

Fluctuation studies in Phobos

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for the  collaboration

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Workshop on “Correlations and fluctuations ”
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PHOBOS collaboration (July 2006)

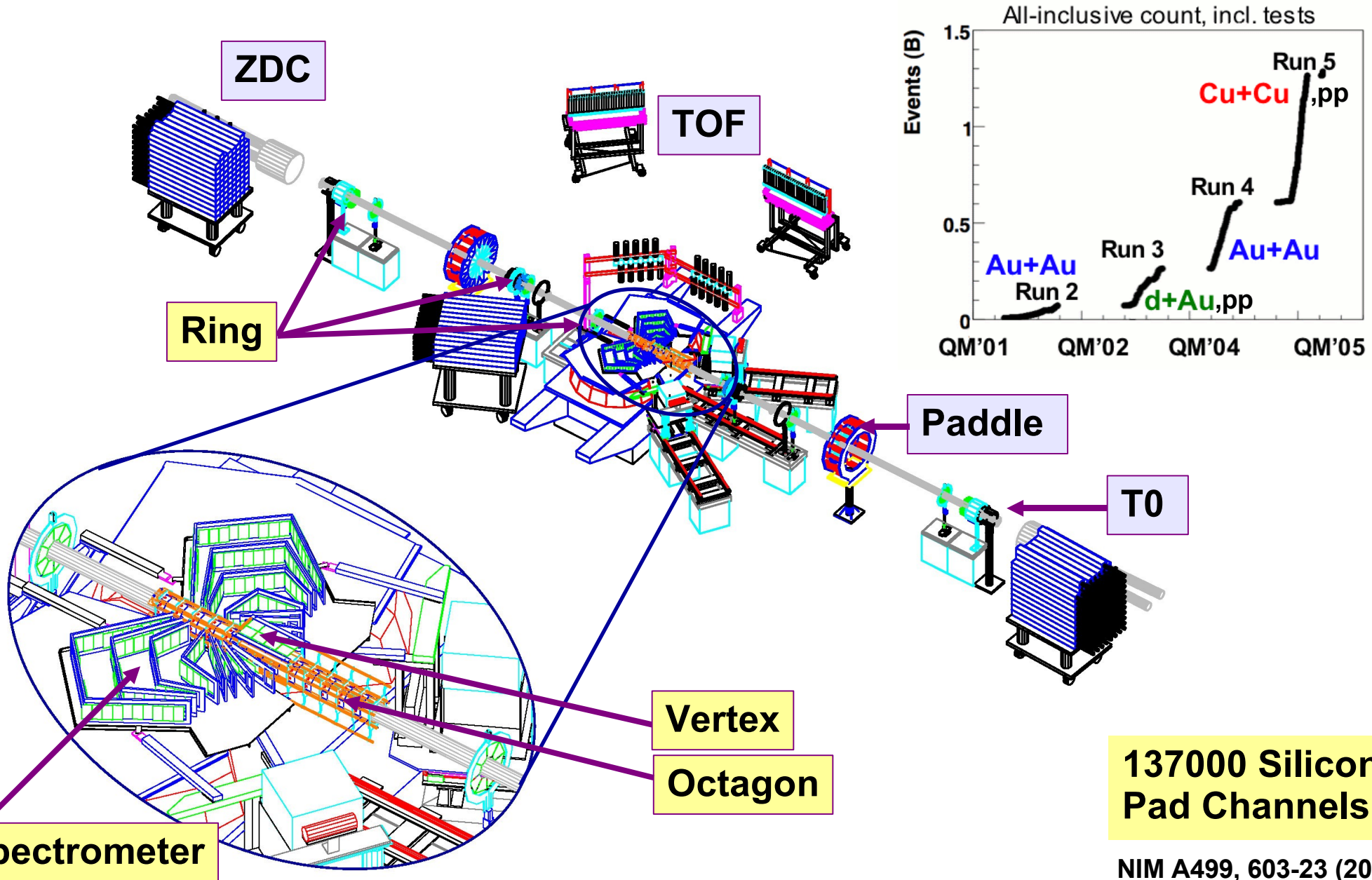


Burak Alver, Birger Back, Mark Baker, Maarten Ballintijn, Donald Barton, Russell Betts, **Richard Bindel**, Wit Busza (Spokesperson), Zhengwei Chai, **Vasundhara Chetluru**, Edmundo García, **Tomasz Gburek**, Kristijan Gulbrandsen, Clive Halliwell, **Joshua Hamblen**, **Ian Harnarine**, Conor Henderson, David Hofman, Richard Hollis, Roman Hołyński, Burt Holzman, Aneta Iordanova, Jay Kane, Piotr Kulinich, Chia Ming Kuo, **Wei Li**, Willis Lin, Constantin Loizides, Steven Manly, Alice Mignerey, Gerrit van Nieuwenhuizen, Rachid Nouicer, Andrzej Olszewski, Robert Pak, **Corey Reed**, **Eric Richardson**, Christof Roland, Gunther Roland, **Joe Sagerer**, Iouri Sedykh, Chadd Smith, **Maciej Stankiewicz**, Peter Steinberg, George Stephans, Andrei Sukhanov, **Artur Szostak**, Marguerite Belt Tonjes, Adam Trzupek, **Sergei Vaurynovich**, Robin Verdier, Gábor Veres, **Peter Walters**, **Edward Wenger**, **Donald Wilhelm**, Frank Wolfs, Barbara Wosiek, Krzysztof Woźniak, **Shaun Wyngaardt**, Bolek Wyślouch

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PHOBOS experiment (Run5)

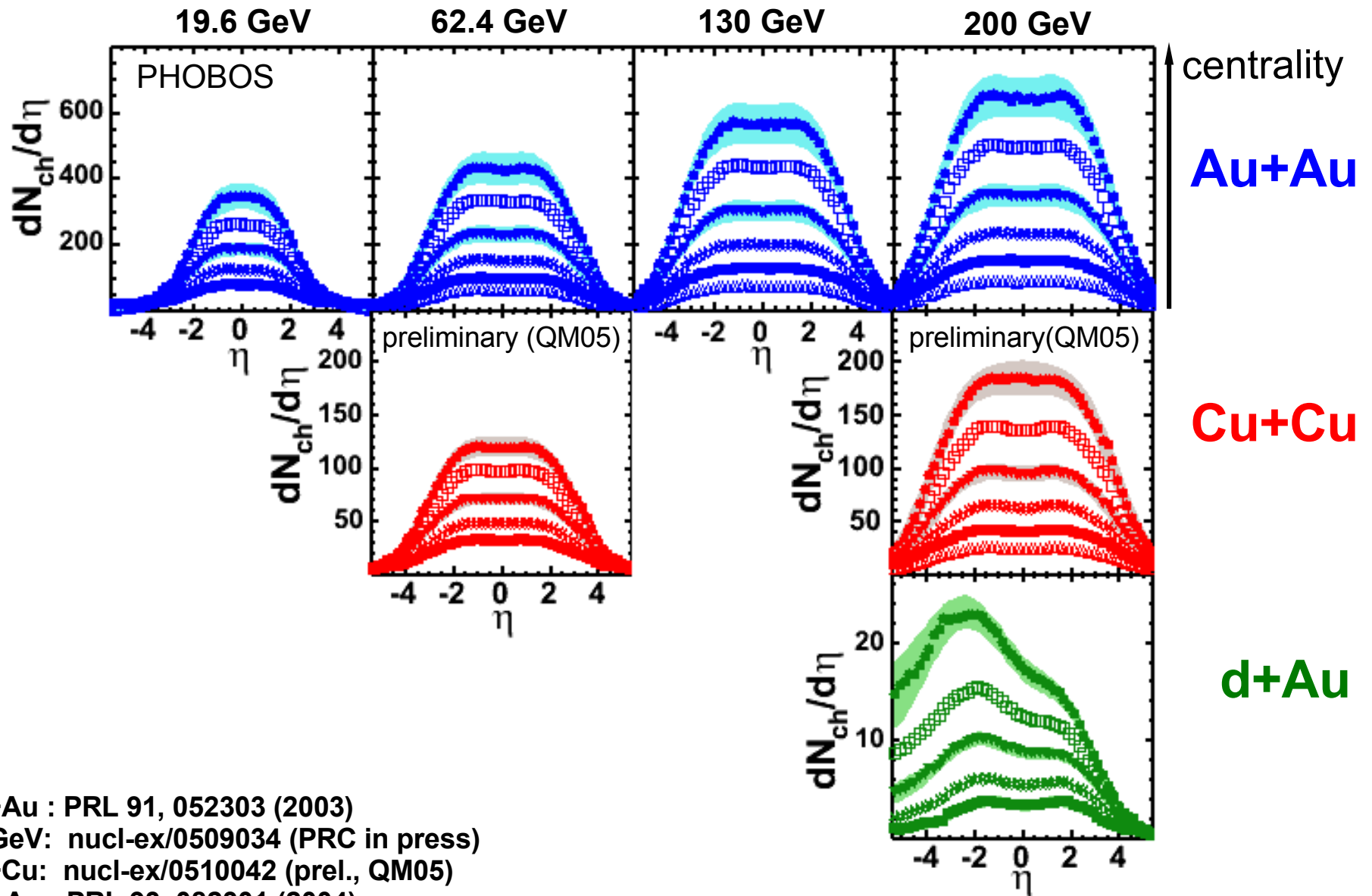


NIM A499, 603-23 (2003)

Outline

- 1) Single-particle distributions
- 2) Unusual event search
- 3) Forward/backward multiplicity correlations
- 4) Two-particle angular correlations
- 5) Eccentricity fluctuations
- 6) Elliptic flow fluctuations

Charged hadron $dN/d\eta$ -distributions (1)



Au+Au : PRL 91, 052303 (2003)
 62 GeV: nucl-ex/0509034 (PRC in press)
 Cu+Cu: nucl-ex/0510042 (prel., QM05)
 d+Au : PRL 93, 082301 (2004)

Charged hadron $dN/d\eta$ -distributions (2)

- Rich data set of p+p, p+A and A+A
- Scaling features of charged hadron multiplicities
 - Npart scaling
 - Limiting Fragmentation
 - Factorization of energy/centrality dependence
 - Universality of total multiplicity in A+A, p+p and e^+e^-
- Seen over a wide range of collision energy

Charged hadron $dN/d\eta$ -distributions (2)

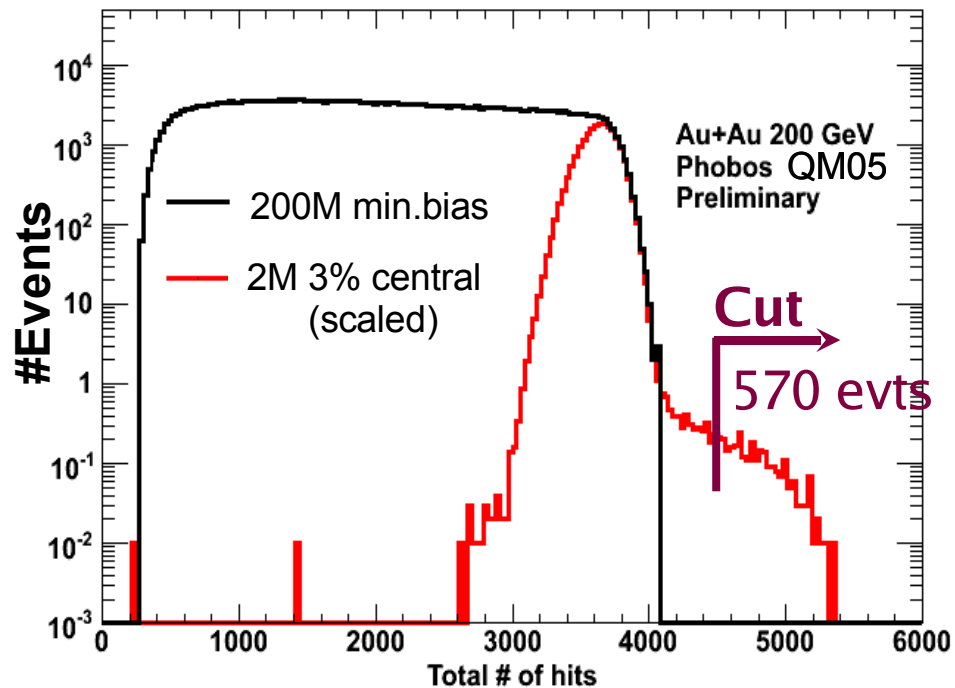
- Rich data set of p+p, p+A and A+A
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In all of the above, $dN/d\eta$ is
single-particle event average

2) Unusual event search

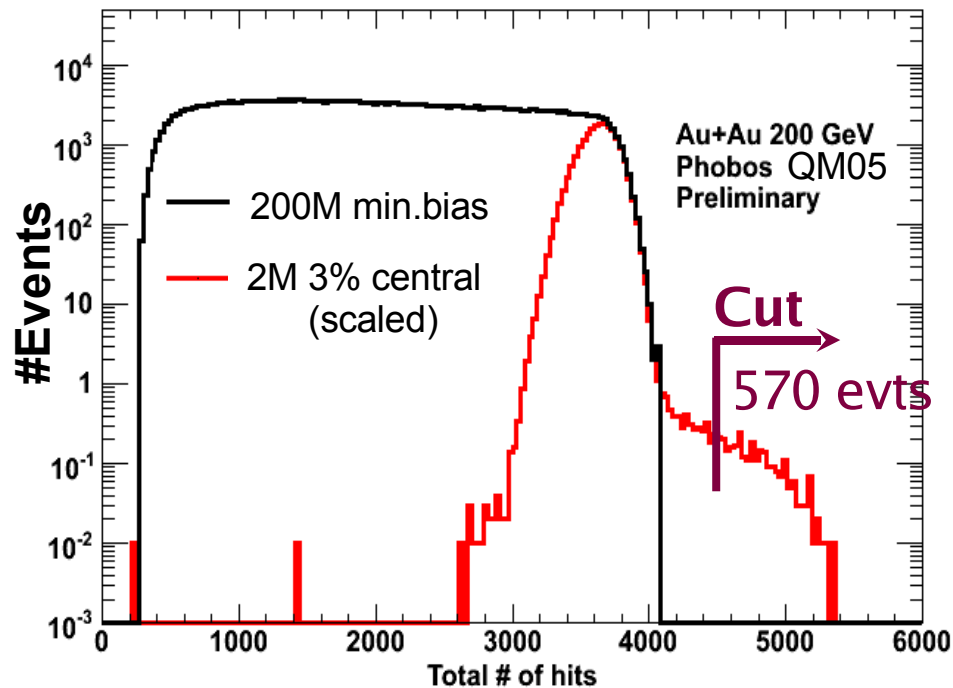
- Beyond the average $dN/d\eta$
 - Are there events with very large multiplicity?
 - Does the $dN/d\eta$ shape vary from event to event?

Unusual events: Large total multiplicity

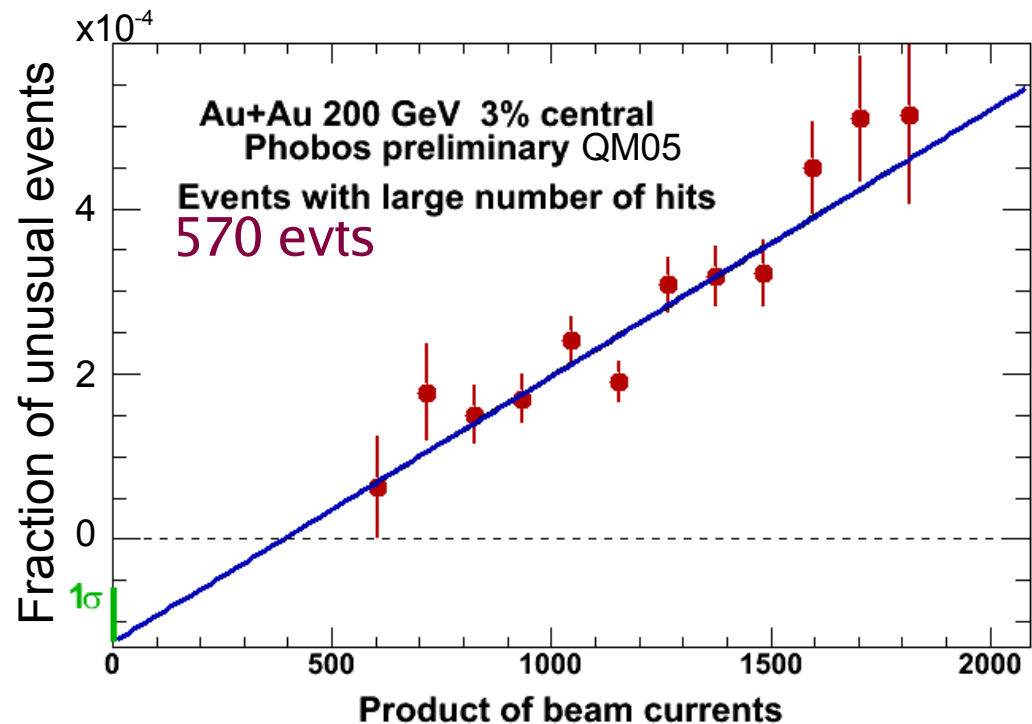


- Use high-statistics Run-4 AuAu data and select 3% central data (with loose data-quality cuts)
- Look at events with a large number of hits: $\sim 10^{-4}$ (570/2M) events

Unusual events: Large total multiplicity

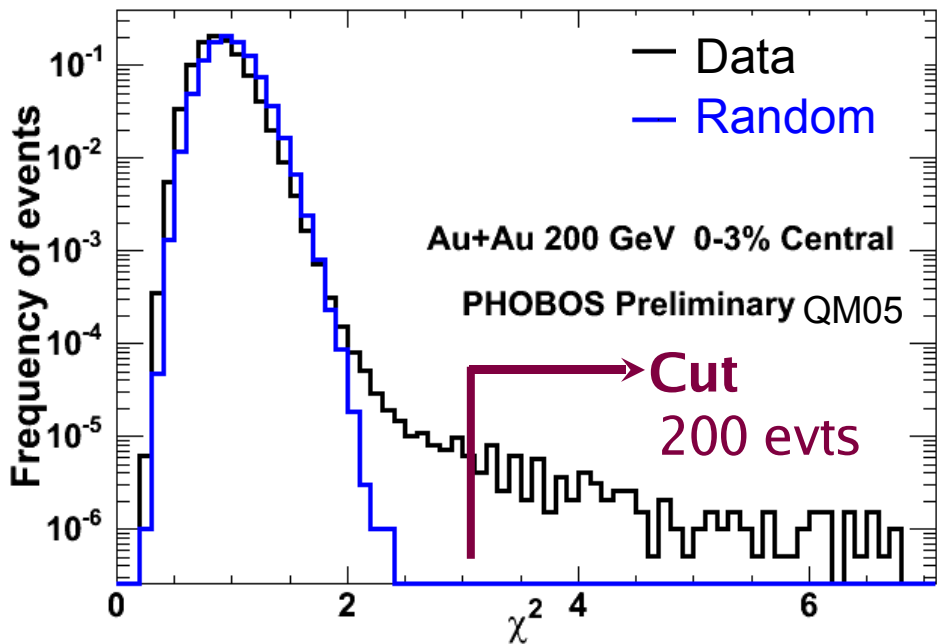


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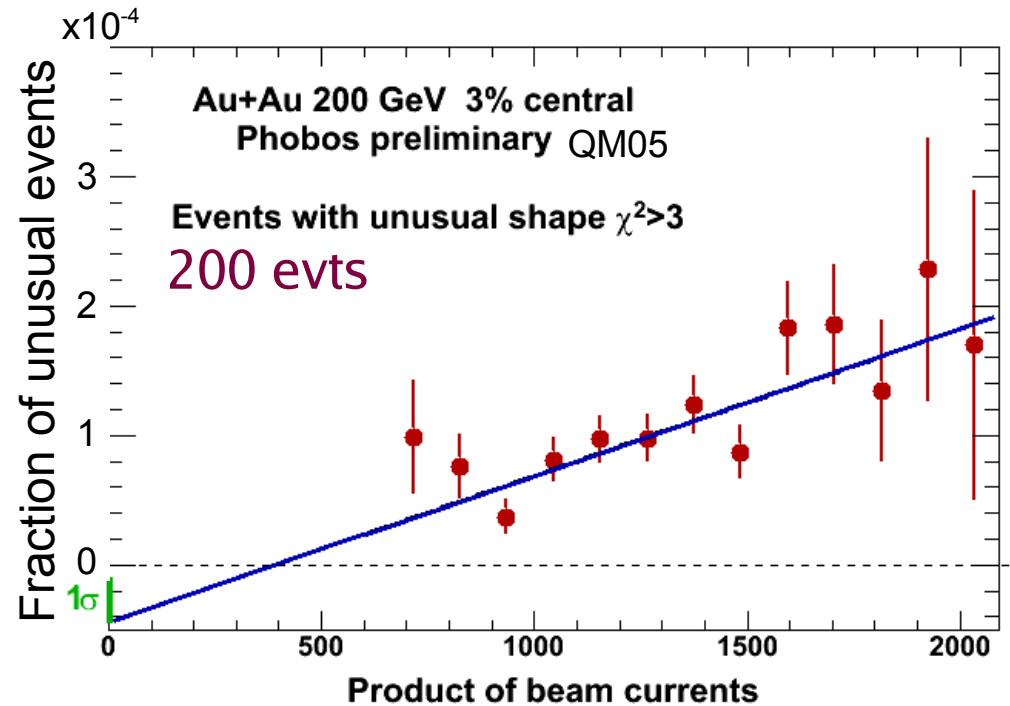


- Events with large number of hits are strongly correlated with beam rate
- Rate of “unusual” events extrapolated to low luminosity is consistent with zero

Unusual events: $dN/d\eta$ -shape



- Devide $dN/d\eta$ into individual bins (η , vertex) to get the average and its variance
- Calculate χ^2 for each event
- Compare to “random” events: distinct tail $\sim 10^{-4}$ (200/2M) events

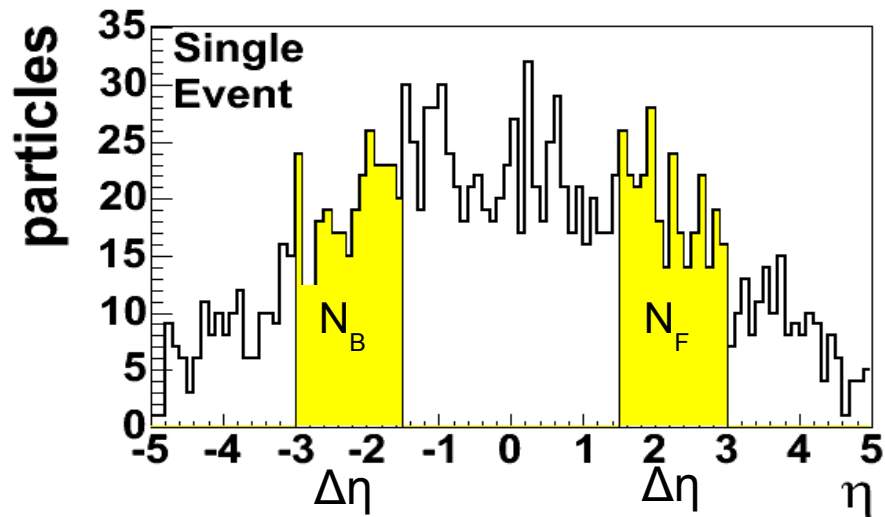


- Events with large χ^2 are again strongly correlated with beam rate
- Rate of “unusual” events extrapolated to low luminosity is again consistent with zero

3) Forward/backward multiplicity fluctuations

- Beyond the average $dN/d\eta$
 - Quantify E-by-E correlations in particle-production over regions in η

Forward/backward multiplicity fluctuations



- Independent particle production

$$\sigma_C^2 = 1$$

- Correlated particle production

- Long range $\sigma_C^2 \rightarrow 0$

- Short range $\sigma_C^2 > 1$

- Clusters of size k within $\Delta\eta$

$$C \rightarrow \sqrt{k} C$$

$$\sigma_C^2 \rightarrow k \sigma_C^2$$

- If limited rapidity window ($\Delta\eta$)

