

Event-by-event fluctuations of azimuthal particle anisotropy in Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV

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This paper presents the first measurement of event-by-event fluctuations of the elliptic flow parameter v_2 in Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV as a function of collision centrality. The relative non-statistical fluctuations of the v_2 parameter are found to be approximately 40%. The results, including contributions from event-by-event elliptic flow fluctuations and from azimuthal correlations that are unrelated to the reaction plane (non-flow correlations), establish an upper limit on the magnitude of underlying elliptic flow fluctuations. This limit is consistent with predictions based on spatial fluctuations of the participating nucleons in the initial nuclear overlap region. These results provide important constraints on models of the initial state and hydrodynamic evolution of relativistic heavy ion collisions.

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Results from the Relativistic Heavy Ion Collider (RHIC) at Brookhaven National Laboratory suggest that a dense state of matter is formed in ultrarelativistic nucleus-nucleus collisions [1, 2, 3, 4]. Studies of final state charged particle momentum distributions show that the produced matter undergoes a rapid collective expansion transverse to the direction of the colliding nuclei. In particular, for collisions at non-zero impact parameter, the expansion shows a significant anisotropy in the azimuthal angle, strongly correlated with the anisotropic shape of the initial nuclear overlap region. The dominant component of this anisotropic expansion is called “elliptic flow” and is commonly quantified by the second coefficient, v_2 , of a Fourier decomposition of the azimuthal distribution of observed particles relative to the event-plane angle [5].

Elliptic flow has been studied extensively in Au+Au collisions at RHIC as a function of pseudorapidity, centrality, transverse momentum and center-of-mass energy [2, 3, 4, 6, 7, 8]. For Au+Au collisions at RHIC energies, the observed dependence of the elliptic flow signal on centrality and transverse momentum is found to be in good agreement with calculations in hydrodynamic models [8, 9]. This is considered evidence for an early equilibration of the colliding system and a low viscosity of the matter produced in the early stage of the collision

process [10]. In such calculations, for given conditions of the produced matter, the elliptic flow magnitude is found to be proportional to the eccentricity characterizing the transverse shape of the initial nuclear overlap region [11].

Measurements of elliptic flow in the smaller Cu+Cu system have shown surprisingly large values of elliptic flow, in particular for the most central collisions where the average eccentricity of the nuclear overlap region was expected to be small [12]. Experimental measurements of v_2 can be affected by event-by-event fluctuations in the initial geometry [13] and it is possible to reconcile the results for Cu+Cu and Au+Au collisions if these fluctuations are properly accounted for [12]. To this end, we have proposed a new definition of eccentricity, which does not make reference to the direction of the impact parameter vector, but rather characterizes the eccentricity through the event-by-event distribution of nucleon-nucleon interaction points obtained from a Glauber Monte-Carlo calculation [12, 14]. This method of calculating the initial state anisotropy, which leads to finite “participant eccentricity” values even for the most central events and has a large effect in the smaller Cu+Cu system, has been found to be crucial for understanding the comparison of Cu+Cu and Au+Au elliptic flow results [12].

Using the probabilistic distribution of interaction

points obtained from a Glauber calculation, performed on an event-by-event basis, leads to relative eccentricity fluctuations of $\sigma_{\epsilon_{\text{part}}}/\langle\epsilon_{\text{part}}\rangle \approx 40\%$ for Au+Au collisions at fixed number of participating nucleons (N_{part}) [14]. Similar calculations taking into account stochastic initial state interaction points in a color glass condensate (CGC) model also yield large relative eccentricity fluctuations of $\sigma_{\epsilon_{\text{part}}}/\langle\epsilon_{\text{part}}\rangle \approx 30\%$ [15]. If v_2 is proportional to ϵ , an event-by-event measurement of elliptic flow should therefore exhibit sizable fluctuations in v_2 , even at fixed N_{part} .

An event-by-event measurement of the anisotropy in heavy ion collisions is expected to yield fluctuations from three sources: statistical fluctuations due to the finite number of particles observed, elliptic flow fluctuations and other many-particle correlations. The statistical fluctuations in the observed v_2 signal can be taken out with a study of the measurement response to the input v_2 signal. Particle correlations other than flow (non-flow correlations) such as HBT, resonance decays and jets can resemble correlations due to elliptic flow and have various effects on different flow measurements. In particular, non-flow correlations can broaden the apparent v_2 distribution and enhance the observed v_2 fluctuations. This letter presents the first measurement of event-by-event dynamic fluctuations in v_2 , which include contributions from elliptic flow fluctuations and non-flow correlations.

