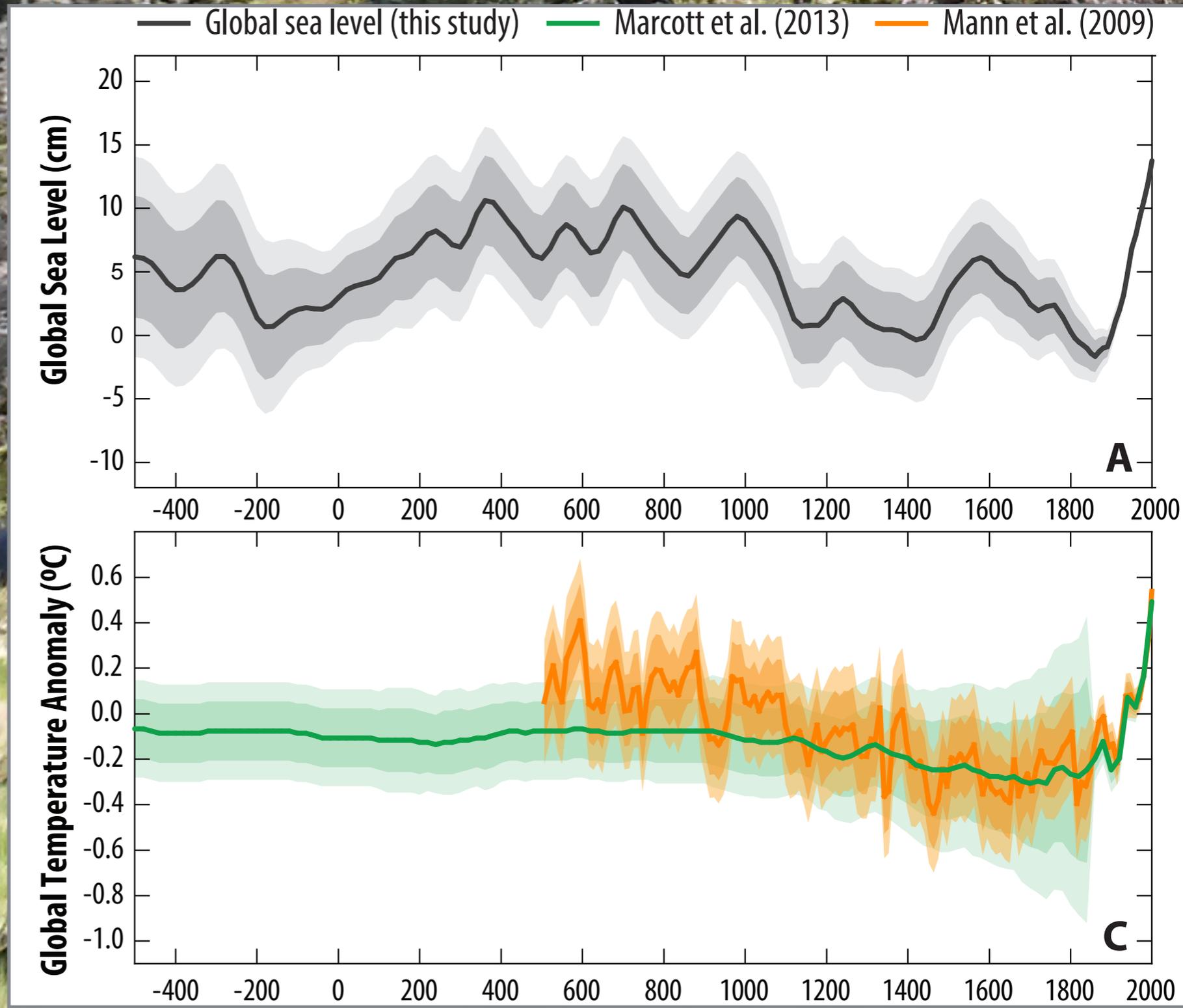
# Consider the past relationship between temperature and sea level

$$\begin{aligned} dh/dt &= a(T(t) - T_0(t)) + c(t) \\ dT_0(t)/dt &= (T(t) - T_0(t))/\tau_1 \\ dc(t)/dt &= -c/\tau_2 \end{aligned}$$

$\tau_1 \approx 100$  to  $200$  years

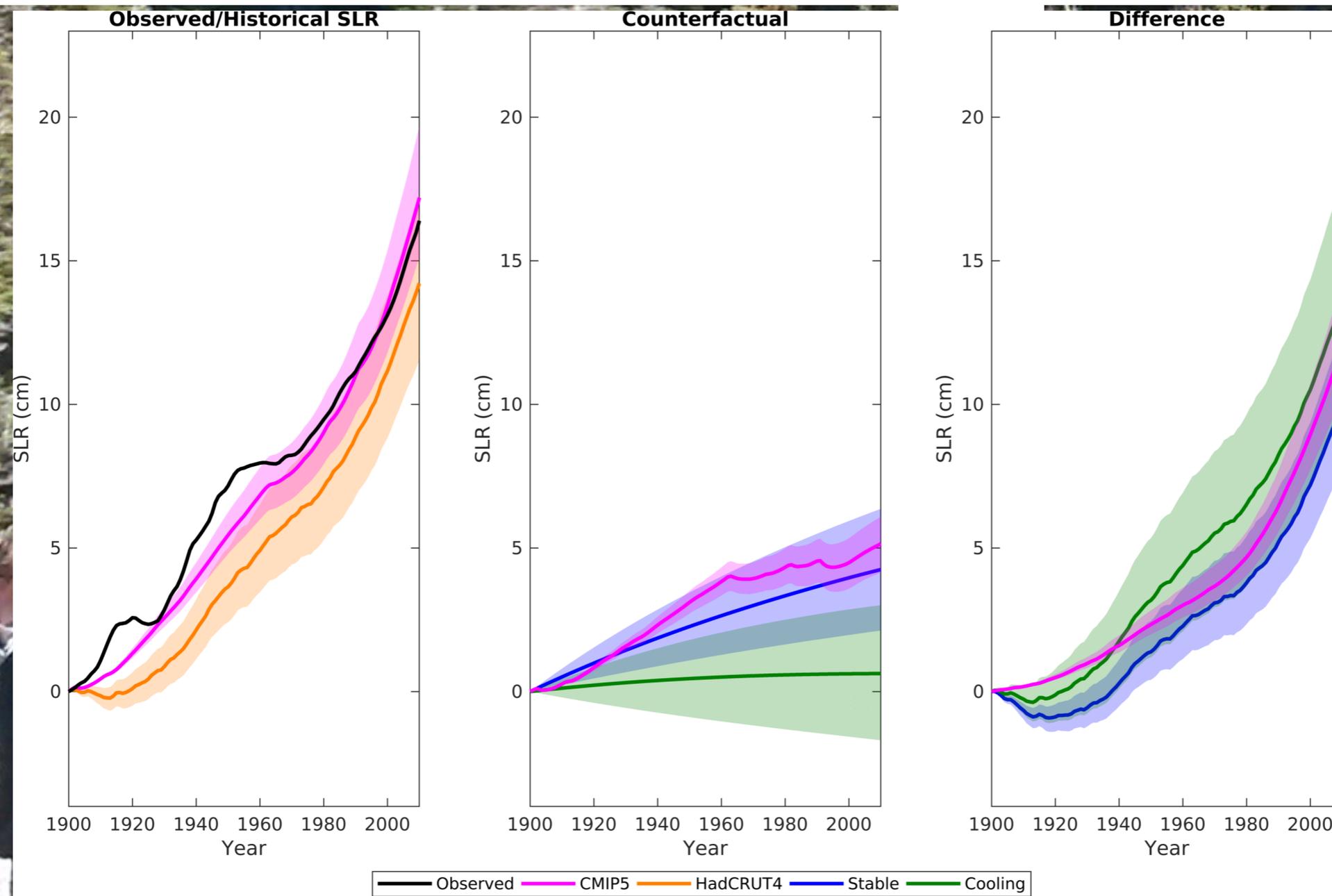
$\tau_2 \approx 3000$  to  $4000$  years

Klaus Bittermann



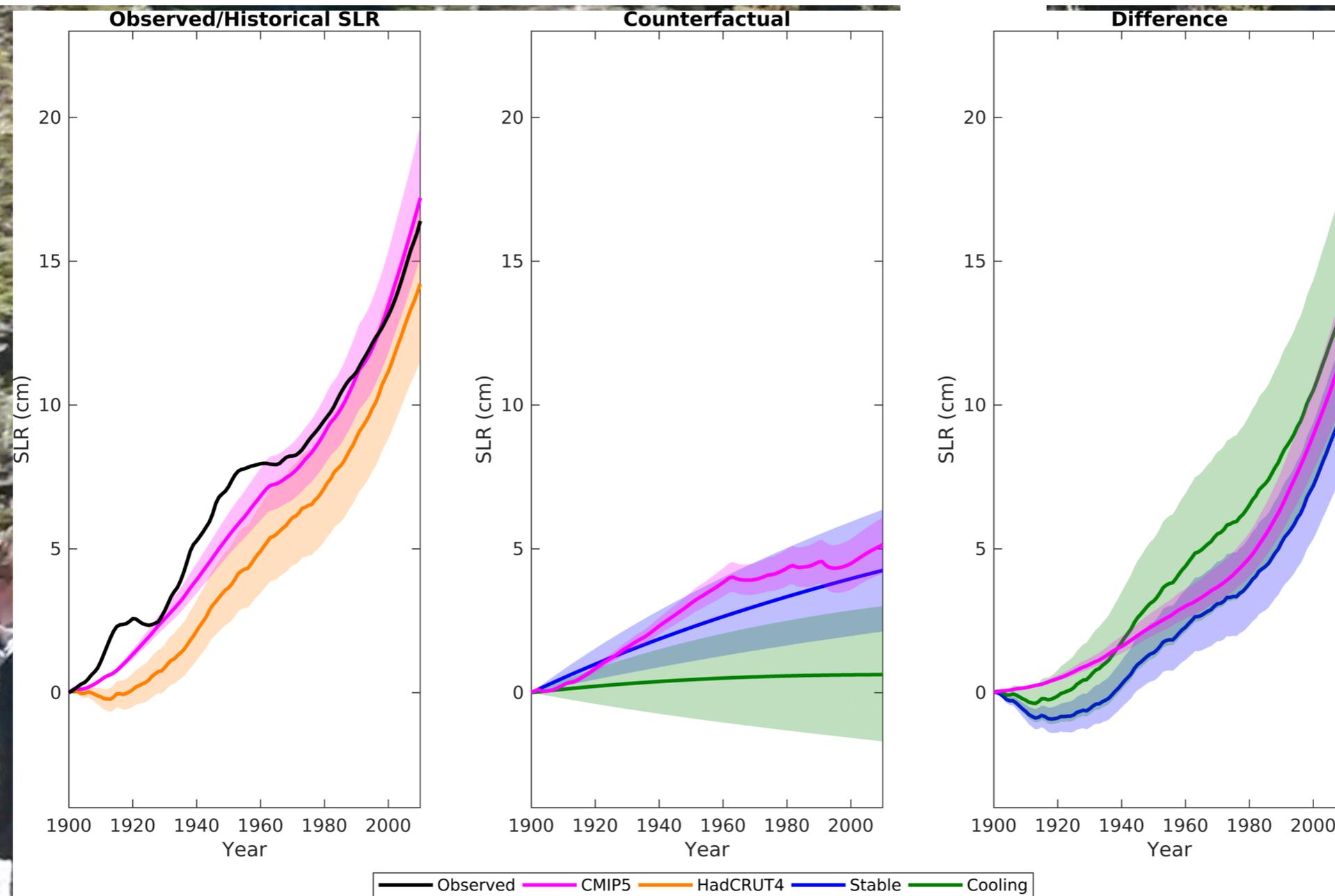
# What does this imply for the historical sea-level change?

