



An overview of stopping at RHIC

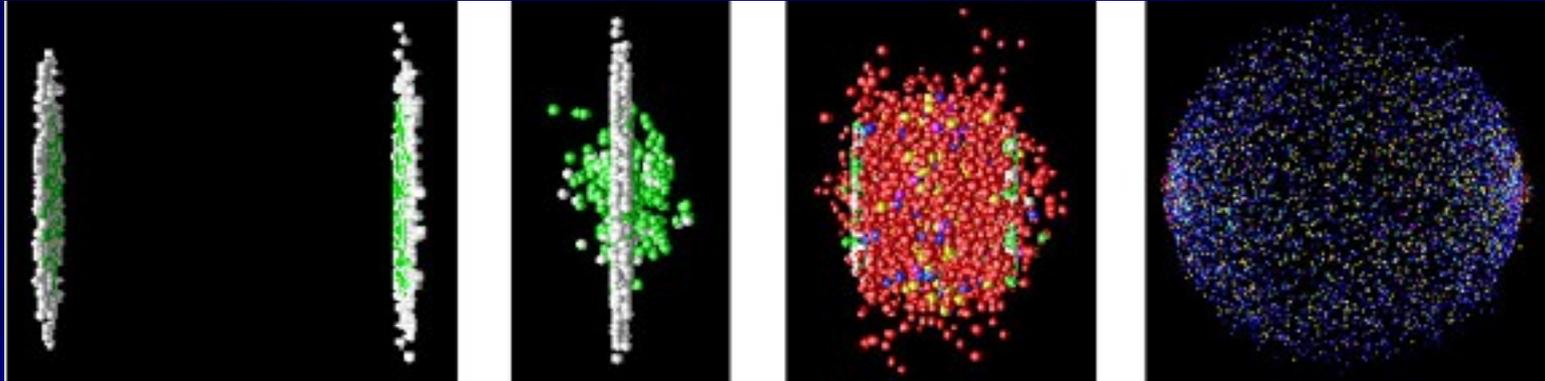
- An introduction to stopping
- How to experimentally measure stopping:
 - $d^2N/dydp_T \rightarrow dN/dy$
 - dN/dy net-p $\rightarrow dN/dy$ net-B / weak decay corrections
 - Important for comparing to theory!
 - Observations about the rapidity loss in A+A
- New results from BRAHMS
- Models of stopping
- How does stopping fit in the big picture of particle production

An Introduction to Stopping





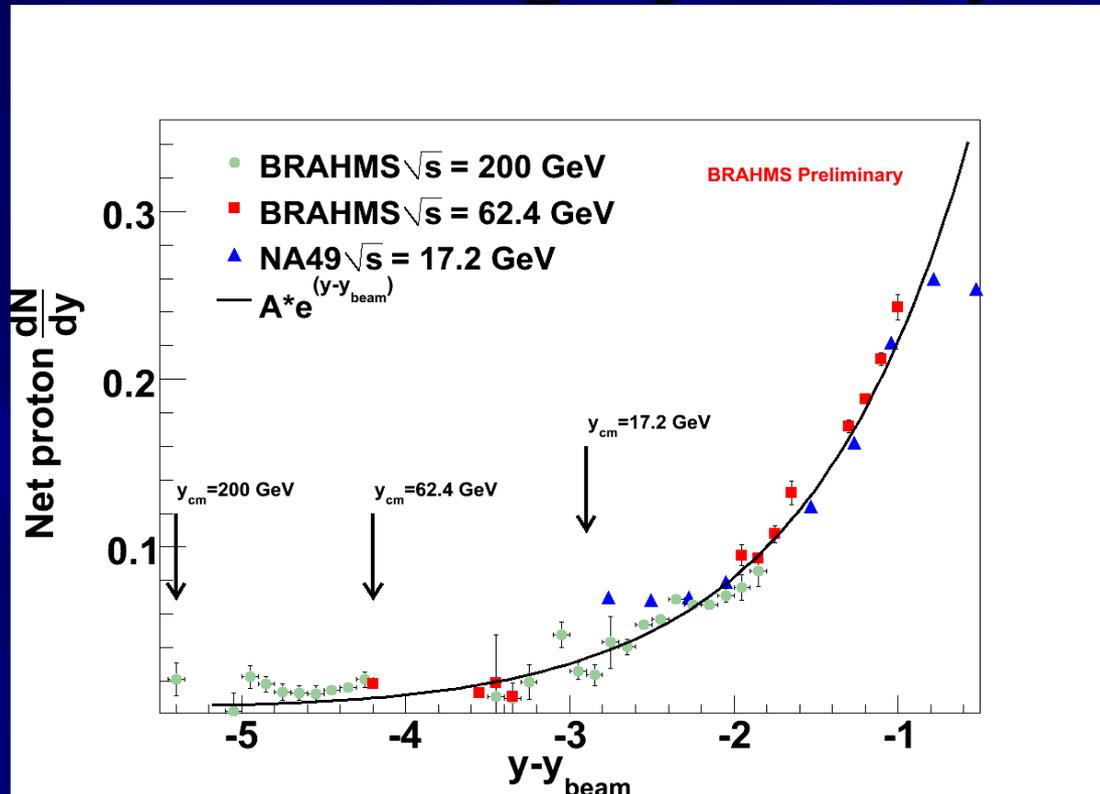
What is stopping ?



- Energy conservation
 - Kinetic energy of initial baryons is used to create a hot and dense zone.
- Baryon (qqq) number conservation
 - Before: $2 \cdot 197$ baryons \rightarrow After: $2 \cdot 197$ net-baryons (B-Bbar)
- Stopping is the study of baryon transport in the collisions
 - Initial interactions \rightarrow understand the formation of the initial state!
 - Rescattering/flow of partons and hadrons
 - Decays



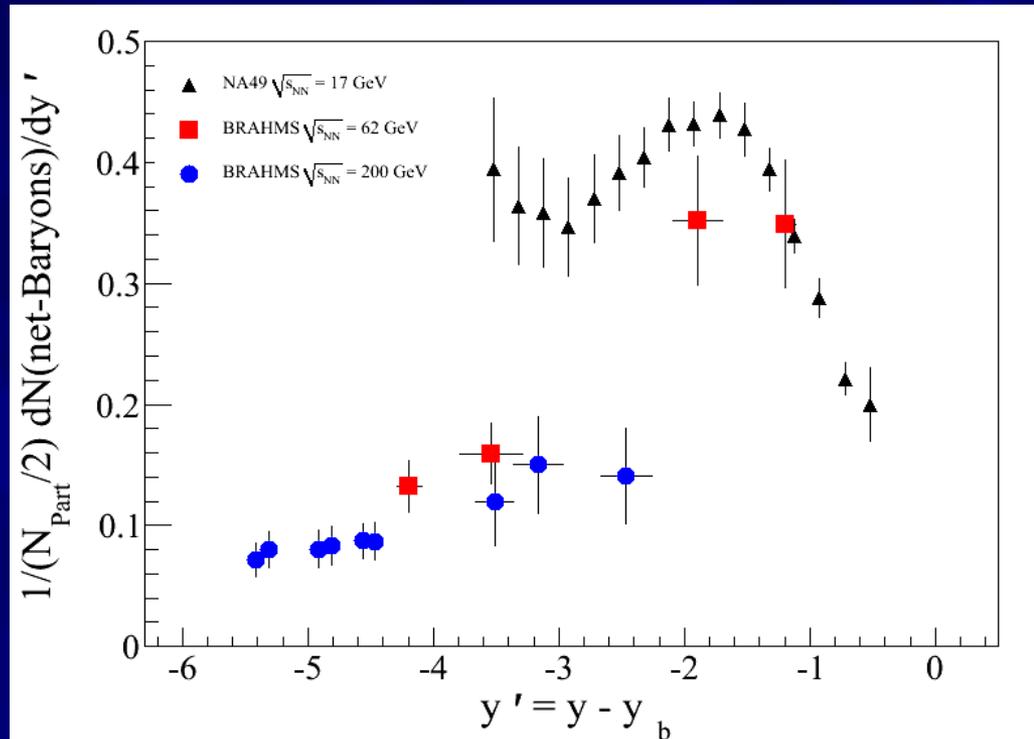
Stopping in $p+p$ collisions: Scaling of dN/dy



- Universal behavior of dN/dy for net-protons when observed in the “projectile” frame



Stopping in $A+A$ collisions: No obvious scaling of dN/dy

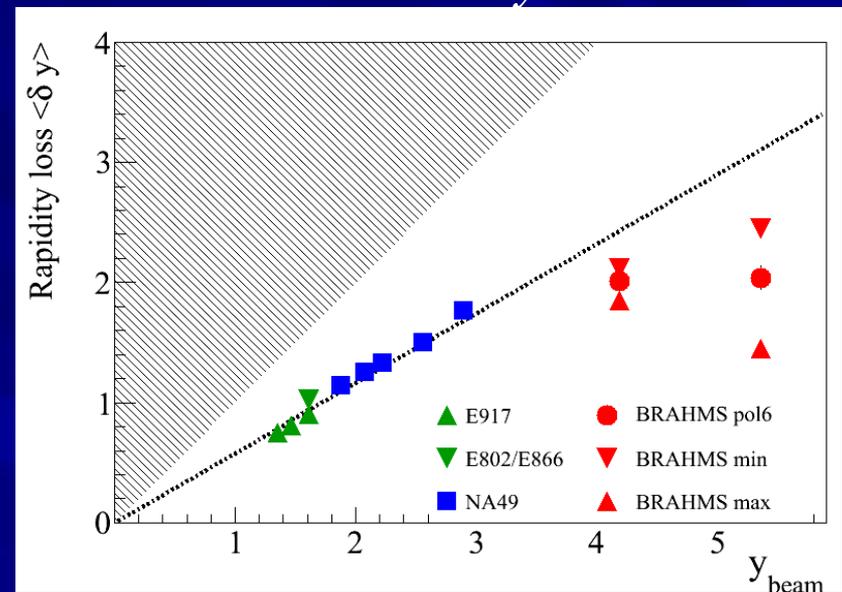
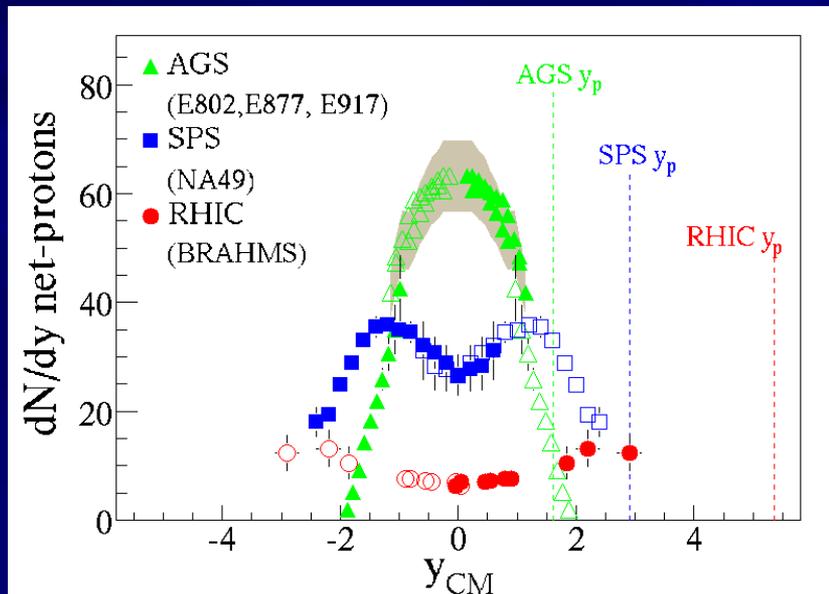


- No obvious scaling in projectile frame
 - But when the target contribution is subtracted there is scaling!



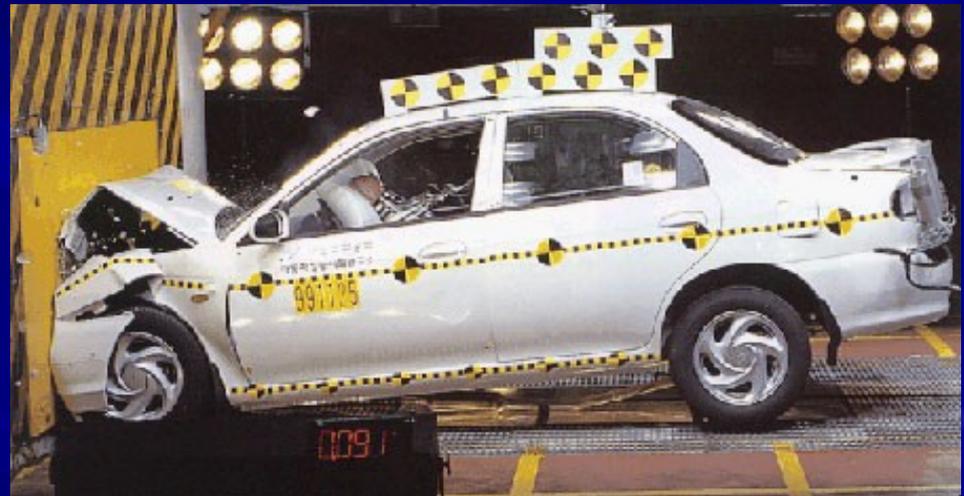
Rapidity loss: A way to quantify stopping

Rapidity loss (in CM): $\langle \delta y \rangle = y_{beam} - \int_0^{y_{beam}} y \frac{dN_{net-b}(y)}{dy} dy$



- At lower energy (until SPS) rapidity loss scales with y_{beam} [Phys.Rev.C52, 2684, (1995)]
- Above SPS energies it seems to saturate

How to Experimentally Measure Stopping





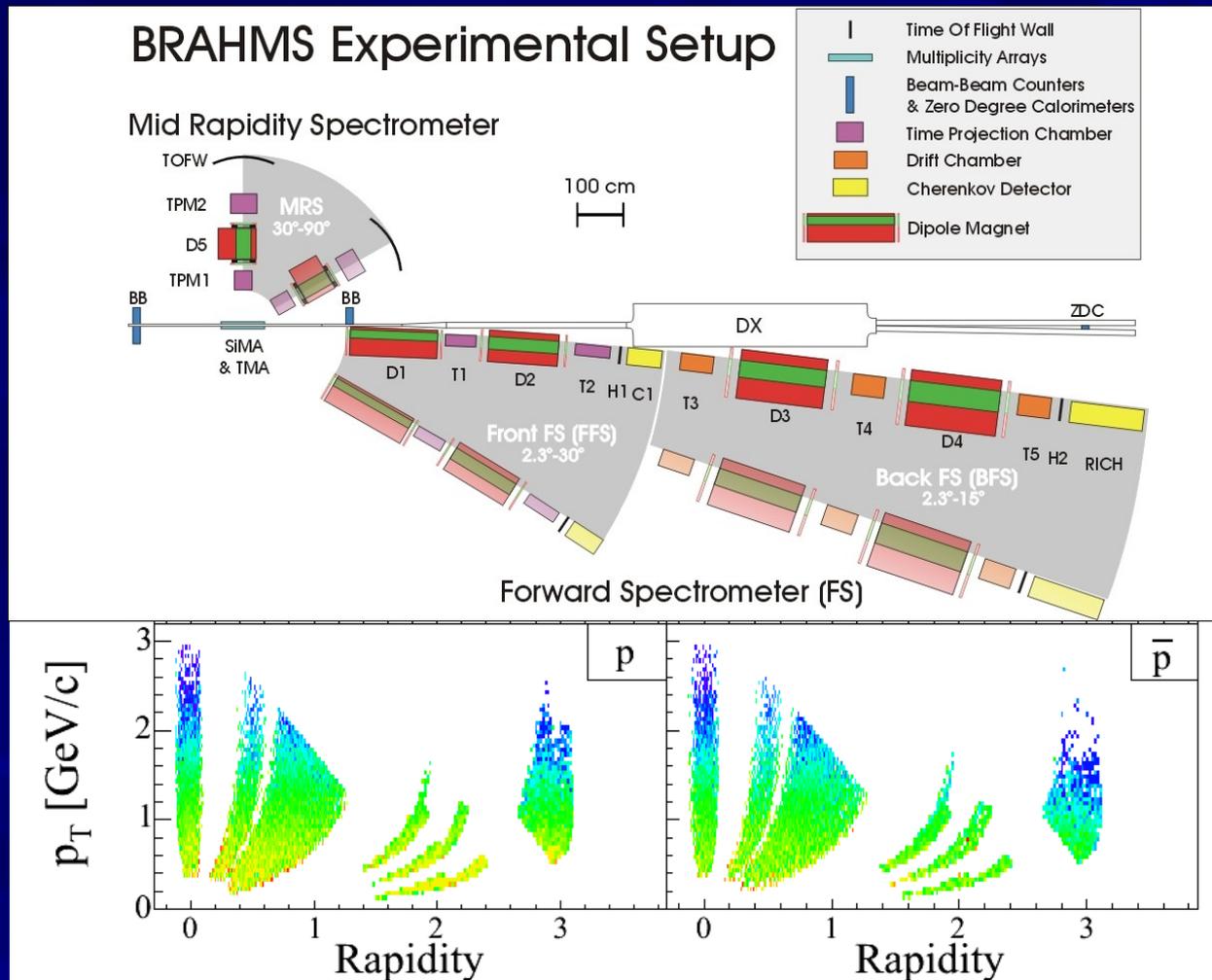
How to measure the net-baryon dN/dy after the collision

- Need good rapidity coverage
 - BRAHMS, (STAR FTPC), NA49
- Need good p_T coverage
 - 1st problem: extrapolate spectra to obtain dN/dy
- Need good particle identification for protons, Λ s and neutrons
 - 2nd problem: Neutrons are hard to measure
 - 3rd problem: BRAHMS can measure protons, but not Λ s. STAR can measure forward Λ s only.