The data shown here were taken with the PHOBOS detector at RHIC during the year 2004. The PHOBOS detector is composed primarily of silicon pad detectors for tracking, vertex reconstruction, and multiplicity measurements. Details of the setup and the layout of the silicon sensors can be found elsewhere [16]. The collision trigger, event selection and centrality determination are described in Ref. [17]. The Monte Carlo (MC) simulations of the detector performance are based on the HIJING event generator [18] and the GEANT 3.21 [19] simulation package, folding in the signal response for scintillator counters and silicon sensors.

The PHOBOS multiplicity array, composed of single layer silicon pad detectors, has a coverage of $|\eta| < 5.4$ over almost the full azimuth. We parametrize the pseudorapidity dependence, $v_2(\eta)$, with a single parameter, $v_2 \equiv v_2(0)$, and a triangular or trapezoidal shape, given by $v_2^{\text{tri}}(\eta) = v_2(1 - \frac{|\eta|}{6})$, or $v_2^{\text{trap}}(\eta) = \begin{cases} v_2 & \text{if } |\eta| < 2 \\ \frac{3}{2} v_2^{\text{tri}}(\eta) & \text{if } |\eta| \geq 2 \end{cases}$, respectively. Both of these parameterizations provide a reasonable description of the measured pseudorapidity dependence of elliptic flow [8].

The event-by-event measurement method has been developed to use all the available information from the multiplicity array to measure the elliptic flow at zero rapidity, v_2 , while allowing an efficient correction for the non-uniformities in the acceptance. Taking into account correlations only due to elliptic flow, the probability of a particle with given pseudorapidity, η , to be emitted in the azimuthal angle, ϕ , in an event with elliptic flow

magnitude, v_2 , and event-plane angle ϕ_0 is given by

$$p(\phi|v_2, \phi_0; \eta) = \frac{1}{2\pi} \{1 + 2v_2(\eta) \cos(2[\phi - \phi_0])\}. \quad (1)$$

The direction of the event-plane angle, ϕ_0 , is expected to align with the reaction plane angle if the initial geometry of heavy ion collisions is defined by two smooth Wood-Saxon distributions or with the participant eccentricity axis if initial geometry fluctuations are indeed present. In this measurement, ϕ_0 is determined from the distribution of final state particles without relying on any model about the initial geometry of the collision.

The angular coordinates (η, ϕ) of charged particles are measured using the location of the energy deposited in the silicon multiplicity detectors. After merging of signals in neighboring pads in cases where a particle travels through more than a single pad, the deposited energy is corrected for the angle of incidence, assuming that the charged particle originated from the primary vertex. Noise and background hits are rejected by placing a lower threshold on this angle-corrected deposited energy. Depending on η , merged hits with less than 50-60% of the energy loss expected for a minimum ionizing particle are rejected [20]. Since the multiplicity array consists of single-layer silicon detectors, there is no p_T , charge or mass information available for the particles. All charged particles above a low- p_T cutoff of about 7 MeV/c at $\eta=3$, and 35 MeV/c at $\eta=0$ (the threshold below which a charged pion is stopped by the beryllium beam pipe) are included on equal footing. We define the probability density function (PDF) for a hit position (η, ϕ) for an event with v_2 and event-plane angle ϕ_0 as

$$P(\phi|v_2, \phi_0; \eta) = \frac{1}{s(v_2, \phi_0; \eta)} p(\phi|v_2, \phi_0; \eta), \quad (2)$$

where the normalization parameter $s(v_2, \phi_0; \eta)$ is calculated in small bins of η such that the PDF folded with the acceptance is normalized to the same value for different values of v_2 and ϕ_0 . The normalization parameter is given by

$$s(v_2, \phi_0, \eta) = \int_{\eta-\Delta\eta}^{\eta+\Delta\eta} A(\eta', \phi) p(\phi|v_2, \phi_0; \eta') d\phi d\eta', \quad (3)$$

where the acceptance function, $A(\eta, \phi)$ denotes the probability of a particle moving in the η, ϕ direction to yield a reconstructable hit.