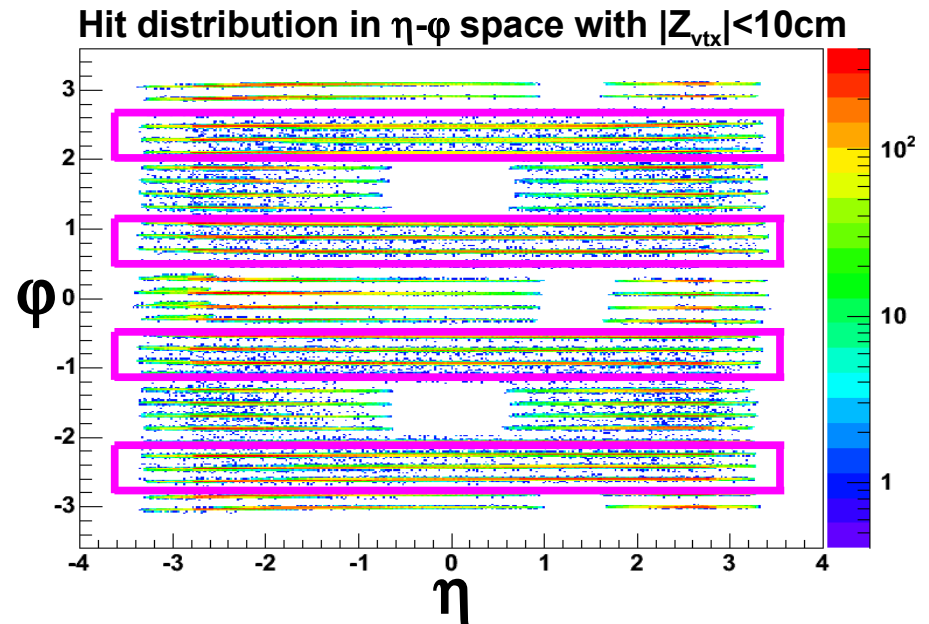
$$k \rightarrow k_{eff}$$

$$C(\eta, \Delta\eta) = \frac{N_F - N_B}{\sqrt{N_F + N_B}}$$

Use variance σ_C^2

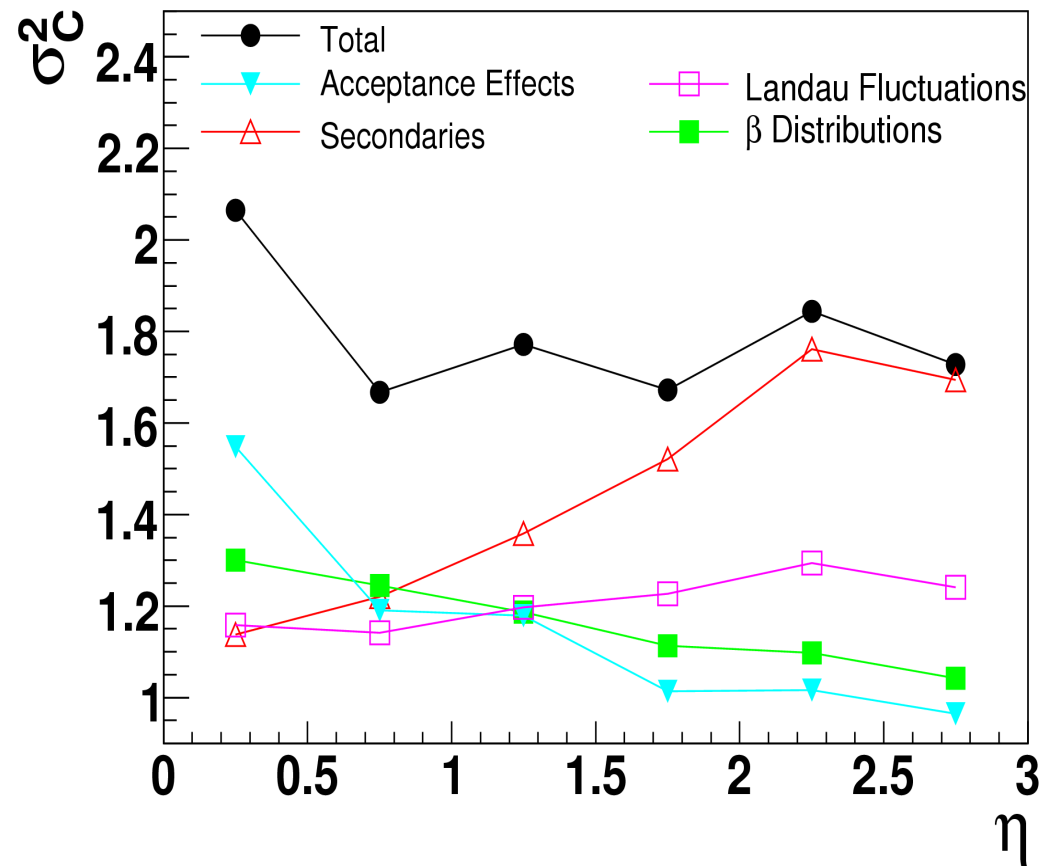
Extraction of σ_C^2

- Deal with large occupancy in the octagon
 - Use η -bin-dependent lower and upper dE/dx cuts on hits to suppress contribution from secondaries
- Deal with limited acceptance
 - Correct gap effects E-by-E with z-vertex dependent offset
 - Avoiding holes in octagon
 - Only **half** acceptance in ϕ
 - Correction **~ 2** , found with MC
- Deal with contribution of detector effect (see next slides)



Contributing sources of detector effects

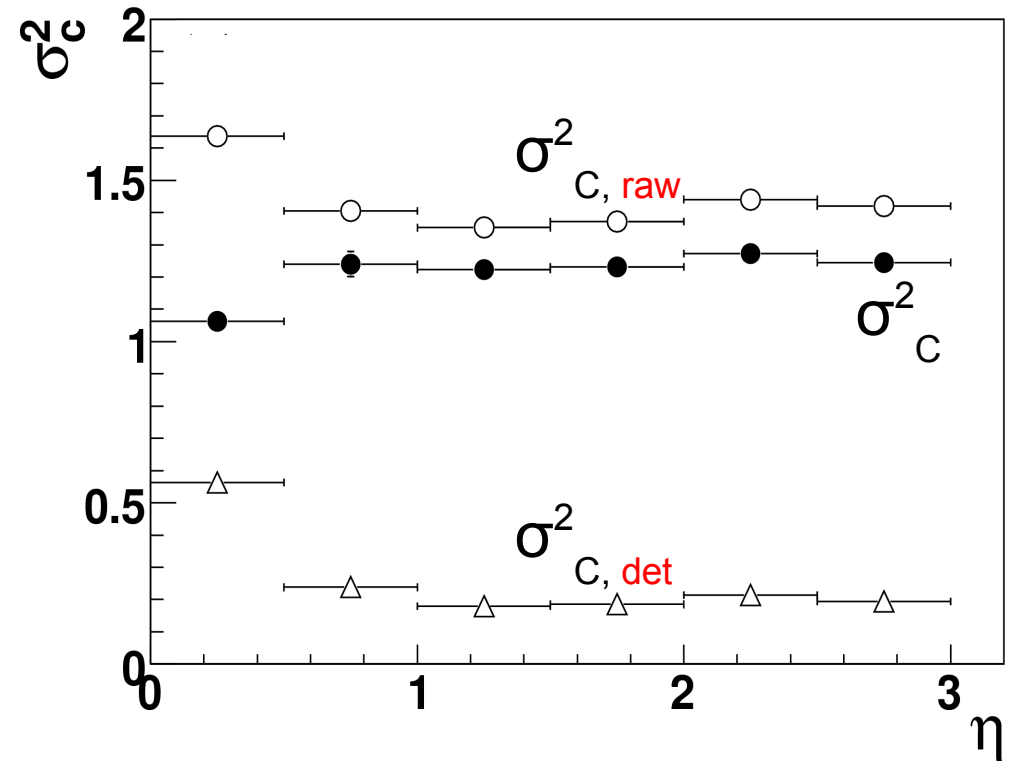
- Acceptance effects
- Secondaries
- dE/dx fluctuations
 - Landau fluctuation
 - Velocity (β) variation



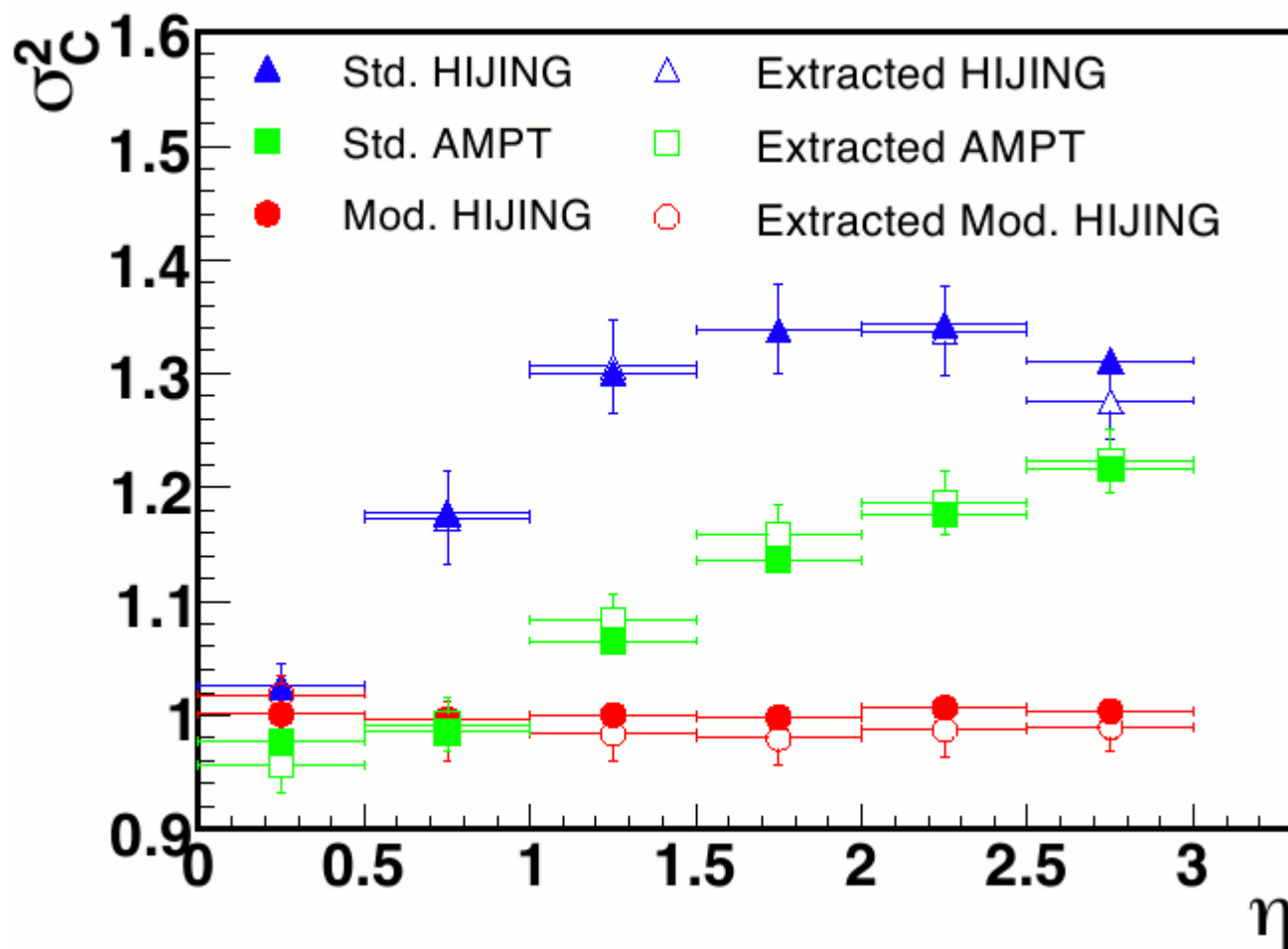
Different contributions add in quadrature and resulting detector effects are flat in η

Removing detector effects

- Assuming $\sigma_{C, \text{raw}}^2 = \sigma_C^2 + \sigma_{C, \text{det}}^2$
- Modified HIJING with randomized sign of particle η to force $\sigma_C^2 = 1$
 - Direct access to $\sigma_{C, \text{det}}^2$
- Correction slightly depends on size of signal
 - Cure residual correlation
 $\sigma_{C, \text{det}}^2 \rightarrow \sigma_{C, \text{det}}^2 - \alpha (\sigma_C^2 - 1)$
 - $\alpha = \text{constant}(\eta, \Delta\eta, \text{cent})$
- Systematic errors estimated to $\Delta\sigma_C^2 = 0.1$ (averaged over η)

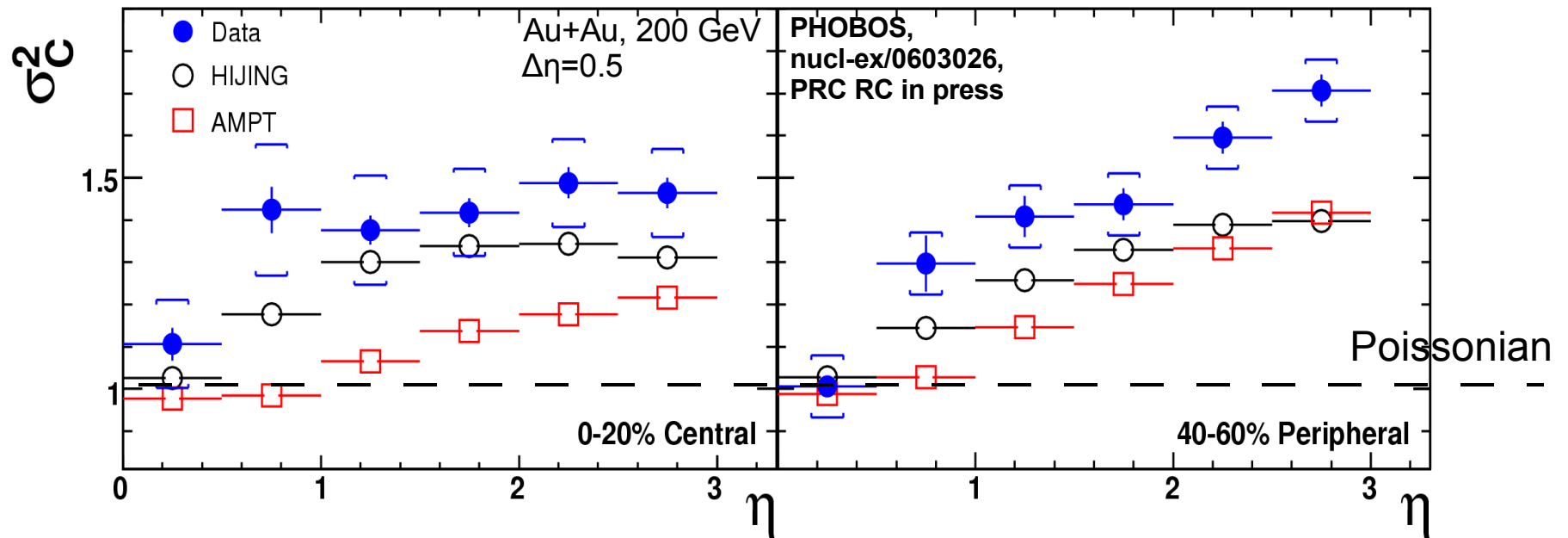


Verification with various MC

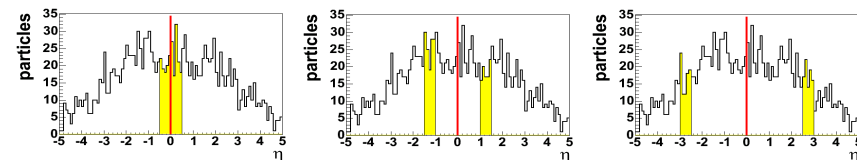


For the same tuning, the reconstructed σ_c^2 agrees with raw σ_c^2 within the errors in all tested models

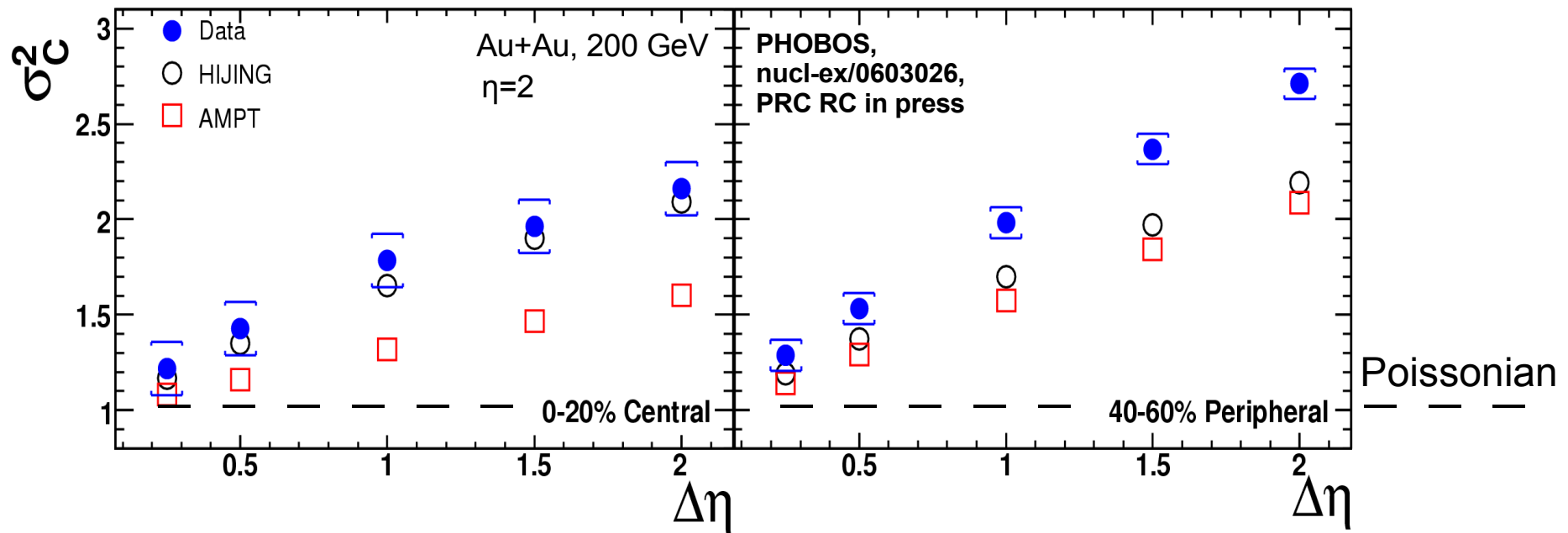
F/B results: σ_C^2 vs. η for fixed $\Delta\eta$



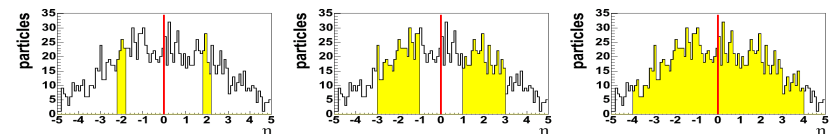
- Centrality dependence in slope observed
 - Models systematically lower (partially within errors)
- HIJING & AMPT agree in peripheral, but diverge in central events
- At $\eta=0$, models and data yield $\sigma_C^2=1$
 - Induced “intrinsic” long-range correlations?



F/B results: σ_C^2 vs. $\Delta\eta$ at fixed $\eta=2$

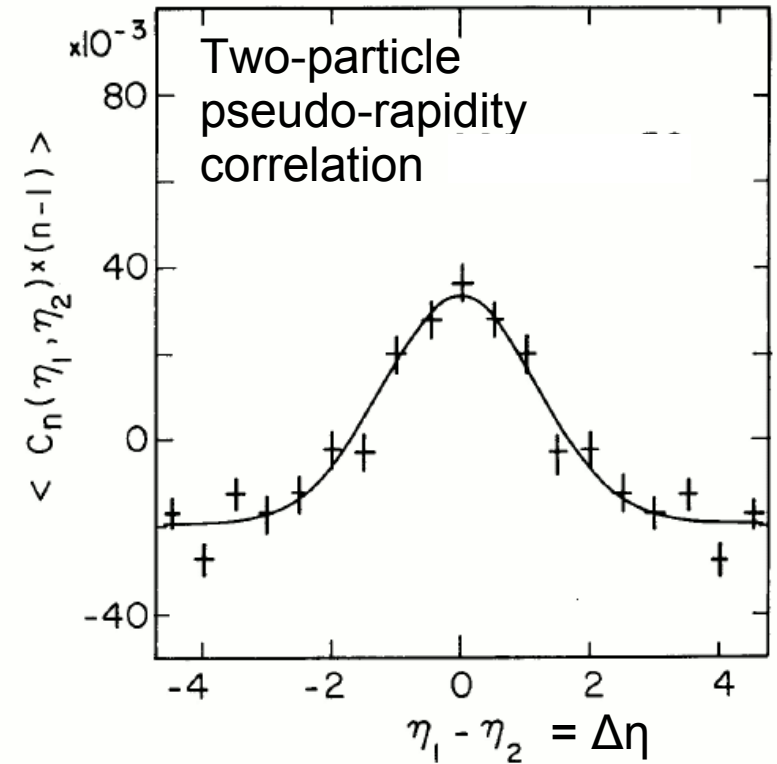
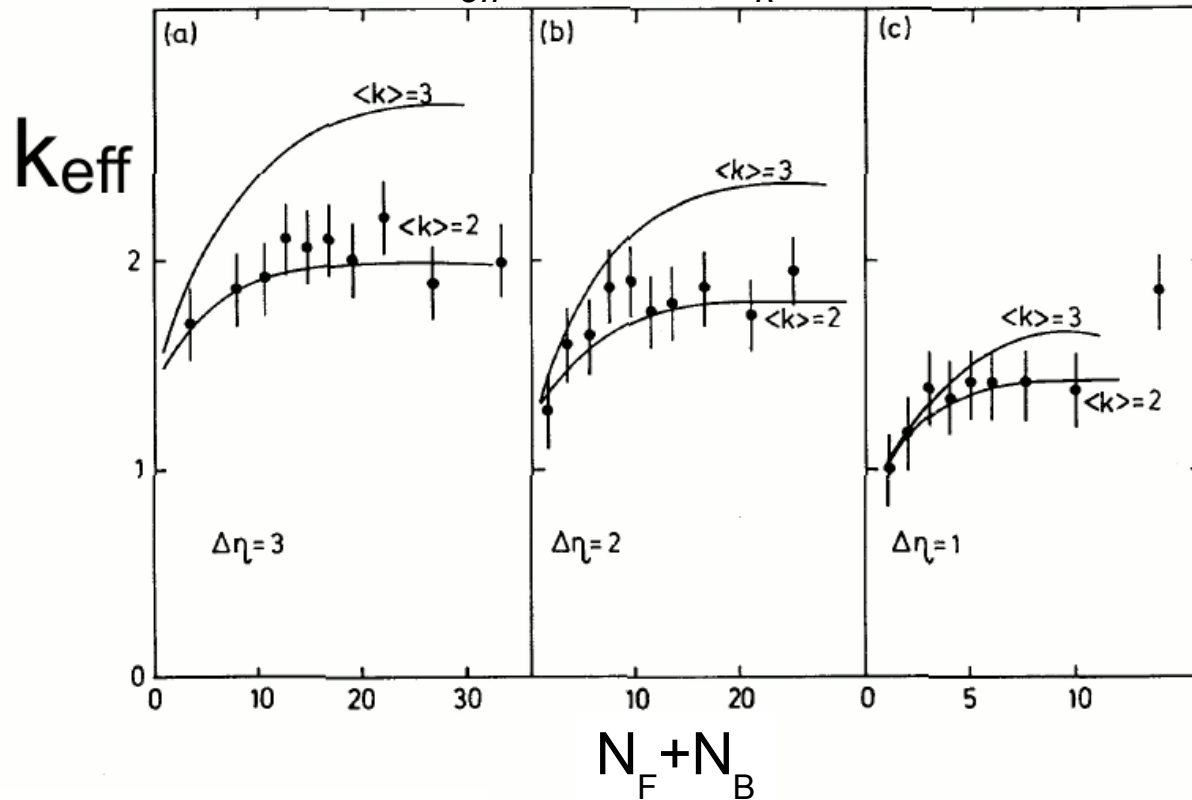