In the following I will use BRAHMS as an example



Starting point:

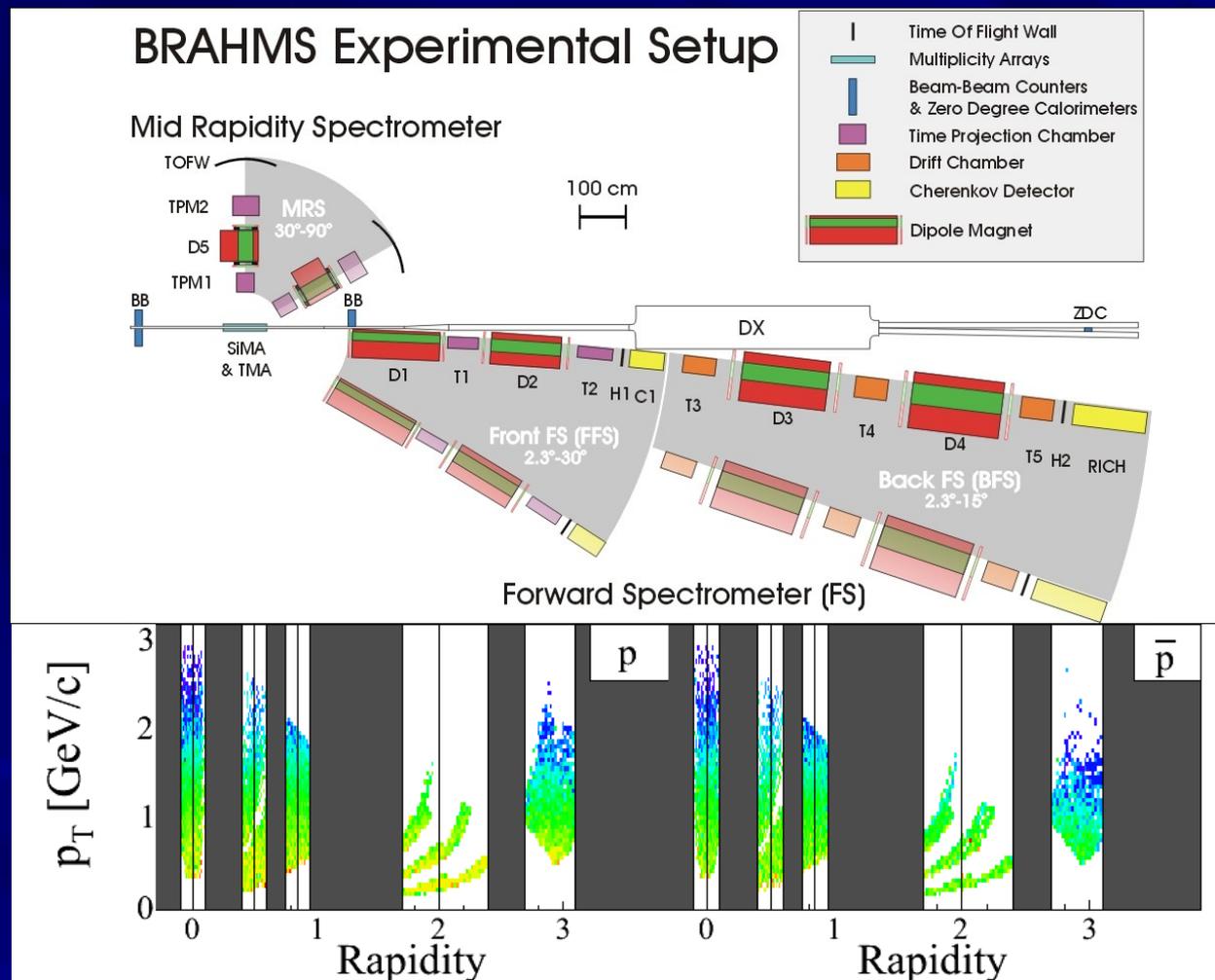
$$1/(2\pi p_T) d^2N/dydp_T$$


A single spectrometer setting covers a small fraction of phase space, but by combining different settings p_T -spectra can be obtained at many different rapidities.

MRS ($0 < y < 1$),
 FFS ($1 < y < 2$),
 FS ($2.0 < y < 3.5$)



Apply cuts in rapidity and project $\rightarrow p_T$ spectra

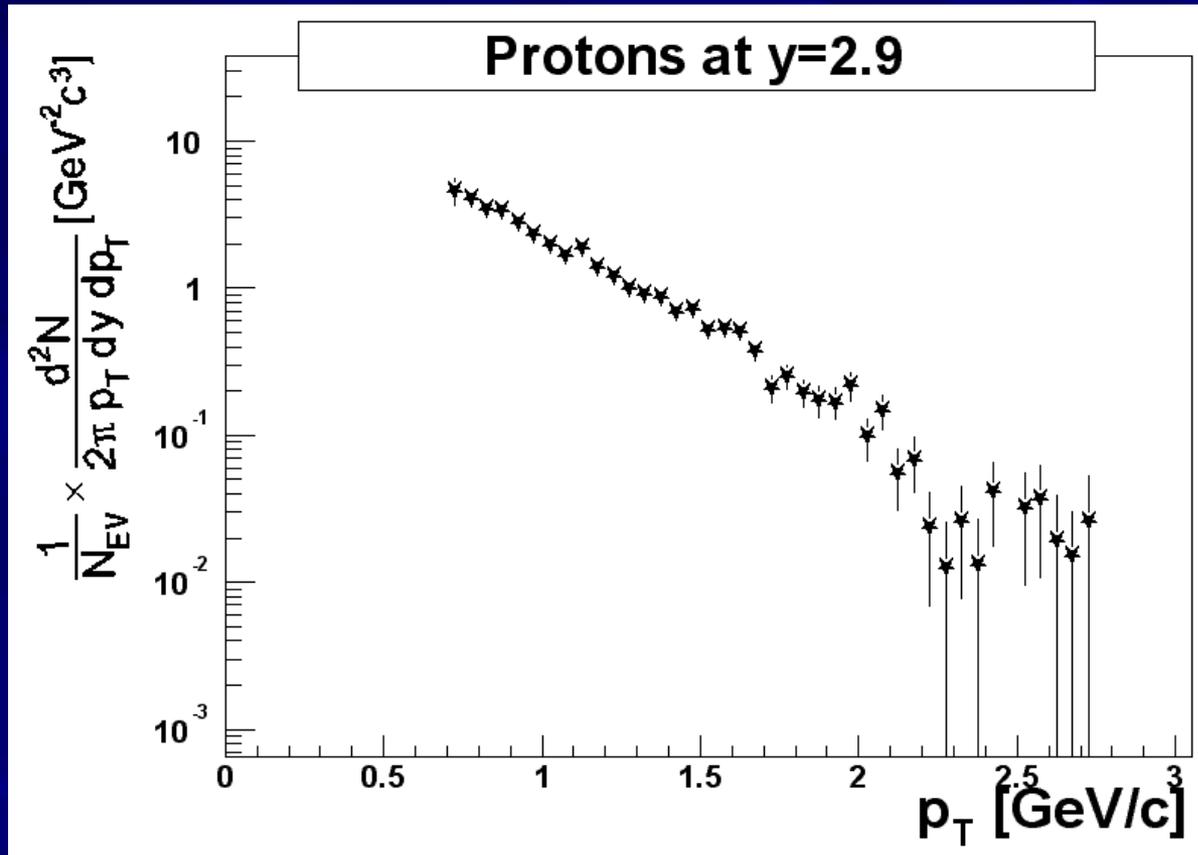


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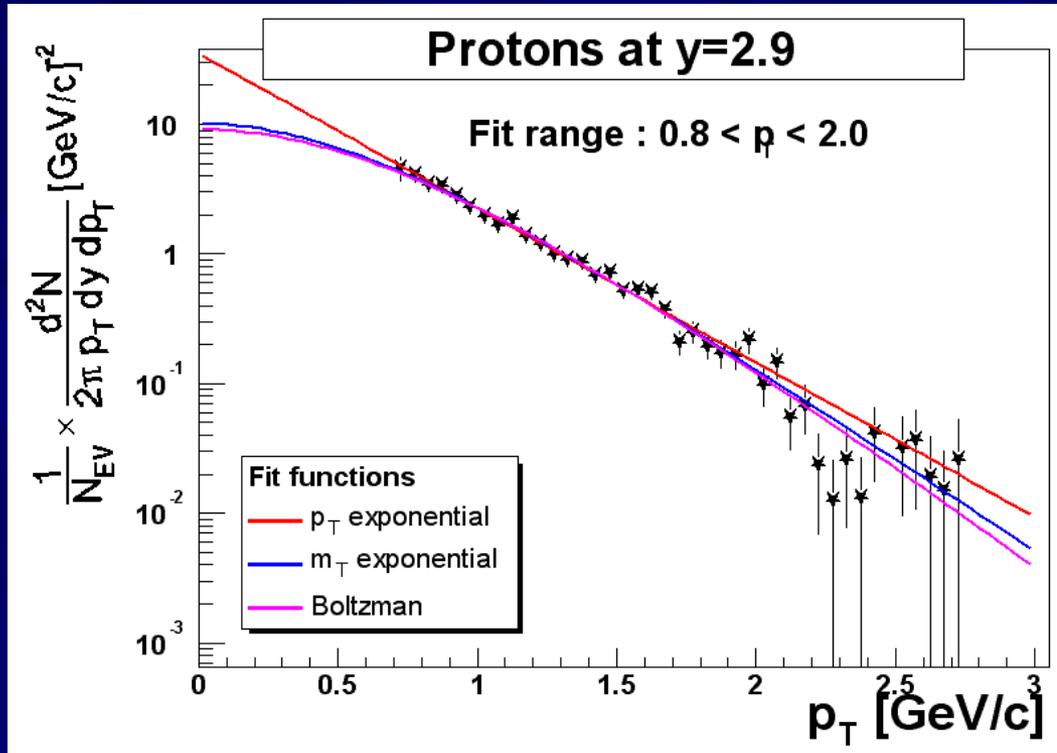
Example of p_T -spectrum



- To obtain dN/dy we need to extrapolate the yield to the regions where there is no experimental coverage



Extracting dN/dy



Fit p_T spectra and use the fit to extrapolate into regions where we don't measure to get dN/dy .

$$m_T = \sqrt{m^2 + p_T^2}$$

$$f(p_T) = N \cdot e^{-p_T/T}$$

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$$f(p_T) = N \cdot m_T \cdot e^{-m_T/T}$$

The fit function used was required to be able to fit at all rapidities.

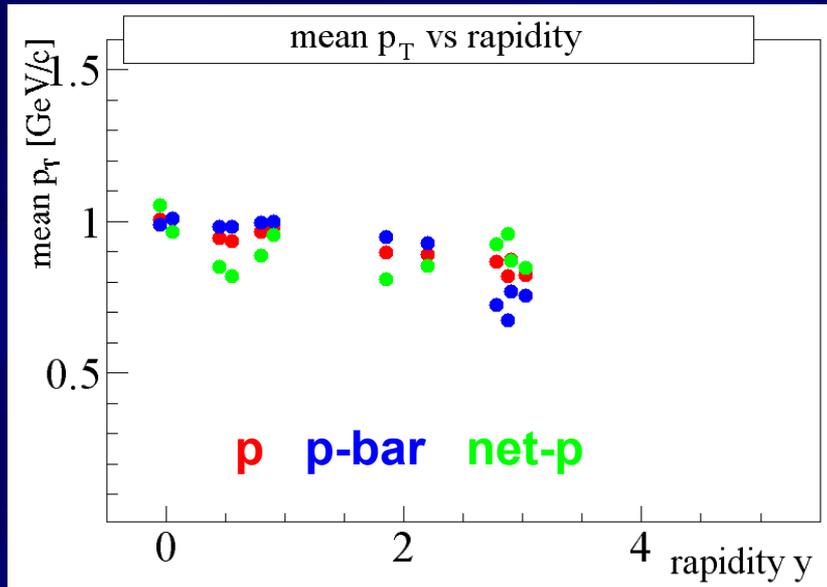
This rules out p_T -exponential and Boltzman.



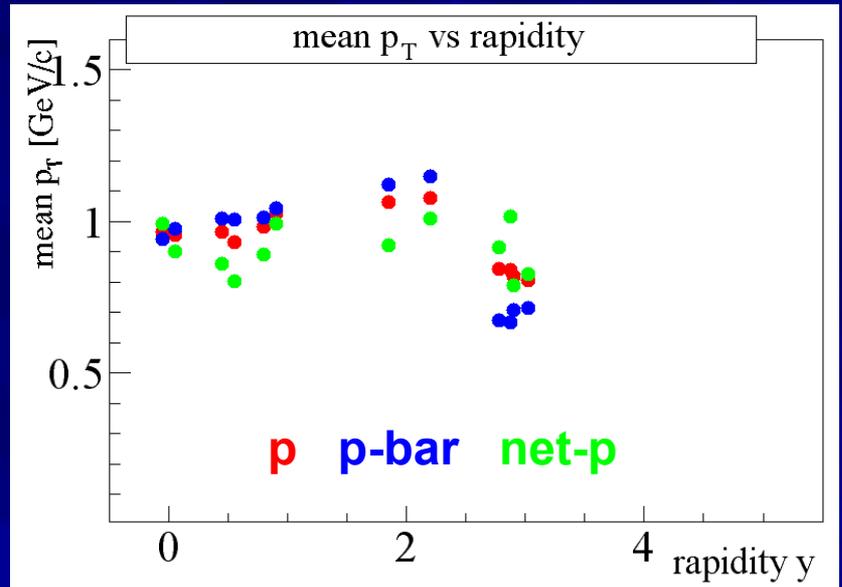
$\langle p_T \rangle$ vs y :

A consistency check for fits

pT-gauss fit



mT-exponential fit



- However, the final fit function used was a Gaussian in p_T :

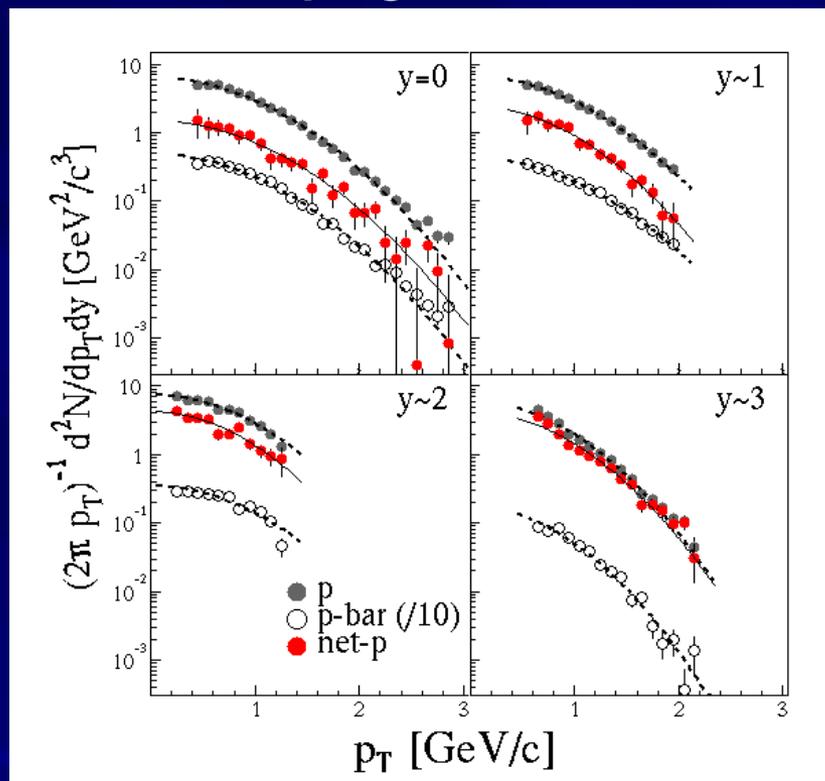
$$f(p_T) = N \cdot e^{-p_T^2/T}$$

- Gave better χ^2 , but also a more consistent behavior of the $\langle p_T \rangle$ as a function of rapidity

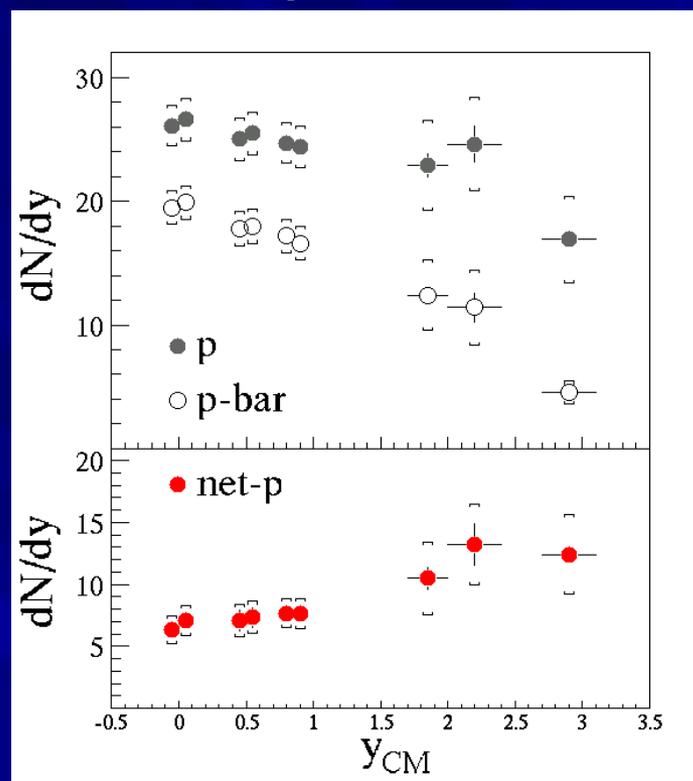


BRAHMS 200 GeV results (1/2)

pT-gauss fit



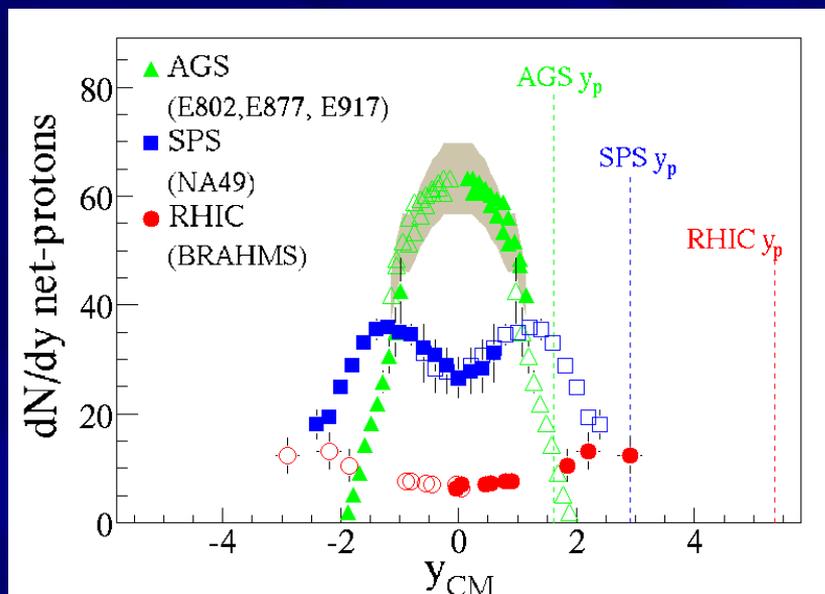
Extrapolated fits



■ Results from PRL93, 102301 (2004)