Counterfactual scenarios for 1900–2012



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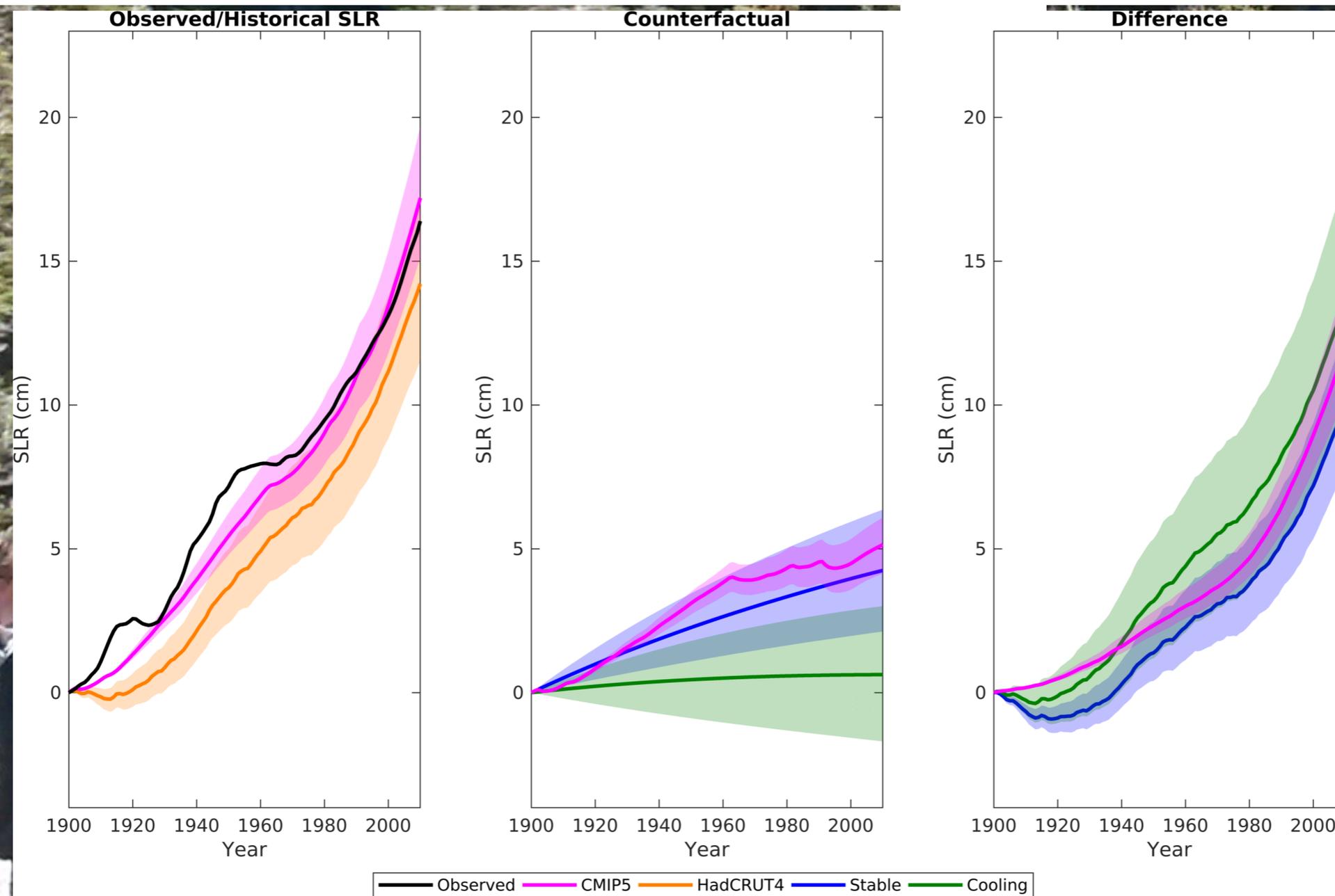
Counterfactual scenarios for 1900–2012



**Depending on assumptions, very likely (90% credible) that between 8 and 18 cm of observed 16 cm of GMSL rise over 1900-2012 is due to human-caused climate change.**

# What does this imply for the historical sea-level change?

Counterfactual scenarios for 1900–2012

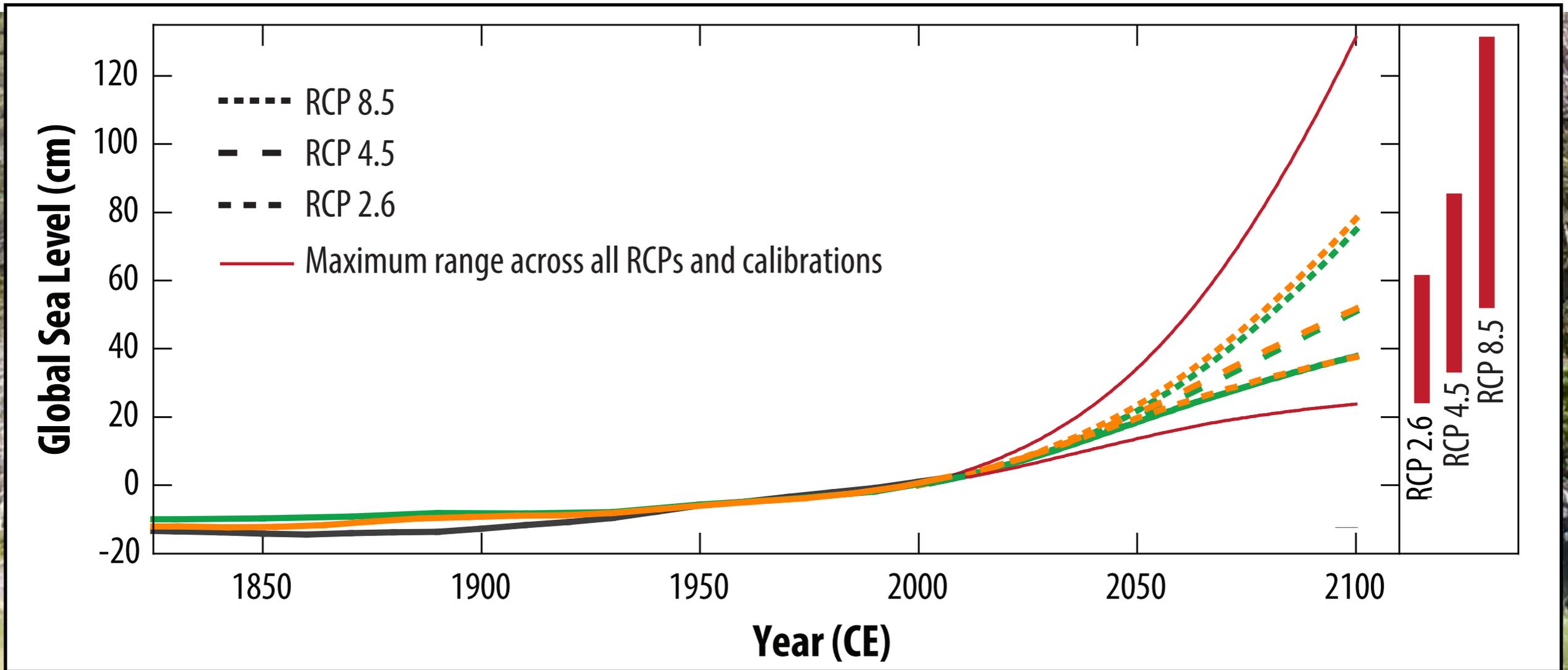


**Depending on assumptions, very likely (90% credible) that between 8 and 18 cm of observed 16 cm of GMSL rise over 1900-2012 is due to human-caused climate change.**

*Implying human-caused SLR is responsible for ~1/6 of Sandy damages...*

# Project forward using the past sea level/temperature relationship

Global mean sea-level rise above year 2000 levels



**Projected SLR by 2100 (90% probability range):**

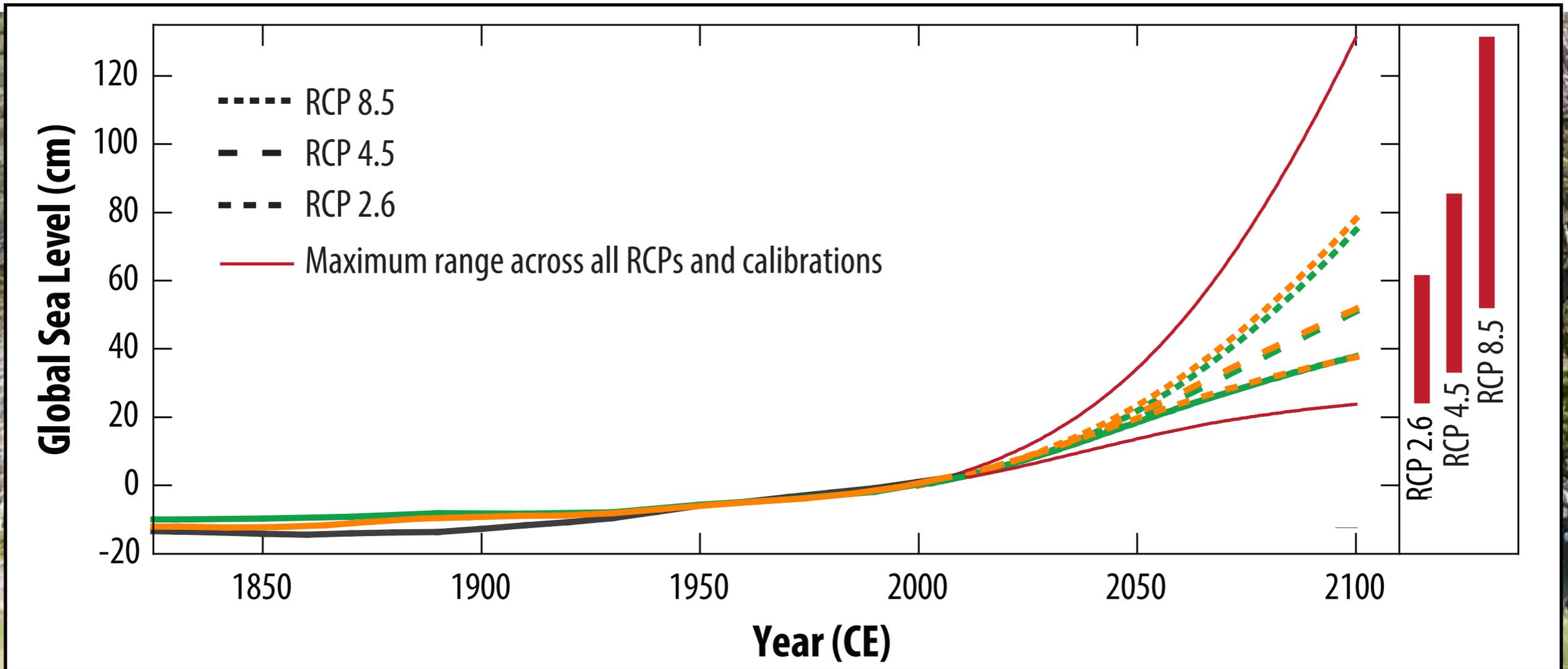
**0.5–1.3 m (1.7–4.3 ft) under high emissions (RCP 8.5)**

**0.2–0.6 m (0.8–2.0 ft) under low emissions (RCP 2.6)**



# Project forward using the past sea level/temperature relationship

Global mean sea-level rise above year 2000 levels



**But: statistical model projects global (not local) changes and is calibrated from a time period when thermal expansion and mountain glaciers (and, regionally, ocean dynamics) dominated sea-level change.**

**Projected SLR by 2100 (90% probability range):**

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**0.2-0.6 m (0.8-2.0 ft) under low emissions (RCP 2.6)**

# Kopp et al. 2014 bottom-up probabilistic framework

## Earth's Future

### RESEARCH ARTICLE

10.1002/2014EF000239

#### Key Points:

- Rates of local sea-level rise differs

## Probabilistic 21st and 22nd century sea-level projections at a global network of tide-gauge sites

Robert E. Kopp<sup>1</sup>, Radley M. Horton<sup>2</sup>, Christopher M. Little<sup>3</sup>, Jerry X. Mitrovica<sup>4</sup>, Michael Oppenheimer<sup>3</sup>, D. J. Rasmussen<sup>5</sup>, Benjamin H. Strauss<sup>6</sup>, and Claudia Tebaldi<sup>6,7</sup>