- Monotonic rise with increasing $\Delta\eta$ -bin width
- Particles produced in effective cluster size
 - Central: $k_{\text{eff}}=2-2.3$
 - Peripheral: $k_{\text{eff}}=2.6-2.8$
- Models do not simultaneously describe centrality and $\Delta\eta$ dependence



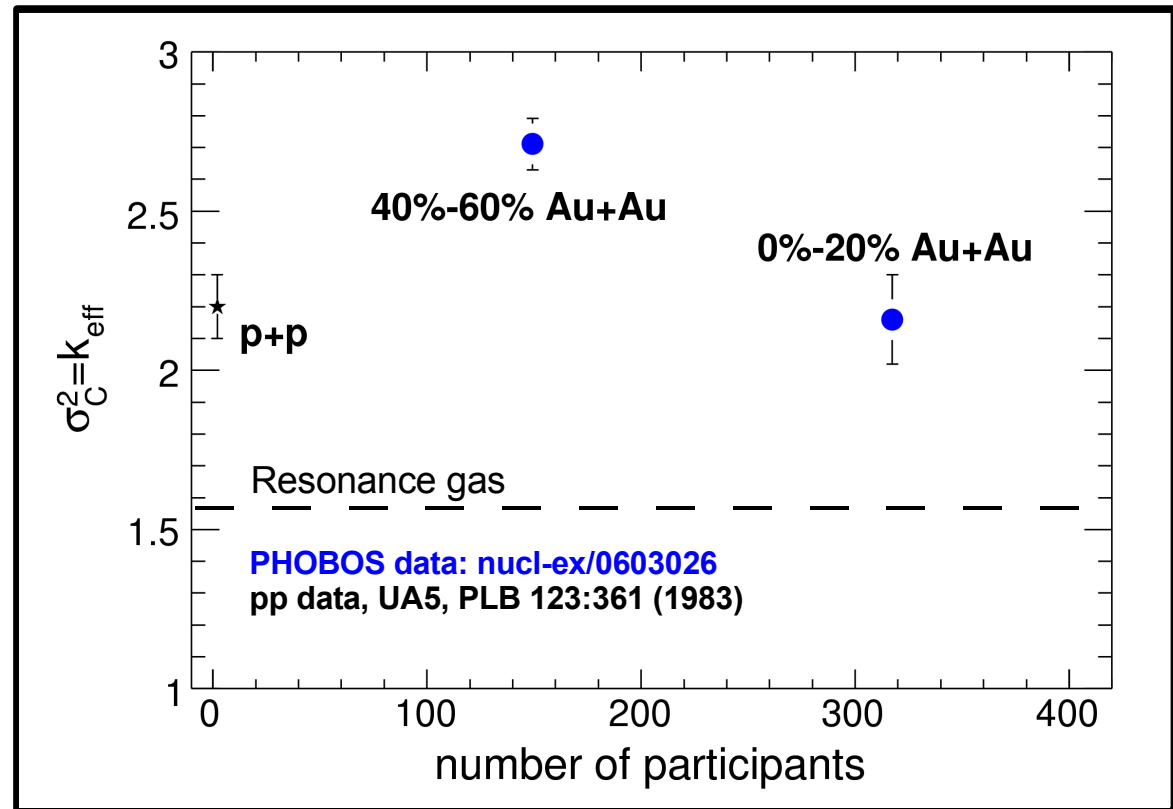
Clusters in elementary collisions

UA5: Phys.Lett.B123:361,1983 $k_{eff} = \langle k \rangle + \sigma_k^2 / \langle k \rangle$



Clusters in Au+Au are reminiscent of results from p+p̄

Centrality dependence of σ_C^2



Centrality dependence of σ_C^2

- Model short and long range contribution

$$\sigma_C^2 = f \sigma_{SR}^2 + (1 - f) \sigma_{LR}^2$$

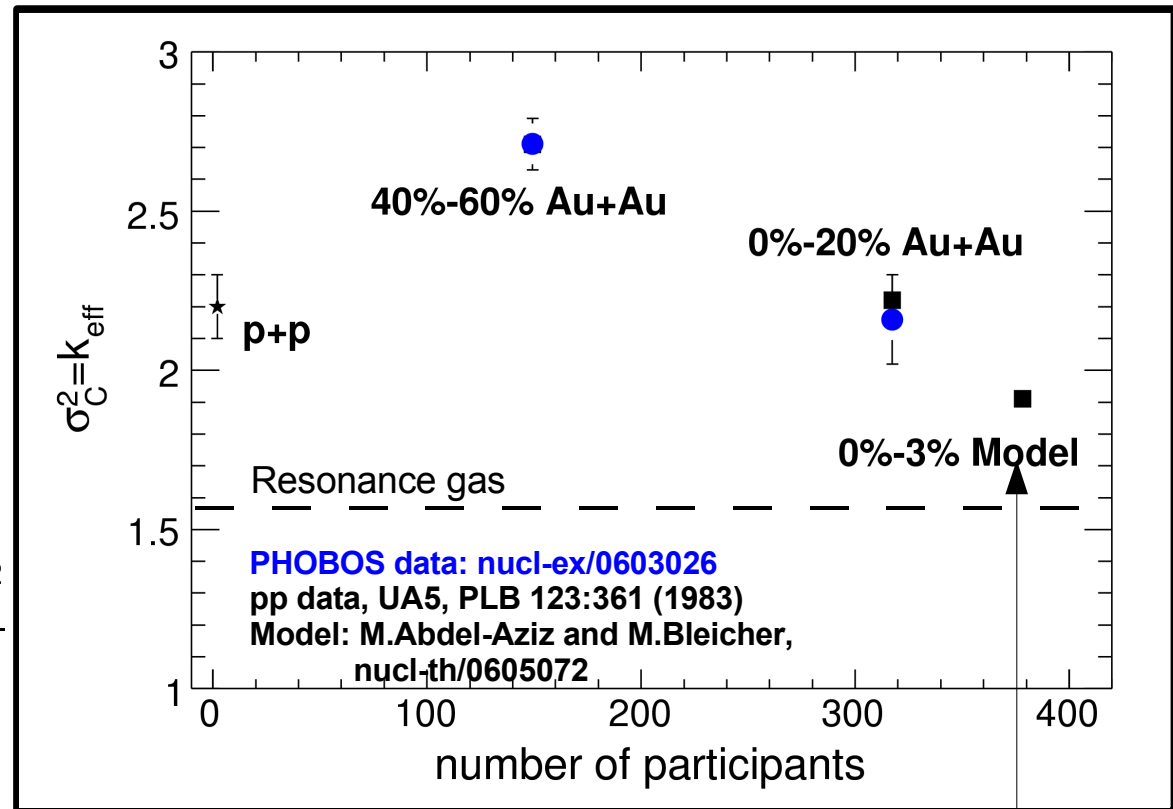
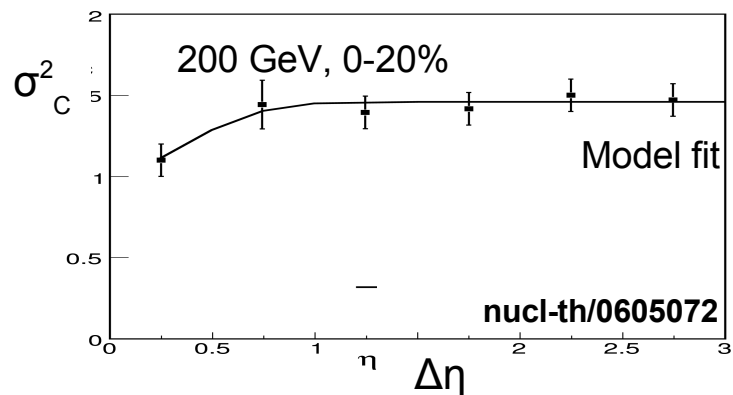
where **short range**

$$\sigma_{SR}^2 = k [1 - \exp(-\Delta\eta / \lambda_{short})]$$

and **long range**

$$\sigma_{LR}^2 = 1 - \frac{\xi}{f} \int d\eta_1 d\eta_2 \exp \frac{-(\eta_1 - \eta_2)^2}{2\lambda_{long}^2}$$

- Constrain parameters



Cent.
Extra-
pola-
tion

data	f	ξ	λ_{short}	λ_{long}
Au+Au 0% - 20%	0.88	1.8	0.4	0.7
Au+Au 40% - 60%	0.99	2.5	0.6	0.9

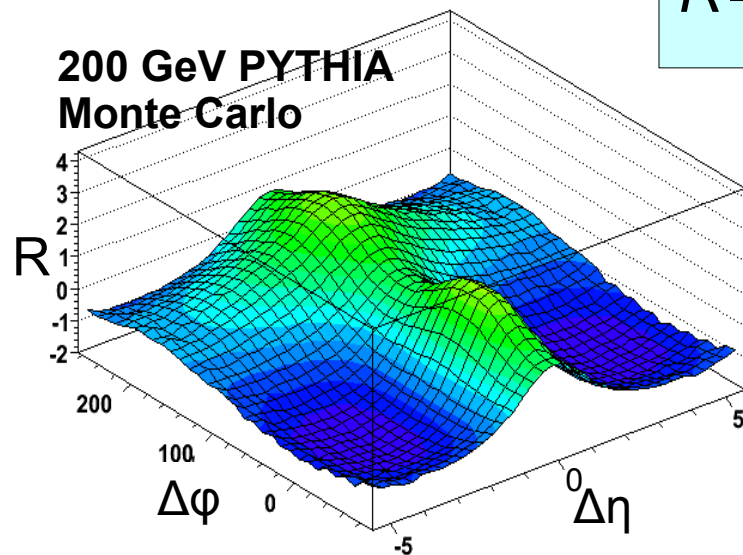
4) Two-particle angular correlations

- Extend correlations from regions in $dN/d\eta$
 - Two-particle angular correlations

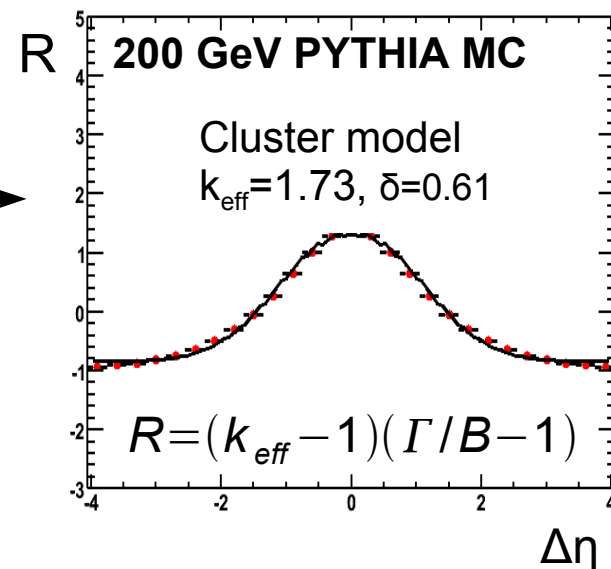
Two-particle angular correlations

See Wei Li's talk

$$R = \left\langle (n-1) \left(\frac{F}{B} - 1 \right) \right\rangle$$



Projection onto η
(altern. onto ϕ)

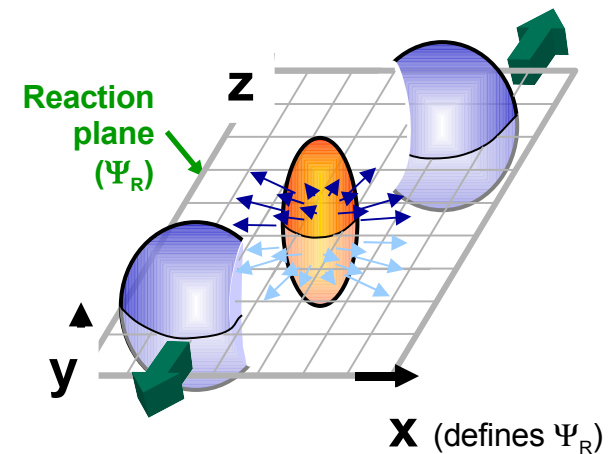
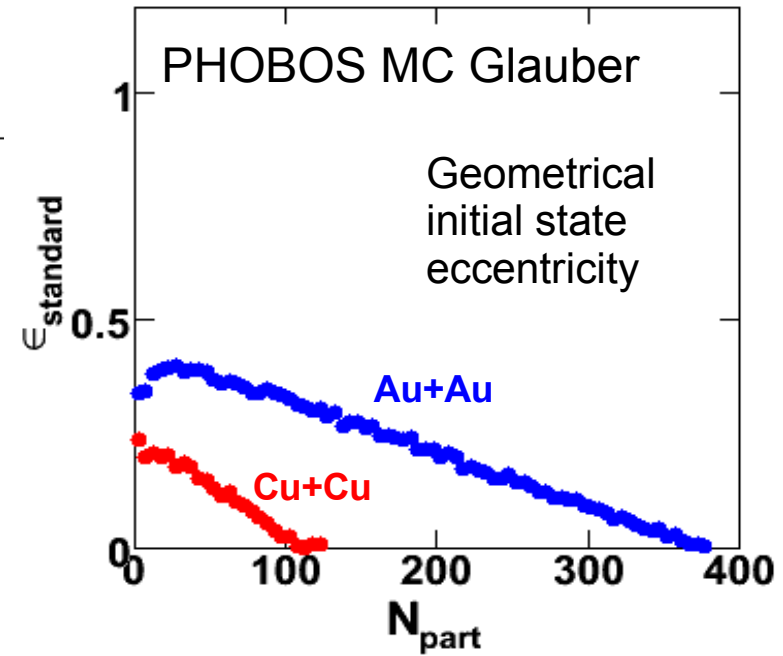
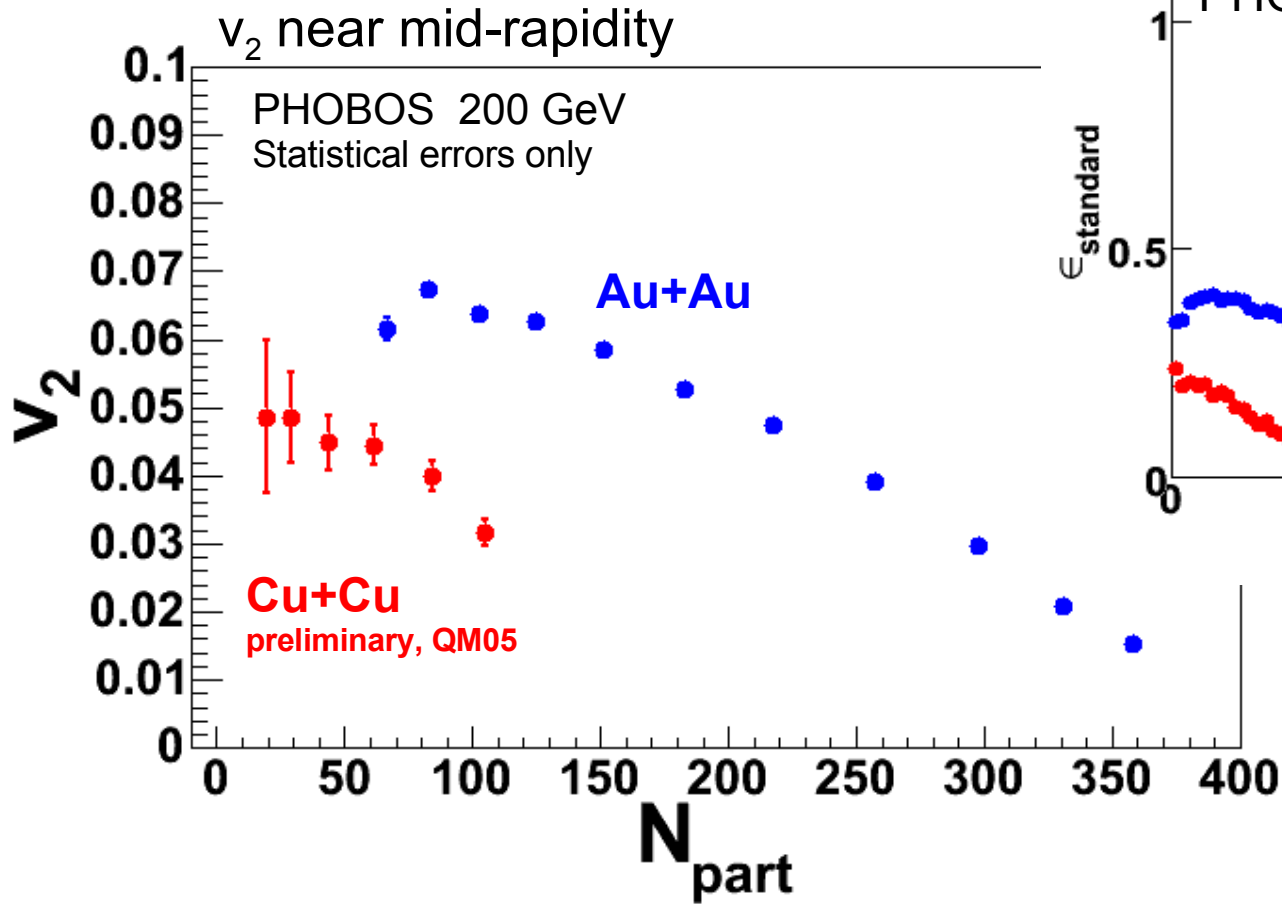


- Construction of R , event-by-event, weighted by event multiplicity
 - Full ϕ and large $|\eta| \leq 3$ coverage ($|\eta| \leq 5$ for future studies)
 - Single hit in silicon layer instead of particle information
 - Need special strategy for secondaries
 - No trigger particle
 - Study soft physics (fragmentation and hadronization processes)
 - Relative to trigger particle under investigation

5) Eccentricity fluctuations

- From two-particle angular correlations (clusters at hadronization times)
 - To fluctuations in the initial-state geometry and its connection to elliptic flow

Elliptic flow in Cu+Cu and Au+Au

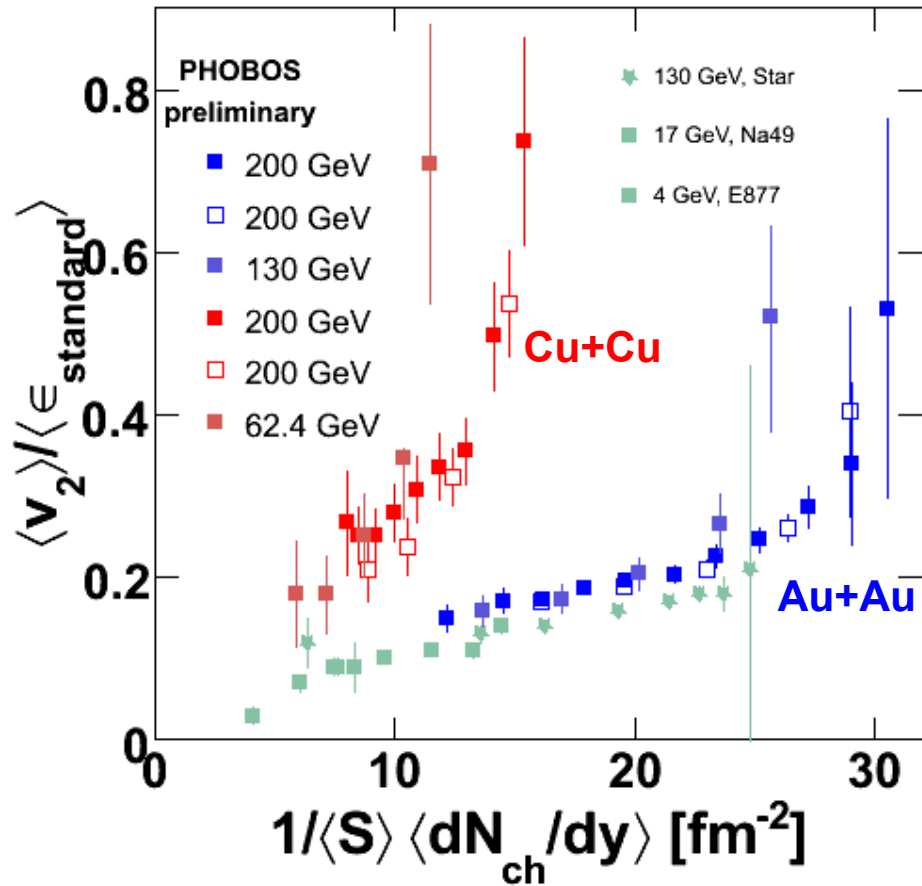


Au+Au: PRL 94, 122303 (2005)
Cu+Cu: prel. QM05, nucl-ex/0510042

$$dN/d(\phi - \Psi_R) = N[1 + 2v_1 \cos(\phi - \Psi_R) + 2v_2 \cos(2\phi - 2\Psi_R) + \dots]$$

Standard eccentricity scaling

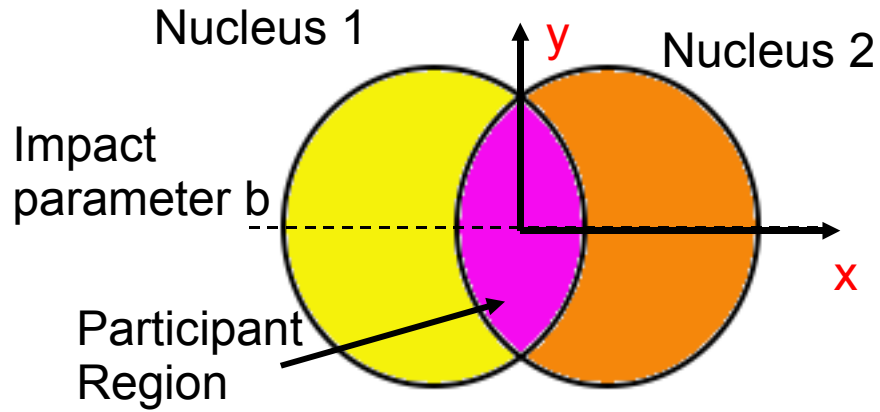
Standard Eccentricity



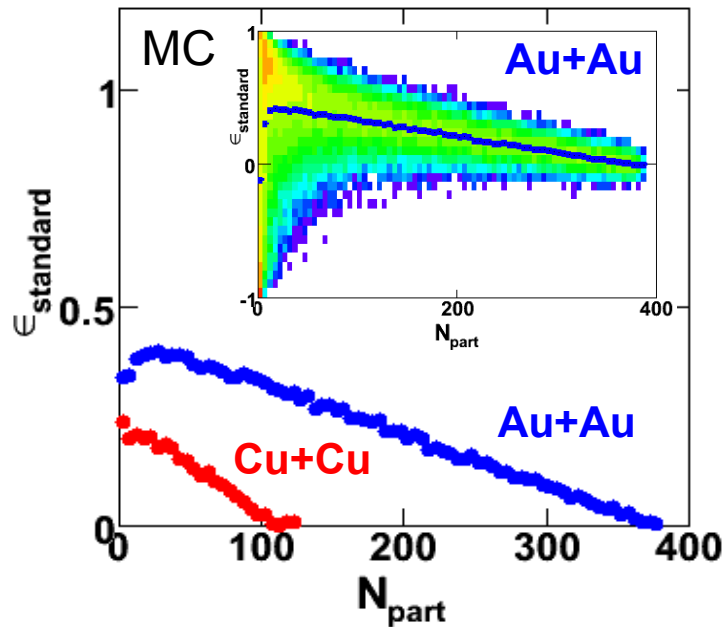
STAR, PRC 66 034904 (2002)
Voloshin, Poskanzer, PLB 474 27 (2000)
Heiselberg, Levy, PRC 59 2716, (1999)