BRAHMS 200 GeV results (2/2)



■ Problems:

- BRAHMS net-protons contains protons from weak decays, e.g:
 - $\Lambda \rightarrow p + \pi^-$
- Bulk of net-protons are outside the acceptance
- How to normalize the BRAHMS results to model calculations



Idea:

Convert net-protons to net-B

- Net-B turns out to be less sensitive to net- Λ than net-p (Mentioned in NA49 stopping paper: PRL82, 2471 (1999))
- Net-B we know how to normalize and we can use the number of participants (=net-B) to constrain our extrapolation to $|y|>3$

- Conversion formula:

$$n_B = n_{p, \text{measured}} \frac{n_p + n_n + n_\Lambda + n_{\Sigma^+} + n_{\Sigma^-}}{n_p + c_1 n_\Lambda + c_2 n_{\Sigma^+}}$$

- Where the n quantities are the net-quantities.
- c1 and c2 is the number of measured protons per Λ and Σ^+ respectively



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- Conversion formula dominant terms only:

$$n_B = n_{p, \text{measured}} \frac{n_p + n_n + n_\Lambda}{n_p + c_1 n_\Lambda}$$

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- Net-B we know how to normalize and we can use the number of participants (=net-B) to constrain our extrapolation to $|y|>3$
- Conversion formula dominant terms only:

$$n_B = n_{p, \text{measured}} \frac{1 + r_n + r_\Lambda}{1 + c_1 r_\Lambda}$$

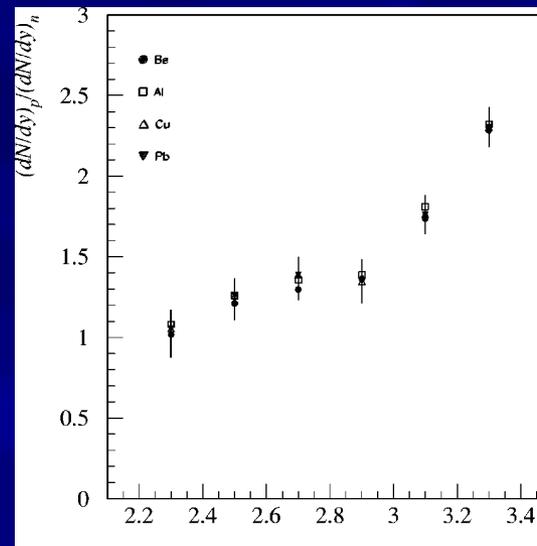
- Where the n quantities are the net-quantities.
- The r quantities are the ratios: $r_x = n_x / n_p$
- c1 is the number of measured protons per Λ



Equilibration of protons and neutrons

- Initially at RHIC: $n/p = (197-79)/79 \sim 1.5$
- E947 observes (PRC65, 014904 (2001)) equilibration after a few units of rapidity:

p/n ratios as a function of rapidity in p+Be, p+Al, p+Cu, and p+Pb collisions at 19 GeV/c. Fixed target with $y_{\text{proton}} = 3.7$.
After ~ 1.5 unit of rapidity, p and n is equilibrated.



- A similar result is obtained with HIJING and AMPT simulations, i.e., isospin in final state is carried by pions.
- In the region covered by BRAHMS $n/p = 1$
 - At 62 GeV and forward rapidity n/p slightly larger than 1



How to determine c_1 (protons observed per Λ)

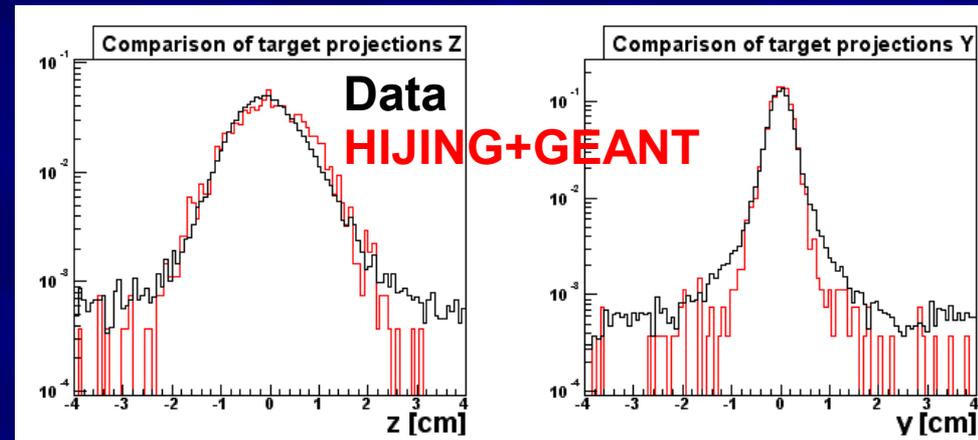
- Obtained from GEANT detector simulation of BRAHMS with HIJING as input

- Plots shown are for the BRAHMS Mid Rapidity Spectrometer ($y=0$)
- Z = along beam
- Y = transverse plane

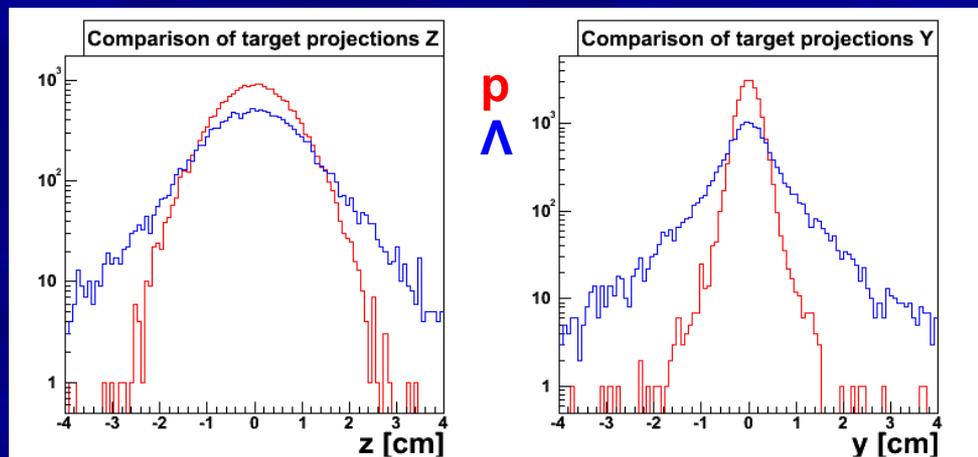
- p_T dependence of c_1 was ignored

- $c_1 = 0.53 \pm 0.05$
- Similar for all settings
- Agrees with detailed study in PRC 72, 014908 (2005)

Tracks projected back to interaction point



Same as above, but for p and Λ only





The correction factor

- The value of r_n and c_1 turns out to make n_B insensitive to n_A :

$$n_B = n_{p, \text{measured}} \frac{2 + r_A}{1 + 0.03 r_A} \sim 2 n_{p, \text{measured}}$$

- Very important point! This is why we think that net-B is better determined than net-p (weak decay corrected)
- For the full correction expression we obtain

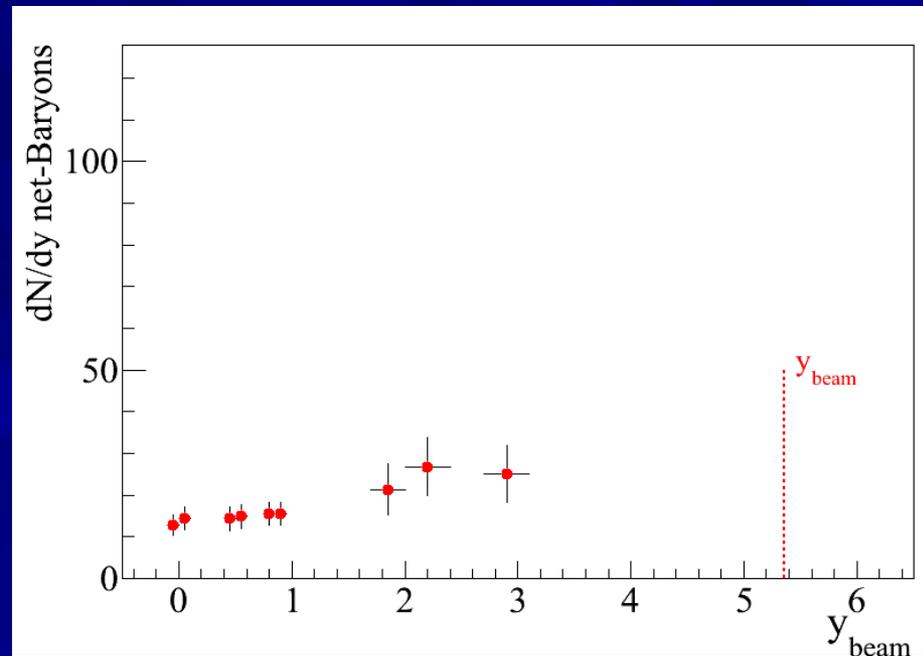
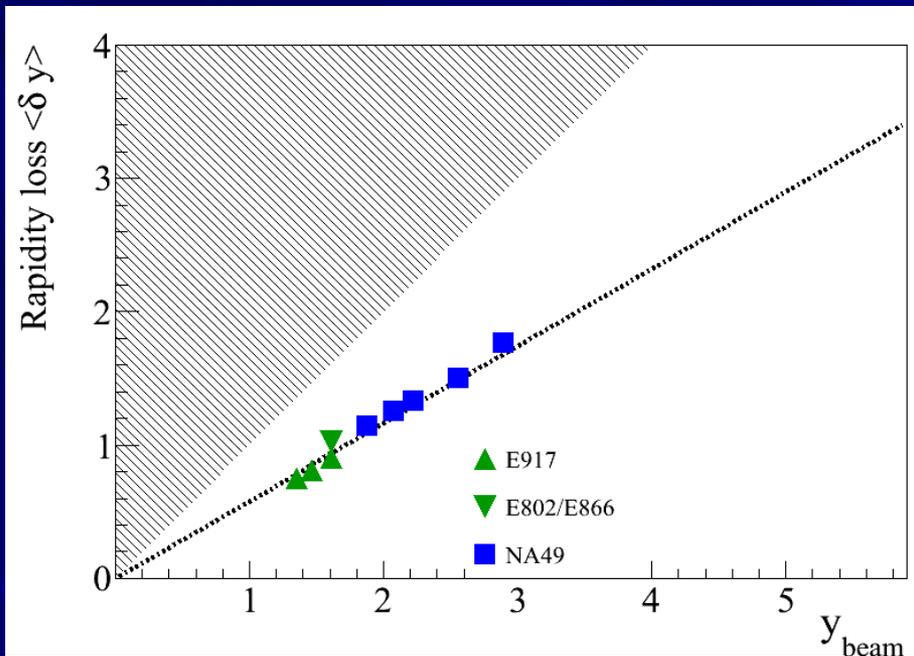
$$n_B = 2.03 \pm 0.08 n_{p, \text{measured}}$$

- And much more uncertainly for feed-down corrected protons: $(n_p = 0.67 \pm 0.12 n_{p, \text{measured}})$



Rapidity loss: 200 GeV

Rapidity loss (in CM): $\langle \delta y \rangle = y_{beam} - \int_0^{y_{beam}} y \frac{dN_{net-b}(y)}{dy} dy$

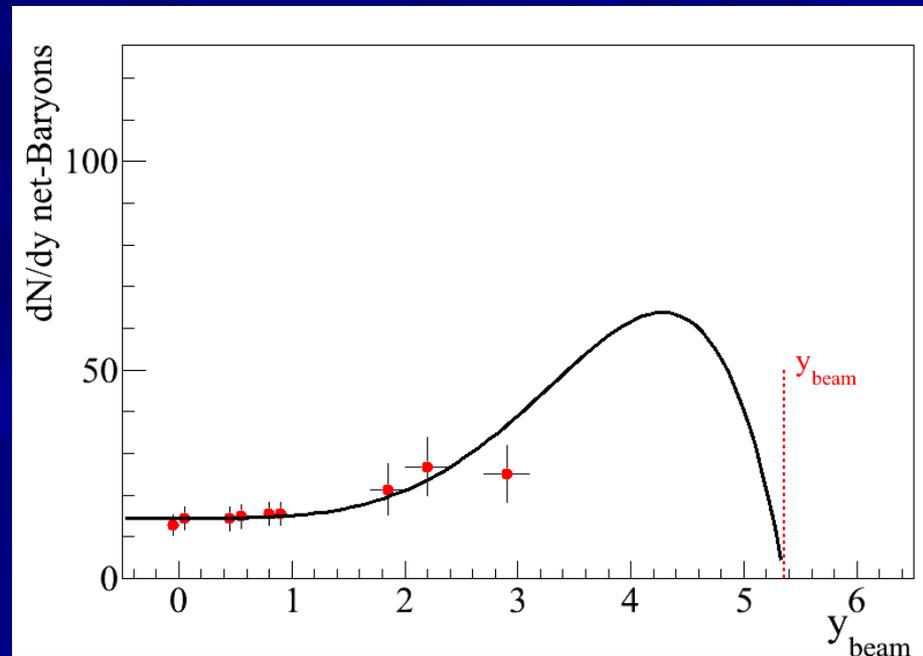
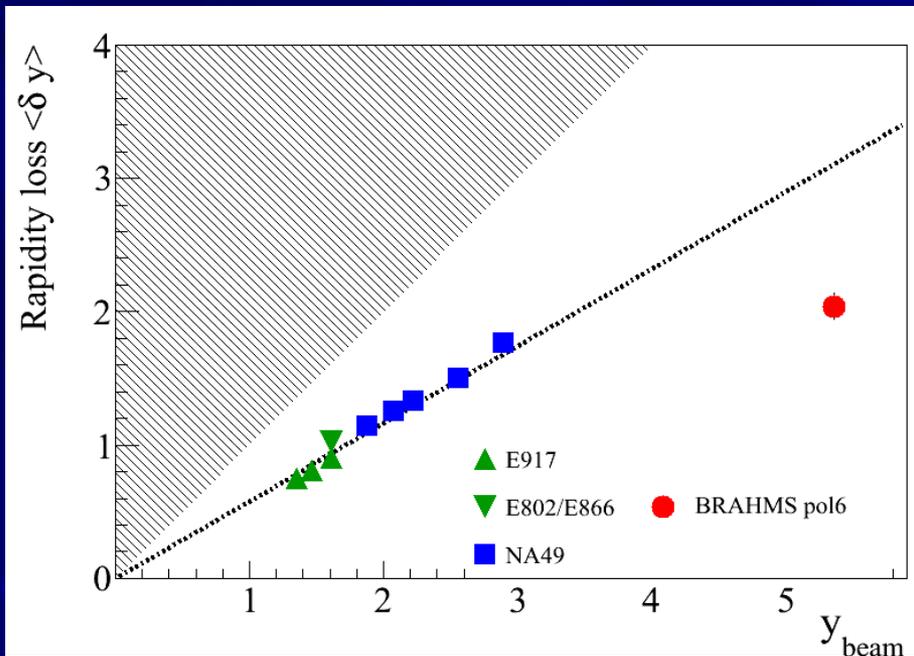


■ NA49 data points from QM06 proceeding [J.Phys.G34, S951, (2007)]