# Kopp et al. 2014 probabilistic framework

## Earth's Future

### RESEARCH ARTICLE

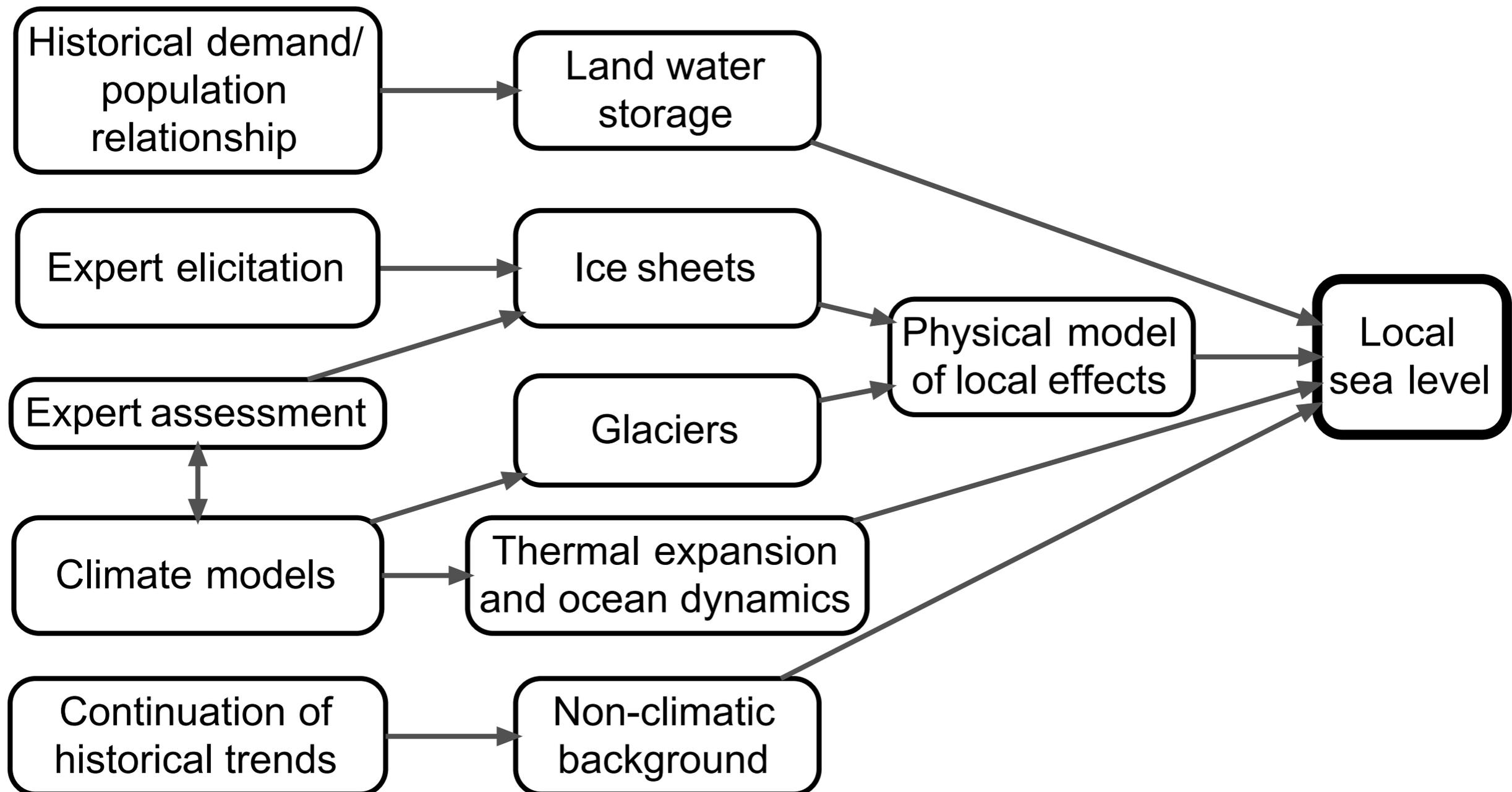
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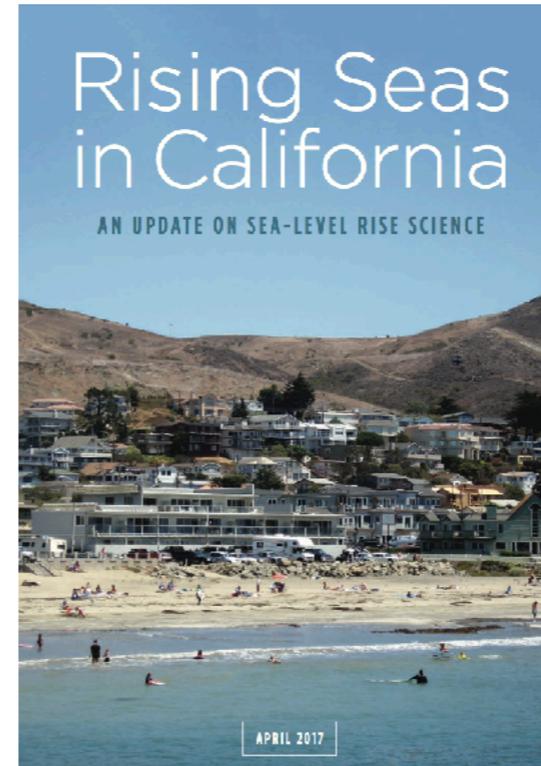
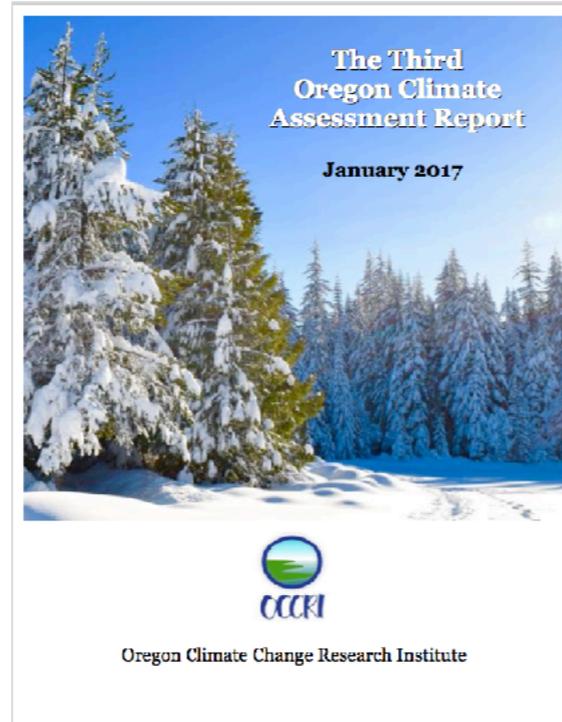
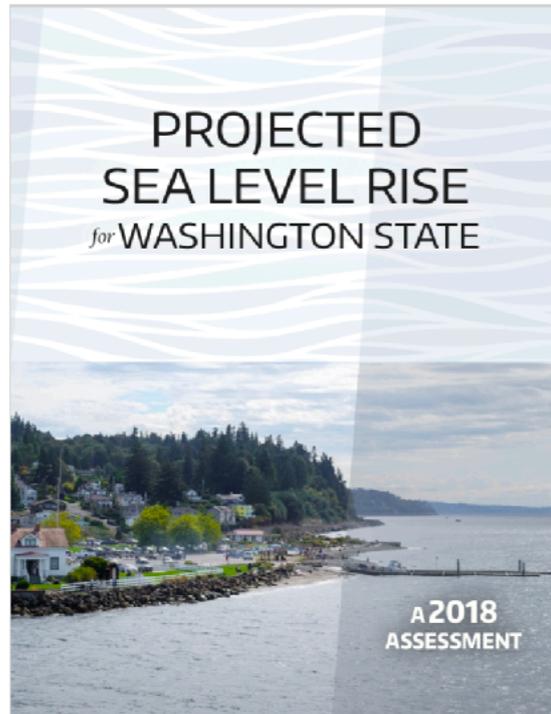
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# Kopp et al. 2014 framework ( $\pm$ modifications) has been widely used in US



NOAA Technical Report NOS CO-OPS 063

## GLOBAL AND REGIONAL SEA LEVEL RISE SCENARIOS FOR THE UNITED STATES



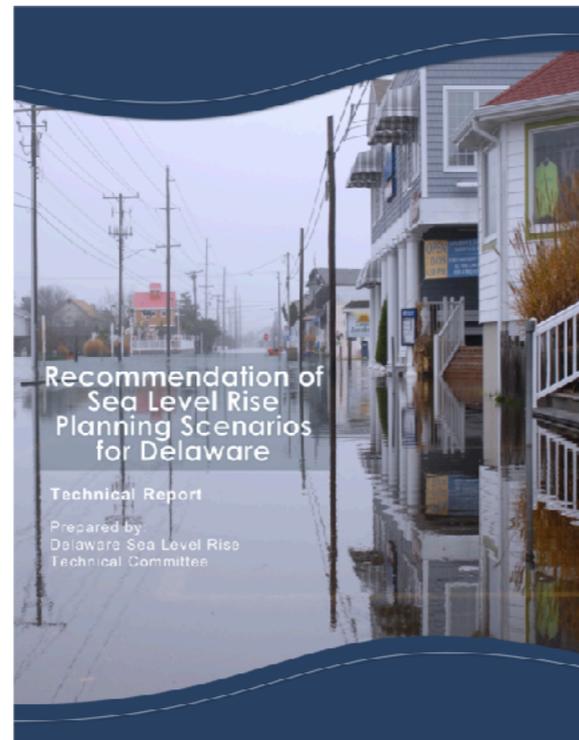
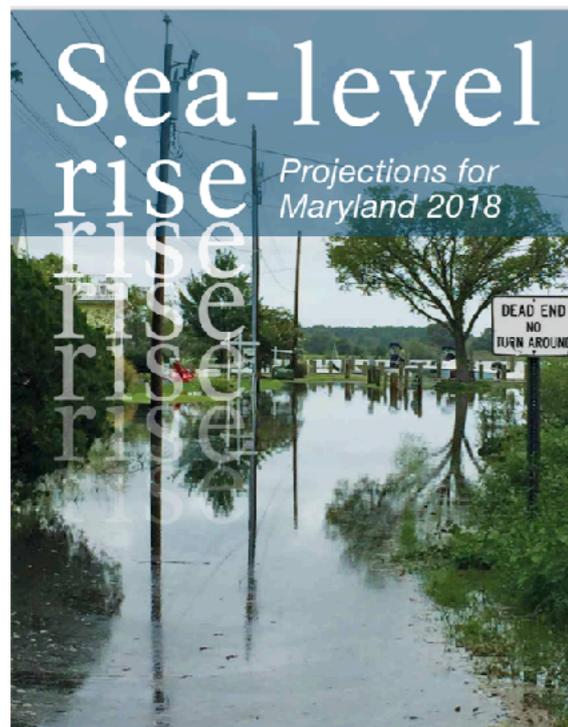
Photo: Ocean City, Maryland

Silver Spring, Maryland  
January 2017



noaa National Oceanic and Atmospheric Administration

U.S. DEPARTMENT OF COMMERCE  
National Ocean Service  
Center for Operational Oceanographic Products and Services



# Data and code availability

[github.com/bobkopp/LocalizeSL](https://github.com/bobkopp/LocalizeSL)

bobkopp / LocalizeSL

Unwatch 5 Star 7 Fork 2

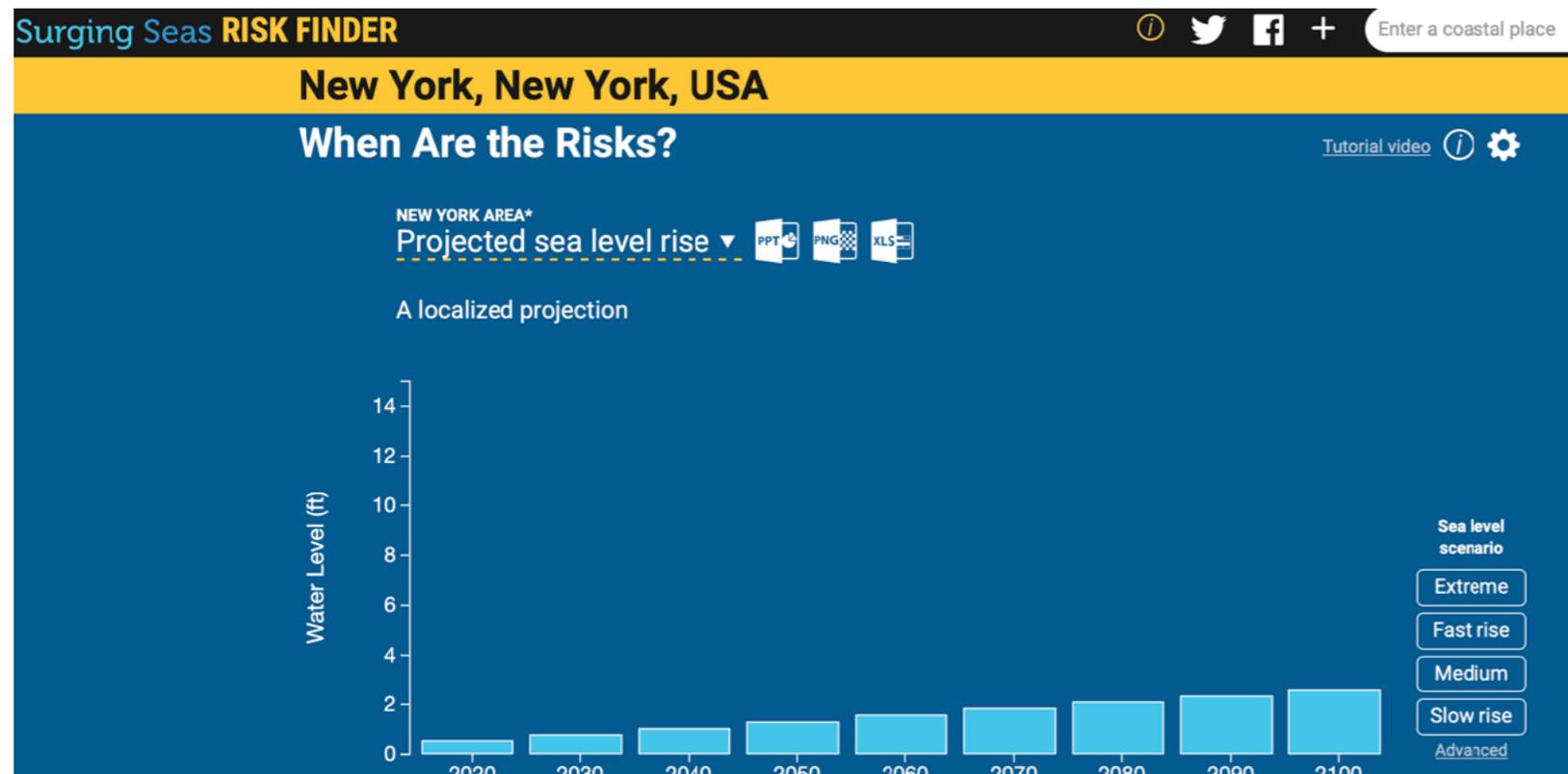
Code Issues 0 Pull requests 0 Projects 0 Wiki Security Insights Settings

LocalizeSL: Sea-level localization code for Kopp et al. (2014) projections framework

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[sealevel.climatecentral.org](https://sealevel.climatecentral.org)



## Forecast settings

These advanced settings give access to multiple models from the continuously evolving scientific and technical literature. Note: Only NOAA 2017 takes account of recent research suggesting high Antarctic ice sheet sensitivity to warming (DeConto and Pollard 2016, Nature).