Standard eccentricity calculation

Standard Eccentricity

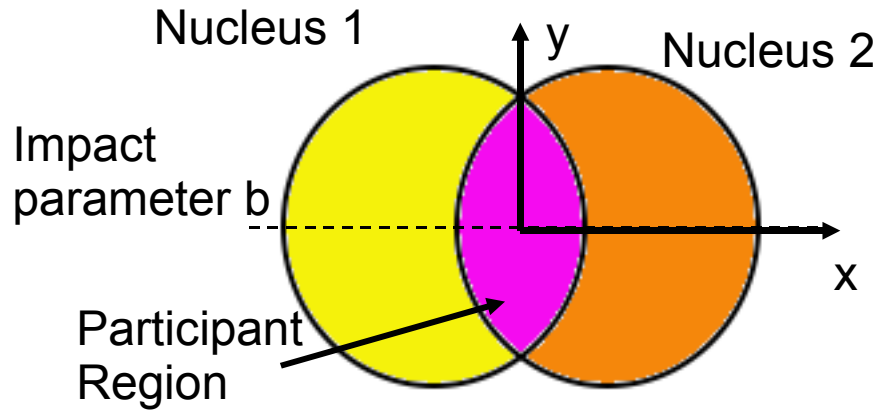


$$\epsilon_{std} = \frac{\sigma_y^2 - \sigma_x^2}{\sigma_y^2 + \sigma_x^2}$$

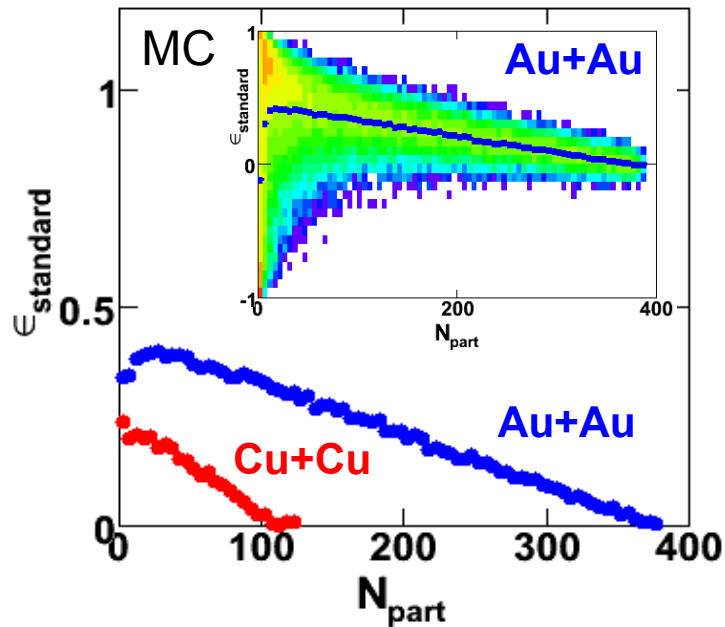


Participant eccentricity calculation

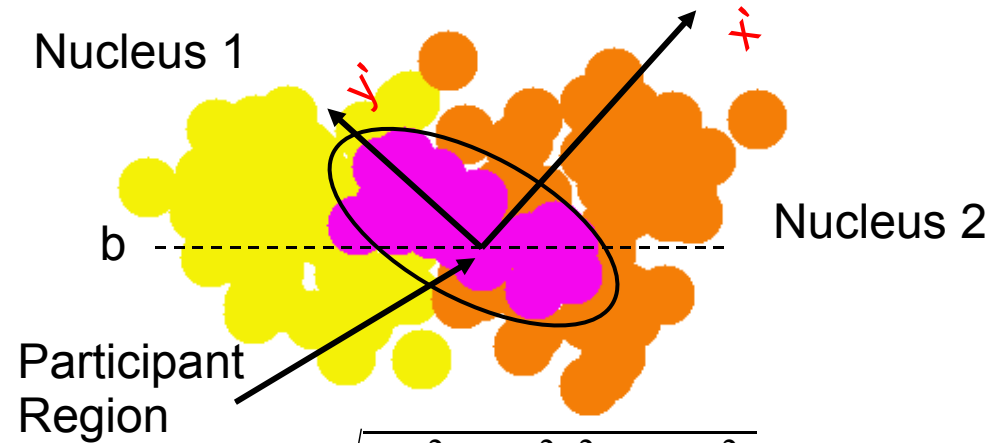
Standard Eccentricity



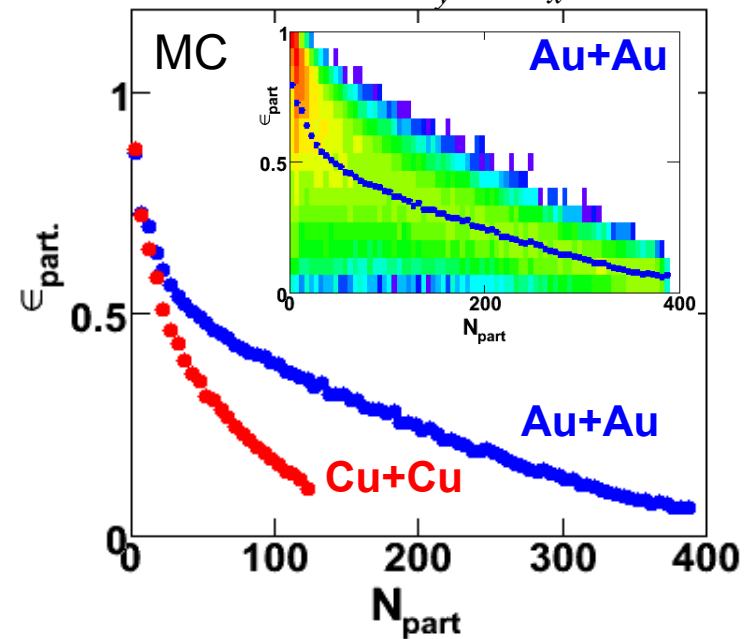
$$\epsilon_{std} = \frac{\sigma_y^2 - \sigma_x^2}{\sigma_y^2 + \sigma_x^2}$$



Participant Eccentricity

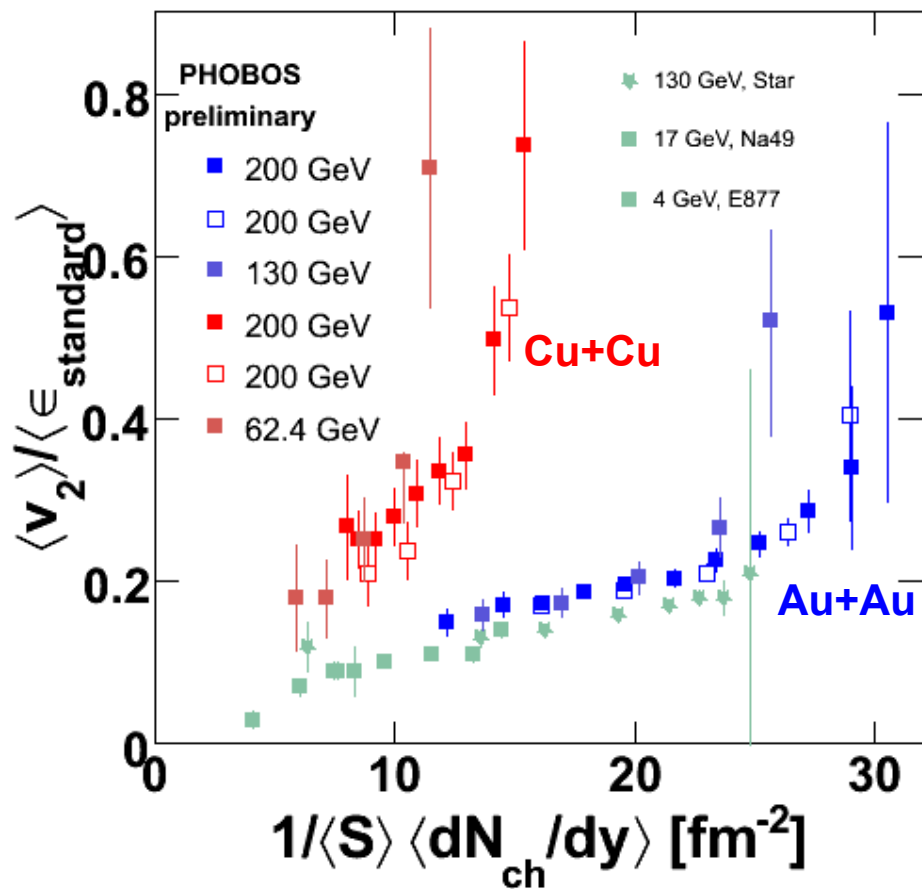


$$\epsilon_{part} = \frac{\sqrt{(\sigma_y^2 - \sigma_x^2)^2 - 4\sigma_{xy}^2}}{\sigma_y^2 + \sigma_x^2}$$

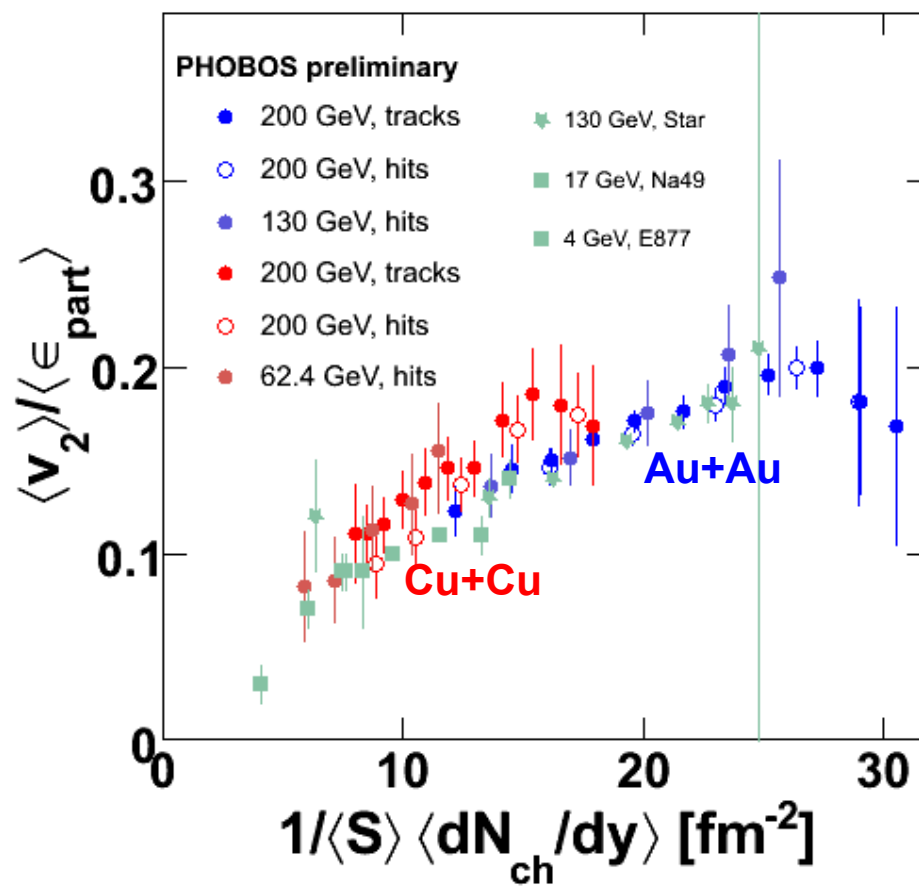


Participant eccentricity scaling

Standard Eccentricity



Participant Eccentricity

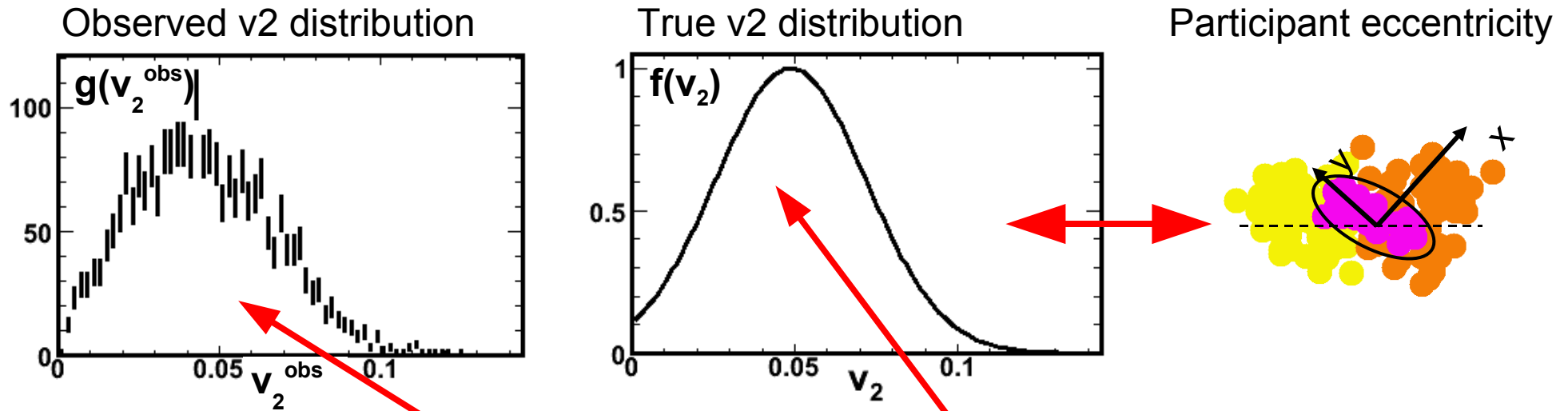


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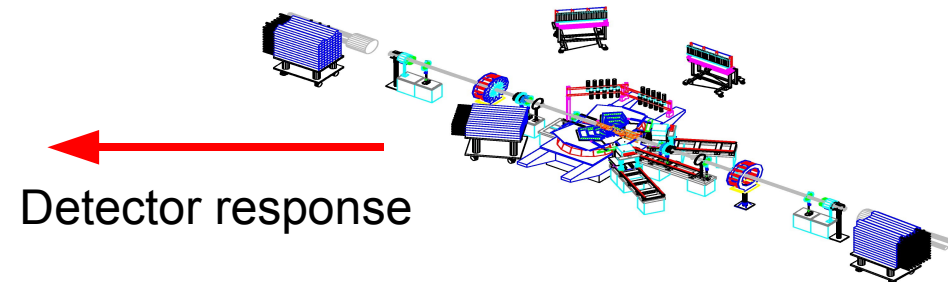
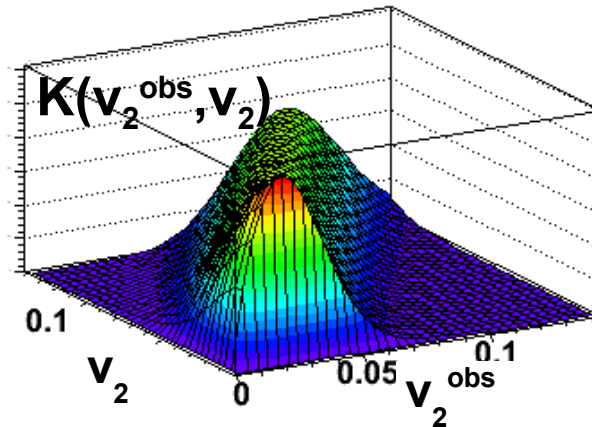
6) Event-by-event elliptic fluctuations

- From eccentricity fluctuations
 - To E-by-E fluctuations of the elliptic flow

Event-by-event elliptic flow fluctuations



$$g(v_2^{obs}) = \int_0^{\infty} K(v_2^{obs}, v_2) f(v_2) dv_2$$



Detector response

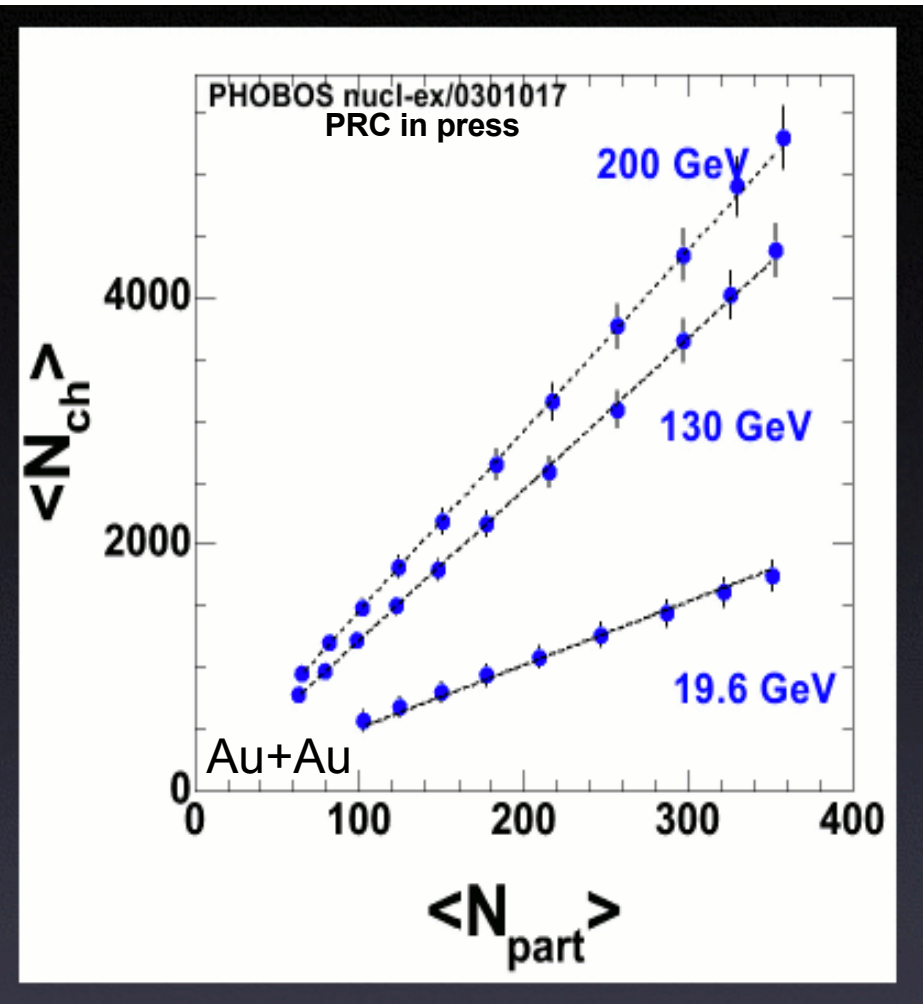
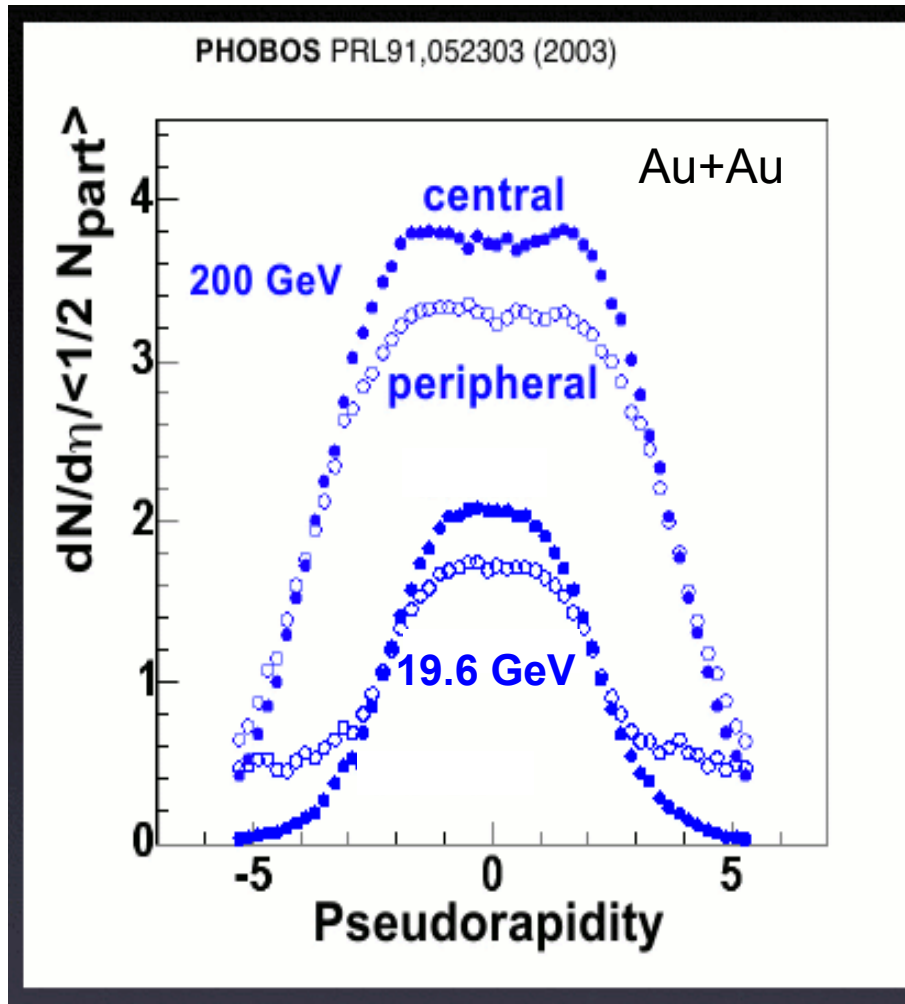
See Burak Alver's talk tomorrow

Summary and Perspectives

- Unusual event search
 - To the level of $\approx 10^{-4}$ (potentially lower) all events are “the same”
 - Refine this upper limit
- Forward-Backward multiplicity correlations
 - Connection of multiplicity fluctuations and hadron clusters
 - Interesting centrality dependence
- Two-particle angular correlation (see Wei Li's talk, 07/07/2006)
 - Comprehensive study of angular correlations in pp, dA and AA systems
- Eccentricity fluctuations
 - Participant vs standard eccentricity
 - Elliptic flow in small system connected to initial geometry fluctuations
- Elliptic flow fluctuations (see Burak Alver's talk, 07/09/2006)

Backup

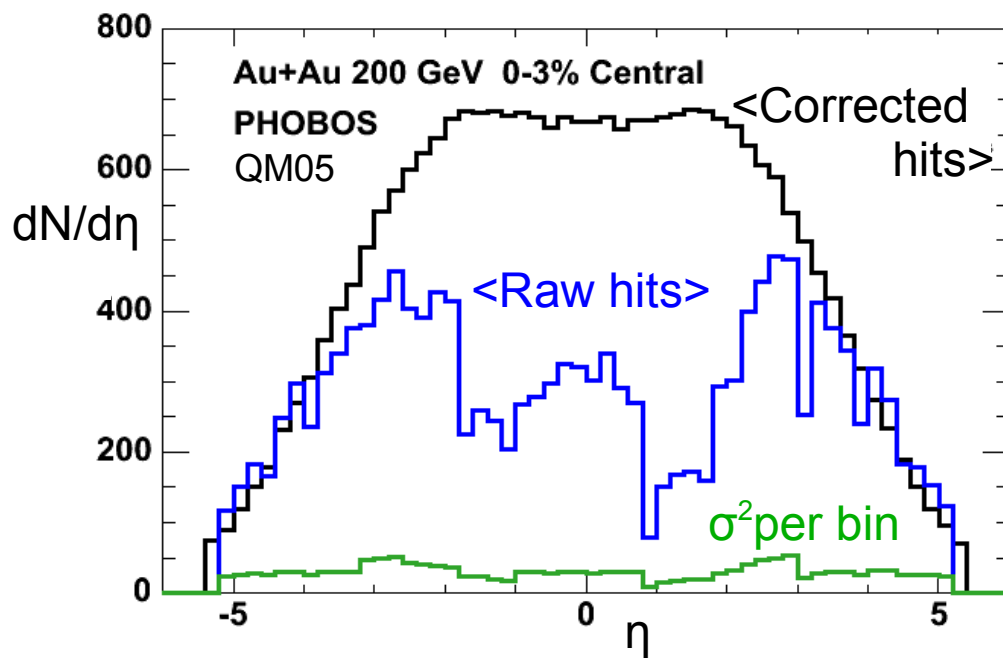
Global properties of $dN/d\eta$ -distributions



- Centrality dependence of $dN/d\eta$ **shape**
- Npart scaling of integrated (4π) **multiplicity**