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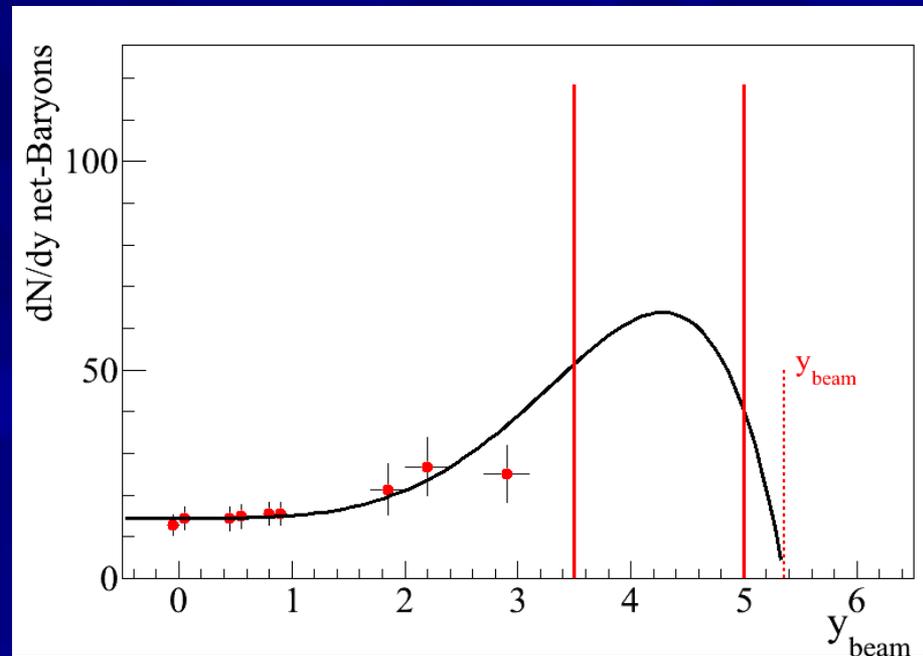
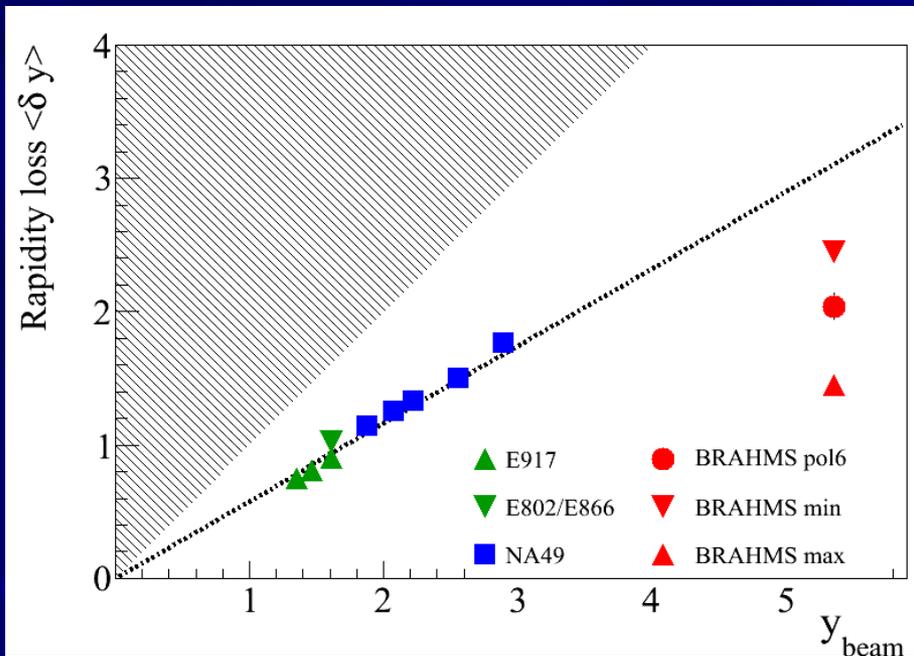


- Fit with symmetric 6th degree polynomial
 - 4 parameters, but ~3 constraints: Integral, $dN/dy(y=0)$, $dN/dy(y_{beam})=0$



Rapidity loss: 200 GeV

Rapidity loss (in CM): $\langle \delta y \rangle = y_{beam} - \int_0^{y_{beam}} y \frac{dN_{net-b}(y)}{dy} dy$

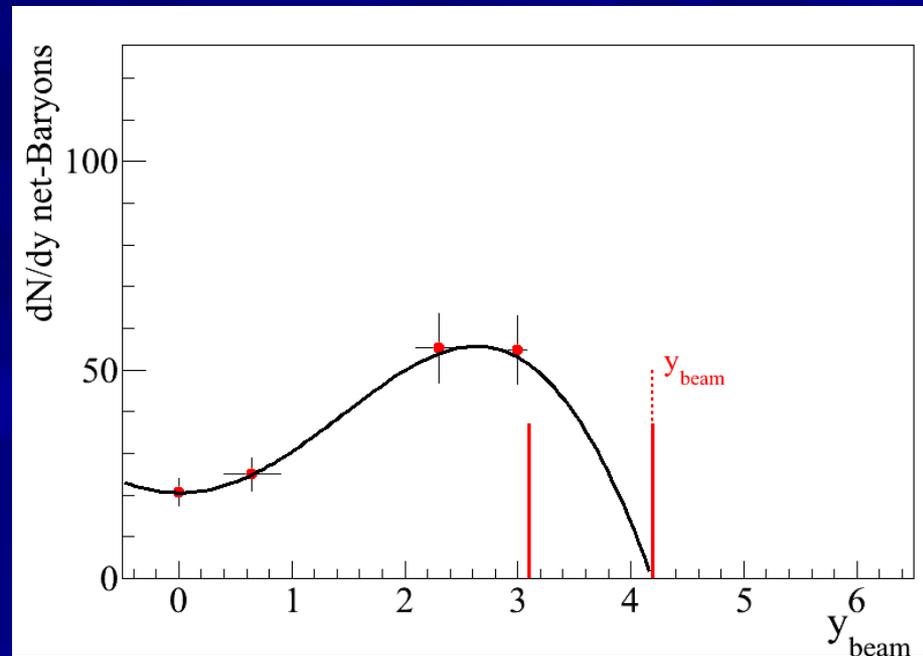
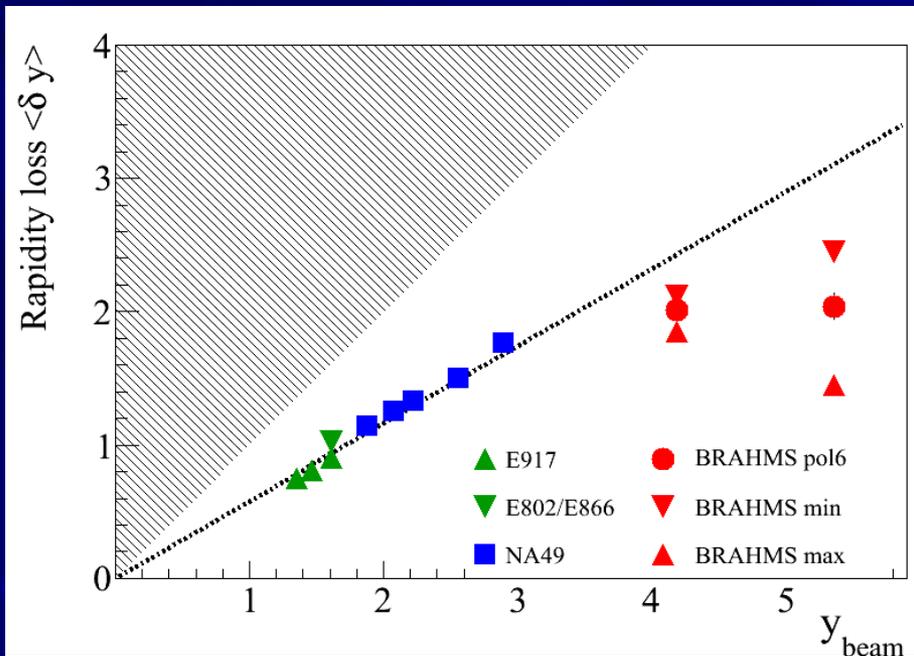


■ Minimum and maximum estimates, but placing remaining net-baryons at $y=3.5$ (max) or $y=5.0$ (min)



Rapidity loss: 62 GeV

Rapidity loss (in CM): $\langle \delta y \rangle = y_{beam} - \int_0^{y_{beam}} y \frac{dN_{net-b}(y)}{dy} dy$



- Similar methods as for 200 GeV → Confirms trend and has much better coverage
- Accepted for publication in PLB (arXiv:0901.0872)

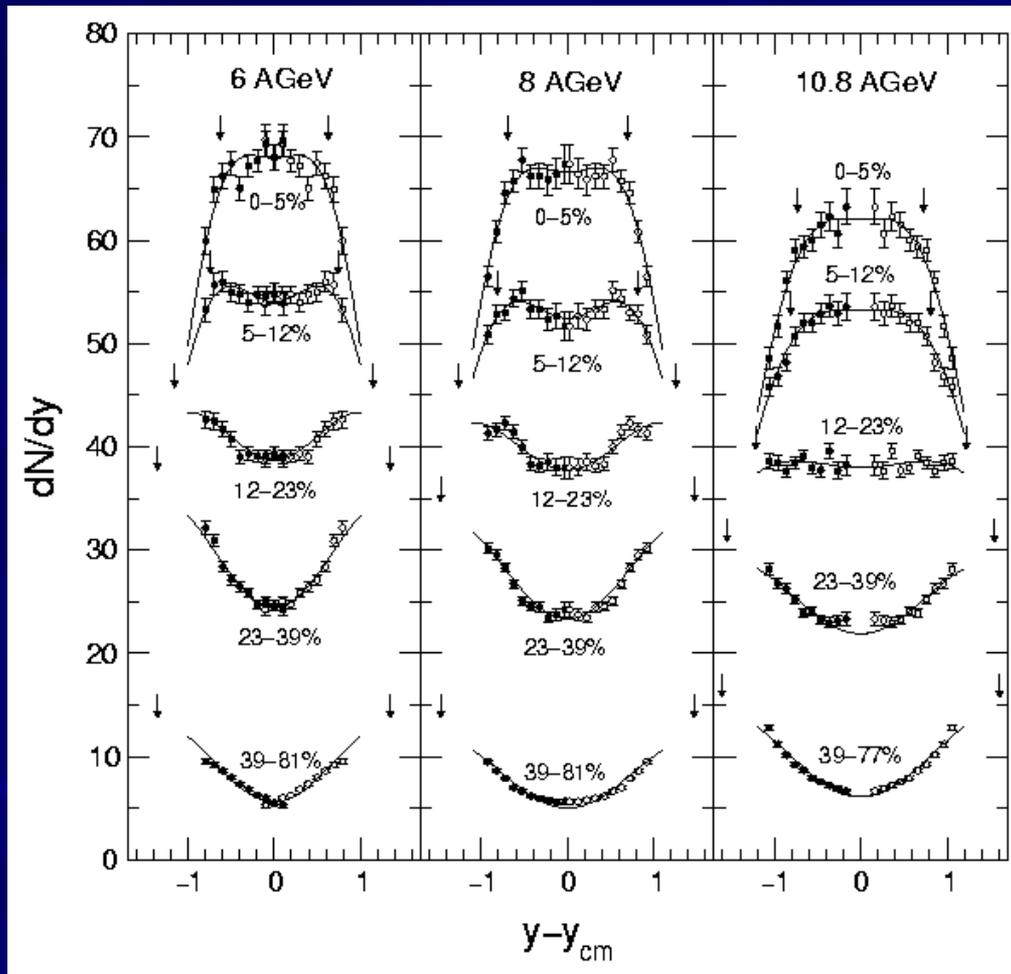


Is the rapidity loss a good measurement of stopping?

- Problem is that at low energy the contributions from the two nuclei (target and projectile) overlap significantly near mid-rapidity
 - Because of symmetry we know there ($y=0$) that half the nucleons actually comes from the target!
 - We **UNDERESTIMATE** the rapidity loss (worse at low beam energy) because we do not take into account rapidity losses that are greater than y_{beam}
- Solution: Try to separate contributions from target and projectile



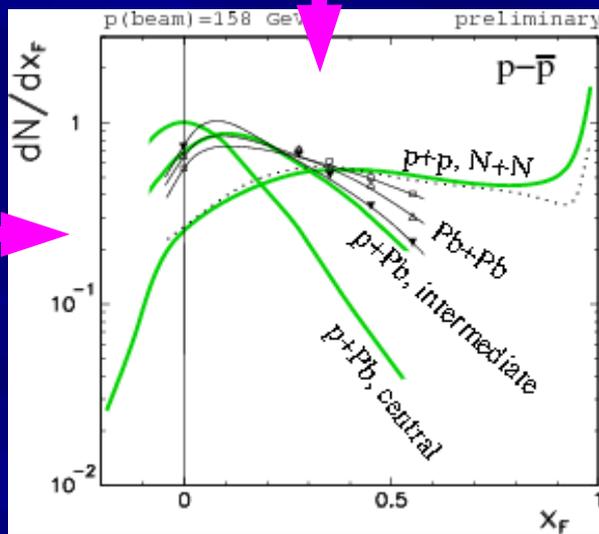
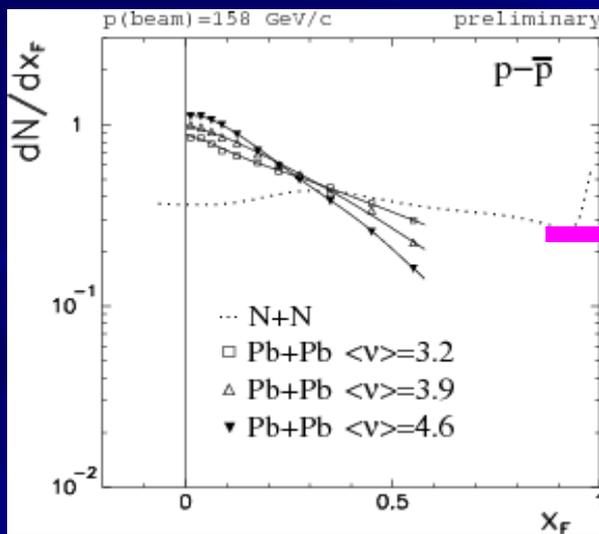
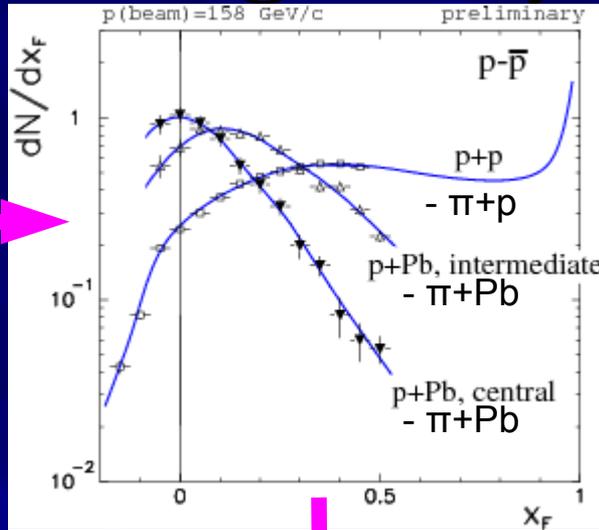
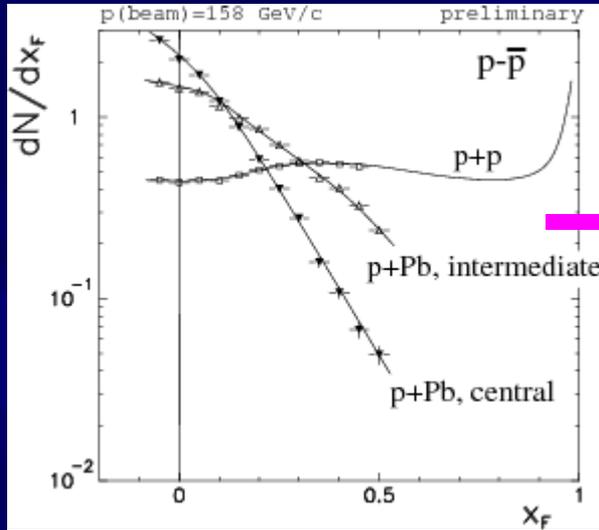
E917: Separating “projectile” and “target” by fitting



- Describe data by the som of two symmetric Gaussians
- Rapidity loss is then approximately y_{beam} minus Gaussian mean (vertical arrow)
 - NB! only meaningful for central collisions
- p+p picture is recovered in peripheral collisions
- Reference: [PRL 86, 1970 (2001)]



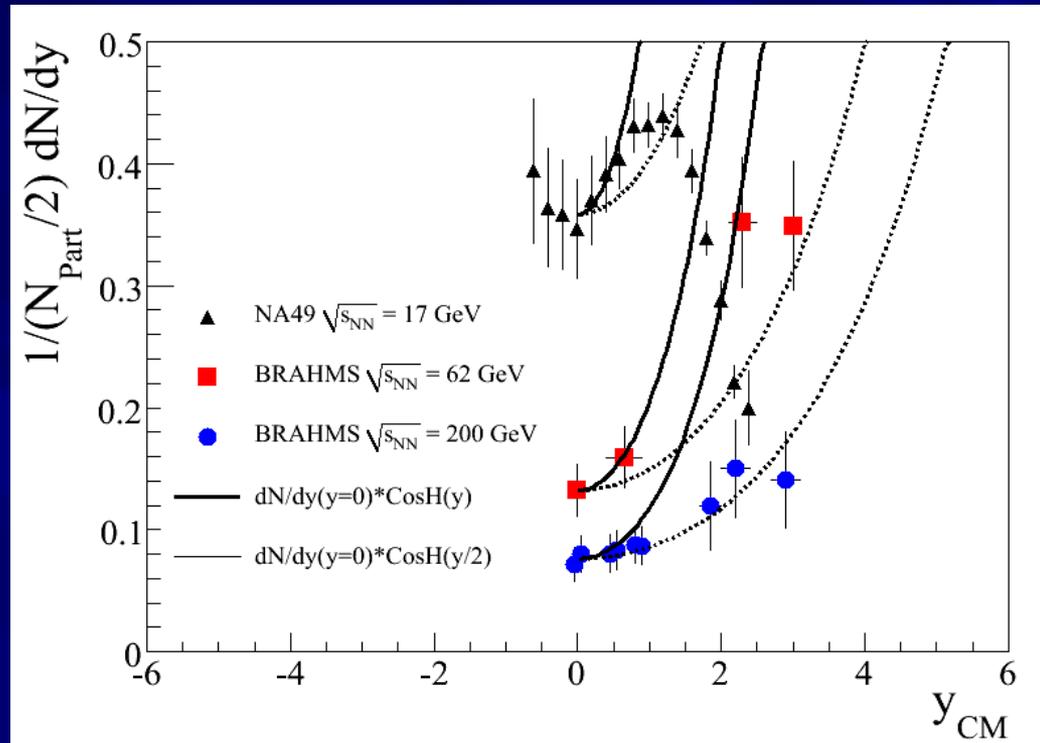
NA49: Separating “projectile” and “target” by $\pi+p/A$



- Left: Uncorrected net-p distributions
- Right: net-p in $p+p/A$ minus net-p in $\pi+p/A$
 - For $Pb+Pb$ only the $x_F=0$ ($y_{CM}=0$) points have been halved
- Stopping is larger in central $p+A$ than in central $Pb+Pb$
- [Acta Phys. Pol. B 33, 1483 (2002)] (unfortunately never published)