+ Kopp et al. (2017): With Antarctic dynamics

+ NOAA (2017)

+ National Climate Assessment (2012/2014)

- Kopp et al. (2014): Probabilistic

Local sea level projections from Kopp et al. 2014 (Earth's Future). Based on different Representative Concentration Pathways (RCPs) of heat-trapping pollution over time, and on different sensitivities of climate and sea level to pollution. Below, low means 5th percentile sensitivity, middle means median, and high means 95th percentile. Climate Central has combined these sea level projections with local data to make local flood risk projections.

Extreme cuts (RCP 2.6)  
Sensitivity:  Low  Middle  High

Moderate cuts (RCP 4.5)  
Sensitivity:  Low  Middle  High

Unchecked pollution (RCP 8.5)  
Sensitivity:  Low  Middle  High

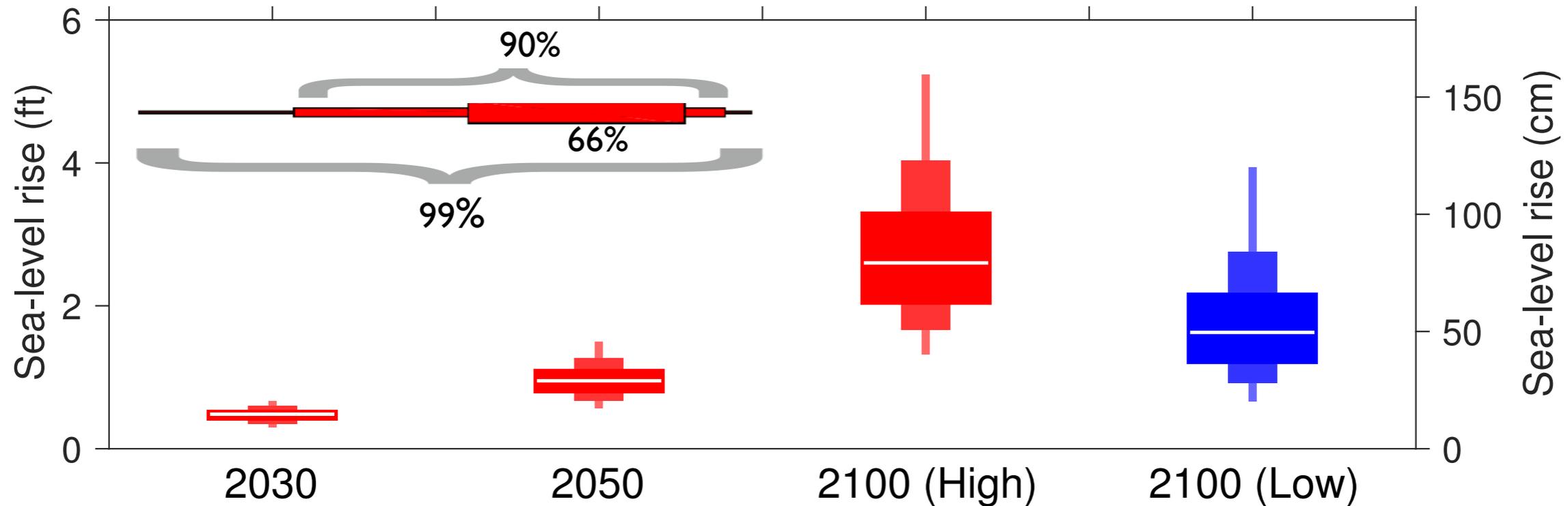
+ IPCC (2013)

+ Army Corps of Engineers (2011)

+ No global warming

# Projected global mean sea-level rise

Above 1991-2009 average sea level



*By 2030: very likely 0.1-0.2 m (0.3-0.6 feet), regardless of emissions*

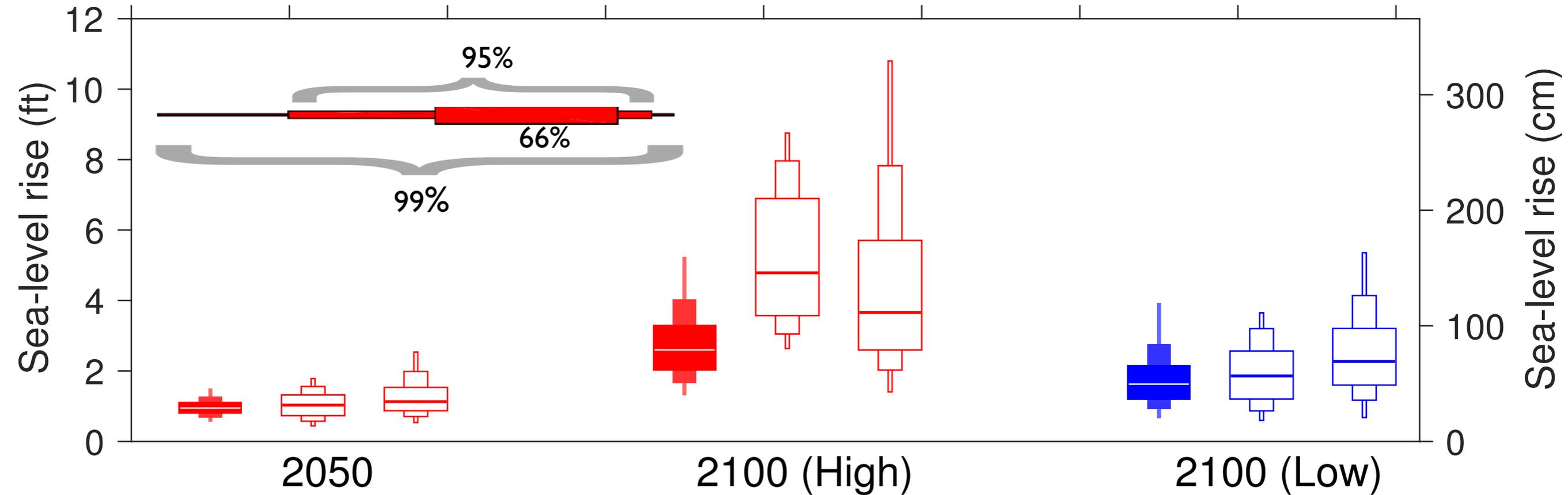
*By 2050: very likely 0.2-0.4 m (0.6-1.3 feet), almost regardless of emissions*

*By 2100: very likely 0.5-1.2 m (1.7-4.0 feet) under high emissions*

*By 2100: very likely 0.3-0.8 m (0.9-2.8 ft) under low emissions*

*In climate scientist (IPCC) speak,  
'very likely' means at least 9 chances in 10.  
(But lower probability outcomes also can be important!)*

# Different treatments of ice sheets give quite different late century global-mean sea-level projections



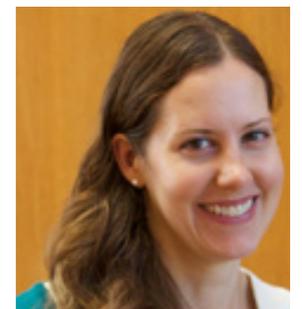
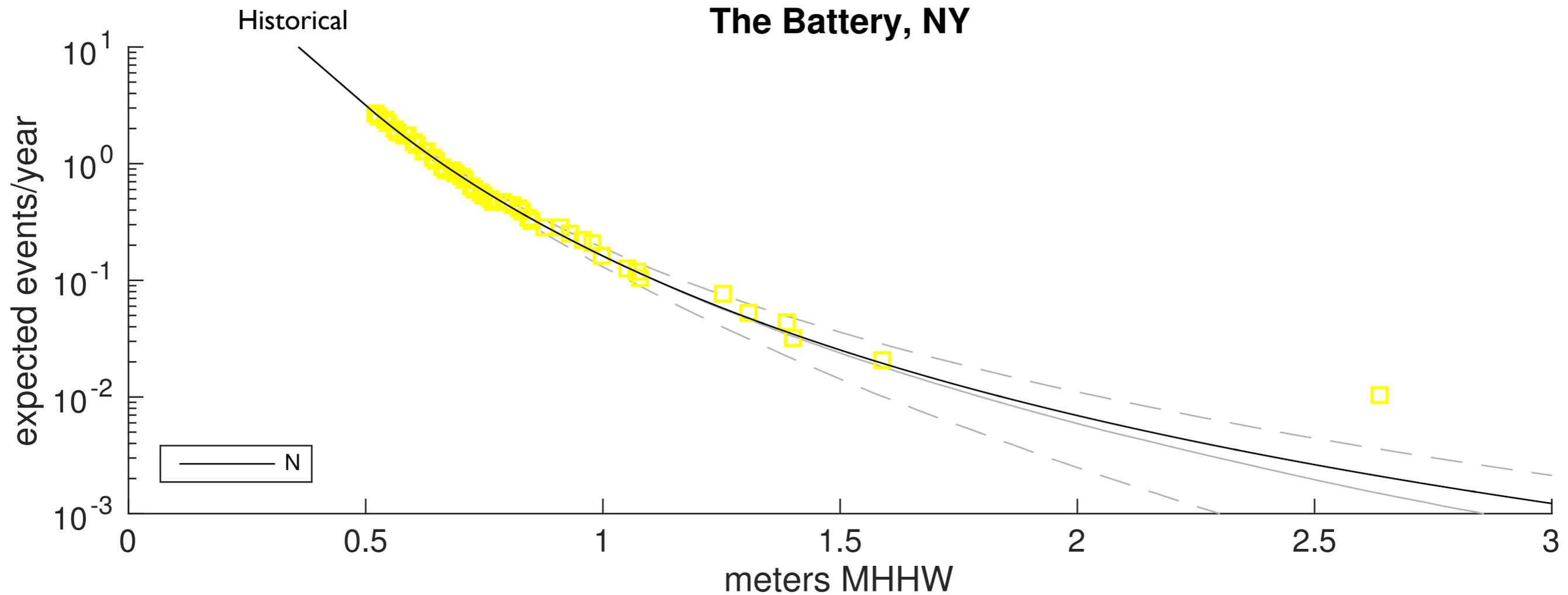
## High emissions

- K14 (sluggish ice): 0.5-1.2 m
- DP16 (fast ice): 0.9-2.4 m
- B19 (structured expert judgement): 0.6-2.4 m