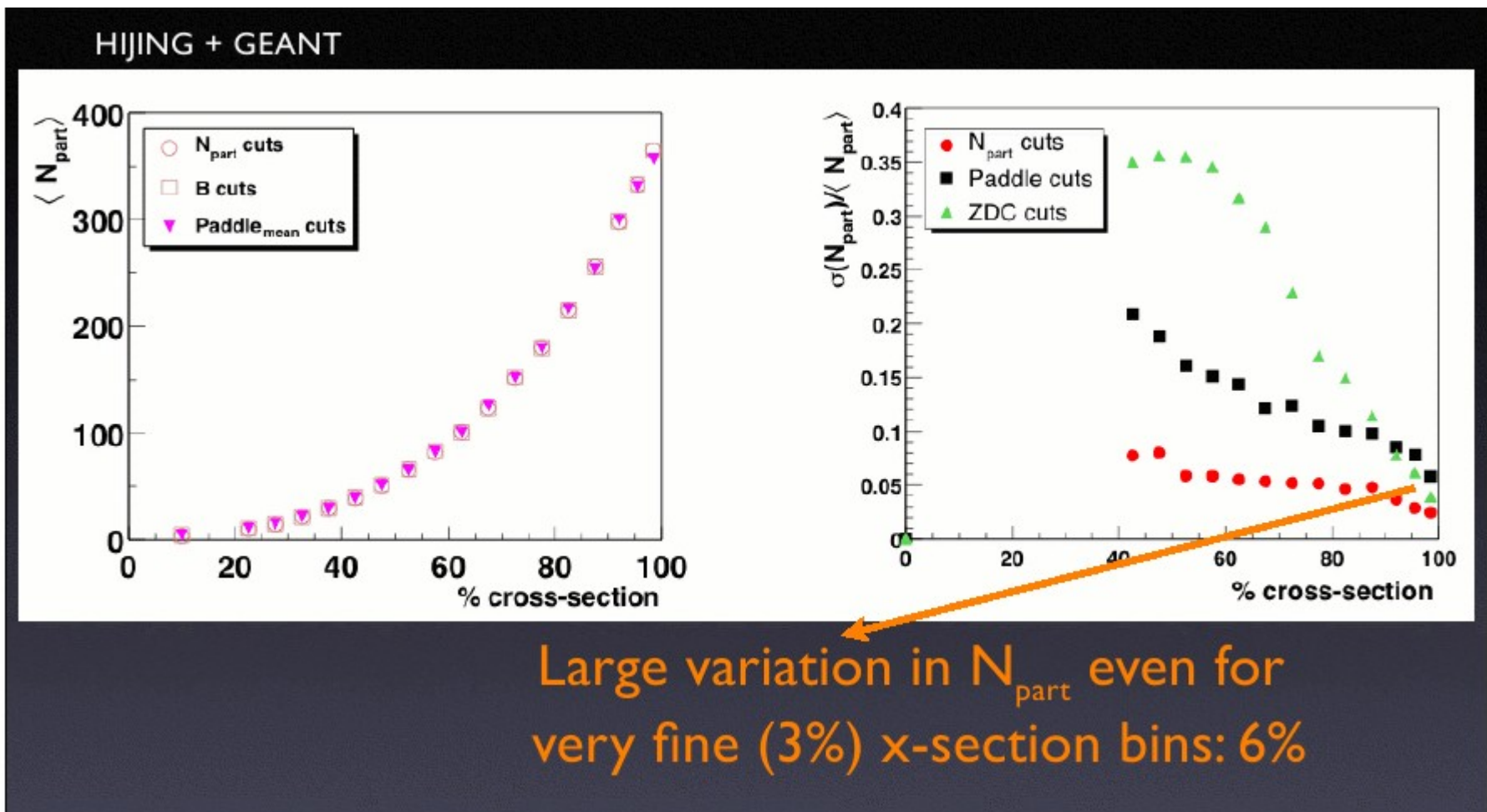
Beyond average $dN/d\eta$ -distributions

- Quantify event-by-event variation of large scale structure
 - Are there events with very large multiplicity?
 - Does the $dN/d\eta$ shape vary from event to event?

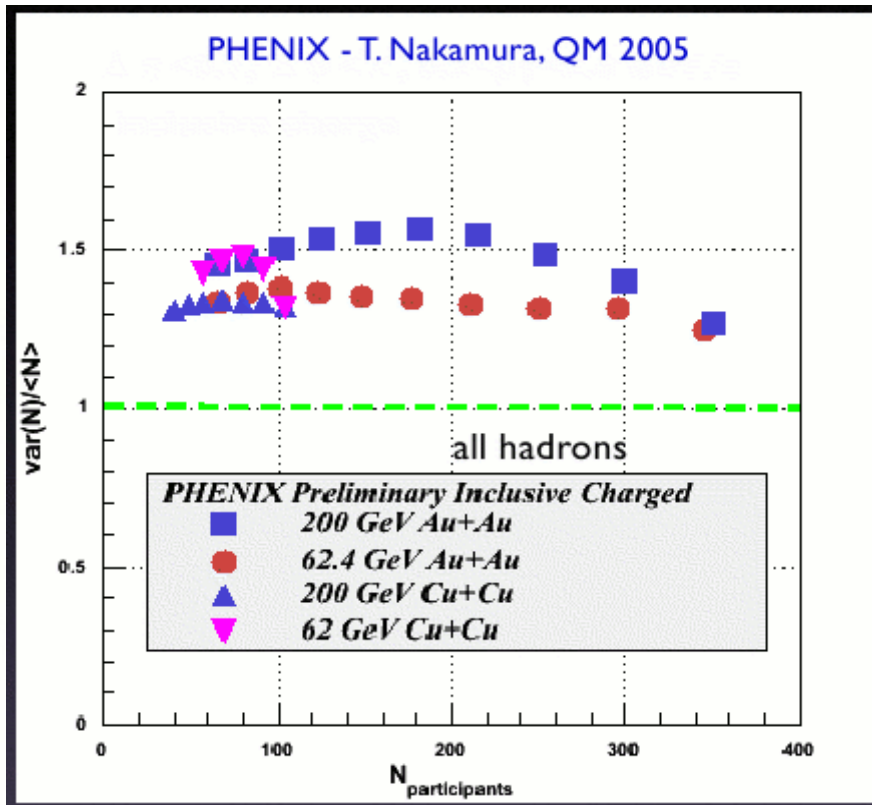


- Multiplicity fluctuations
 - Integral of raw $dN/d\eta$
- Shape fluctuations
 - χ^2 of single event vs raw (average) $dN/d\eta$

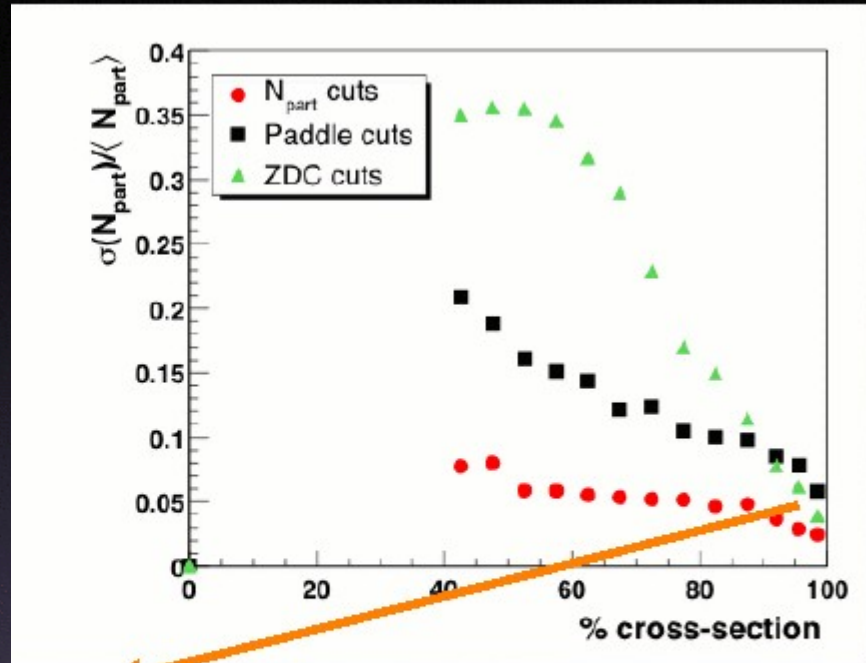
Multiplicity vs. participant fluctuations



Multiplicity vs. participant fluctuations



Deviation from Poisson
(30% for highest bin)

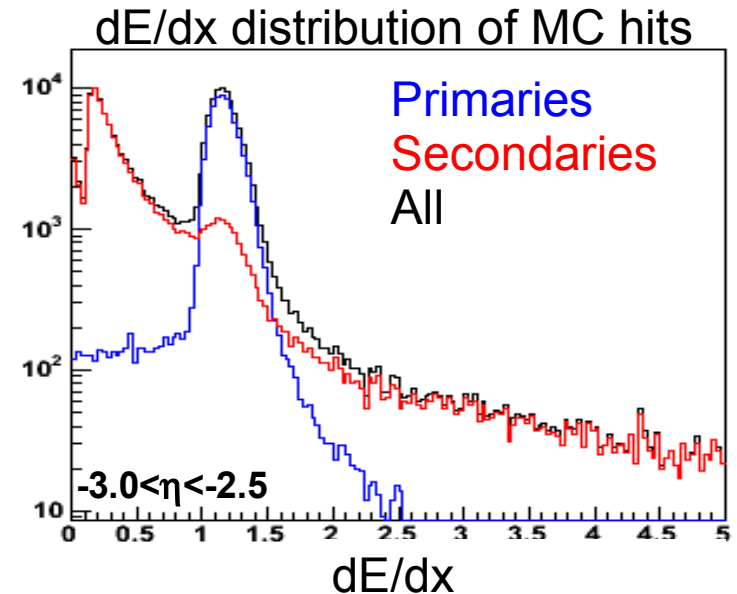
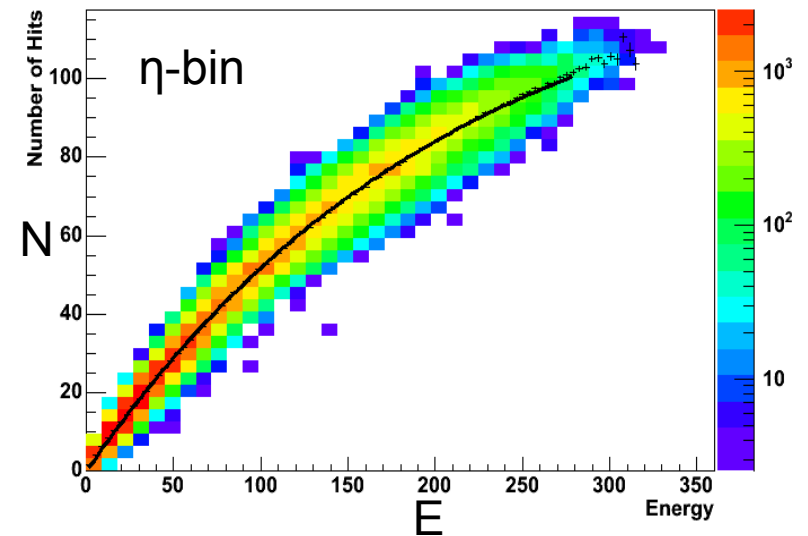


variation in N_{part} even for
(3%) x-section bins: 6%

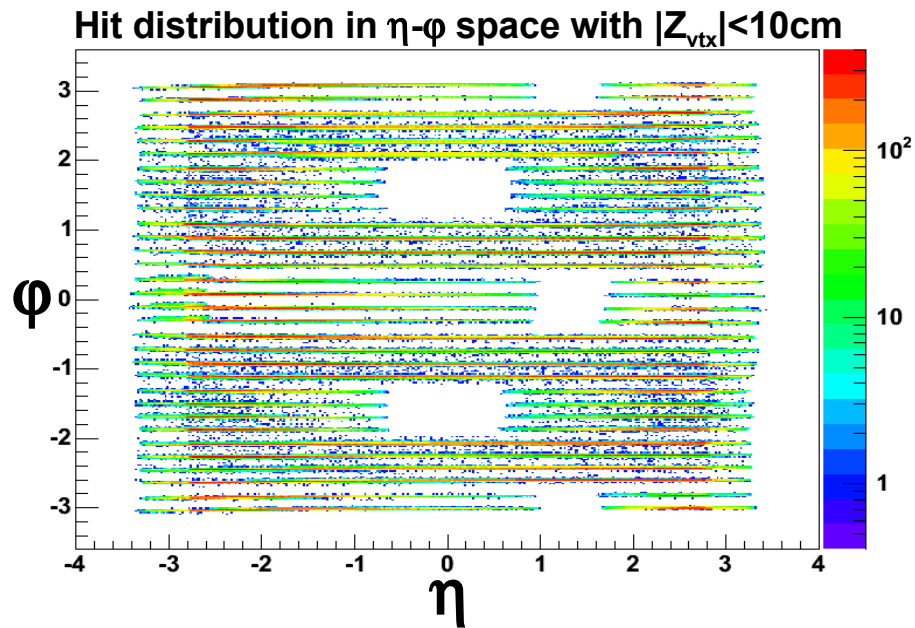
Todo: Conclusion

Extracting number of particles per bin

- Octagon silicon sensors
 - Number of hits, N_{hit}
 - Sum of angle-corrected dE for charged particles, $E = \Sigma dE$
- Poissonian ansatz
 - $N_{\text{hit}} = N_{\text{max}} (1 - \exp(-E/E_{\text{max}}))$
- Average $\langle dE \rangle$ in η -bin given by $E_{\text{max}} / N_{\text{max}}$
- Estimated multiplicity in η -bin
$$N = E / (E_{\text{max}} / N_{\text{max}})$$
- Use η -bin-dependent lower and upper dE/dx cuts on hits to suppress contribution from secondaries



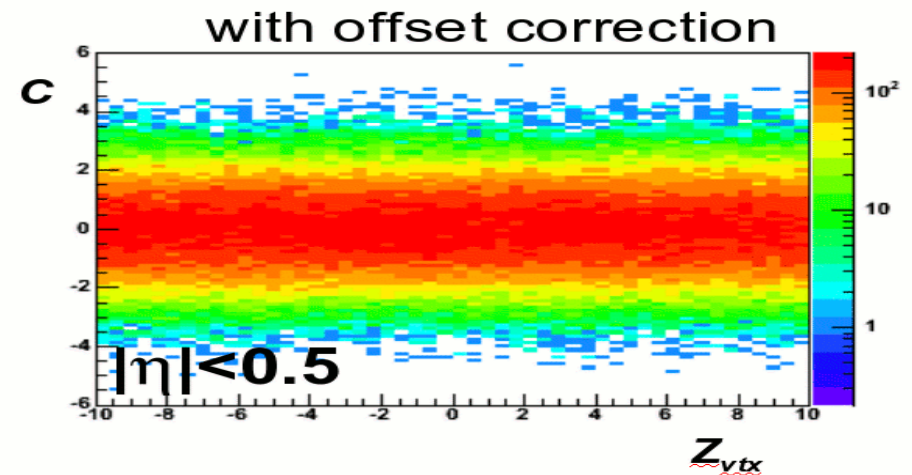
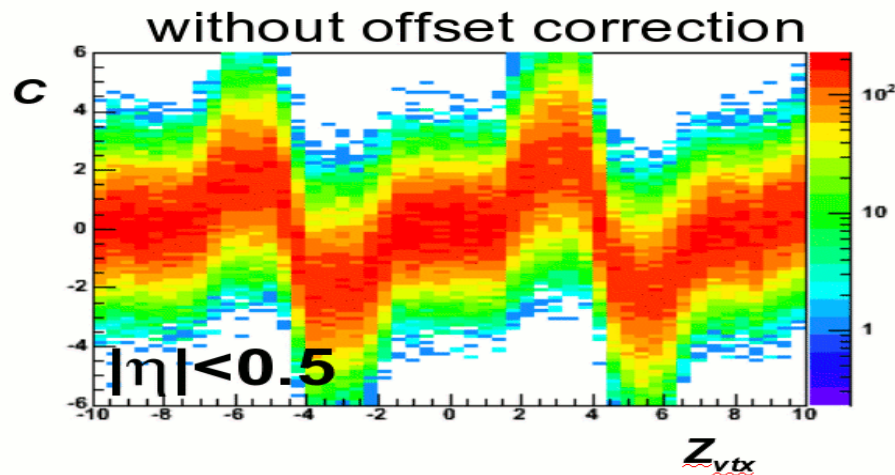
Acceptance correction



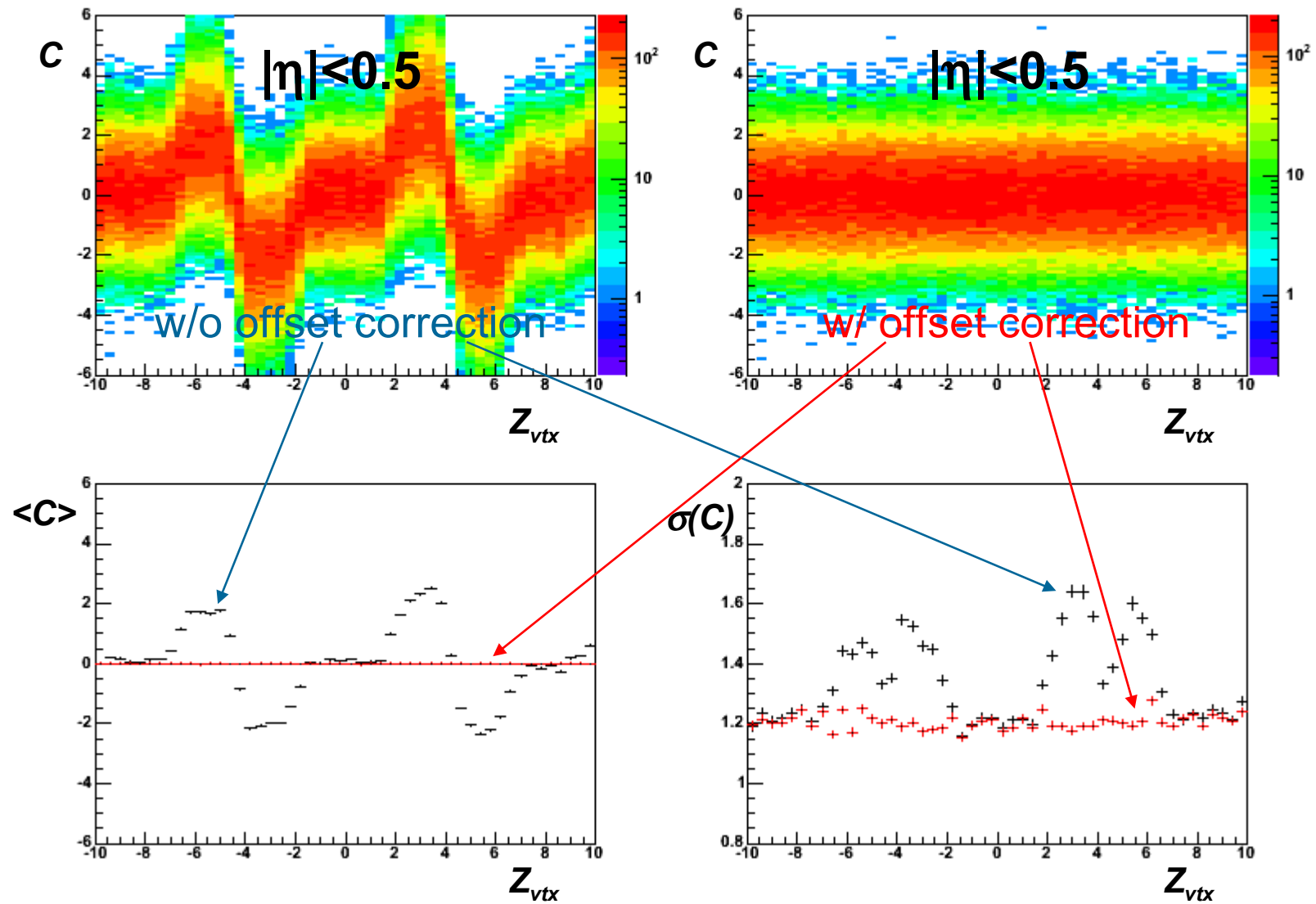
- Calculate average C per η , vertex and centrality bin

$$\Delta C = \frac{\langle N_1 - N_2 \rangle}{\sqrt{N_1 + N_2}}$$

- Subtract it event-by-event from C (according to simulations this leaves fluctuations unaffected)

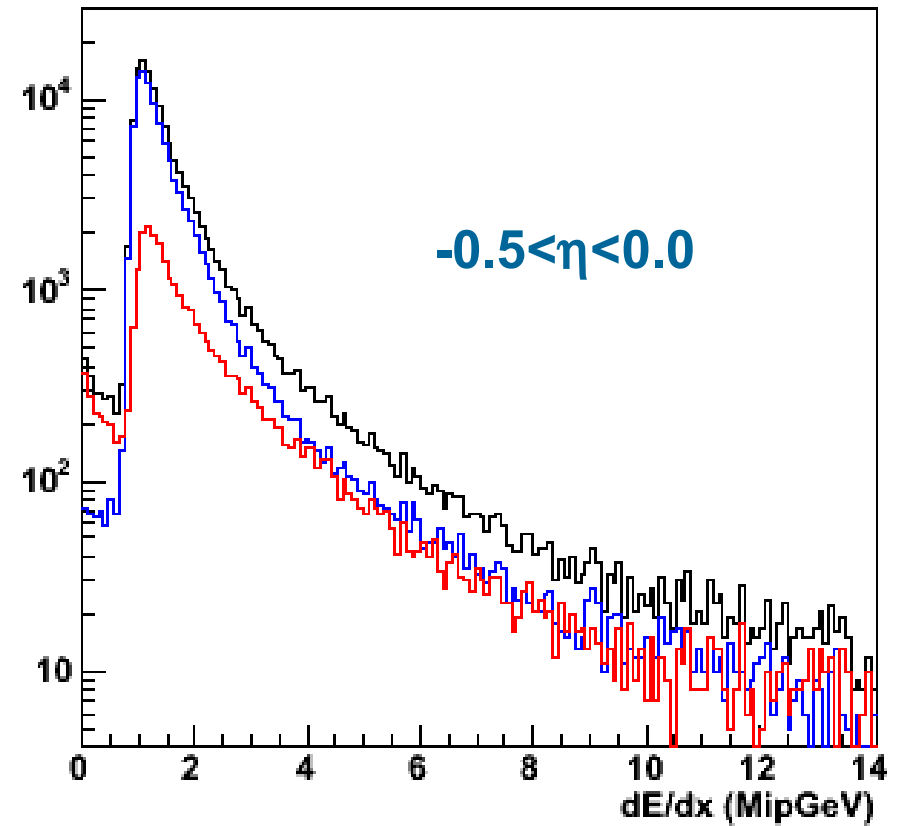
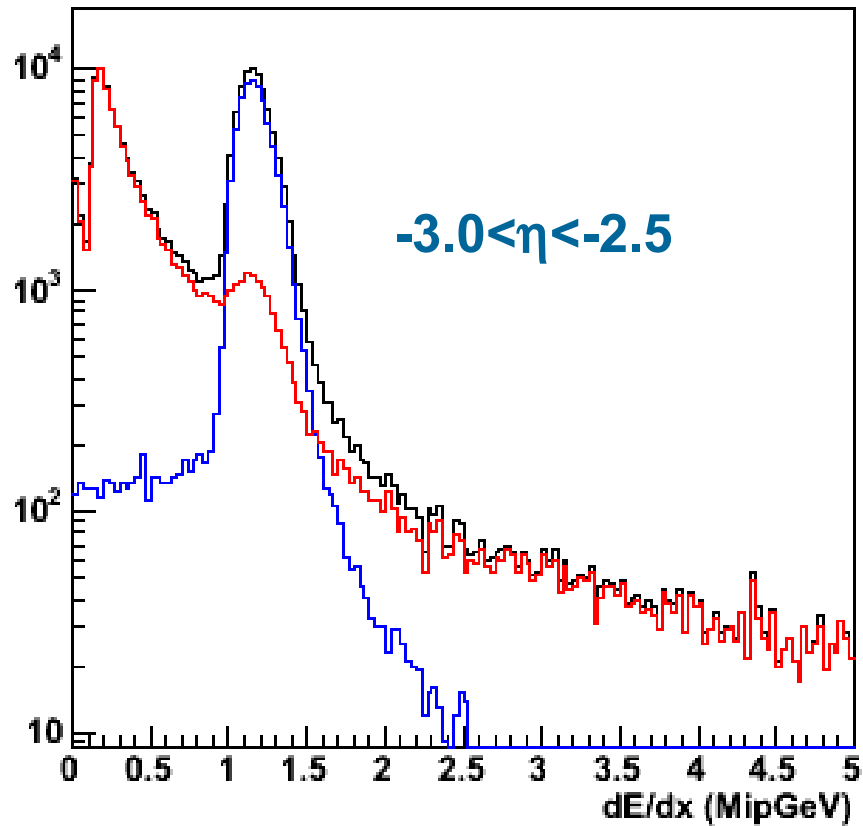