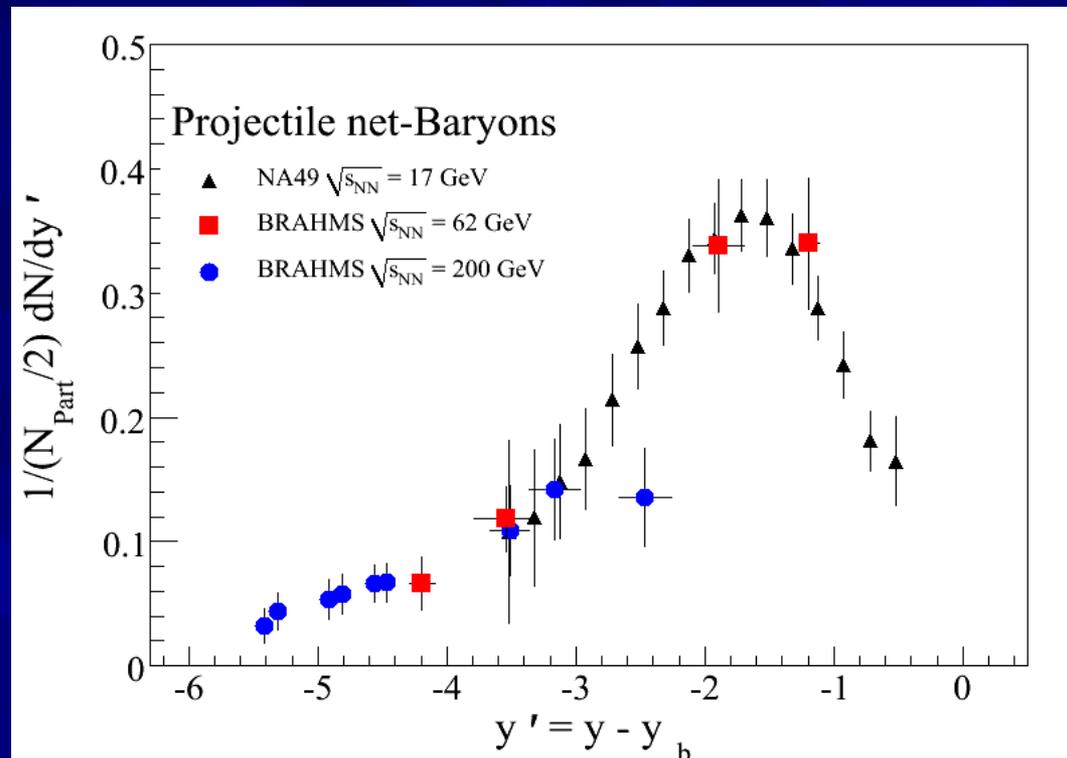
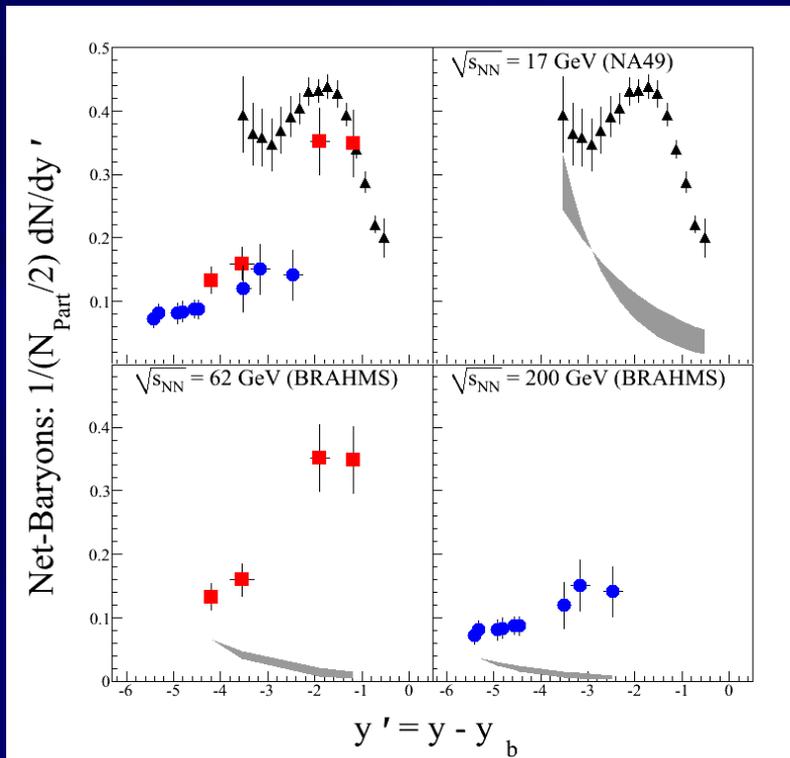
Separating “projectile” and “target” by tail approximation



- Separate “projectile” and “target” using pp expectations
 - $\exp(-y')$ tail is coming from pp data $\rightarrow \text{Cosh}(y)$
 - $\exp(-y'/2)$ proposed for baryon junction $\rightarrow \text{Cosh}(y/2)$
 - See reference: [Z. Phys.C 43, 241 (1989)]



“Projectile” net-baryons shows rapidity scaling



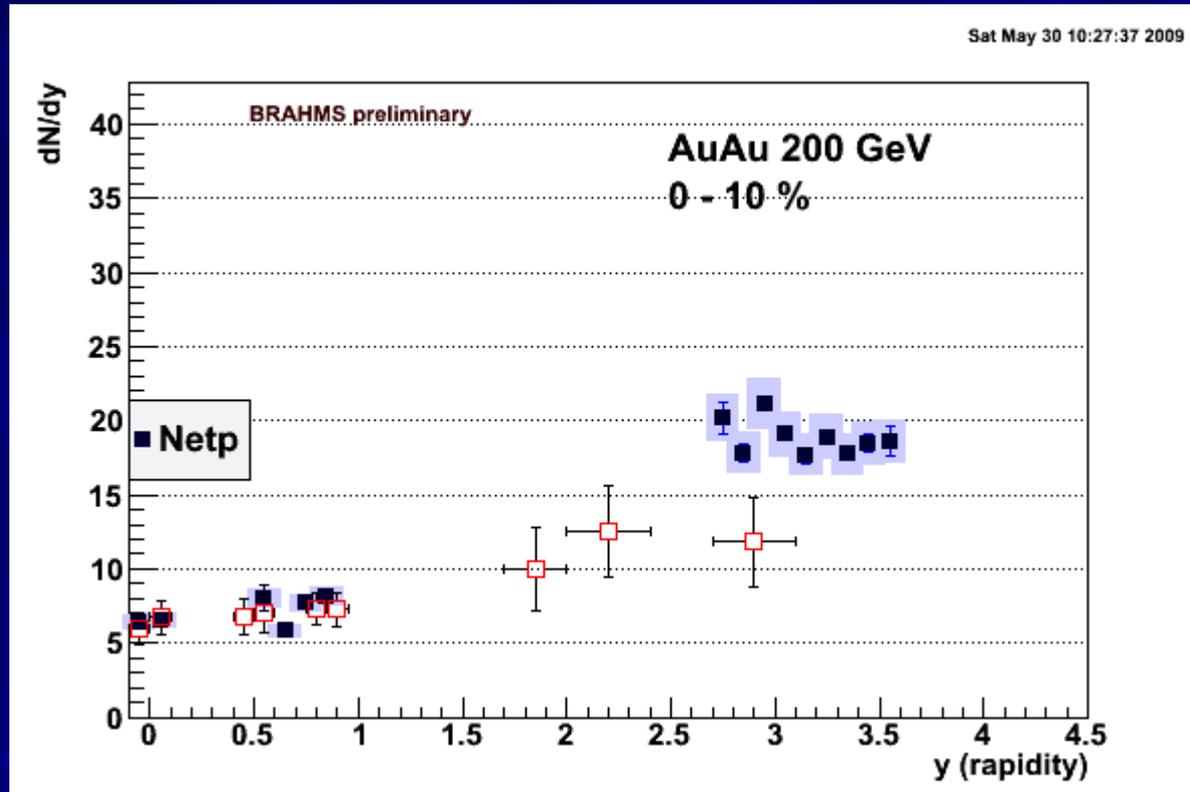
- When the net-Baryons are corrected for the “target” contribution universal scaling is also observed in A+A collisions – Particularly for the large rapidity losses!
- The stopping mechanism at SPS and RHIC is similar! (?)

New results from BRAHMS *(Taken from Videbæks QM talk)*



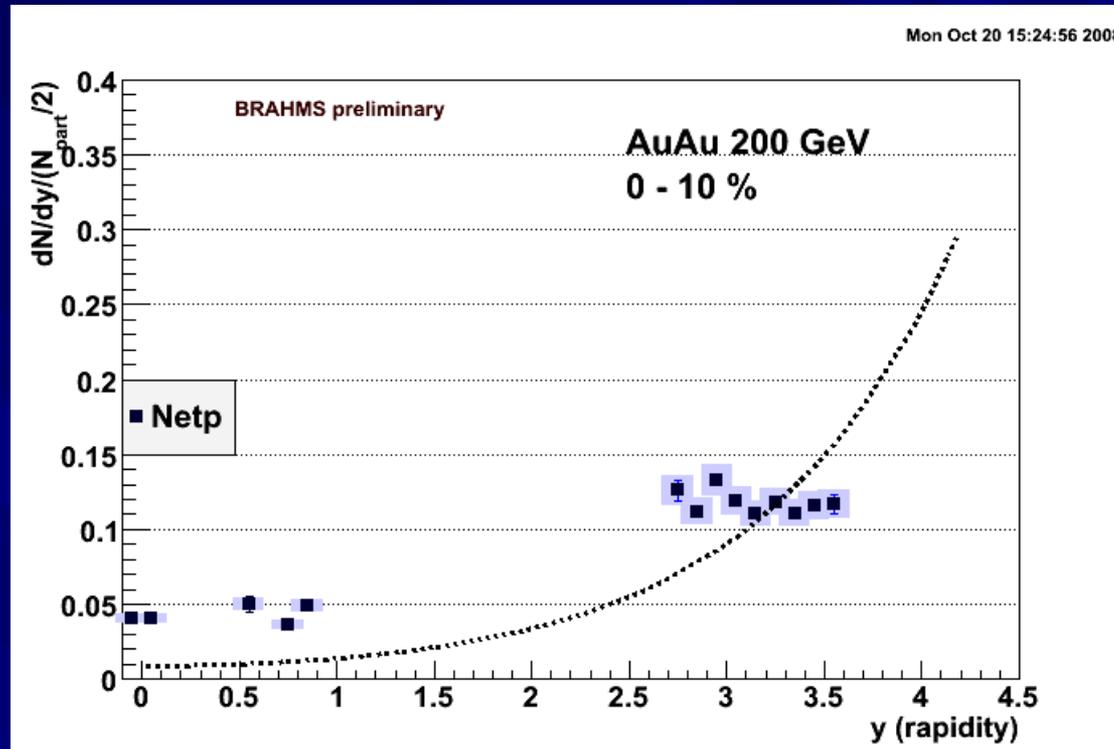


New results from BRAHMS vs published results





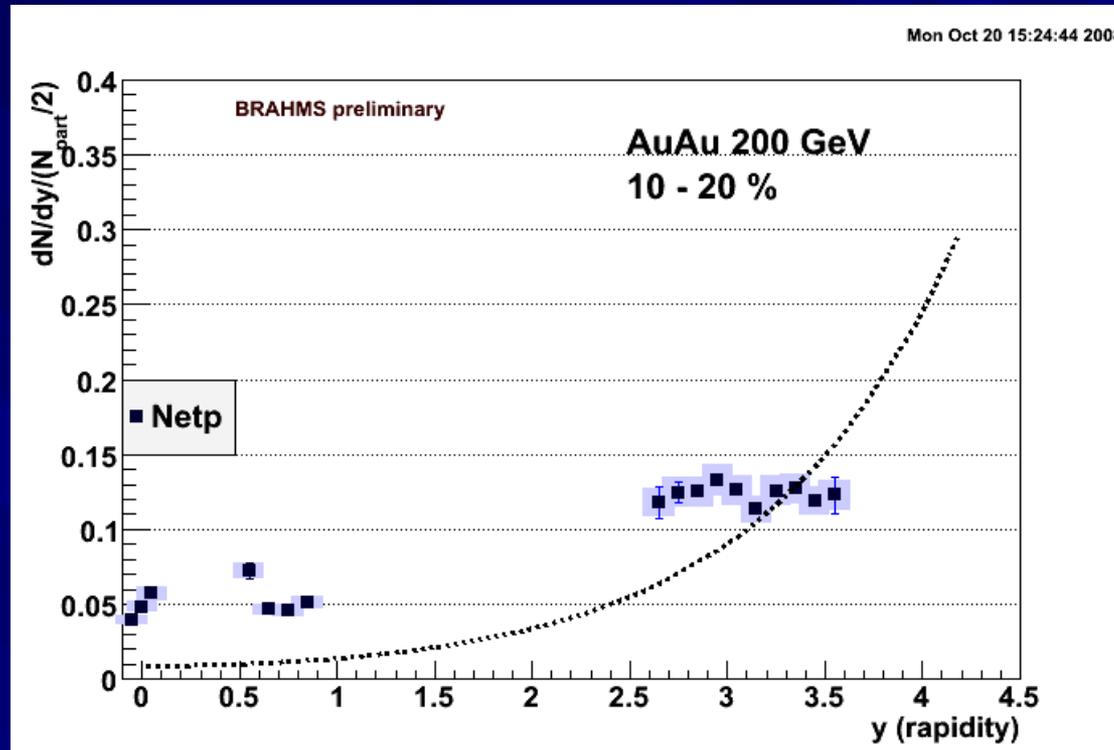
Centrality dependence of dN/dy for net-protons at 200 GeV