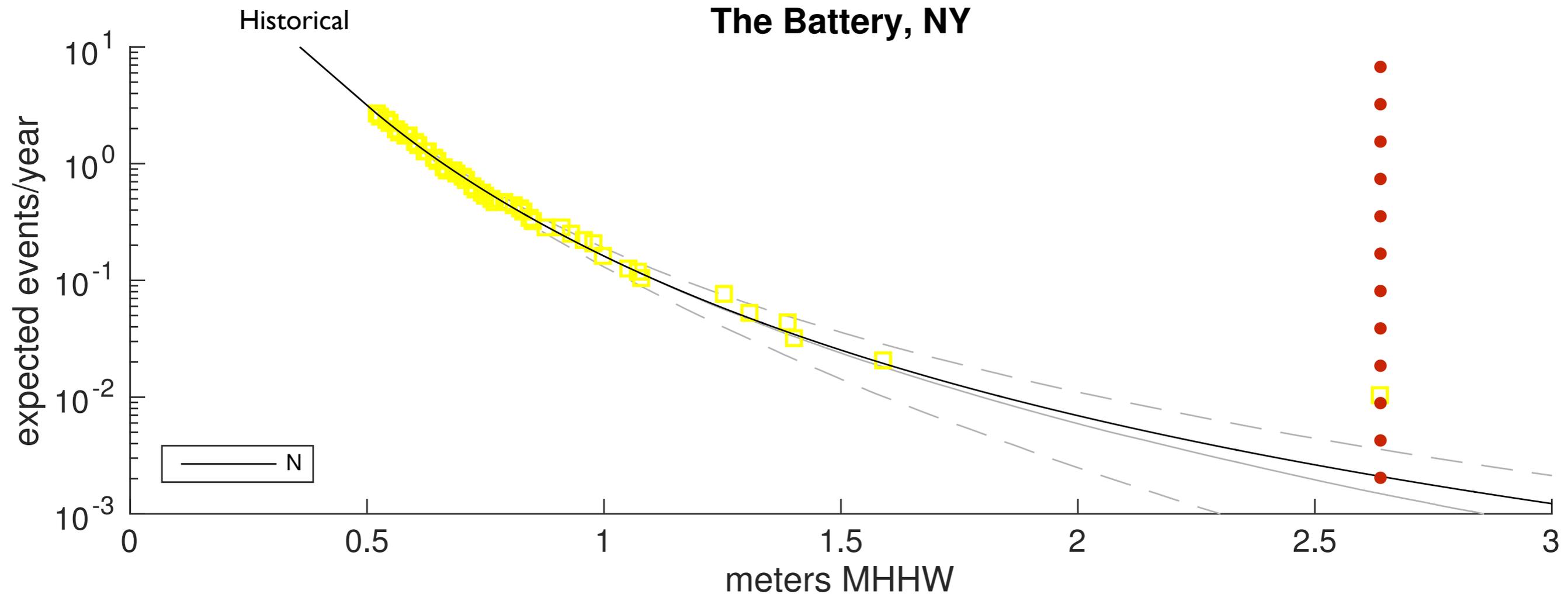
## Low emissions

- K14: 0.3-0.8 m
- DP16: 0.3-1.0 m
- B19 0.4-1.3 m

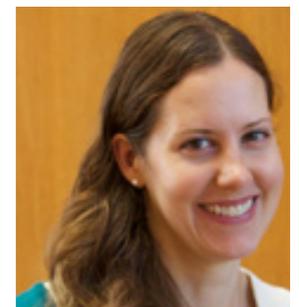
# Bayesian probabilistic projections can be cautiously combined with frequentist extreme value distributions



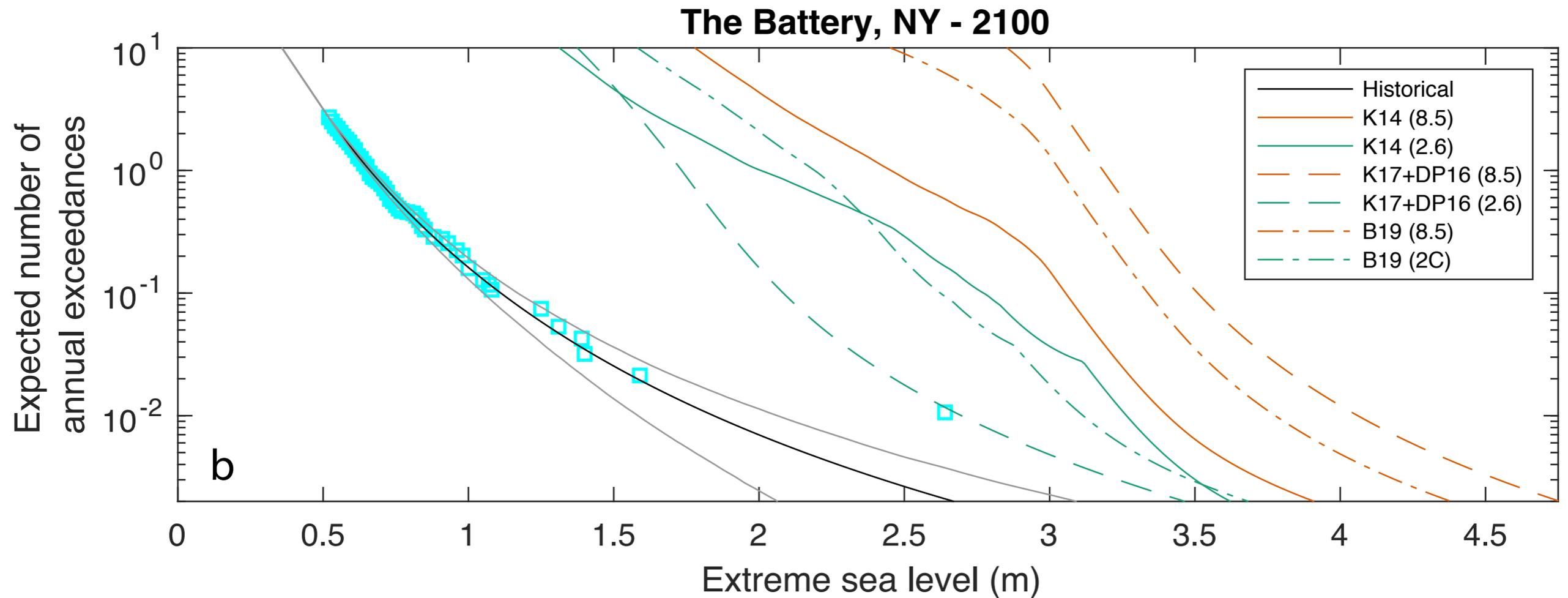
# Bayesian probabilistic projections can be cautiously combined with frequentist extreme value distributions



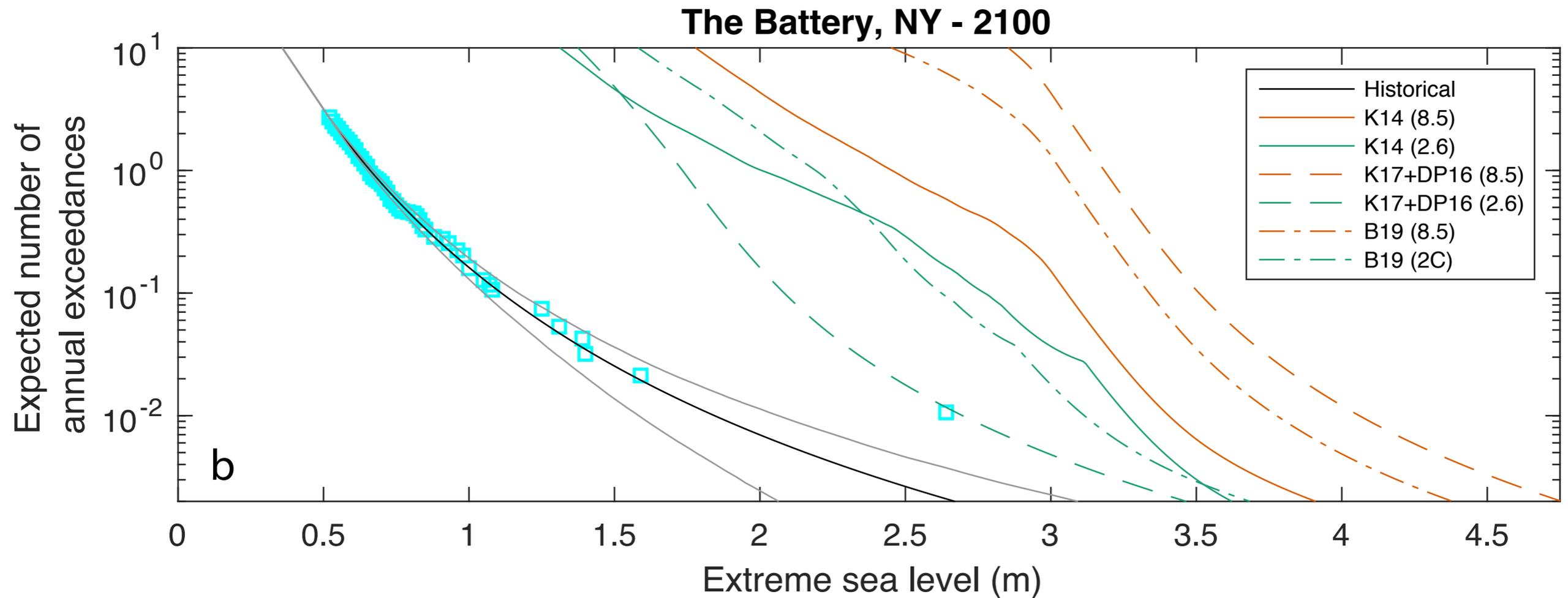
**Sandy-scale extreme sea-level (2.6 m above mean higher high water) has an expected return period of about 450 years.**



# Bayesian probabilistic projections can be cautiously combined with frequentist extreme value distributions



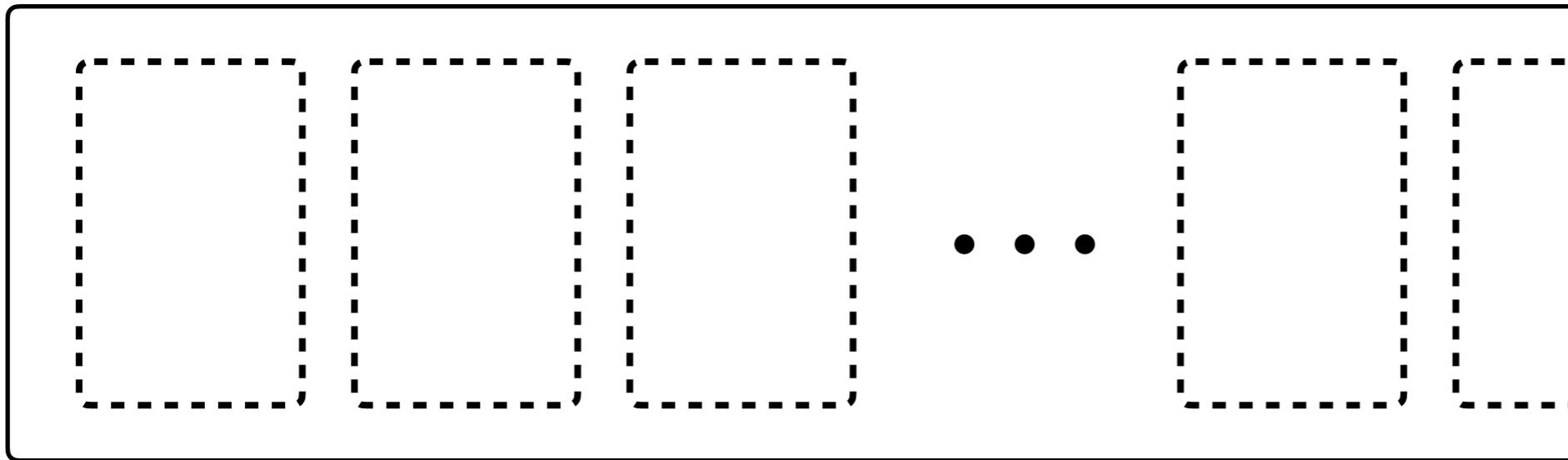
# Bayesian probabilistic projections can be cautiously combined with frequentist extreme value distributions



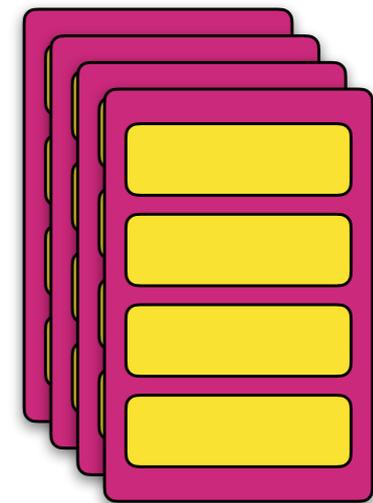
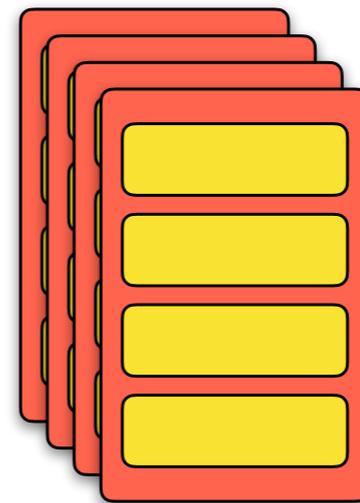
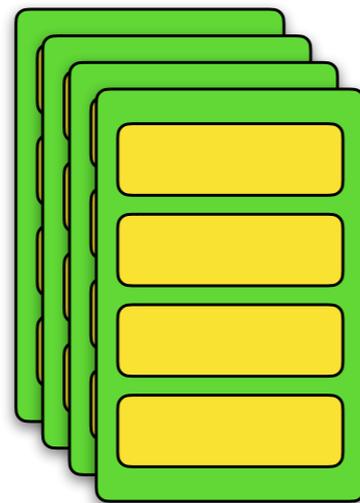
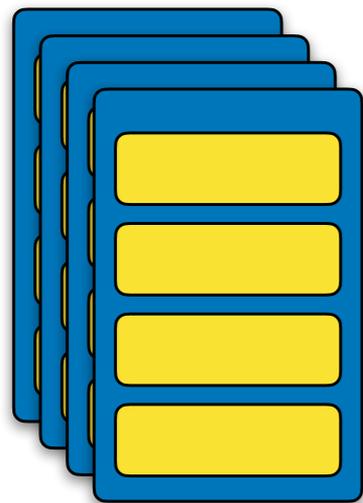
**Under low emissions, Sandy-scale extreme sea-level (2.6 m above mean higher high water, ~450 year return period) has an expected return period in 2100 under low emissions of 5–76 years and under high emissions of 2 weeks–1.5 years.**