F/B: Acceptance correction

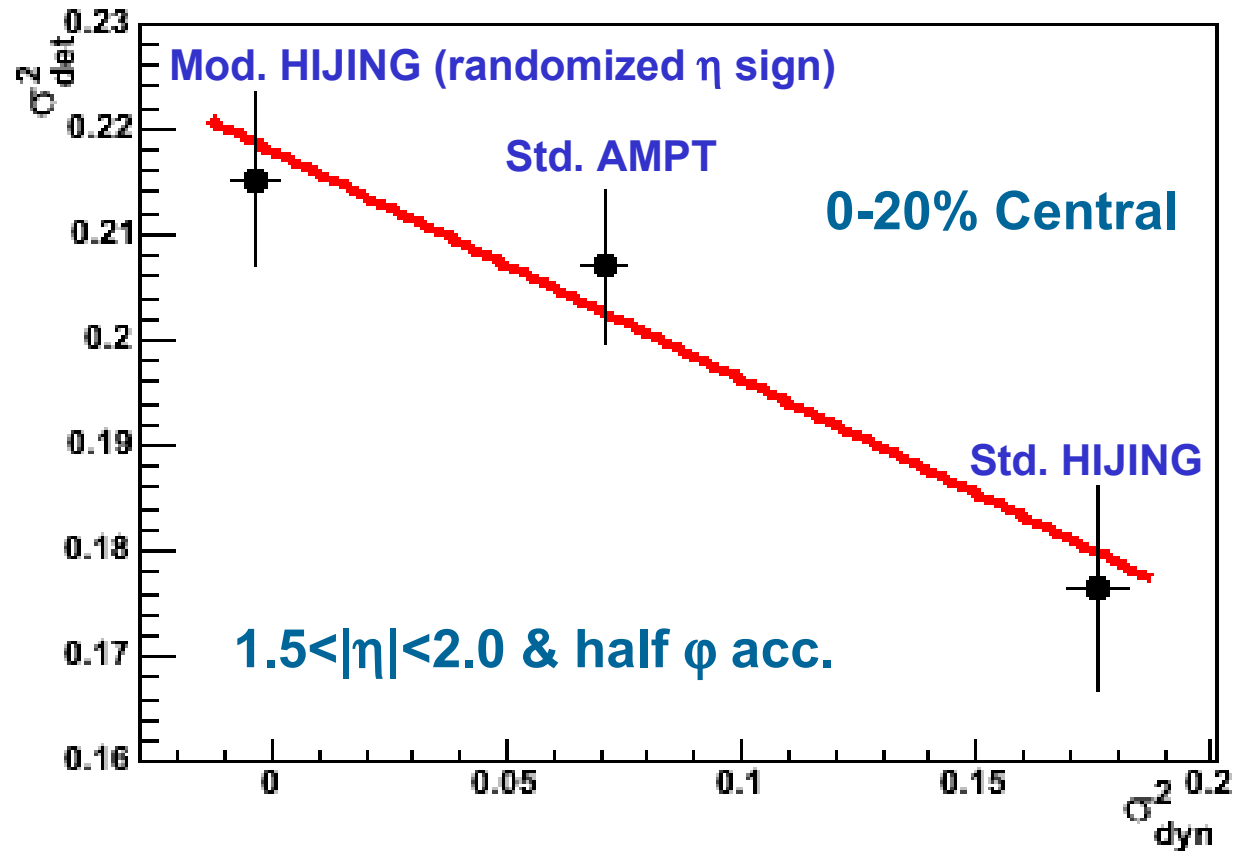


F/B: dE/dx distributions of MC hits

Black: Primaries + Secondaries, Red: Secondaries, Blue: Primaries



F/B: 1st order detector effects



Charge fluctuation

Studies by Jeon, et al

nucl-th/0503085

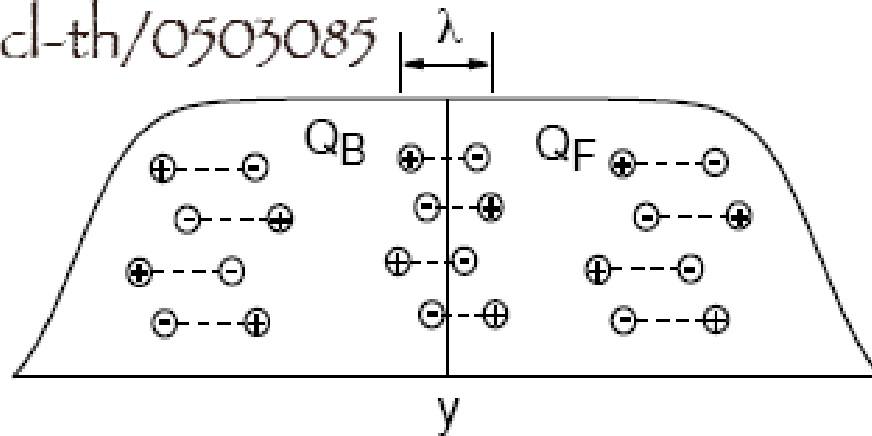
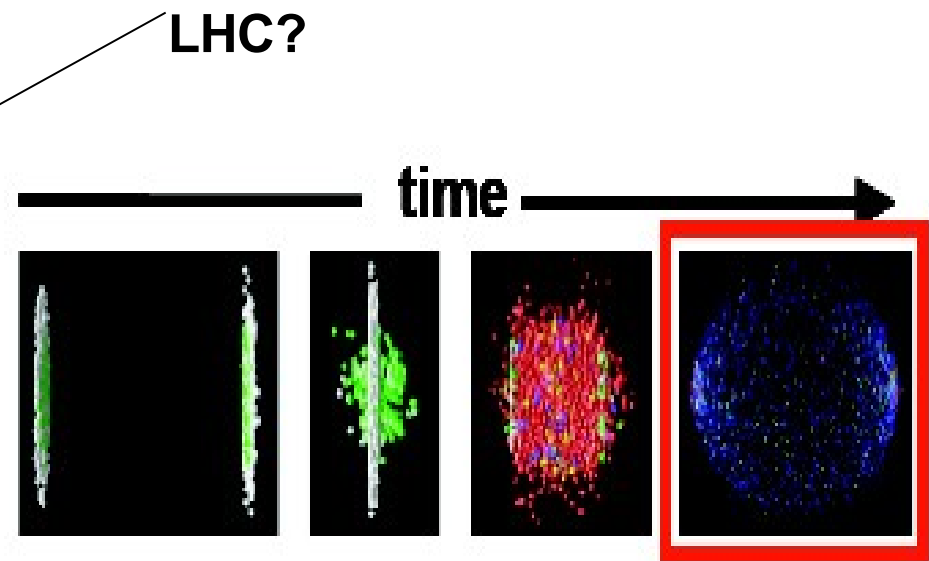
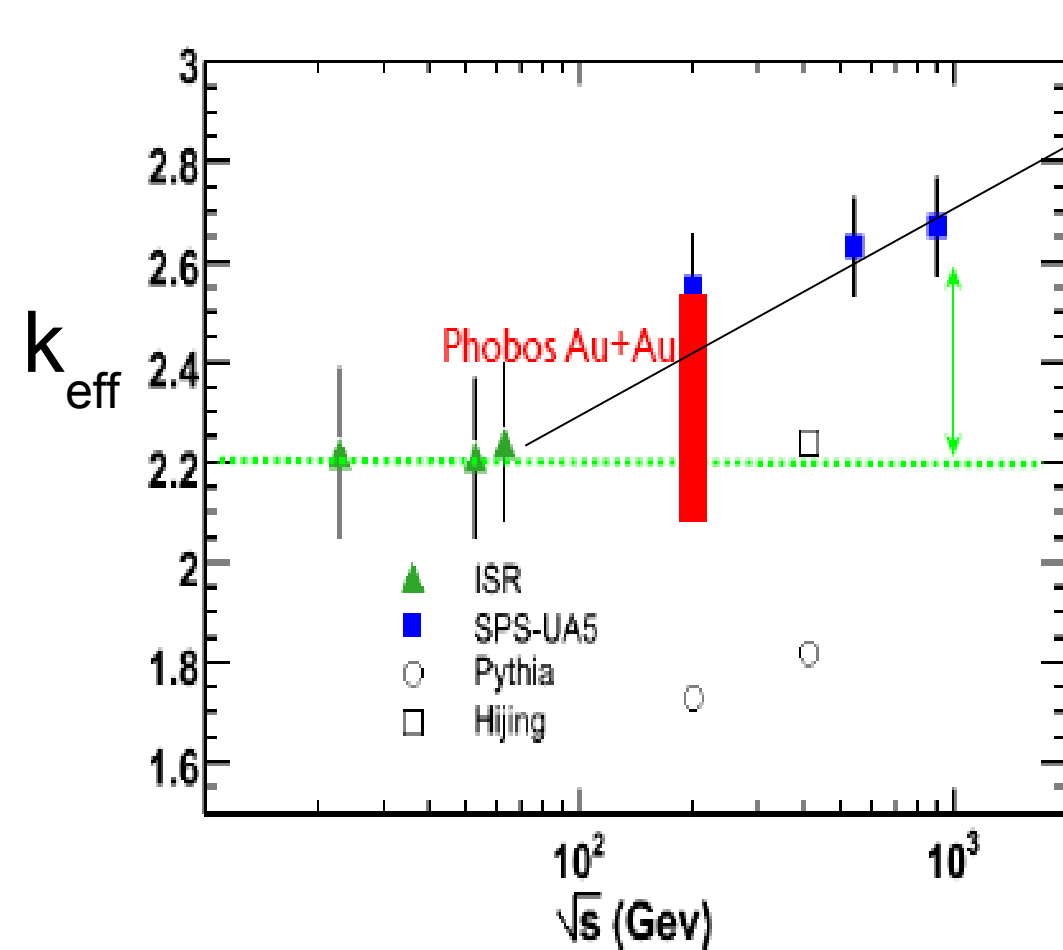


FIG. 1: A schematic illustration of the charge transfer fluctuations in the rapidity space. Only the pairs within $\lambda/2$ of y can contribute to the charge transfer fluctuation $D_u(y)$. Here λ is the rapidity correlation length, or the rapidity distance of the decay particles from a single cluster. If λ is a function of y , then $D_u(y)$ also changes with y .

- Model predicts at central region, QGP will decrease the cluster size.
- F&B method is restricted by the overlapping of F and B region near mid-rapidity.
- PHOBOS angular correlation analysis can be a useful tool to test the model.

Clusters in pp and AA



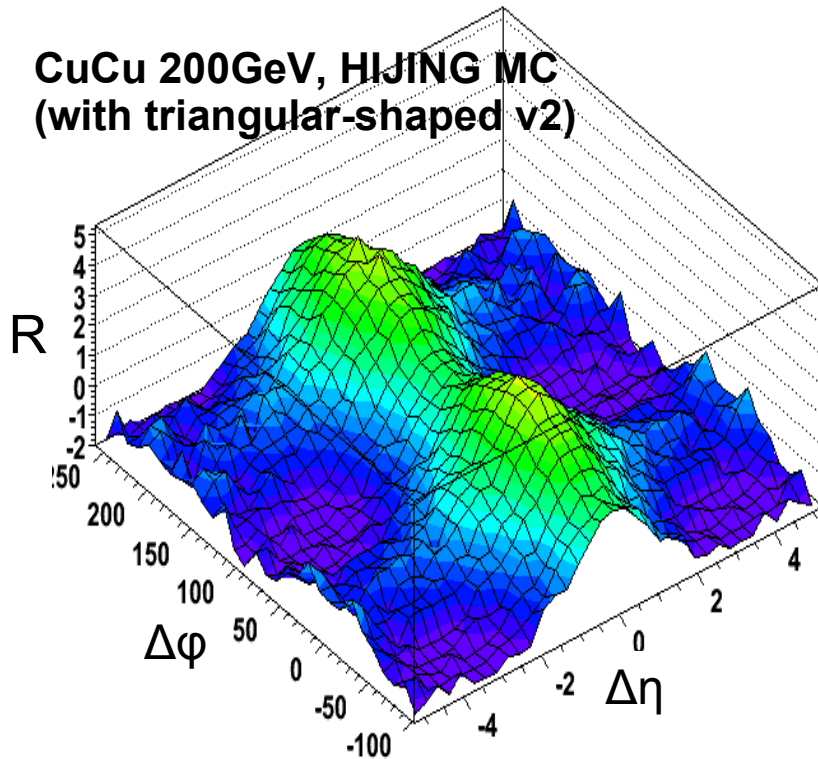
Cluster in AA is very similar to pp:

- Effects of Hadronization?
- Have to understand centrality dependence in AA
- Energy dependence: mini-jets?

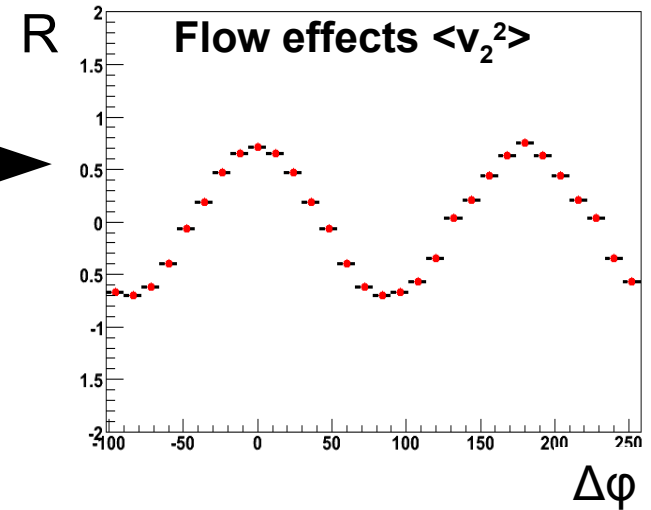
Nucl. Phys. B 86, 201 (1975)
 Nucl. Phys. B 155, 269 (1979)
 Z. Phys. - Particle and Fields C 37,191 (1988)

Two-particle angular correlations in A+A

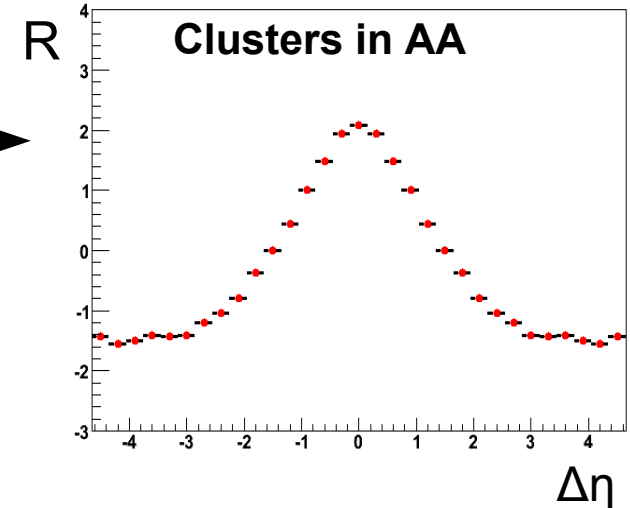
See Wei Li's talk



Projecting onto ϕ
from $0 < |\Delta\phi| < 180$

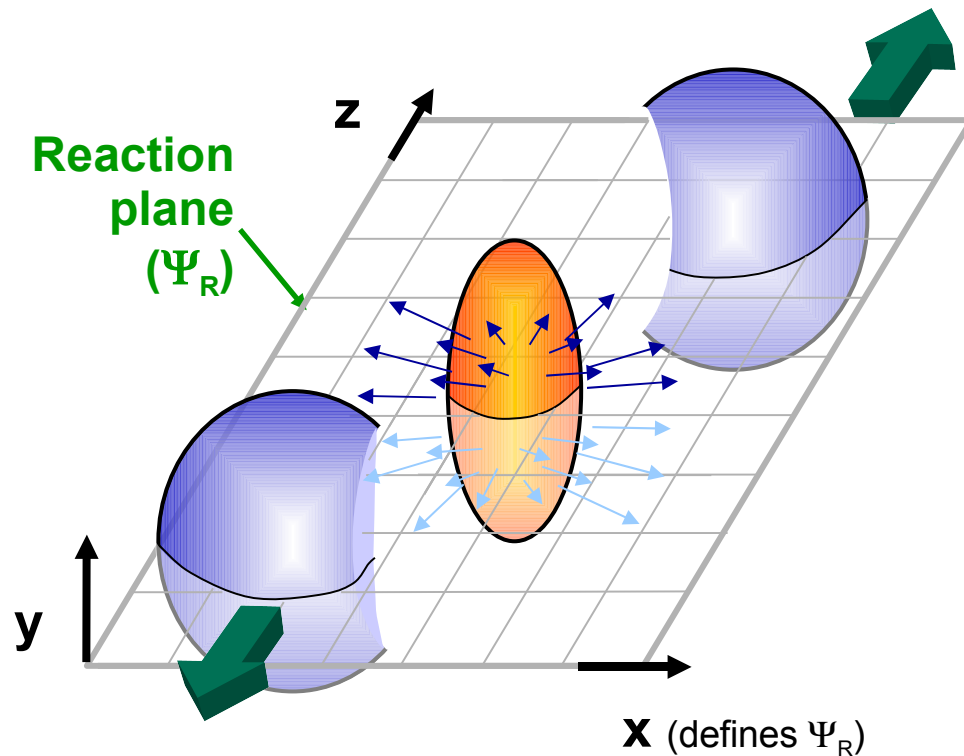


Projecting onto η
from $0 < |\Delta\eta| < 6$

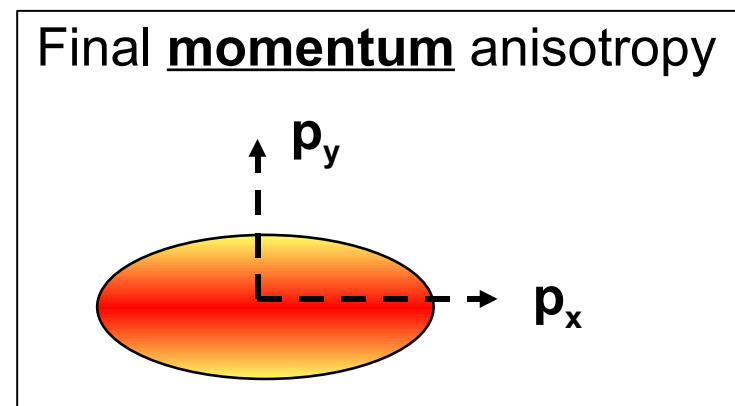
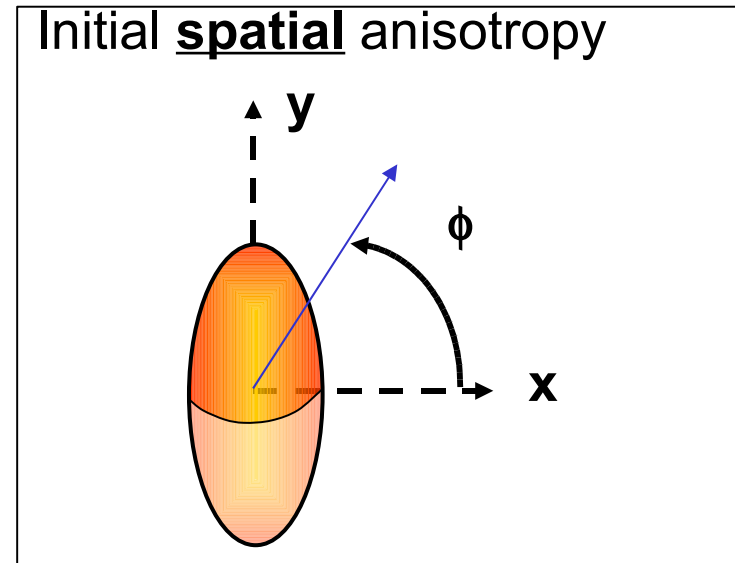


Comprehensive study of two-particle correlations in pp, dA and AA will help distangle different effects in HI systems