■ Dashed line is universal pp fit

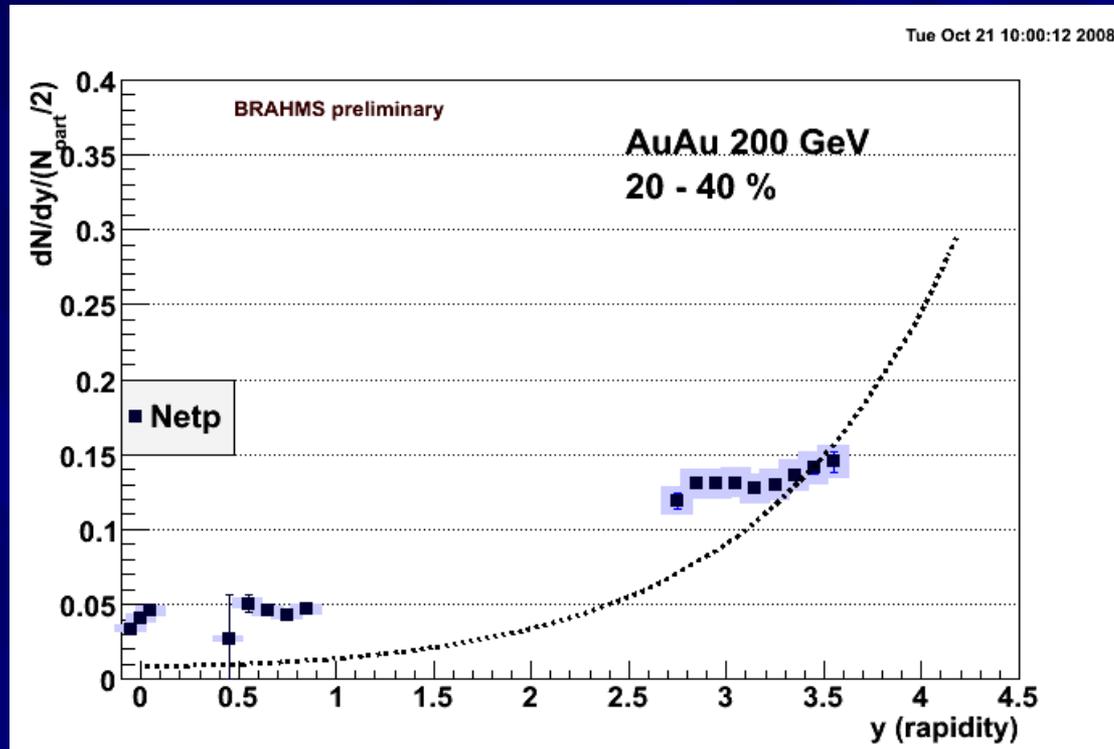


Centrality dependence of dN/dy for net-protons at 200 GeV



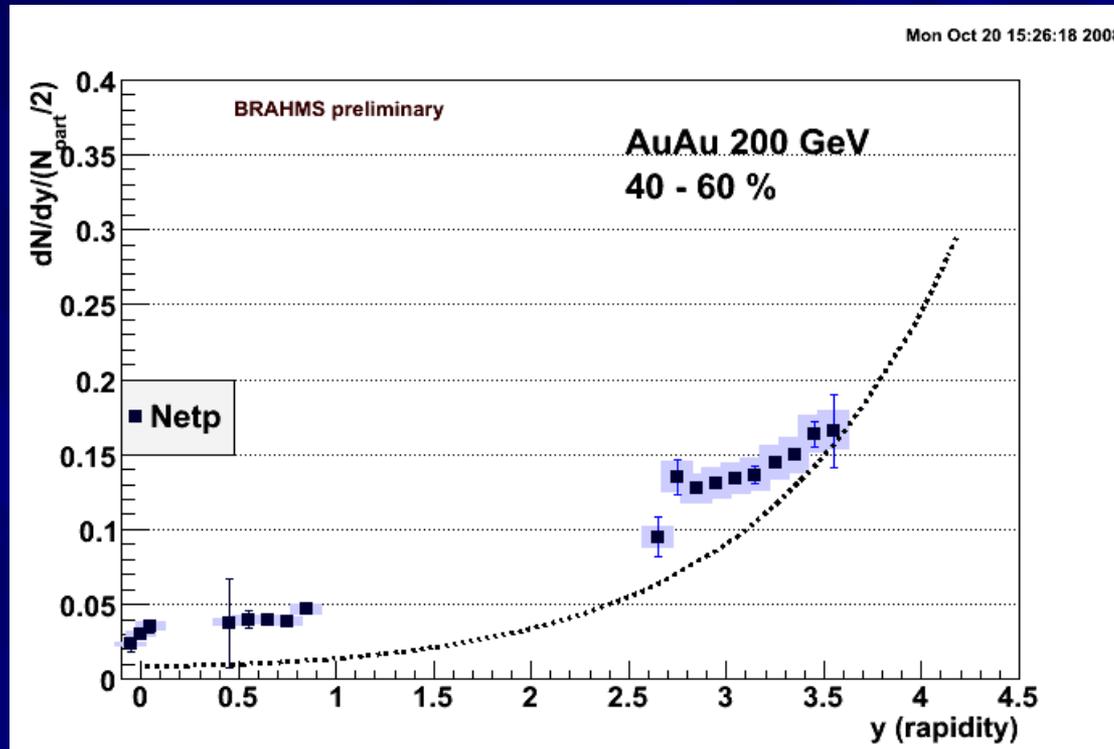


Centrality dependence of dN/dy for net-protons at 200 GeV



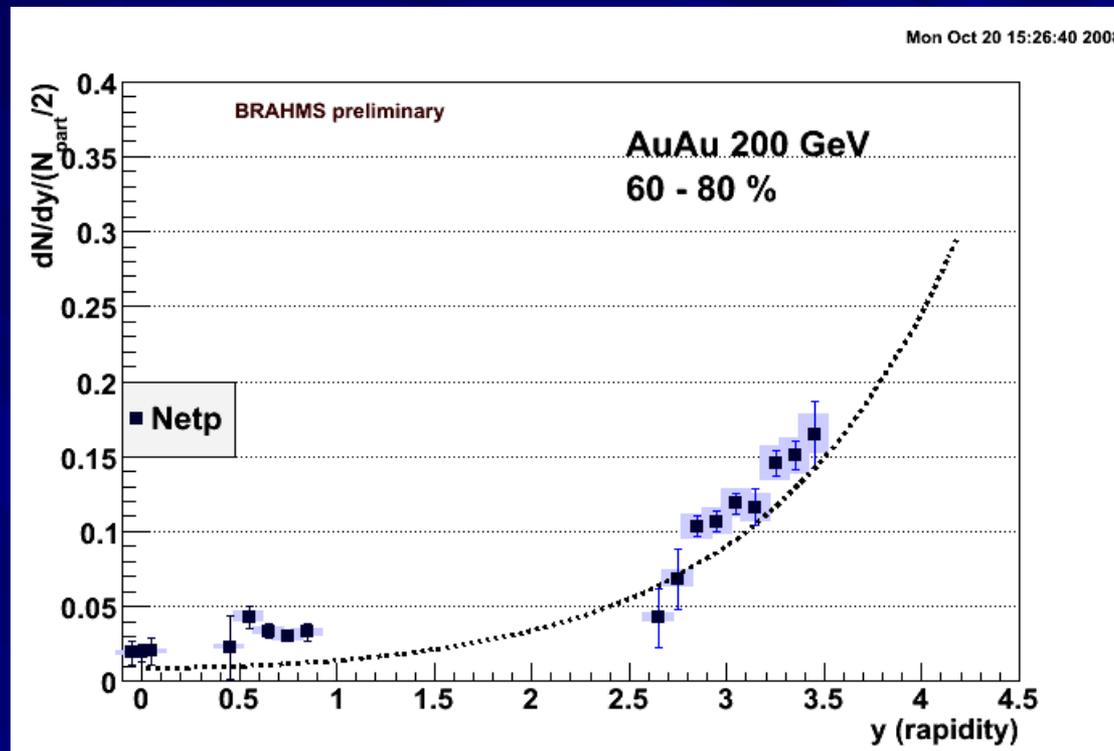


Centrality dependence of dN/dy for net-protons at 200 GeV





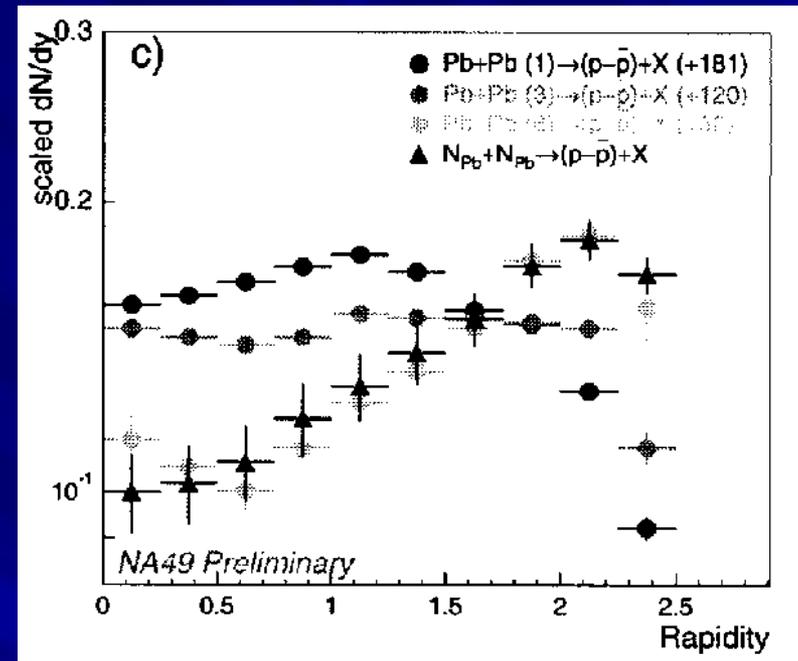
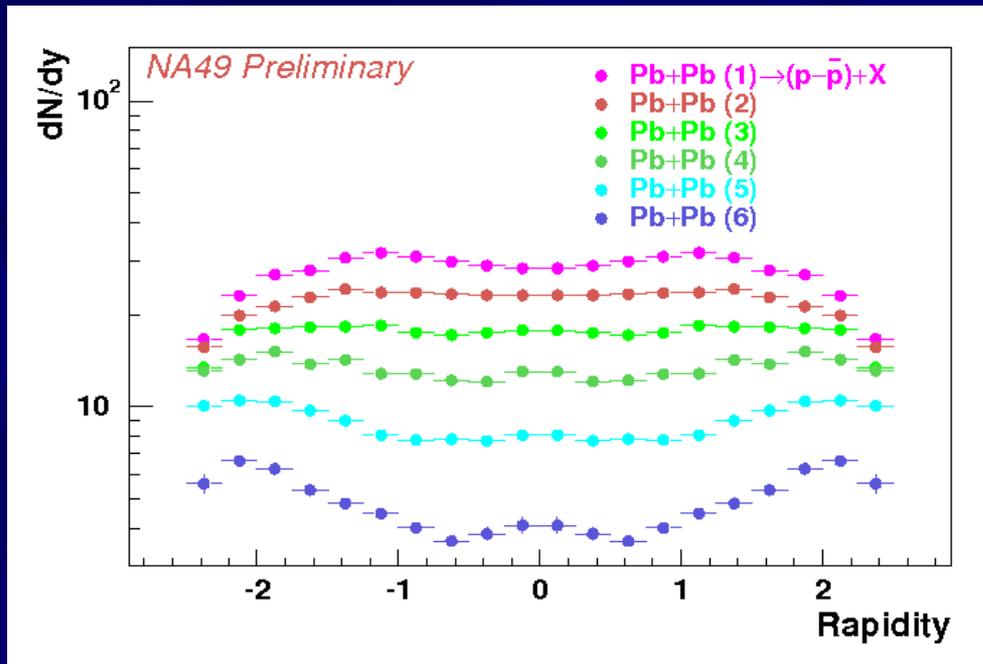
Centrality dependence of dN/dy for net-protons at 200 GeV



- Significant centrality dependence
 - Peripheral collisions are similar to pp

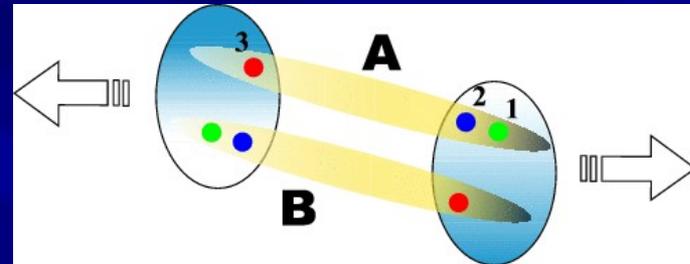


NA49 centrality dependence



- NA49 has observed similar centrality dependence, see [NPA661,362(1999)].
- Pb+Pb and p+p net-protons are similar for the centrality class 48-100% (some trigger bias)

Models



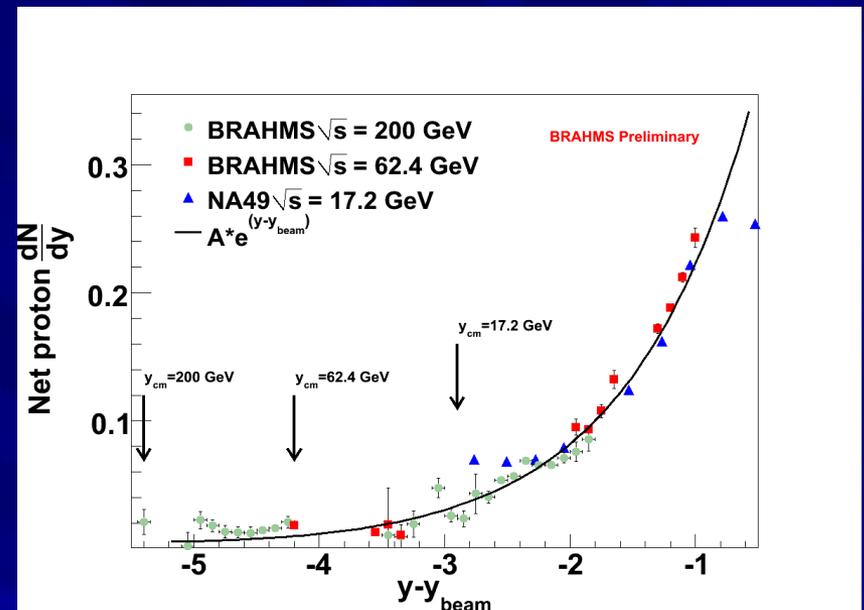
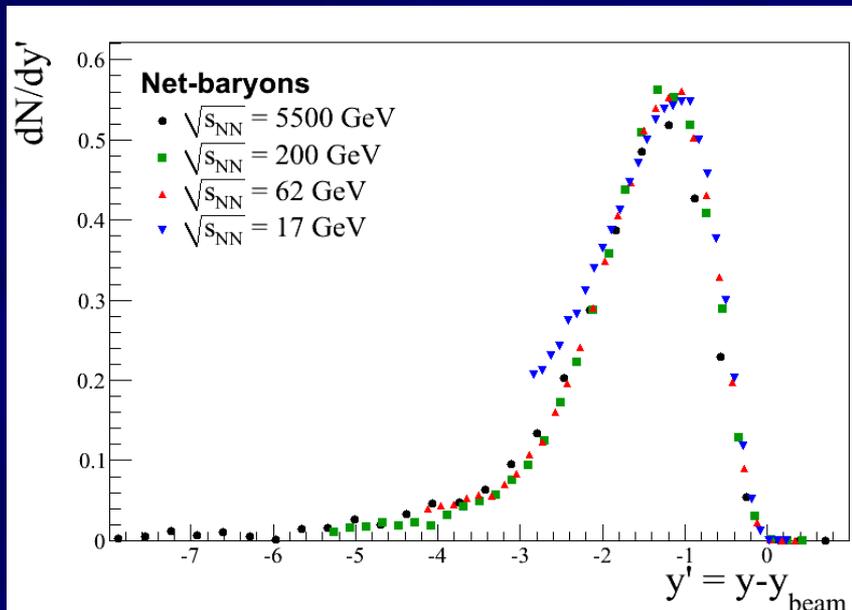


Some questions for models (and experiments)

- Are the observed universal scaling relations for pp and AA accidental or fundamental?
- Stopping in pp from PYTHIA
 - is stopping a purely soft (string breaking/fragmentation) process or does hard processes contribute?
 - Important for centrality dependence
- Stopping in AA
 - New “coherent” models
 - Q^2 dependence of valence quark pdfs



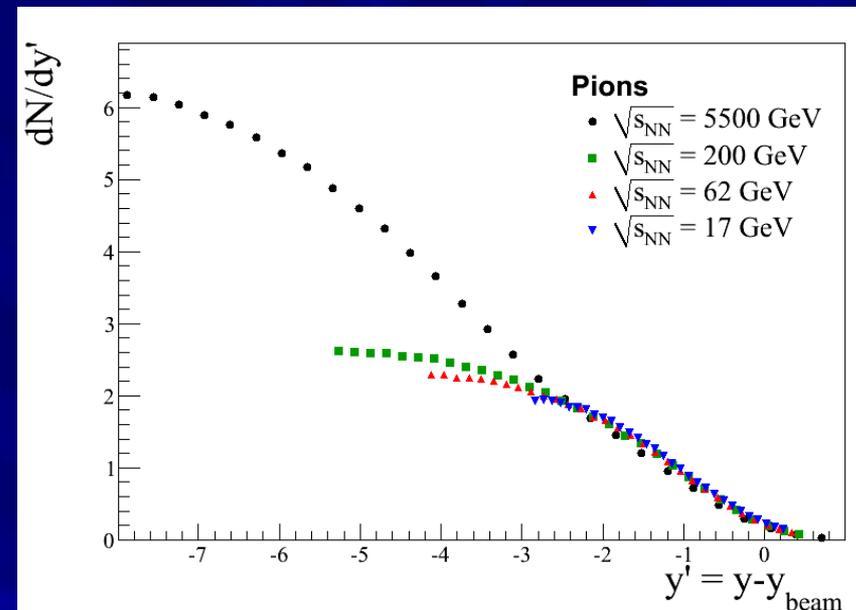
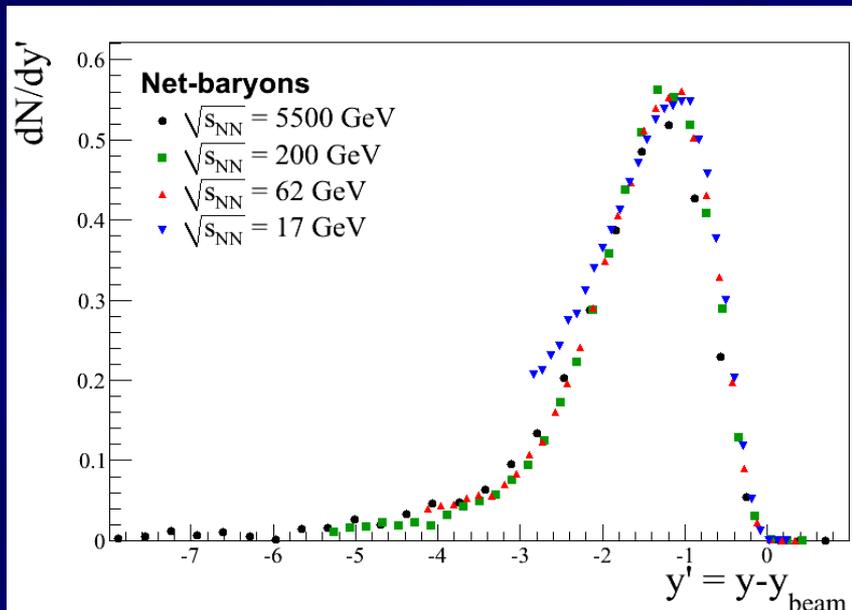
Stopping in *PYTHIA*



- *PYTHIA* (v 8.108, w.o. tuning) shows an almost universal stopping curve from SPS to LHC energies
- Stopping is dominated by string breaking (soft processes)
 - Universality is in the model



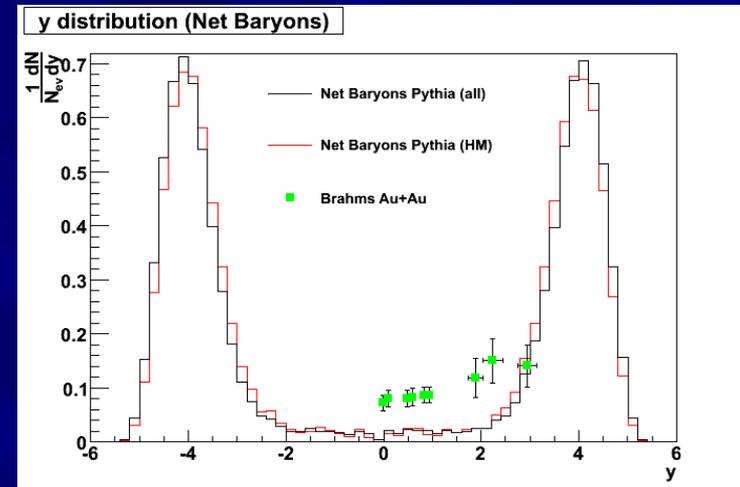
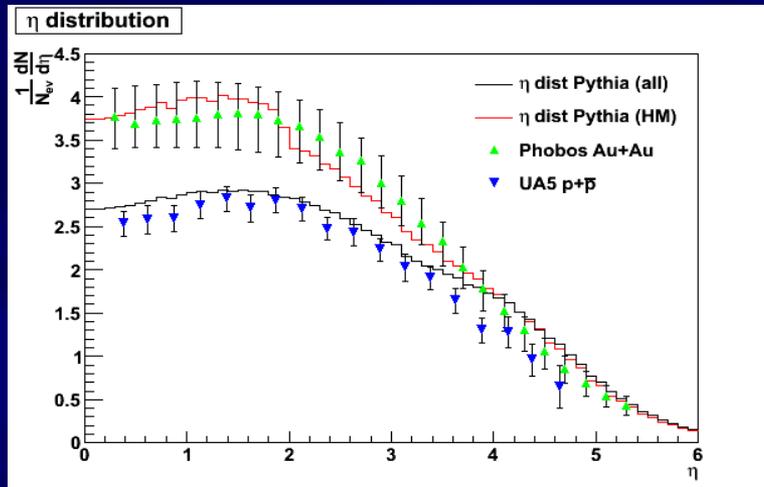
Perhaps related to limiting fragmentation



- Forward physics seems more or less universal
- Hard physics dominates around mid-rapidity because of phase space
- At large energies more multiple interactions and more activity per interaction (initial and final state radiation)



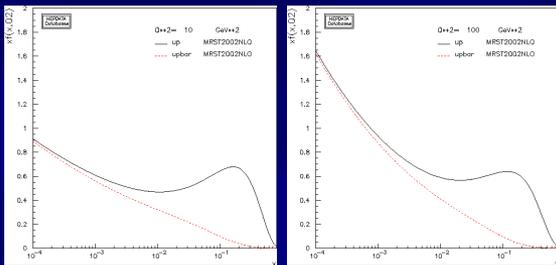
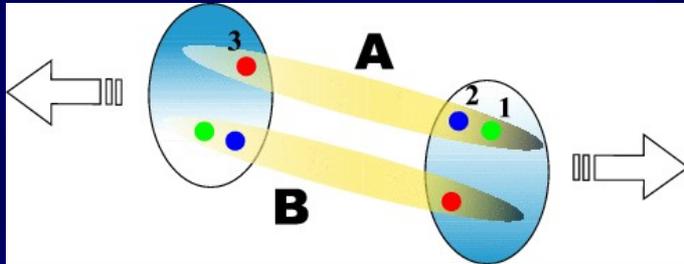
$p+p$ is not only min bias: Could we learn more?!