# Toward a modular, scalable Python-based framework

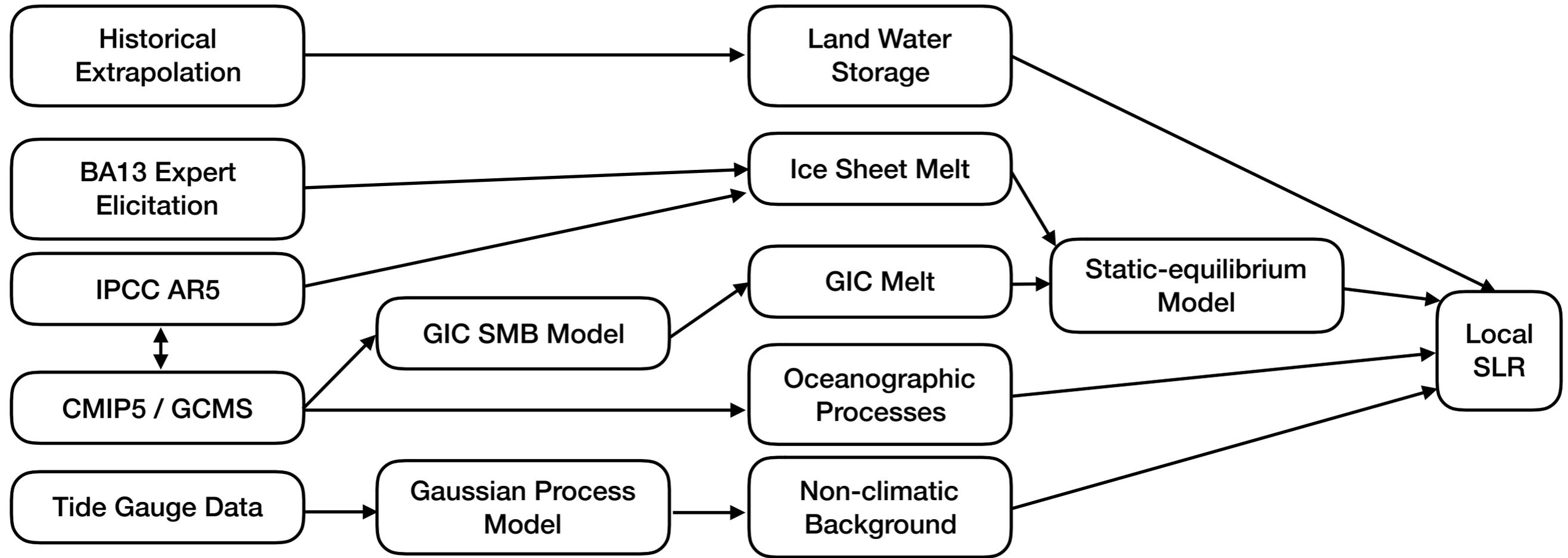
## FACTS: Framework for Assessing Changes To Sea-level