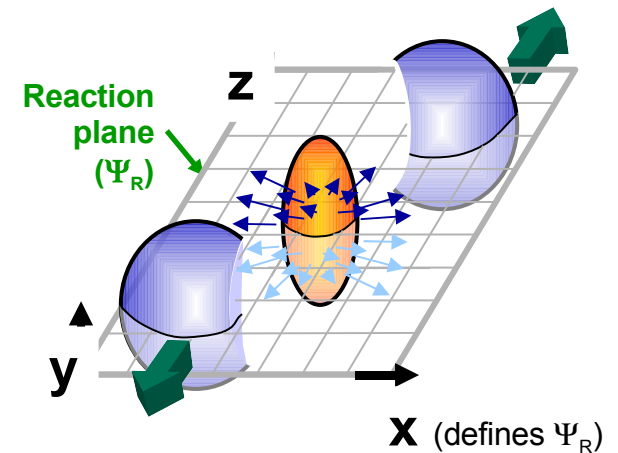
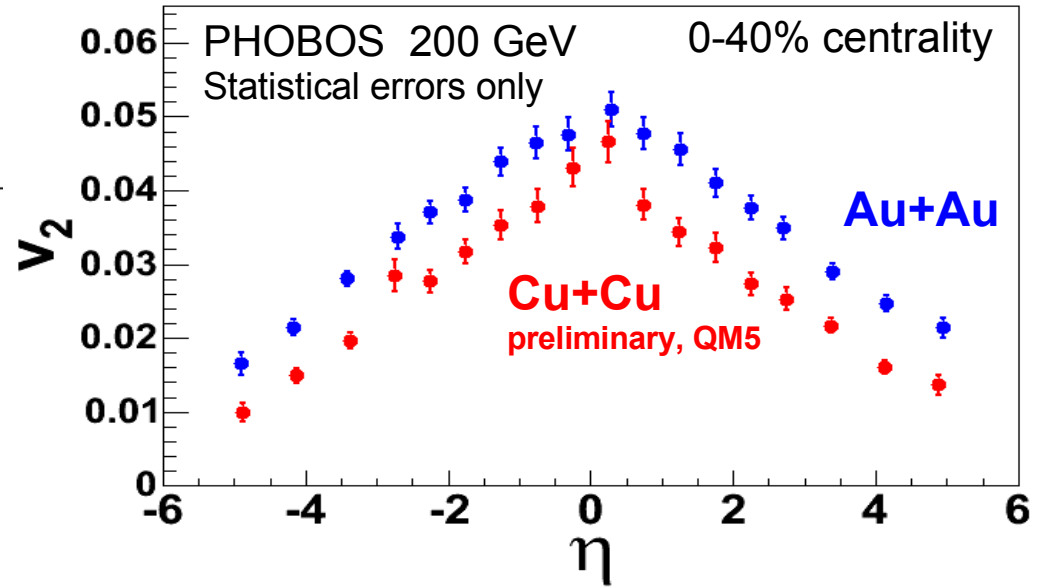
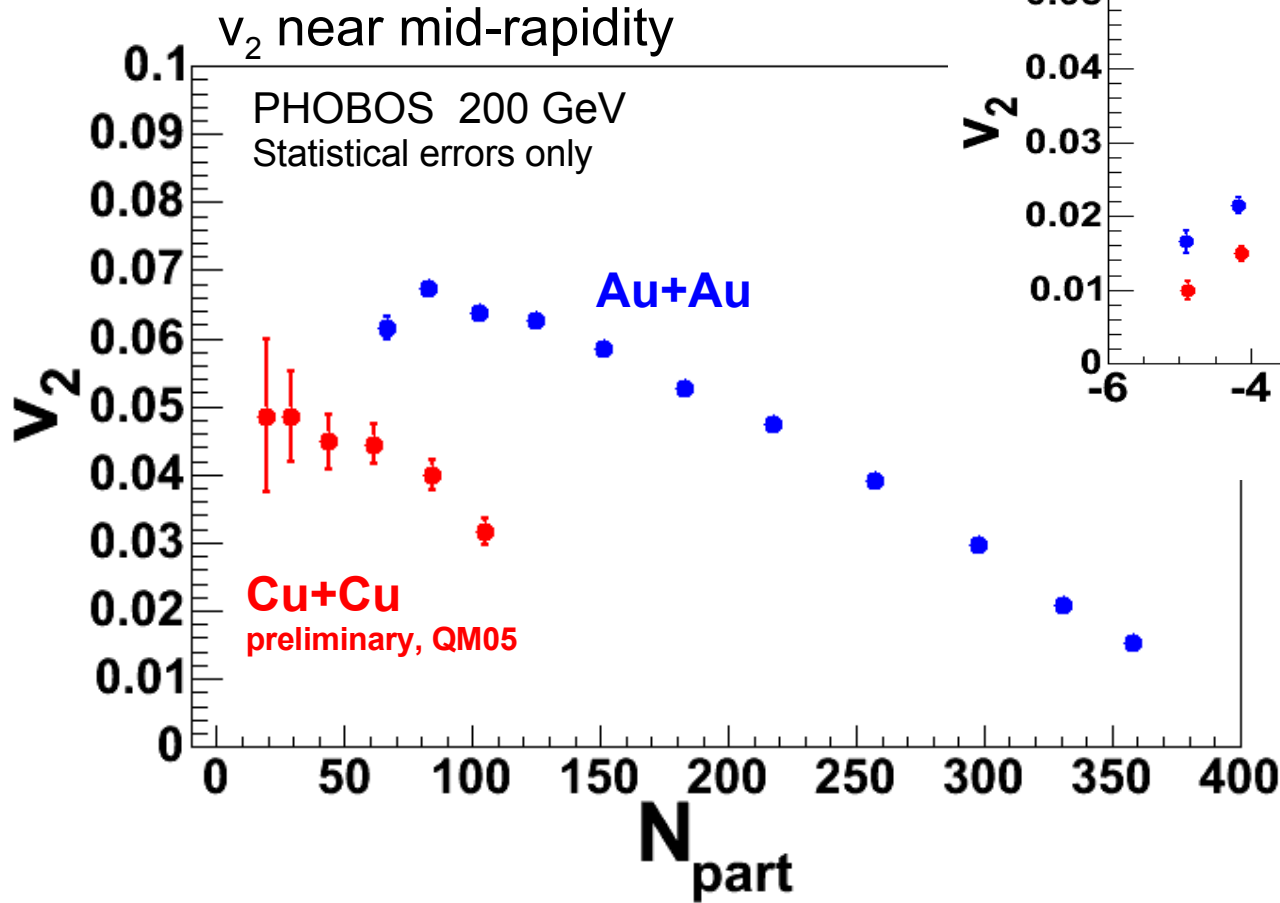
Direct (v_1) and elliptic (v_2) flow



$$\frac{dN}{d(\phi - \Psi_R)} = N_0 (1 + 2v_1 \cos(\phi - \Psi_R) + 2v_2 \cos(2(\phi - \Psi_R)) + \dots)$$



Elliptic flow in Cu+Cu and Au+Au

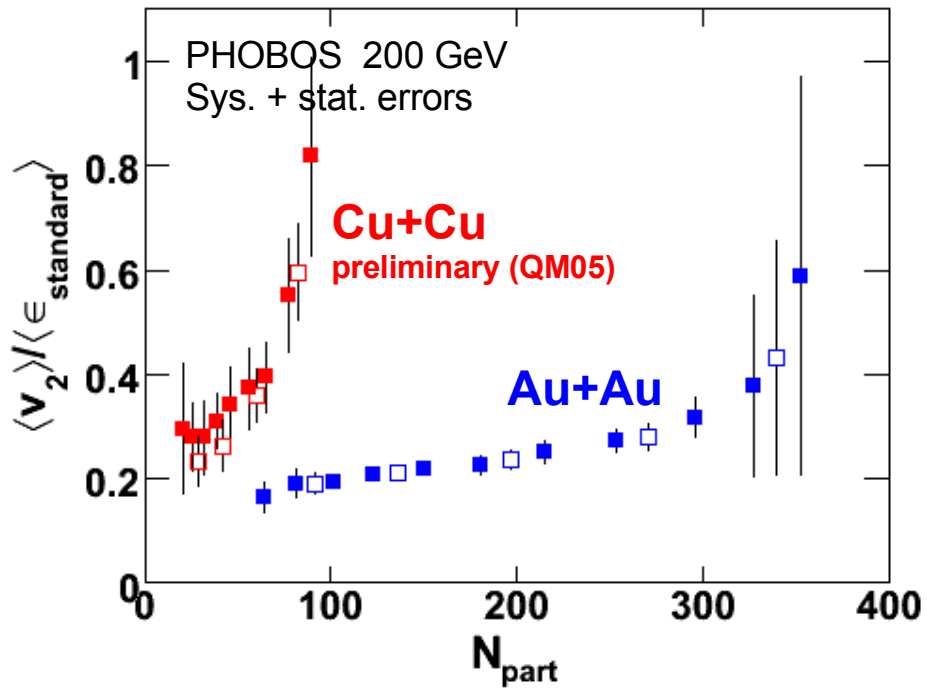


Au+Au: PRL 94, 122303 (2005)
Cu+Cu: prel. QM05, nucl-ex/0510042

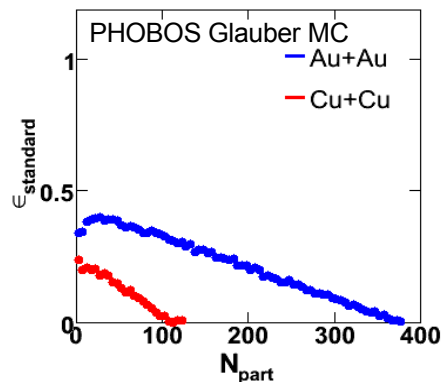
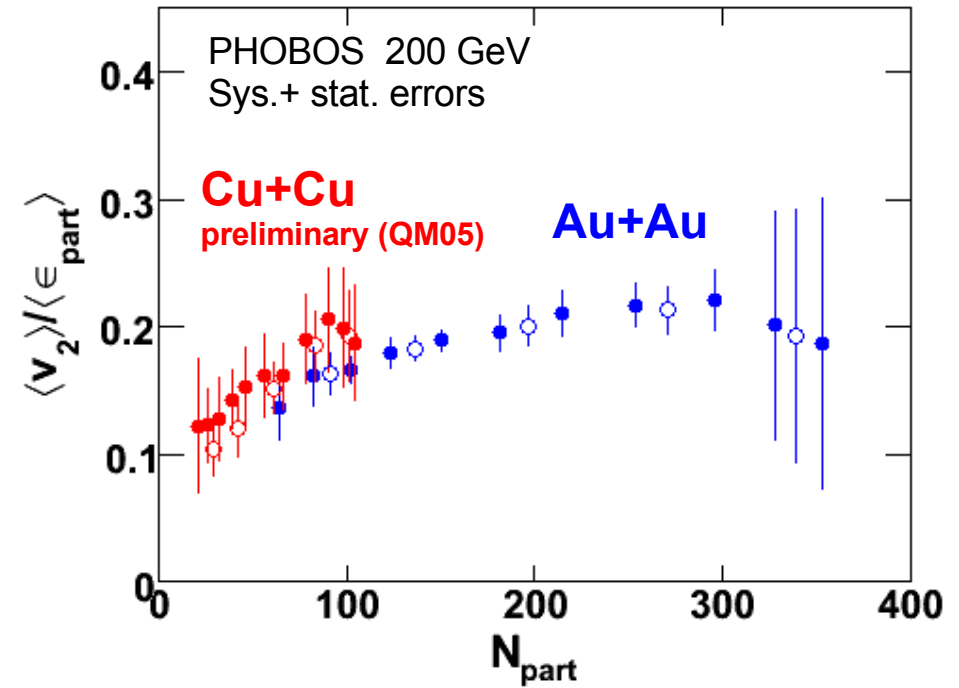
$$dN/d(\phi - \Psi_R) = N [1 + 2v_1 \cos(\phi - \Psi_R) + 2v_2 \cos(2\phi - 2\Psi_R) + \dots]$$

Scaled elliptic flow vs N_{part}

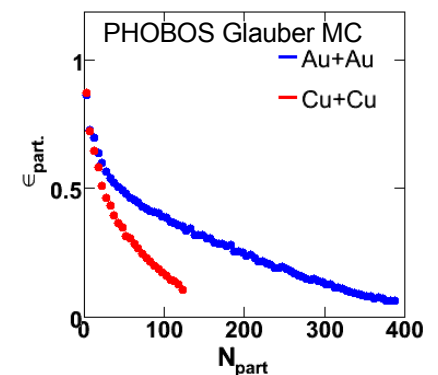
Standard Eccentricity



Participant Eccentricity



“Participant Eccentricity”
allows v_2 -scaling from
Cu+Cu to Au+Au

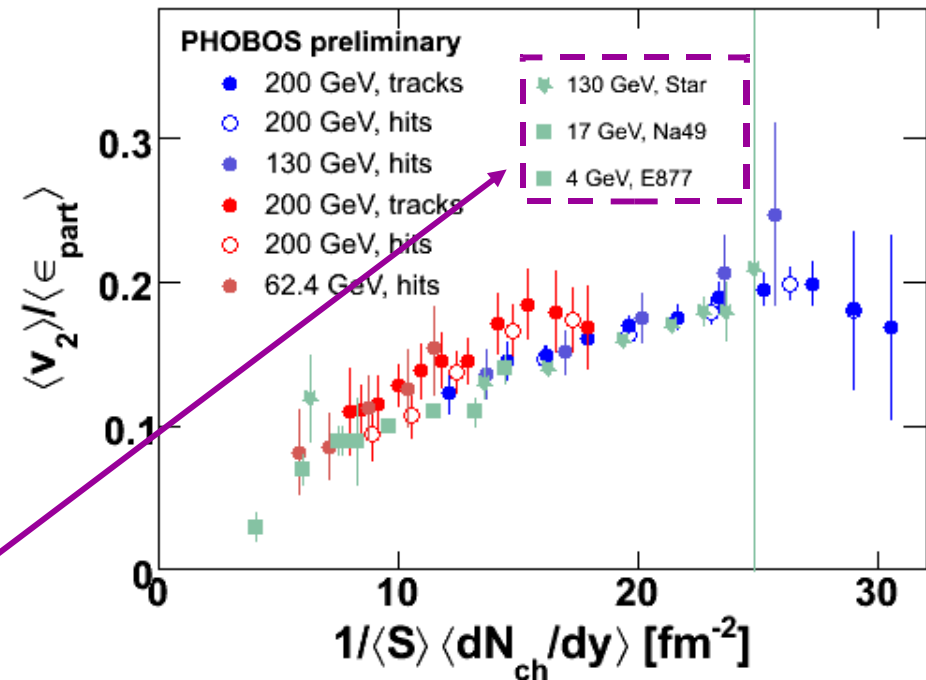


Low-density limit scaling (some details)

➤ **Caution:** we used ϵ_{part} for PHOBOS data. Important for Cu-Cu, less critical for Au-Au.

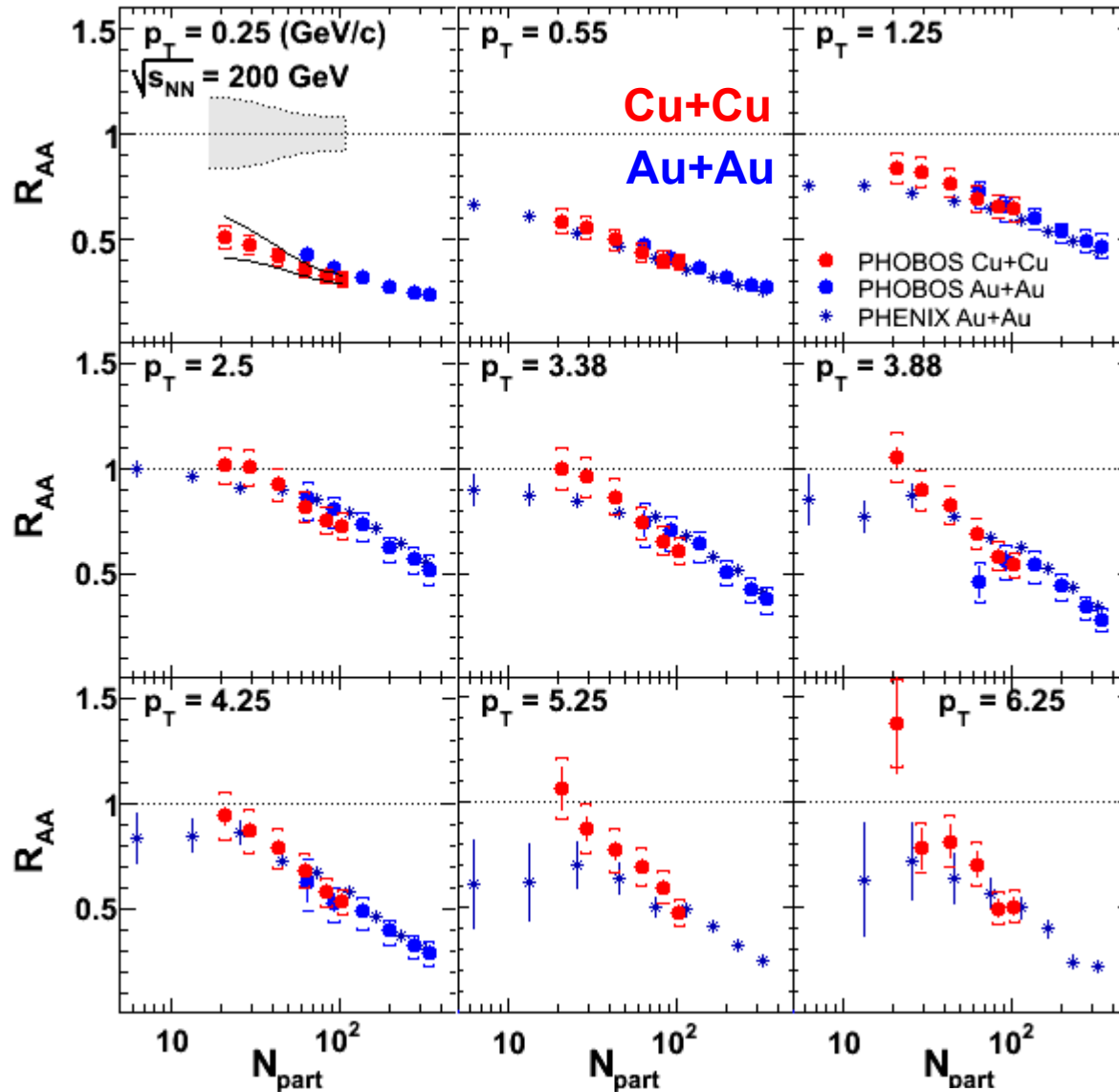
➤ Scale $v_2(\eta)$ to $\sim v_2(y)$ (10% lower)

➤ Scale $dN/d\eta$ to be $\sim dN/dy$ (15% higher)



Points for STAR, NA49 and E877 data taken from STAR Collaboration, Phys.Rev. C66 (2002) 034904 with no adjustments

Yields vs N_{part} at 200 GeV



$0.2 < \eta < 1.4$

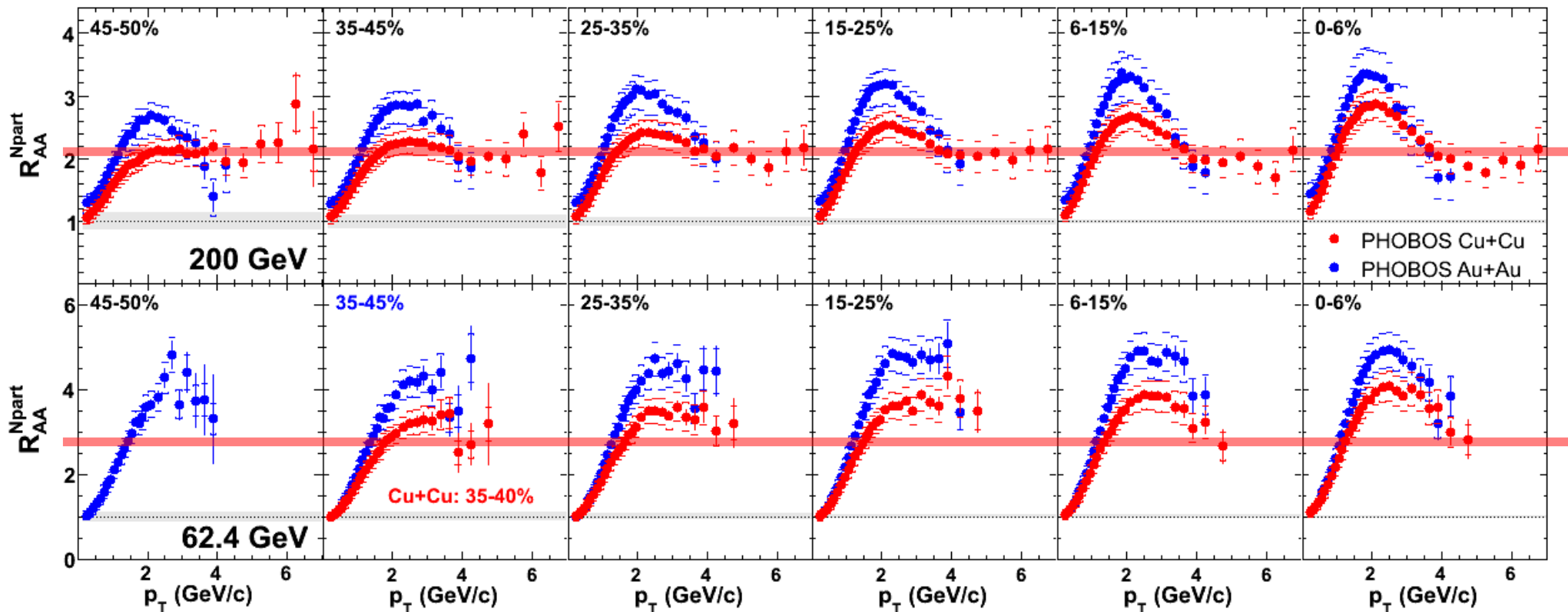
System-size
scaling
observed!

Au+Au: PRL 94, 082304 (2005), PLB 578, 297 (2004)
 Phenix: PLB 561, 82 (2003), PRC 69, 034910 (2004)
 Cu+Cu: PRL 96, 212301 (2006)
 p+p: UA1 -2.5 < η < 2.5 (acc. correction with PYTHIA)

$$R_{AA} = \frac{\sigma_{pp}^{inel}}{\langle N_{coll} \rangle} \frac{d^2 N_{AA} / dp_T d\eta}{d^2 \sigma_{p\bar{p}} / dp_T d\eta}$$

$R_{AA}^{N_{part}}$ in Au+Au and Cu+Cu at 200 GeV

$0.2 < \eta < 1.4$



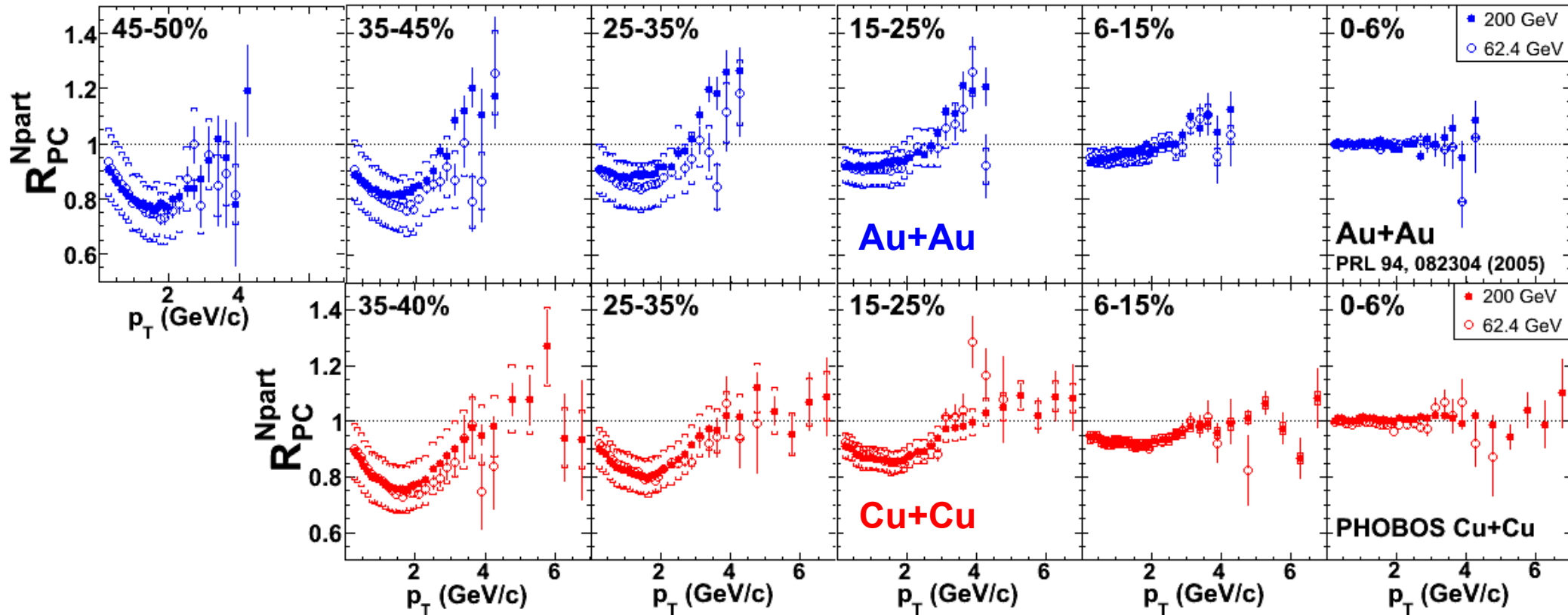
Yields normalized by N_{part} less centrality-dependent

Au+Au: PRL 94, 082304 (2005)
 Cu+Cu: PRL 96, 212301 (2006)

$$R_{AA}^{N_{part}} = \frac{\sigma_{pp}^{inel}}{\langle N_{part}/2 \rangle} \frac{d^2 N_{AA}/dp_T d\eta}{d^2 \sigma_{pp}/dp_T d\eta}$$