- Large multiplicity in pp coupled to hard scatterings
 - Small effect on stopping in PYTHIA
 - Large stopping at RHIC is not essential for larger particle production!
- But is PYTHIA true? problems with p/p-bar ratios and p_T dependence
- Experiment could (should?) decide if this is true!
 - BRAHMS (problem to cut on multiplicity)
 - STAR (less rapidity coverage)



A p+p and A+A stopping model based on strings

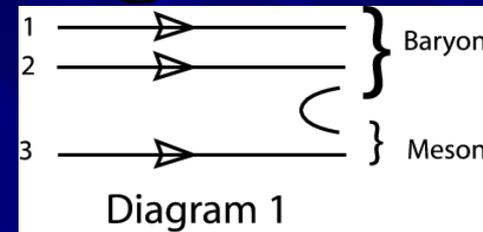


- Input are the pdf's for valence quarks: $x_1 > x_2 > x_3$ (and $x_3 < 0$) taken at:

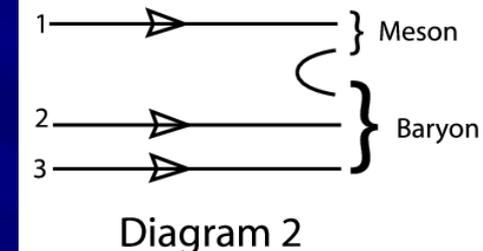
$$Q_A^2 = \left(\frac{N_{part}}{2} \right)^\alpha Q_0^2 \left(\frac{s}{s_0} \right)^{\lambda_v}$$

- Where α and λ_v are to be

determined from fits to data [J. Alvarez-Muniz et-al, arXiv:0903.0975]



$$x_1 - x_2 < x_2 - (-x_3)$$

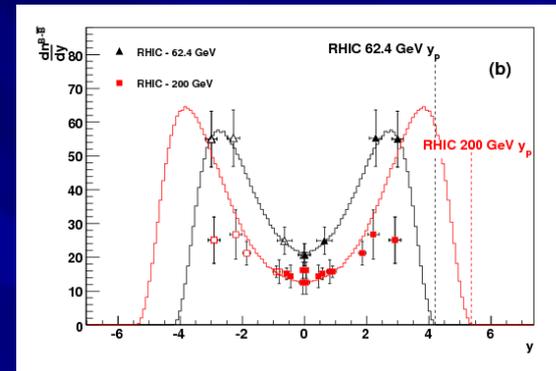
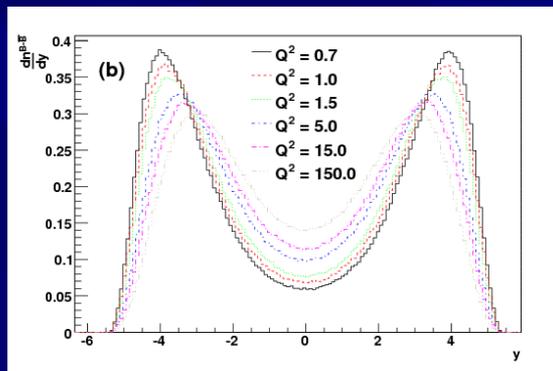
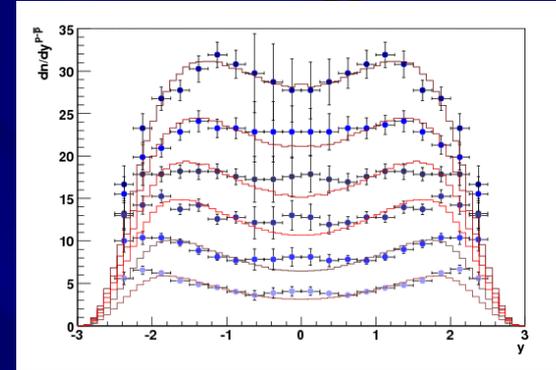
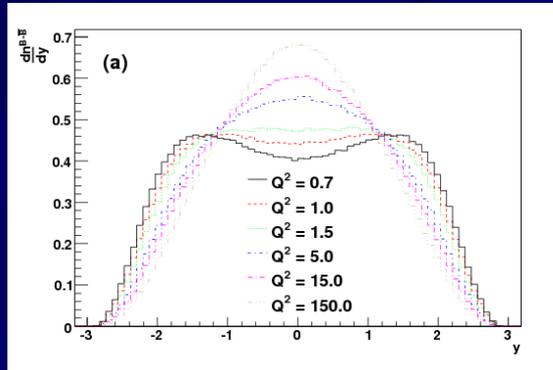


$$x_1 - x_2 > x_2 - (-x_3)$$

- Fragmentation by q+q-bar string breaking between “closest” valence quarks
 - Diagram 2 gives large rapidity losses



A $p+p$ and $A+A$ stopping model based on strings



■ Is it universal? Probably if energy dependence of Q^2 is weak.



A CGC model for stopping: CGC kicks out valence quarks

d/Au
quarks



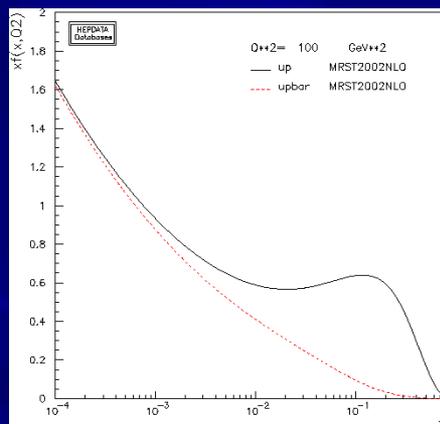
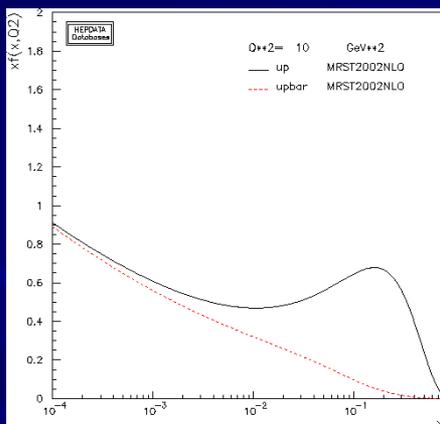
Au
gluons



- CGC saturation momentum:

$$Q_s^{\Upsilon}(x) = A^{1/3} Q_0^2 x^{-\lambda}$$

- Where $\lambda \sim 0.2-0.3$ controls the rapidity/energy dependence



- Mehtar-Tani and Wolschin. [PRL 102, 182301 (2009)]

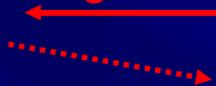


A CGC model for stopping: CGC kicks out valence quarks

d/Au
quarks



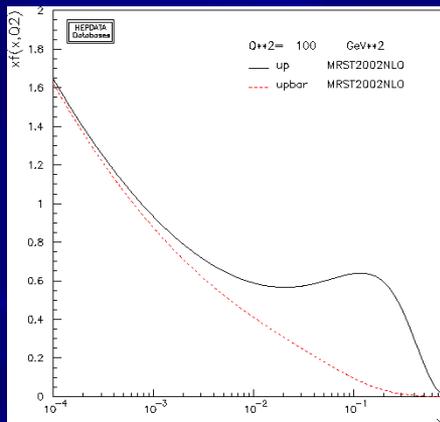
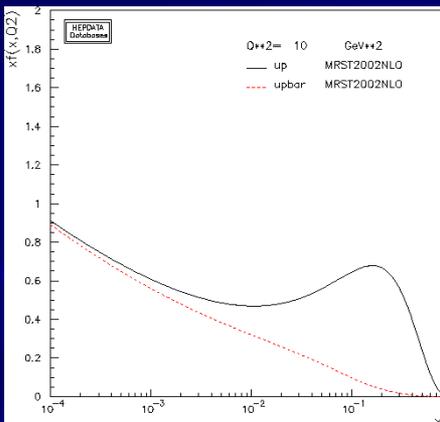
Au
gluons



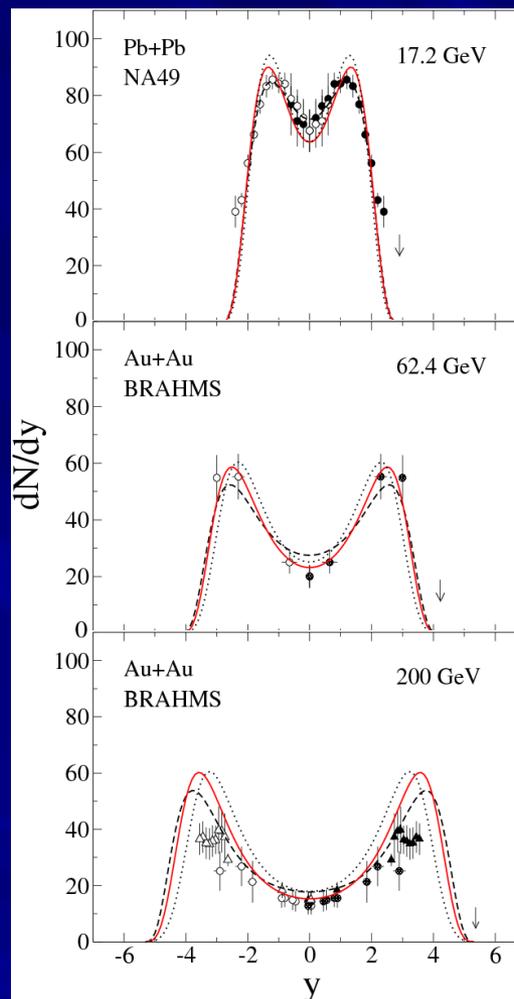
- CGC saturation momentum:

$$Q_s^{\gamma}(x) = A^{1/3} Q_0^2 x^{-\lambda}$$

- Where $\lambda \sim 0.2-0.3$ controls the rapidity/energy dependence



- Mehtar-Tani and Wolschin. [PRL 102, 182301 (2009)]



- Curves corresponds to different values for λ and Q_0

Dashed: $\lambda=0$ (universal) and $Q_0^2=0.08 \text{ GeV}^2$

$\lambda=0.15$ and $Q_0^2=0.07 \text{ GeV}^2$

Dotted: $\lambda=0.3$ (\sim HERA) and $Q_0^2=0.06 \text{ GeV}^2$

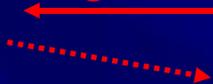


A CGC model for stopping: CGC kicks out valence quarks

d/Au
quarks



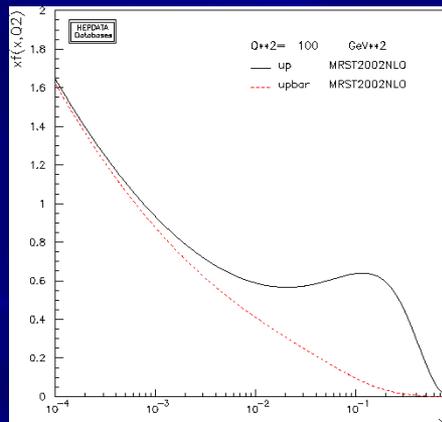
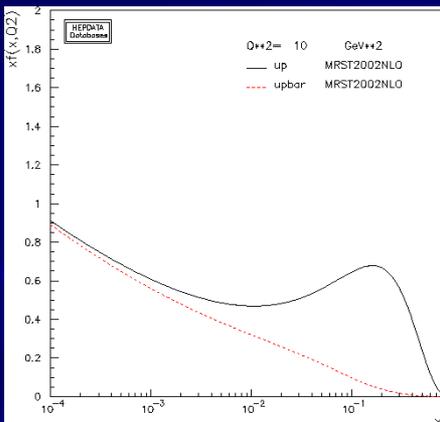
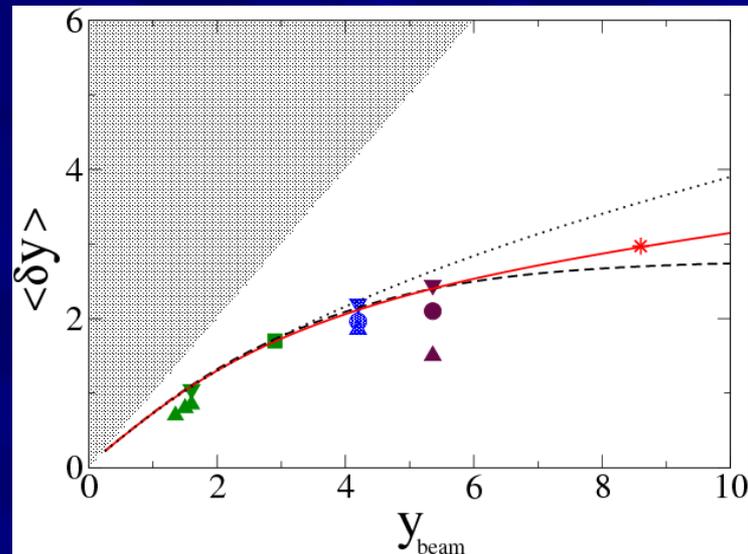
Au
gluons



- CGC saturation momentum:

$$Q_s^2(x) = A^{1/3} Q_0^2 x^{-\lambda}$$

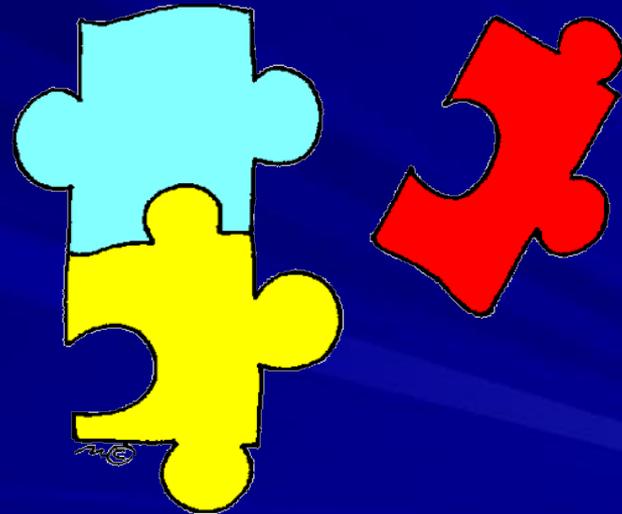
- Where $\lambda \sim 0.2-0.3$ controls the rapidity/energy dependence



- Two universal parameters controls stopping and particle production
- Universality is broken by λ
 - Mostly at forward rapidity (very small x)
- Centrality dependence?