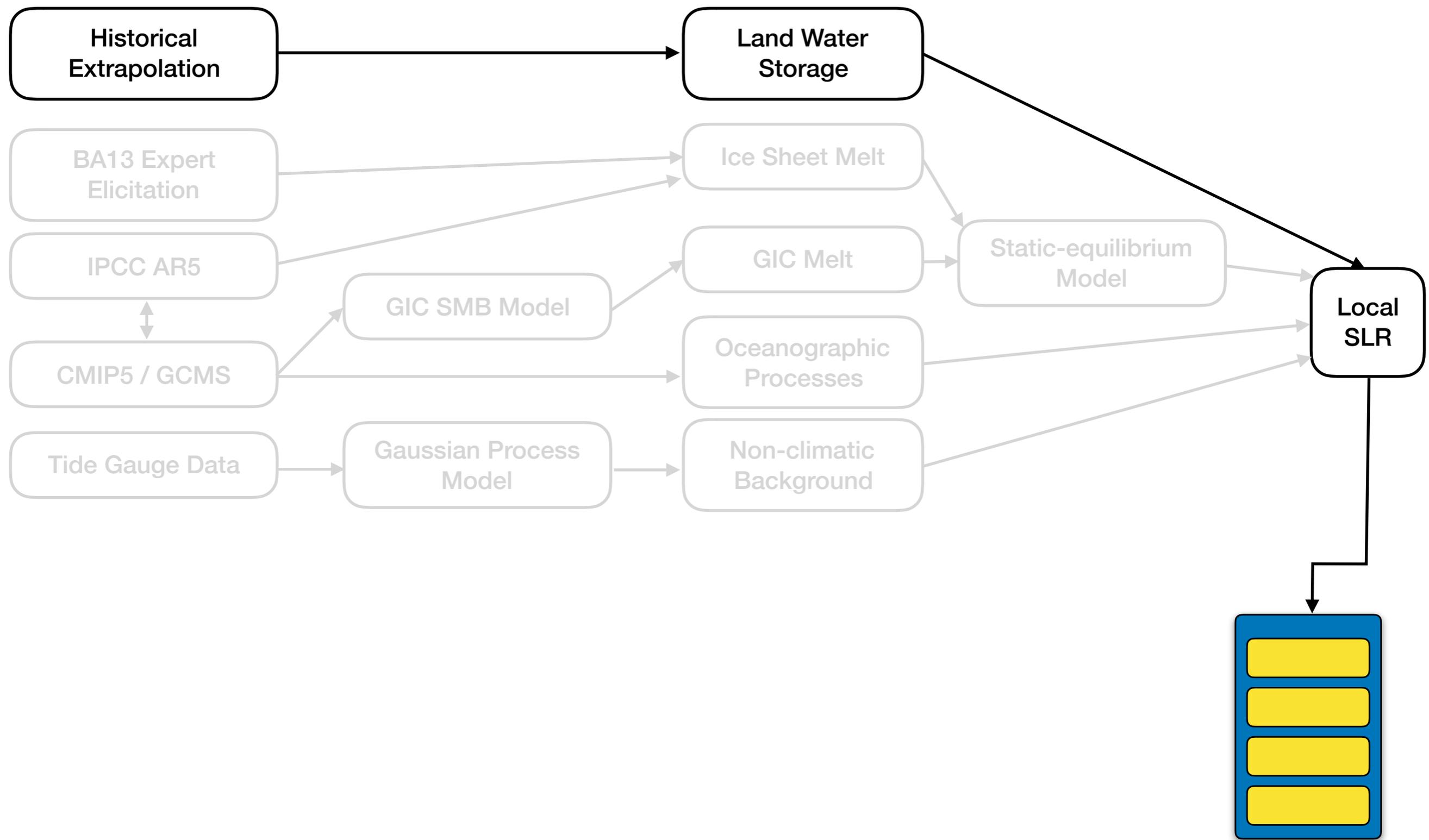
**Framework**



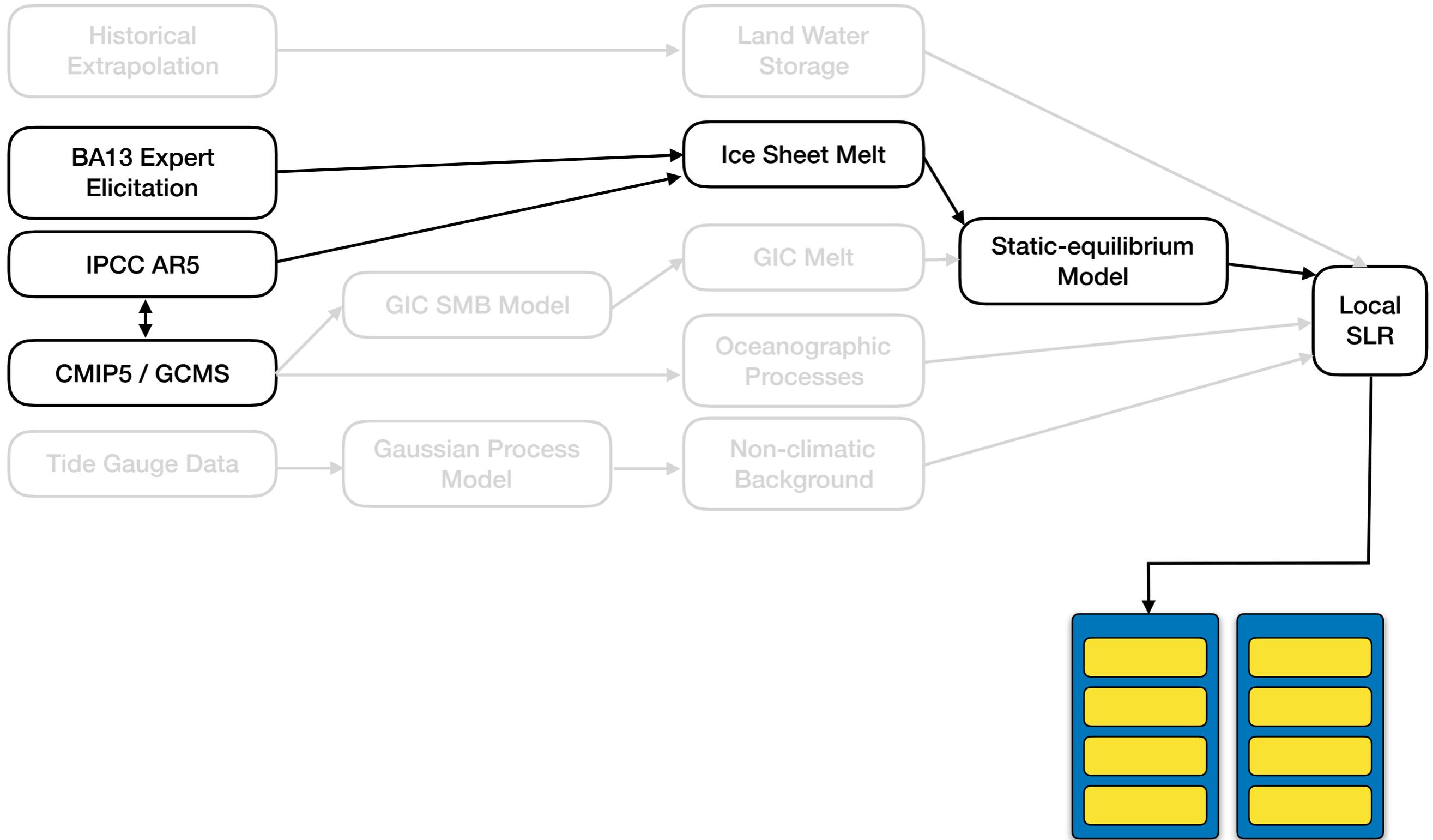
**Workflows**



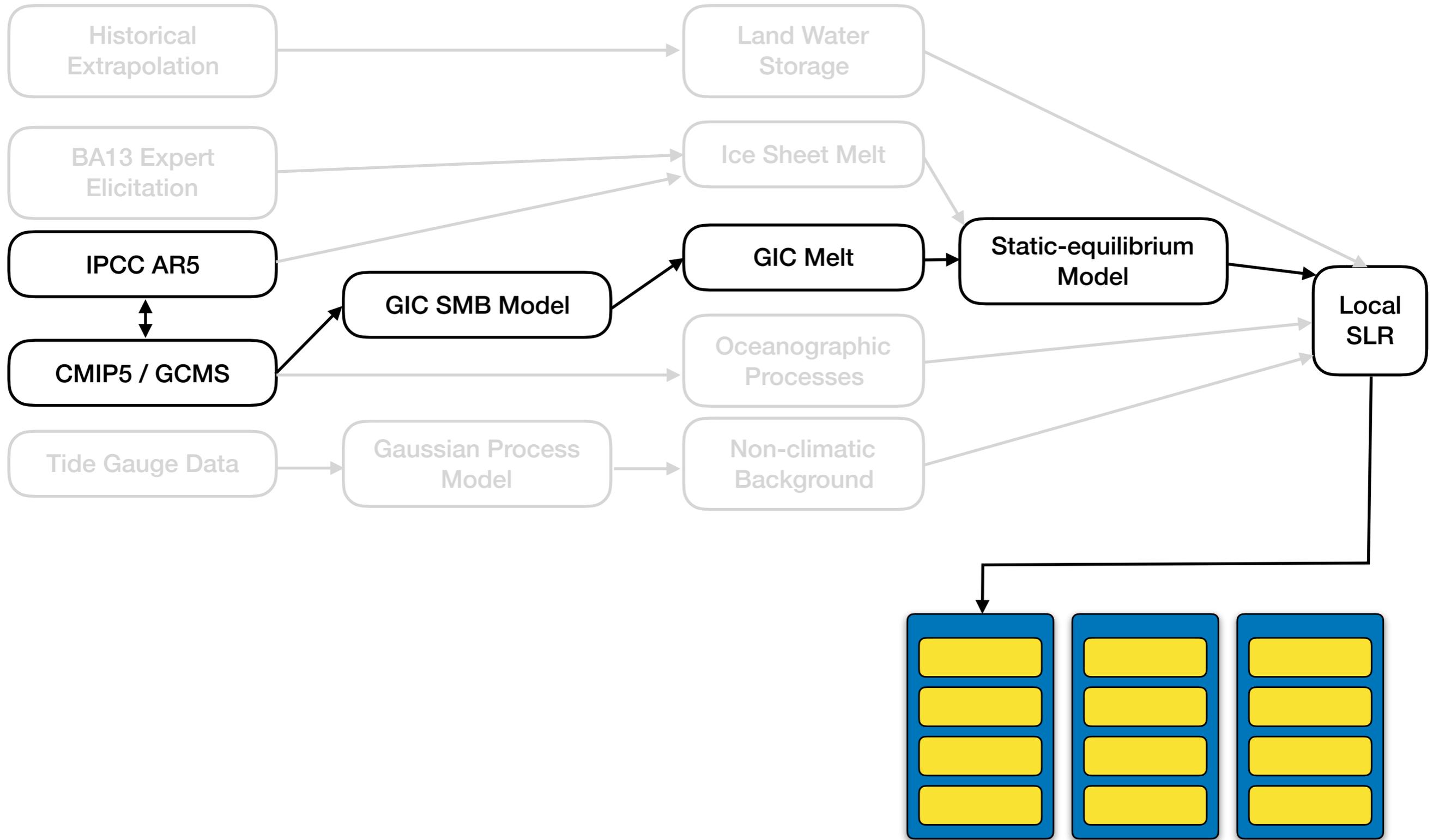
**Kopp 2014 Workflow**



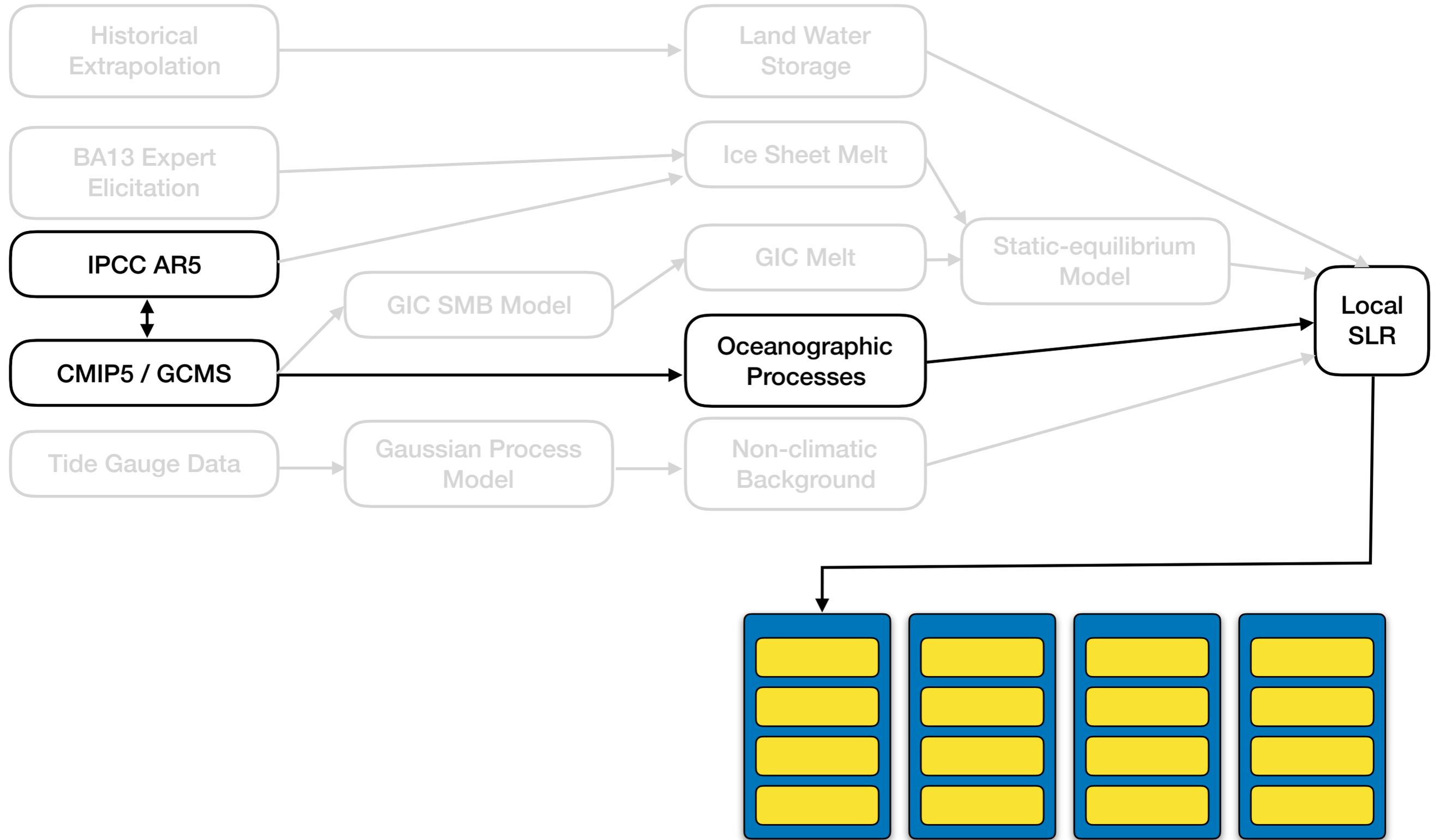
**Kopp 2014 Workflow**



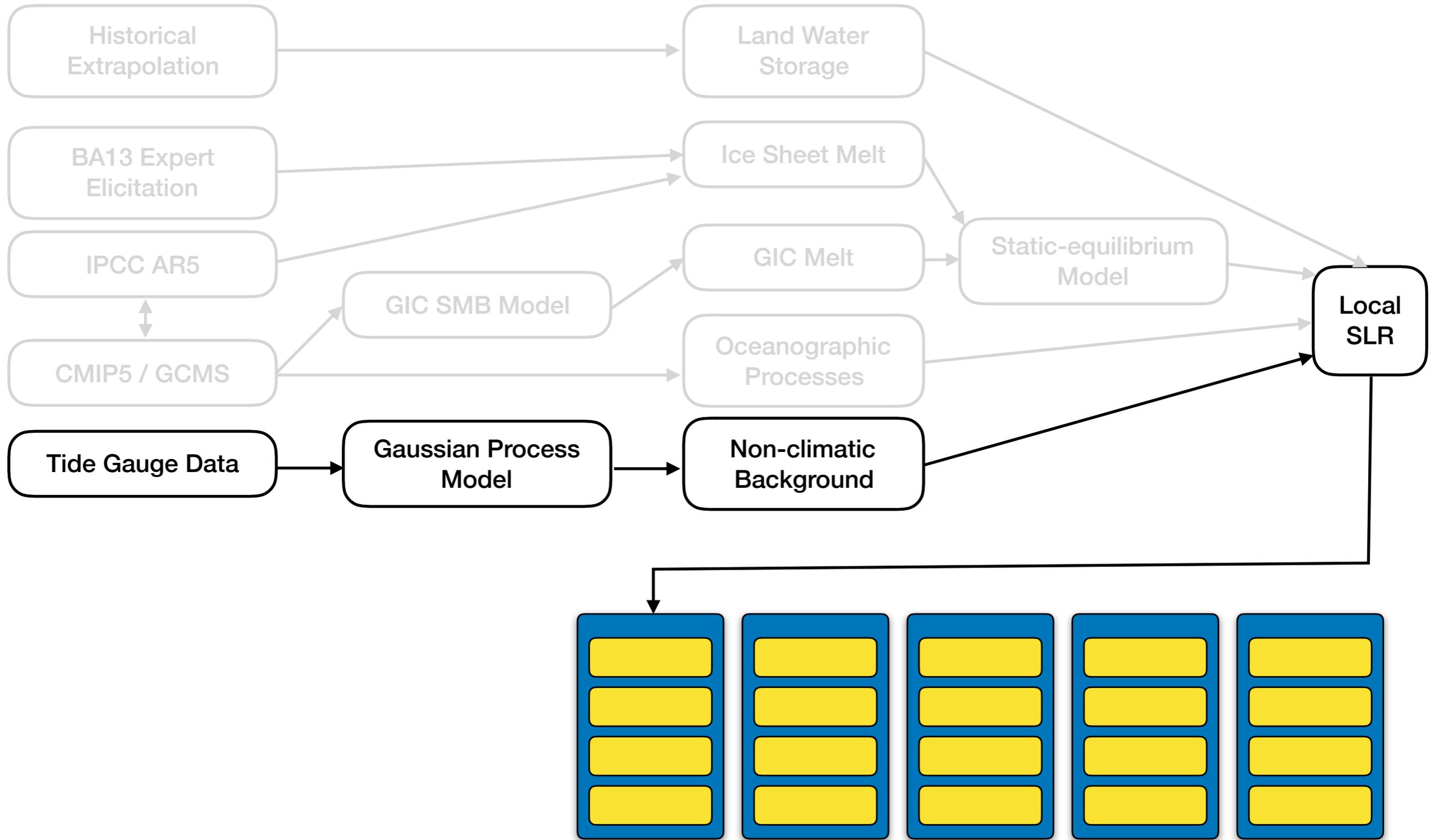
**Kopp 2014 Workflow**



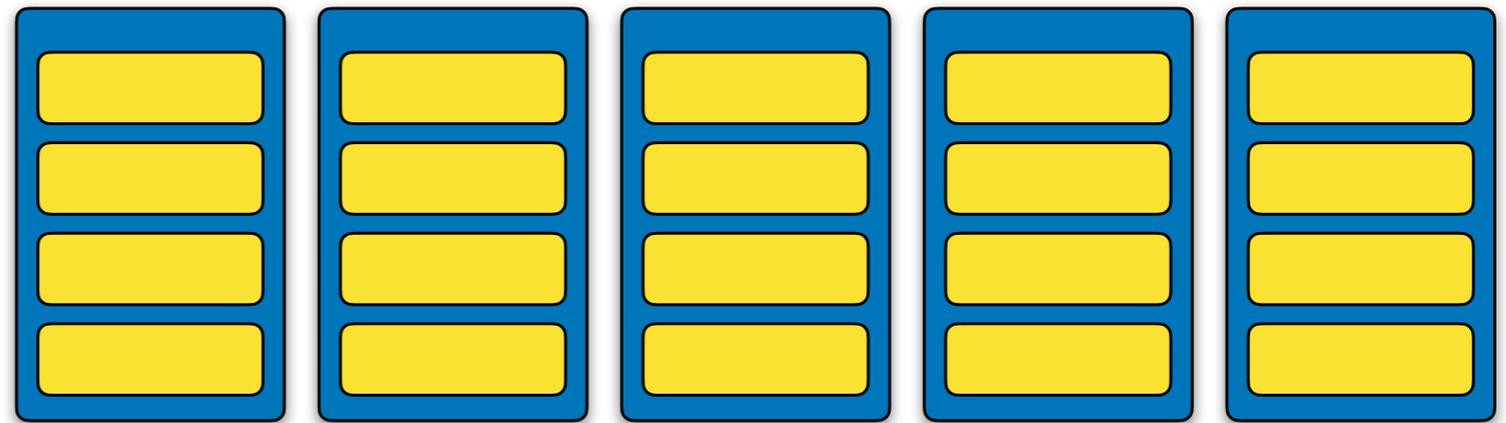
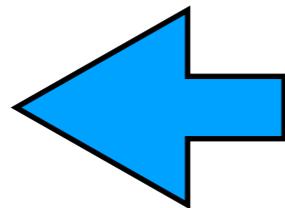
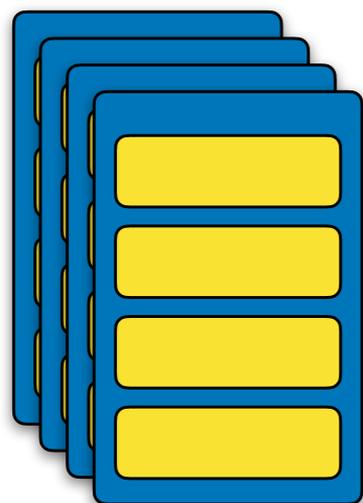
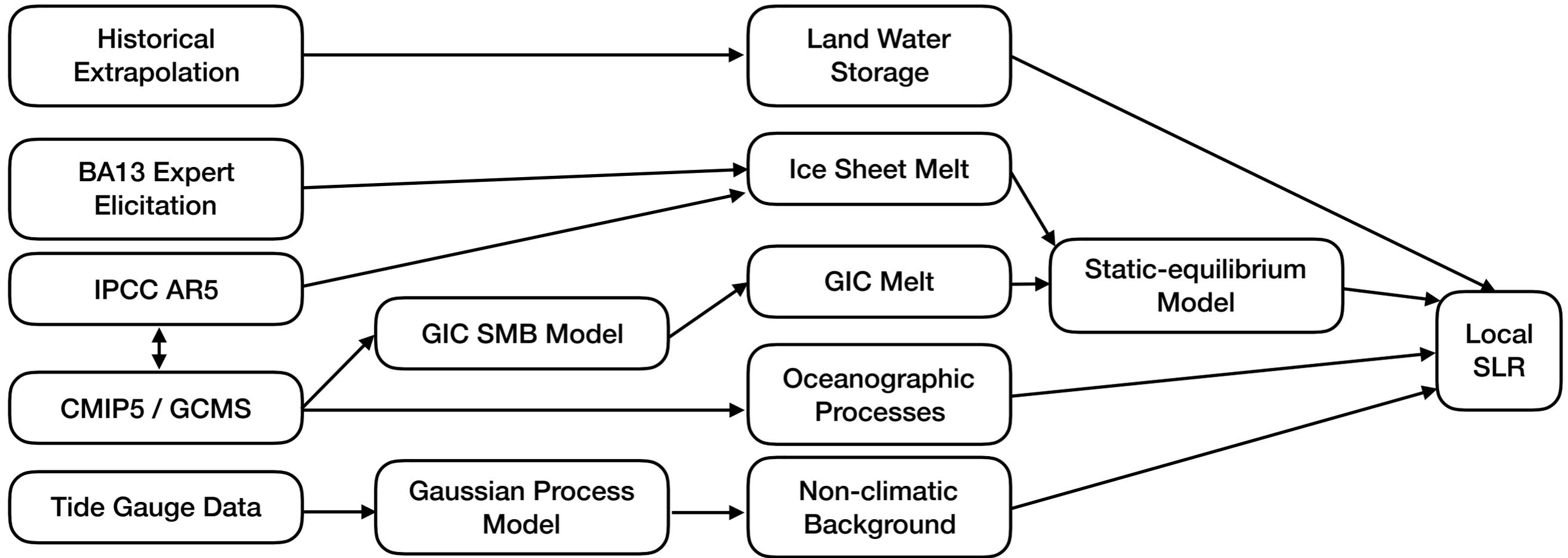
**Kopp 2014 Workflow**