For a single event, the likelihood function of v_2 and ϕ_0 is defined as $L(v_2, \phi_0) \equiv \prod_{i=1}^n P(\phi_i|v_2, \phi_0; \eta_i)$, where the product is over all n hits in the detector. The likelihood function describes the probability of observing the hits in the event for the given values of the parameters v_2 and ϕ_0 . The parameters v_2 and ϕ_0 are varied to maximize the likelihood function and estimate the observed values, v_2^{obs} and ϕ_0^{obs} , for each event.

The response of the event-by-event measurement is non-linear and depends on the observed multiplicity n . Therefore, a detailed study of the response function is

required to extract the true v_2 distribution from the measured v_2^{obs} distribution. Let $f(v_2)$ be the true v_2 distribution for a set of events in a given centrality bin, and $g(v_2^{\text{obs}})$ the corresponding observed distribution. The true and observed distributions are related by

$$g(v_2^{\text{obs}}) = \int K(v_2^{\text{obs}}, v_2, n) f(v_2) dv_2 N(n) dn, \quad (4)$$

where $N(n)$ is the multiplicity distribution of the given set of events and $K(v_2^{\text{obs}}, v_2, n)$ is the expected distribution of v_2^{obs} for events with fixed input flow v_2 , and constant observed multiplicity n .

The response function, $K(v_2^{\text{obs}}, v_2, n)$ is determined by performing the event-by-event analysis on modified HIJING events with flow of fixed magnitude v_2 . The flow is introduced by redistributing the generated particles in each event in the ϕ direction according to the probability distribution given by Eq. 1 and the assumed pseudorapidity dependence of v_2 . For the two parameterizations of $v_2(\eta)$, triangular and trapezoidal, used in the event-by-event measurement, the corresponding response functions, K^{tri} and K^{trap} , are calculated. Fitting smooth functions through the observed response functions decreases bin-to-bin fluctuations and allows for interpolation in v_2 and n . The response of a perfect detector can be determined as a function of event multiplicity [11]. In practice, some empirical modifications to the ideal relation, accounting for detector effects, significantly improve fits to the response function, leading to

$$K(v_2^{\text{obs}}, v_2, n) = \frac{v_2^{\text{obs}}}{\sigma^2} \times \exp\left(-\frac{(v_2^{\text{obs}})^2 + (v_2^{\text{mod}})^2}{2\sigma^2}\right) I_0\left(\frac{v_2^{\text{obs}} v_2^{\text{mod}}}{\sigma^2}\right), \quad (5)$$

with $v_2^{\text{mod}} = (An + B)v_2$ and $\sigma = C/\sqrt{n} + D$, and where I_0 is the modified Bessel function. The four parameters (A, B, C, D) are obtained by fits to observed $K(v_2^{\text{obs}}, v_2, n)$ in the modified HIJING samples.

Correcting for all known effects incorporated in our MC, we obtain the true event-by-event v_2 distribution, $f(v_2)$, which includes contributions from elliptic flow fluctuations and non-flow correlations. We assume $f(v_2)$ to be a Gaussian in the range $v_2 > 0$ [21] with two parameters, \bar{v}_2 and σ_{v_2} , denoting the mean and standard deviation in the given range. For given values of the parameters, it is possible to take the integral in Eq. 4 numerically to obtain the expected v_2^{obs} distribution. Comparing the expected and observed distributions, the values of \bar{v}_2 and σ_{v_2} are found by a maximum-likelihood fit. Midrapidity ($|\eta| < 1$) results from the two parameterizations of $v_2(\eta)$, triangular and trapezoidal, are averaged to obtain the mean $\langle v_2 \rangle = 0.5(\frac{11}{12}\bar{v}_2^{\text{tri}} + \bar{v}_2^{\text{trap}})$ and standard deviation $\sigma_{\text{dyn}} = 0.5(\frac{11}{12}\sigma_{v_2}^{\text{tri}} + \sigma_{v_2}^{\text{trap}})$ of the elliptic flow parameter v_2 , where the factor $\frac{11}{12}$ comes from integration over η .