Factorization in bins of p_T

Normalized for central events



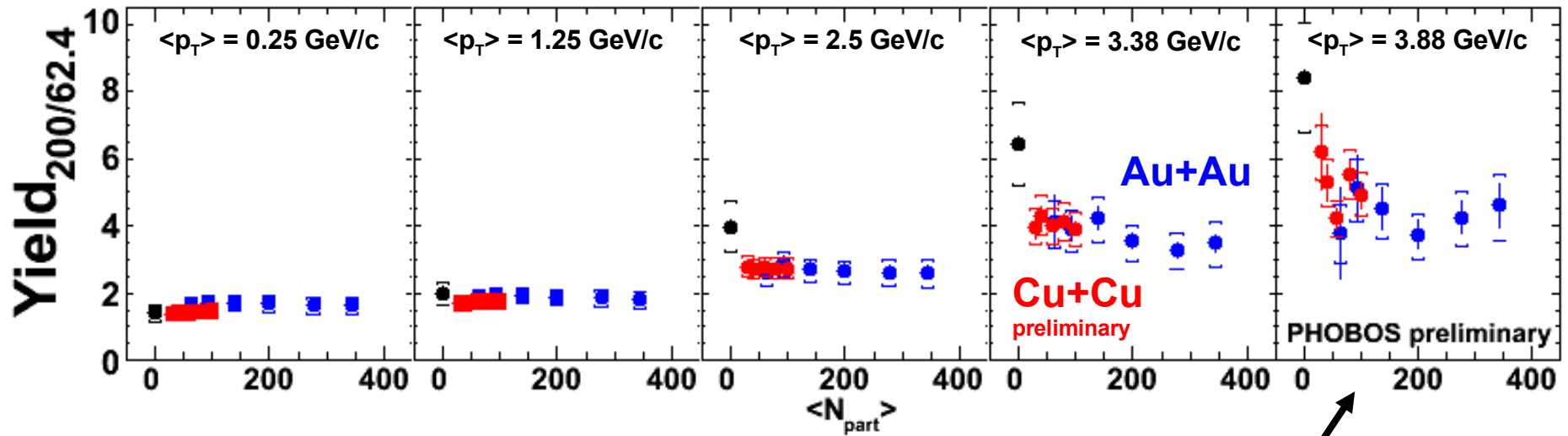
Same shape evolution from central to peripheral at 200 GeV and 62 GeV

Au+Au: PRL 94, 082304 (2005)
Cu+Cu: PRL 96, 212301 (2006)

$$R_{PC}^{N_{part}} = \frac{\langle N_{part}^{0-6\%} \rangle}{\langle N_{part} \rangle} \frac{d^2 N_{AA} / dp_T d\eta}{d^2 N_{AA}^{0-6\%} / dp_T d\eta}$$

Factorization in bins of p_T (2)

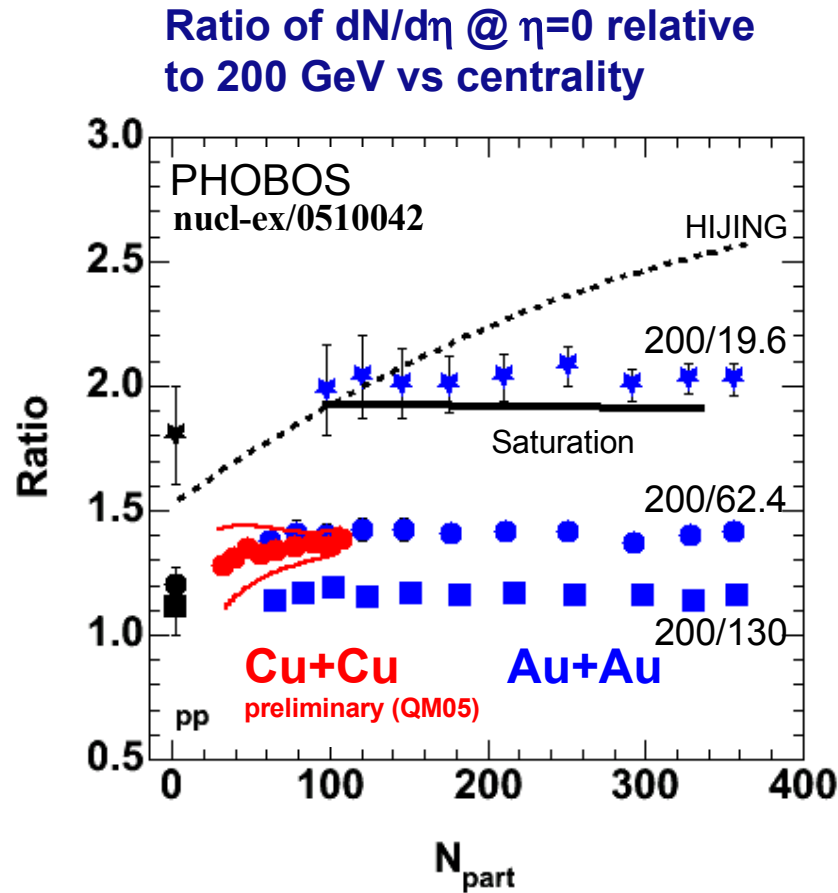
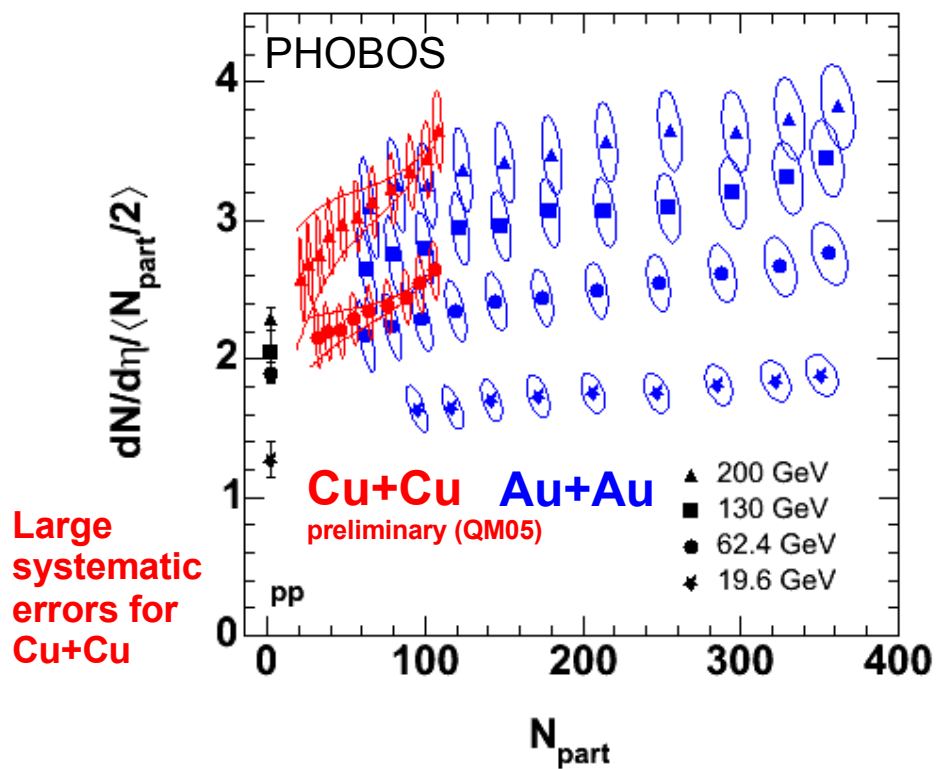
Ratio of charged hadron yields in 200 GeV to 62 GeV



Energy/centrality factorization
up to $p_T \approx 4$ GeV/c for $N_{part} > 40$

Au+Au: PRL 94, 082304 (2005)
Cu+Cu: PRL 96, 212301 (2006)

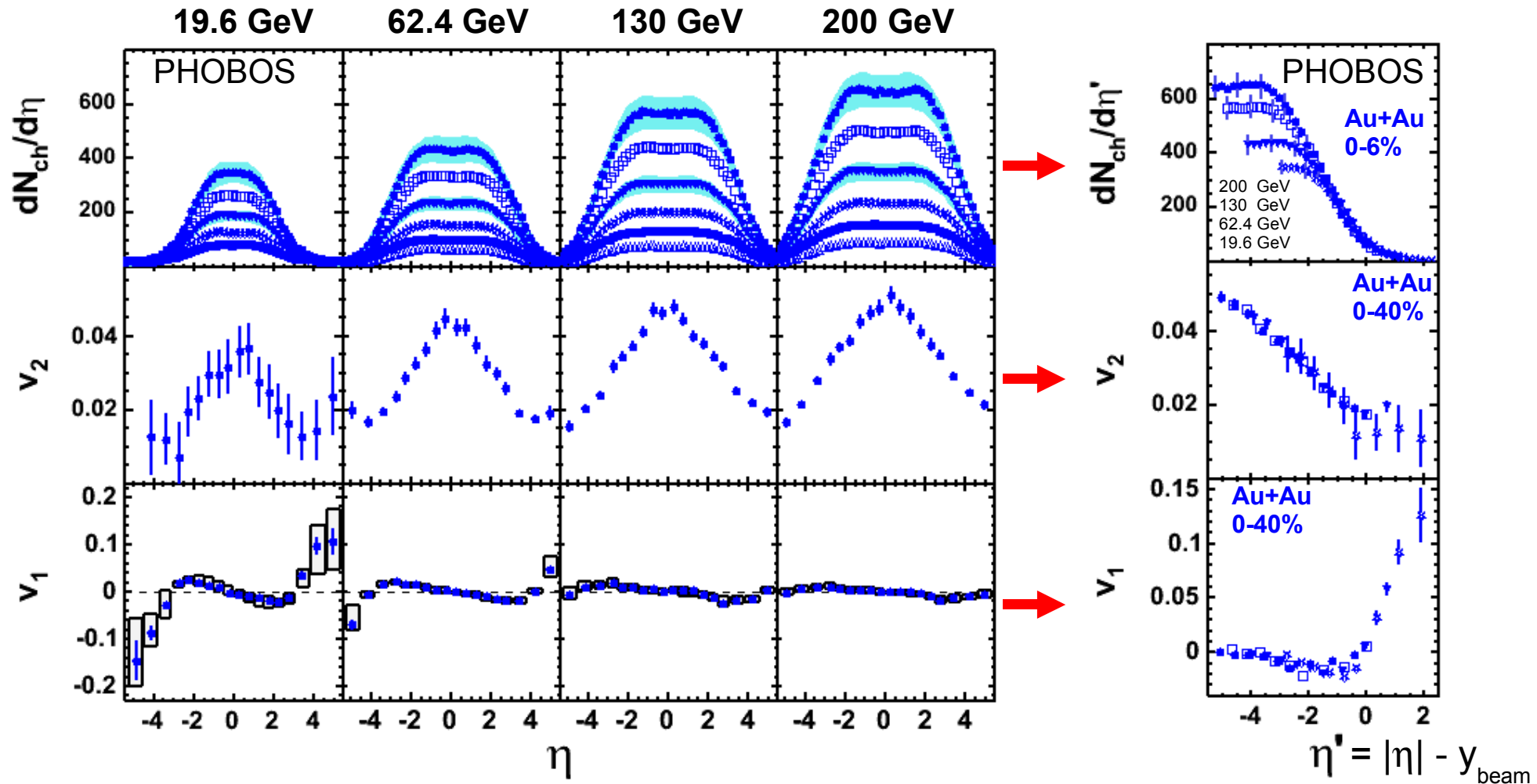
Factorization of energy and centrality



Factorization of energy and centrality due to initial state effect?

Au+Au: Phys. Rev. C70, 021902(R) (2004)
 62.4 GeV Au+Au: nucl-ex/0509034 (sub.to PRC)
 Cu+Cu (preliminary): QM05, nucl-ex/0510042

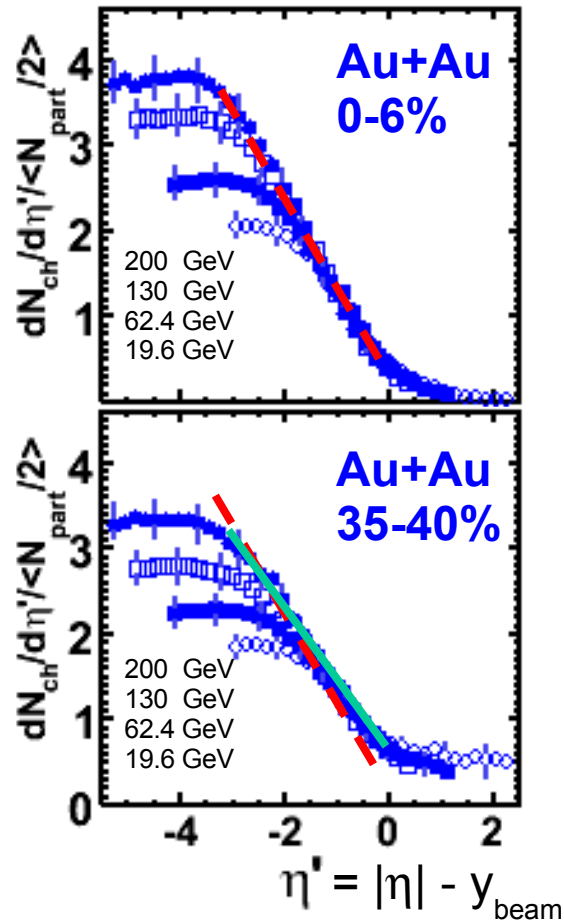
Limiting fragmentation (Au+Au)



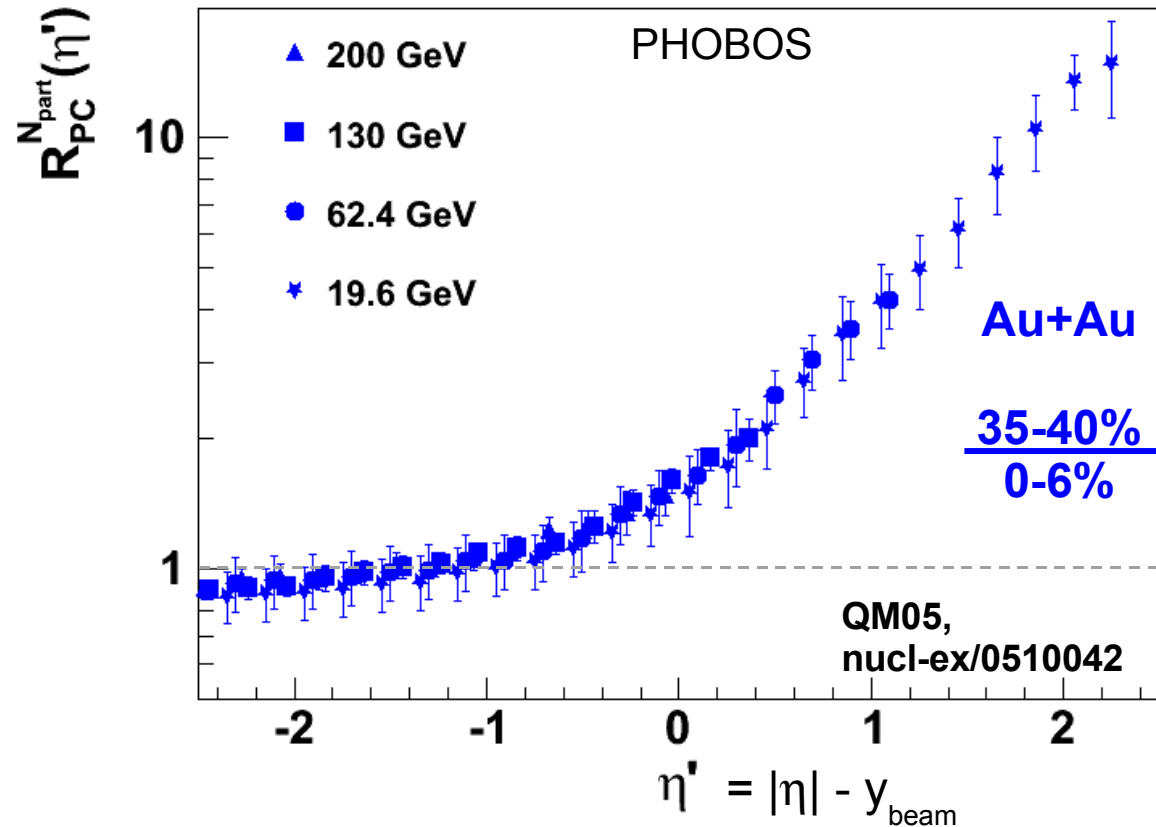
“Extended Longitudinal Scaling” of all longitudinal distributions
(same for Cu+Cu collisions)

QM05, nucl-ex/0510042

Factorization of longitudinal dynamics

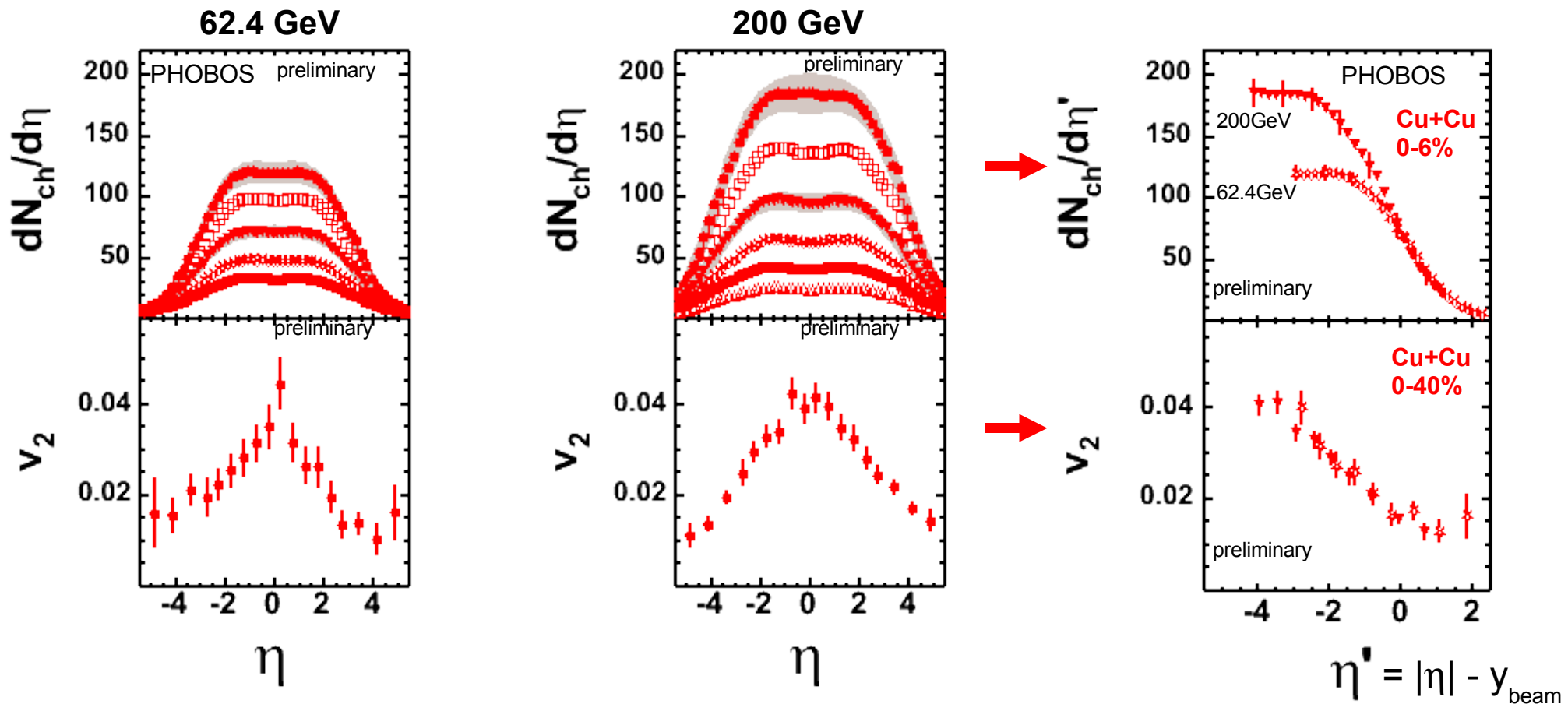


Ratio of 0-6% and 35-40% centrality bins, each normalized by N_{part}



$R_{\text{PC}}^{N_{\text{part}}}$ is energy independent!

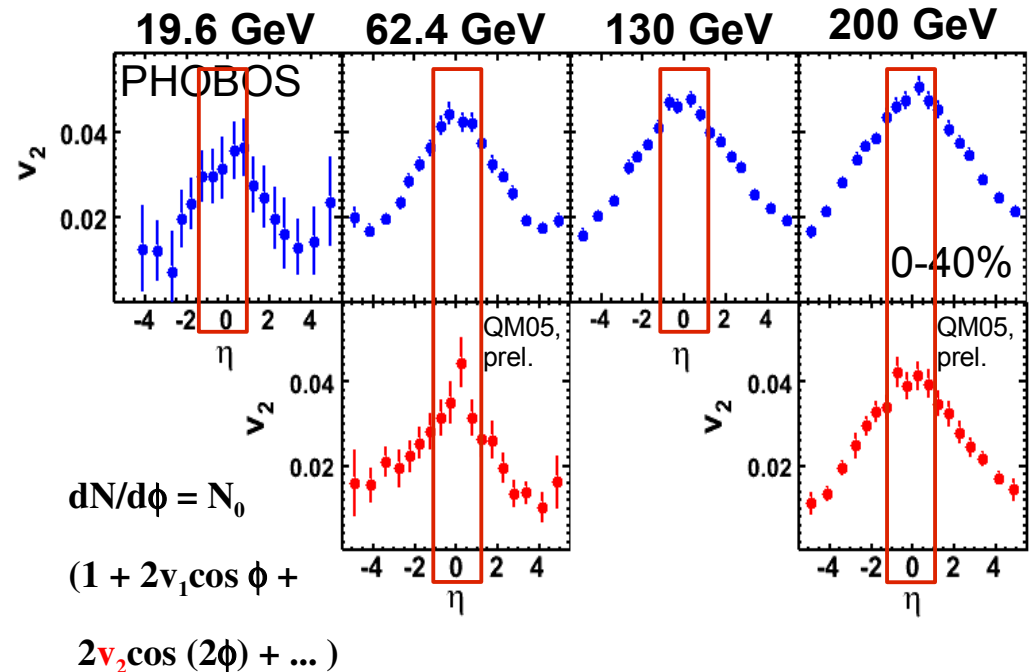
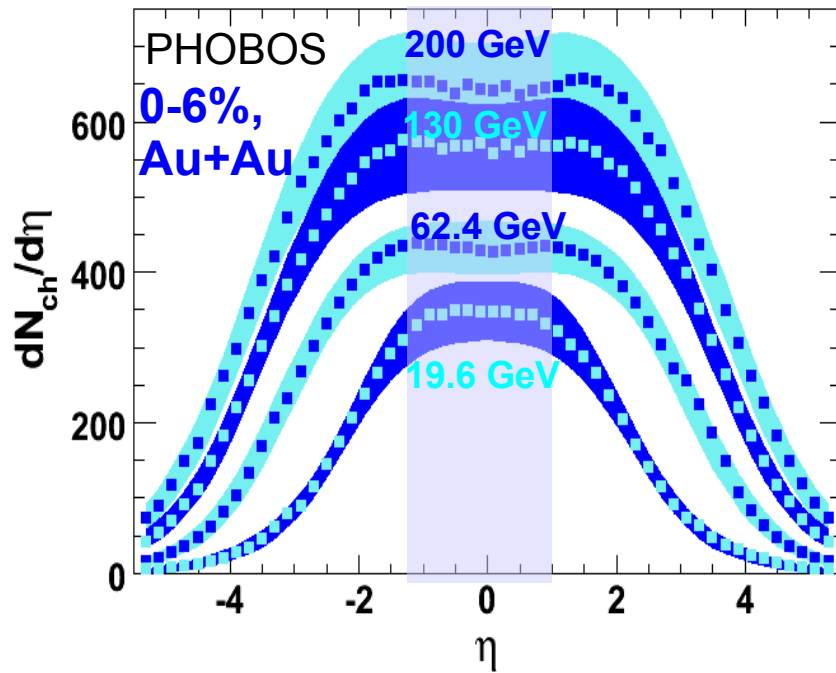
Limiting fragmentation (Cu+Cu)



**'Extended Longitudinal Scaling' also seen in Cu+Cu
Persists from p+p to Au+Au over large range in η '**

QM05, nucl-ex/0510042

Properties of the medium (2)



At 200 GeV:

$\epsilon > 3 \text{ GeV}/\text{fm}^3$

$$\epsilon = \frac{\langle E \rangle \times dN/d\eta \times \text{corr}}{\pi R^2 \times (0.1 - \text{few fm})}$$

PHOBOS WhitePaper

Strongly interacting medium
with extremely high energy density

WhitePaper: NPA, 757 28 (2005)
 v_2 Au+Au: PRL 94, 122303 (2005)
 v_2 Cu+Cu (prel.): QM05, nucl-ex/0510042