**Kopp 2014 Workflow**

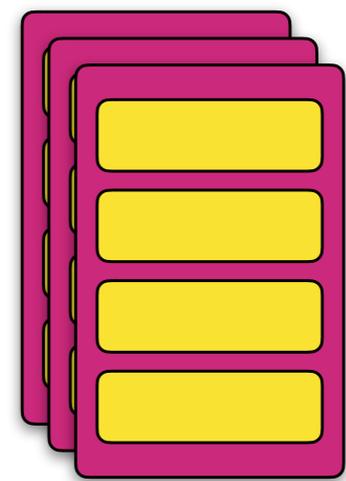
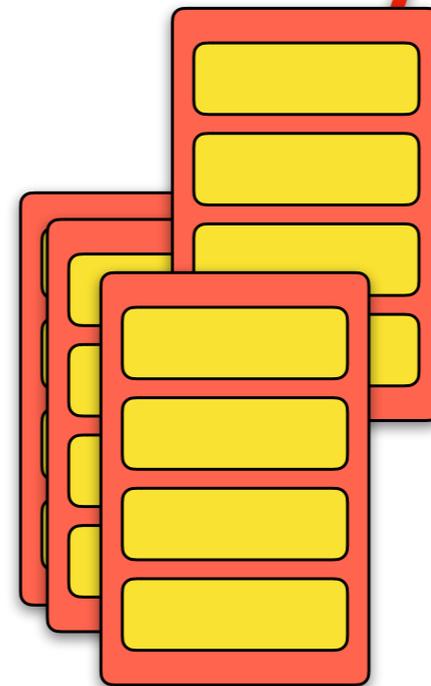
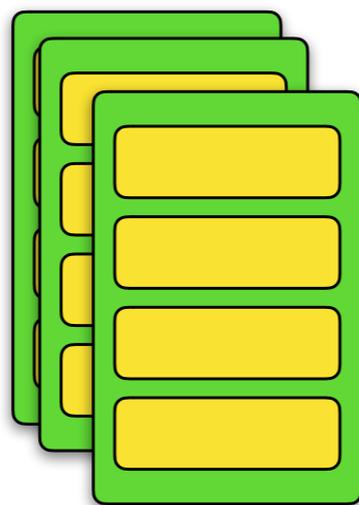
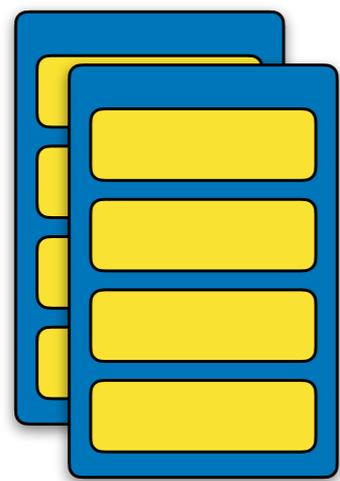
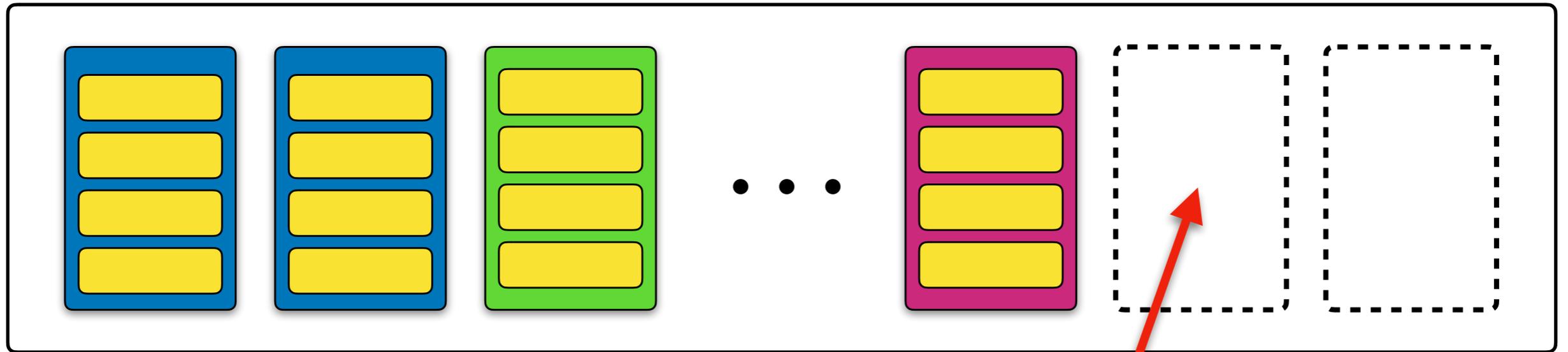


**Kopp 2014 Workflow**

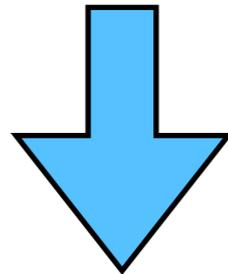
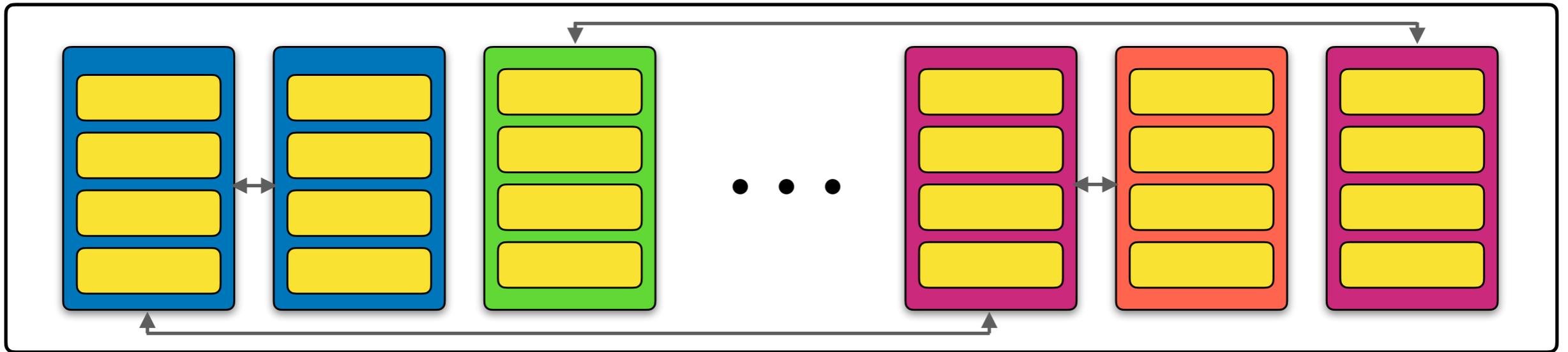


**Kopp 2014 Workflow**

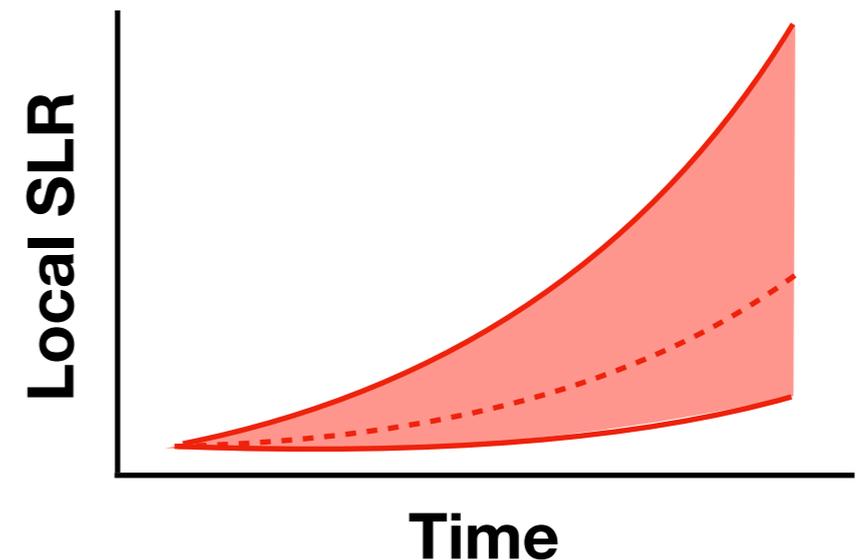
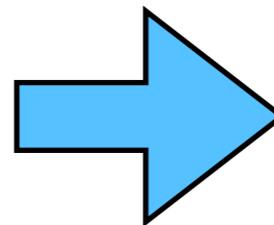
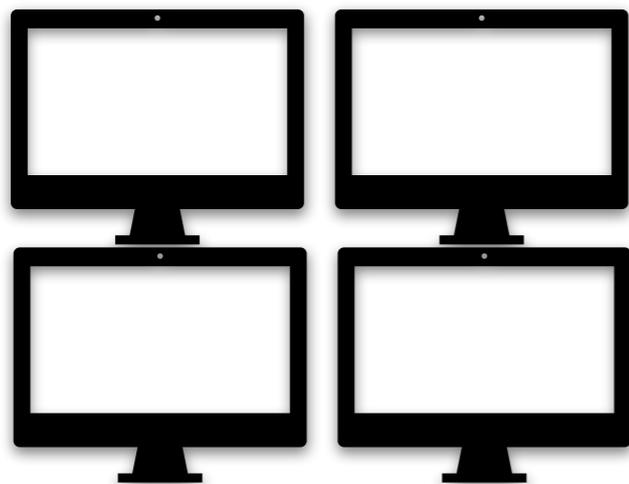
# Mix and match sub-models from multiple workflows



## Enable cross-communication among modules



Leverage local or high-performance computing resources



built upon RADICAL Cybertools – Ensemble Toolkit

## In short:

- Sea-level rise is a complex, spatiotemporally varying process of considerable societal importance.
- Reconstructions of past sea-level change provide a crucial baseline for understanding current changes, and producing these reconstructions requires fusing data from multiple different sources with different error structures, sparsity, and process-sensitivity.
- Local sea-level rise projections are a key input to coastal risk management, and require synthesizing many different lines of evidence. In some cases, alternative approaches to estimating different processes highlight areas of deep uncertainty.
- We are working to produce flexible, scalable, open-source tools to facilitate both these tasks.

# Mapping sea-level change in time, space, and probability

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