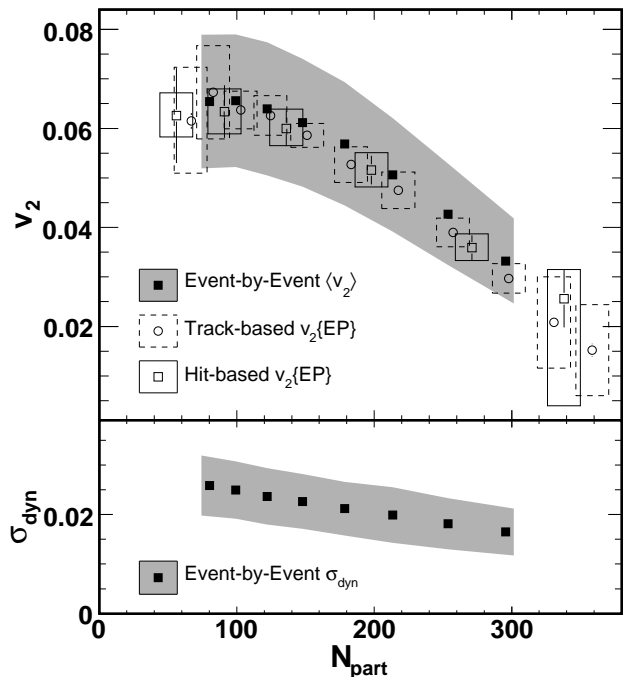


FIG. 1: $\langle v_2 \rangle$ (top) and σ_{dyn} (bottom) versus N_{part} for Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV. Previously published event-plane v_2 results for the same collision system are shown for comparison [7]. Boxes and gray bands show 90% C.L. systematic errors and the error bars represent 1- σ statistical errors. The results are for $0 < \eta < 1$ for the track-based method and $|\eta| < 1$ for hit-based and event-by-event methods.

The induced v_2 fluctuations arising from fluctuations in the number of participating nucleons are calculated by parameterizing the $\langle v_2 \rangle$ versus N_{part} results and folding them with the N_{part} distributions in each centrality bin. The relative contribution of these fluctuations to σ_{dyn} is found to be less than 8%. Results in this letter are presented after subtraction of N_{part} induced fluctuations.

Systematic errors have been investigated in three main classes: variations to the event-by-event analysis, response of the analysis procedure to known input σ_{dyn} , and intrinsic differences between HIJING events and data. Various modifications to the event-by-event analysis have been applied. Corrections, previously used in the hit-based event-plane analysis [6, 7], to account for signal dilution due to detector occupancy and to create an appropriately symmetric acceptance have been applied to both HIJING and data events. The thresholds for background hit rejection have been varied. These changes lead to at most 4% variations in the observed relative fluctuations demonstrating a good understanding of the response function. The determination of the response function and the final fitting procedure have been studied by performing the analysis on sets of modified HIJING events with varying input σ_{dyn} . Differences between input and reconstructed σ_{dyn} are identified as a contribution to the systematic uncertainty.

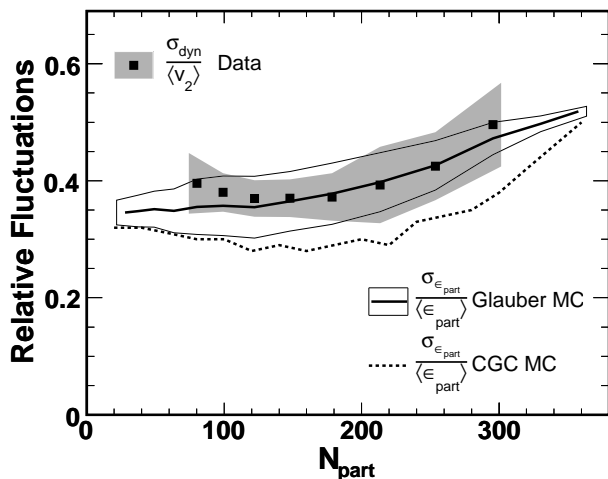


FIG. 2: $\sigma_{\text{dyn}}/\langle v_2 \rangle$ versus N_{part} for Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV. The continuous and dashed thick black lines show $\sigma(\epsilon_{\text{part}})/\langle \epsilon_{\text{part}} \rangle$ calculated in Glauber MC [14] and CGC [15] models, respectively. The shaded grey band (for data) and thin black contour line (for Glauber MC) show 90% C.L. systematic errors. See text for discussion of comparing the plotted data to the models.

The sensitivity of the measurement is observed to be limited for very low $\langle v_2 \rangle$ values. Therefore the 0-6% most central events, where the reconstructed $\langle v_2 \rangle$ is below 3%, have been omitted. Differences between HIJING and data in terms of $dN/d\eta$ and $v_2(\eta)$ can, in principle, lead to a miscalculation of the response function. A sample of MC events has been generated, in which the $dN/d\eta$ distribution of HIJING events is widened by a simple scaling to match the measurements in data within the errors. The difference between results obtained with and without this modification, as well as the difference between results with two different parameterizations of $v_2(\eta)$ are identified as contributions to the systematic uncertainty. Other systematic studies include using a flat, rather than Gaussian, ansatz for the true v_2 distribution, $f(v_2)$, and performing the analysis in different collision vertex and event-plane angle bins. The uncertainty in the contribution of N_{part} induced fluctuations has also been estimated via different parameterizations of the $\langle v_2 \rangle$ versus N_{part} results. Contributions from all error sources described above are added in quadrature to derive the 90% confidence level error.

Fig. 1 shows the mean, $\langle v_2 \rangle$, and the standard deviation, σ_{dyn} , of the elliptic flow parameter v_2 at midrapidity as a function of the number of participating nucleons, in Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV for 6-45% most central events. The results for $\langle v_2 \rangle$ are in agreement with the previous PHOBOS v_2 measurements [7], which were obtained with the event-plane method for charged hadrons within $|\eta| < 1$. The uncertainties in $dN/d\eta$ and $v_2(\eta)$, as well as differences between HIJING and the data in these quantities, introduce a large uncertainty in the overall scale in the event-by-event analysis due

to the averaging procedure over the wide pseudorapidity range. The event-plane method used in the previous PHOBOS measurements are known to be sensitive to the second moment, $\sqrt{\langle v_2^2 \rangle}$, of elliptic flow [14]. The fluctuations presented in this letter would lead to a difference of approximately 10% between the mean, $\langle v_2 \rangle$, and the RMS, $\sqrt{\langle v_2^2 \rangle}$, of elliptic flow at a fixed value of N_{part} . However, a detailed comparison is not possible for our $\langle v_2 \rangle$ measurements due to the scale errors, which dominate the systematic uncertainty on $\langle v_2 \rangle$ and σ_{dyn} . Most of the scale errors cancel in the ratio, $\sigma_{\text{dyn}}/\langle v_2 \rangle$, shown in Fig. 2, revealing large relative fluctuations of approximately 40%.

These results include contributions from both elliptic flow fluctuations and non-flow correlations. With no prior information on the direction of the reaction plane, it is not possible to disentangle these two contributions completely. However, several methods have been proposed to estimate the contribution of non-flow correlations to the observed dynamic v_2 fluctuations. One can assume that the correlations in A+A collisions can be modeled by superimposing p+p collisions [22]. However, data from RHIC reveal many differences between the overall correlation structure in Au+Au and p+p (e.g. [23, 24, 25, 26]). A more data-driven approach assumes that non-flow correlations will be small for particle pairs with large pseudorapidity separations (for example, $\Delta\eta > 2$) [27]. Under this latter assumption, it is estimated that the relative fluctuations in the actual elliptic flow account for a very large fraction (79-97%) of the observed relative dynamic fluctuations in the v_2 parameter [27]. No attempt was made to correct the data in Fig. 2 for non-flow effects since the validity of the large $\Delta\eta$ assumption cannot be unambiguously tested with existing data.

The measured dynamic fluctuations in v_2 are directly comparable to models that incorporate both elliptic flow and two particle correlations. Furthermore, without making any assumptions about non-flow, these data establish an upper limit on the magnitude of underlying elliptic flow fluctuations. Also shown in Fig. 2 are $\sigma_{\epsilon_{\text{part}}}/\langle \epsilon_{\text{part}} \rangle$ at fixed values of N_{part} obtained in MC Glauber [14] and color glass condensate (CGC) [15] calculations. The 90% confidence level systematic errors for MC Glauber calculations (shown as a contour line in Fig. 2) are estimated by varying Glauber parameters as discussed in Ref. [12]. Due to the uncertainties in non-flow effects discussed previously, it is not possible to conclude which of these two models is more consistent with the measured dynamic v_2 fluctuations.

In summary, we have presented the first measurement of event-by-event v_2 fluctuations in Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV. The relative non-statistical fluctuations of the v_2 parameter are found to be approximately 40%. Independent estimates of the non-flow correlation magnitude suggest that the major contribution to these fluctuations are due to intrinsic elliptic flow fluctuations. We show that the magnitude and centrality dependence

of observed dynamic fluctuations are consistent with predictions for fluctuations of the initial shape of the collision region. These results provide qualitatively new information on the initial conditions of heavy ion collisions and the subsequent collective expansion of the system.

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