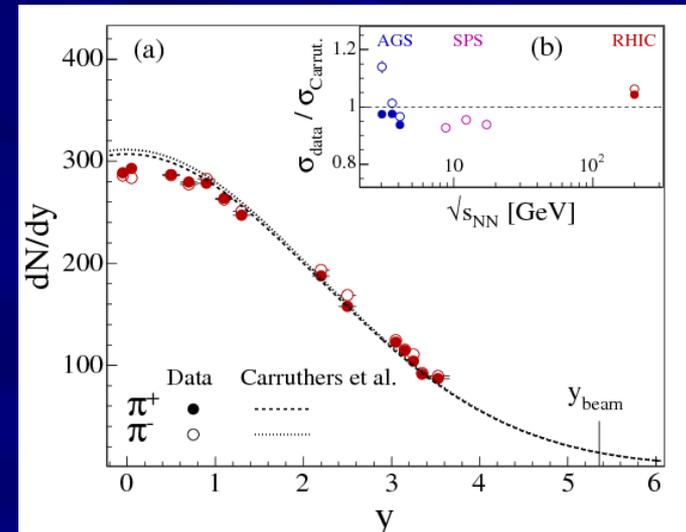
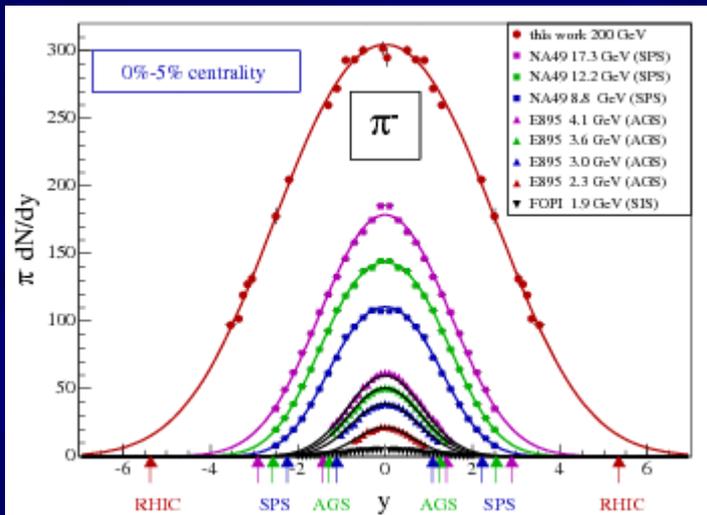
- Mehtar-Tani and Wolschin. [PRL 102, 182301 (2009)]

What is the relation to particle production in general





Landau hydrodynamics



- Landau hydrodynamics predicts Gaussian rapidity distributions with a width σ given by:

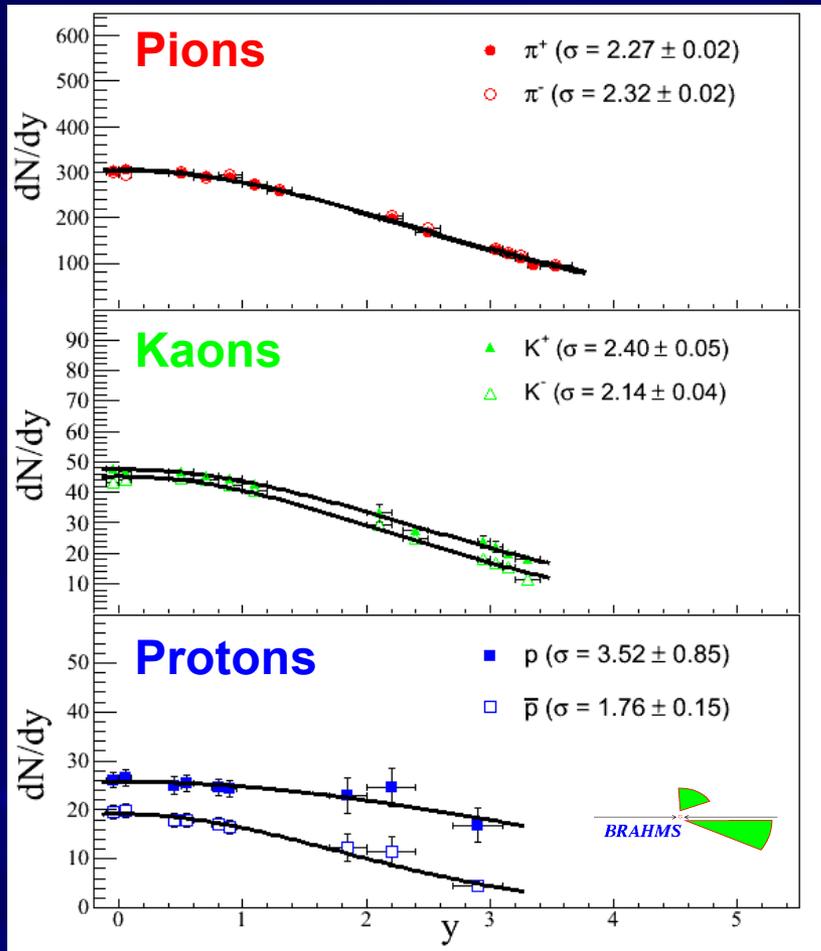
$$\sigma^2 = \ln \left(\frac{\sqrt{s}}{2m_p} \right) = \ln y_{CM} \sim y_{CM} - \ln 2$$

- Recent reference with exact result [PRC 78, 054902 (2008)]

[L.D. Landau, Izv. Akad. Nauk SSSR 17 (1953) 52
P.Carruthers, M.Duong-van, PRD 8 (1973) 859]



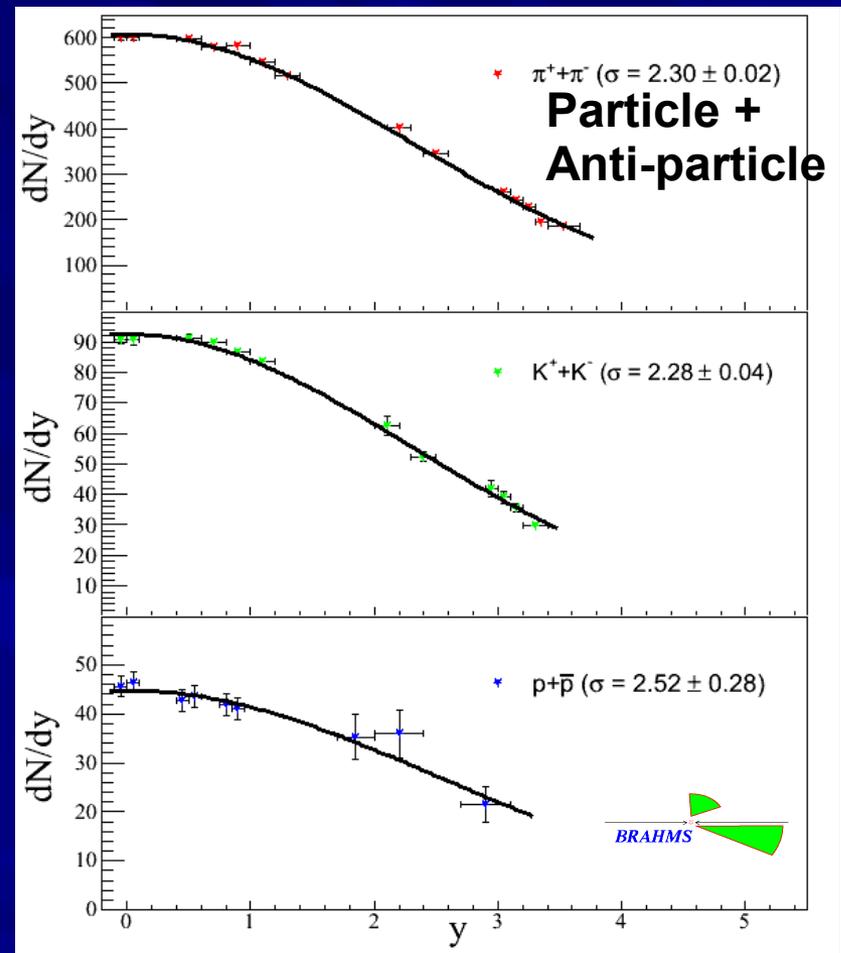
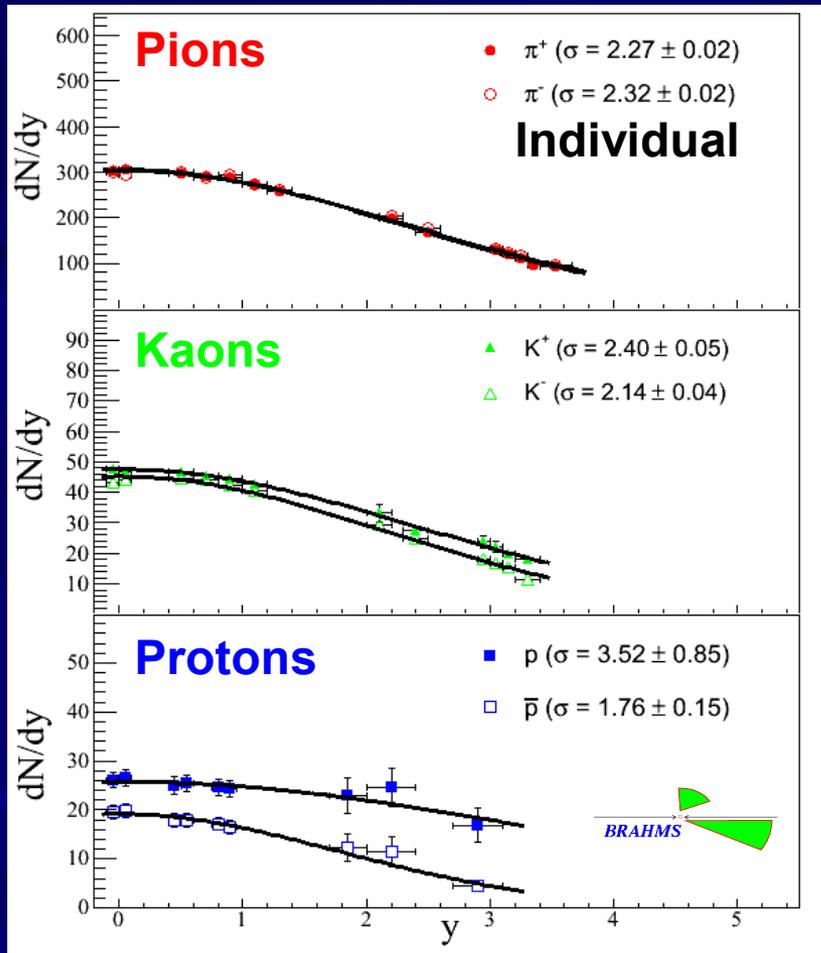
Does other dN/dy behave as Landau hydro?



Ordering of individual sigmas:
 $\bar{p} < K^- < \pi^+ < \pi^- < K^+ < p$



Does other dN/dy behave as Landau hydro?

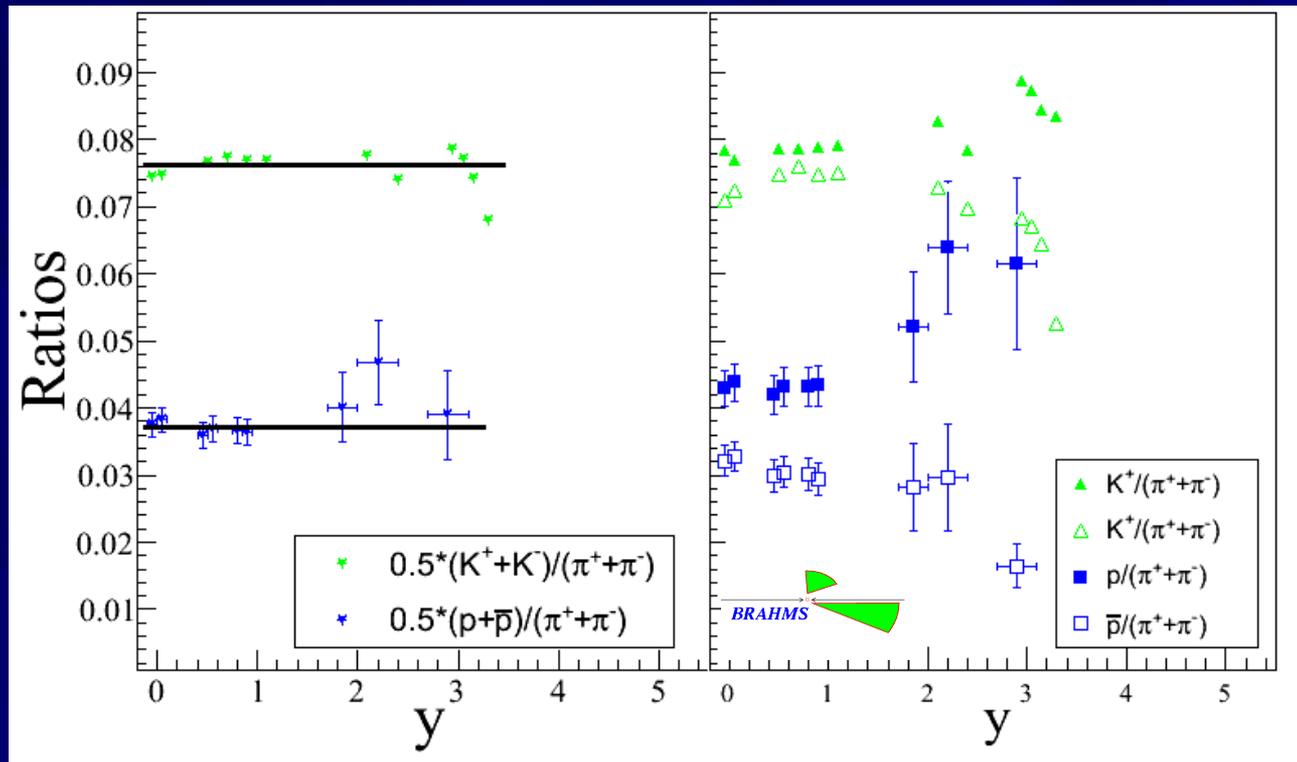


Ordering of individual sigmas:
 $\bar{p} < K^- < \pi^+ < \pi^- < K^+ < p$

Particle + anti-particle sigmas
are similar and \sim Landau



Interpretation a la statistical model via T and $\mu_B(y)$



For small chemical potentials ($\mu < T$):
 $\exp(-\mu/T) + \exp(\mu/T)$
 $(= 2 \cosh(\mu/T))$
 $\sim 1 - \mu/T + 1 + \mu/T \sim 2$
 i.e. constant

- The chemical freezeout temperature seems to be independent of rapidity so that it is only the baryon chemical potential which changes
- Might be just accidental



Summary

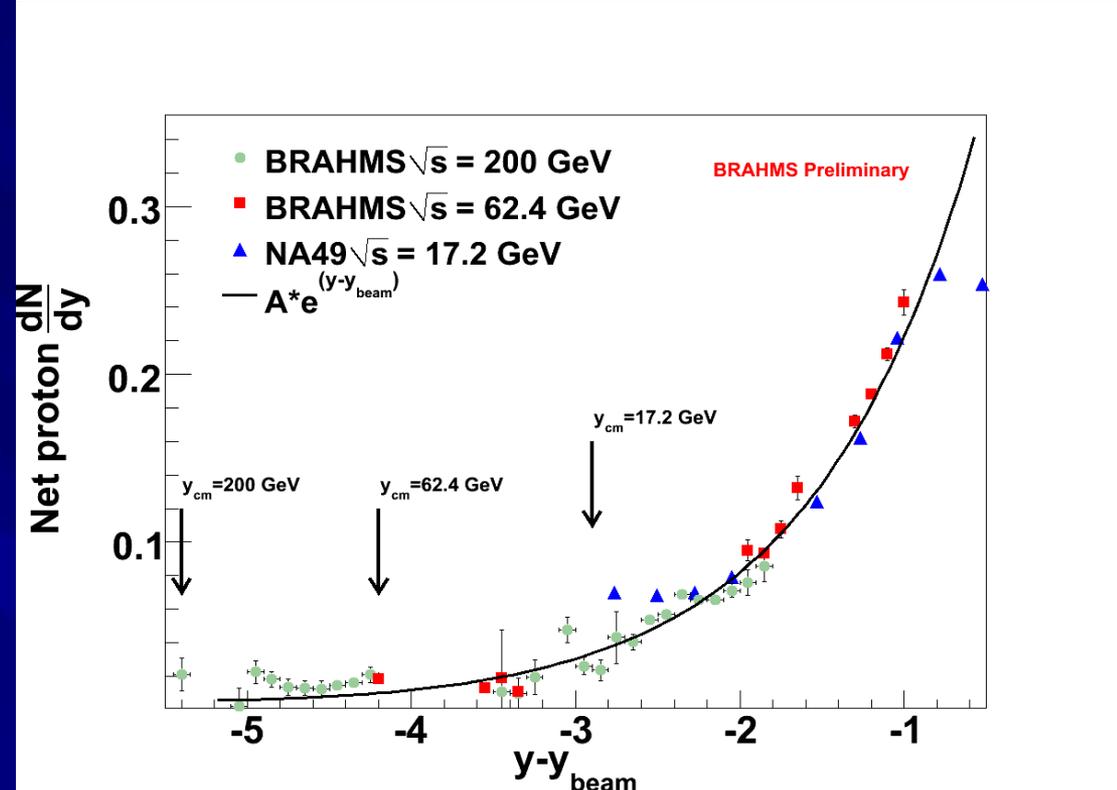
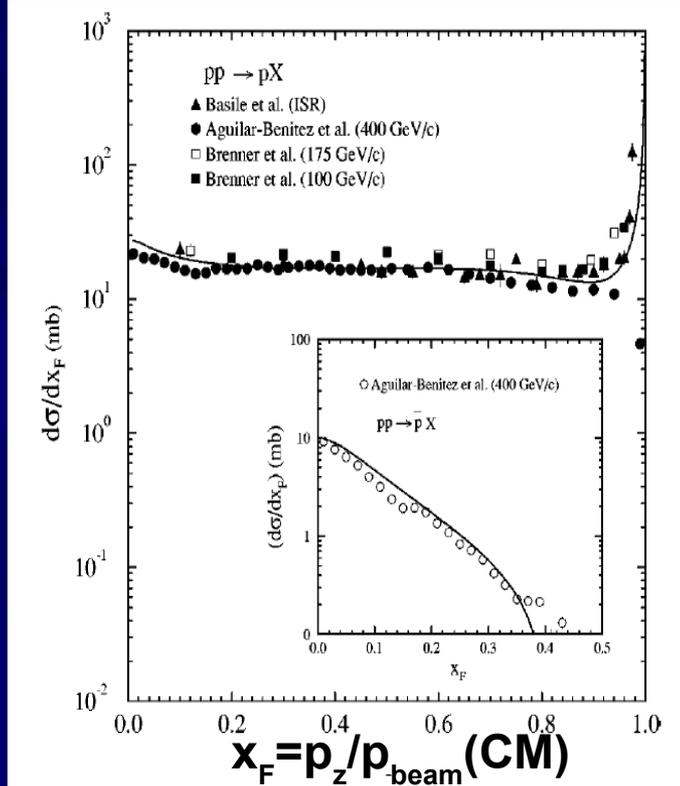
- Experimental data indicates
 - The net-baryon rapidity loss does not change significantly from AGS/SPS to RHIC for p+p and central A+A
 - Peripheral (60-80%) A+A shows same rapidity loss as p+p
 - Need more published data at SPS and RHIC (p+p, p/d+A, A+A)
- New coherent models shows reasonable agreement with data
 - Mechanism of stopping is clearer
 - Can the new models handle p+p, p+A, and A+A
- For models it would be particularly interesting to study (if possible) stopping for the projectile only
- Same mechanism of stopping from AGS/SPS to LHC?
 - PYTHIA indicates breaking of rapidity scaling at LHC due to the increase of the hard scale → more multiple interactions with higher activity



Backup slides



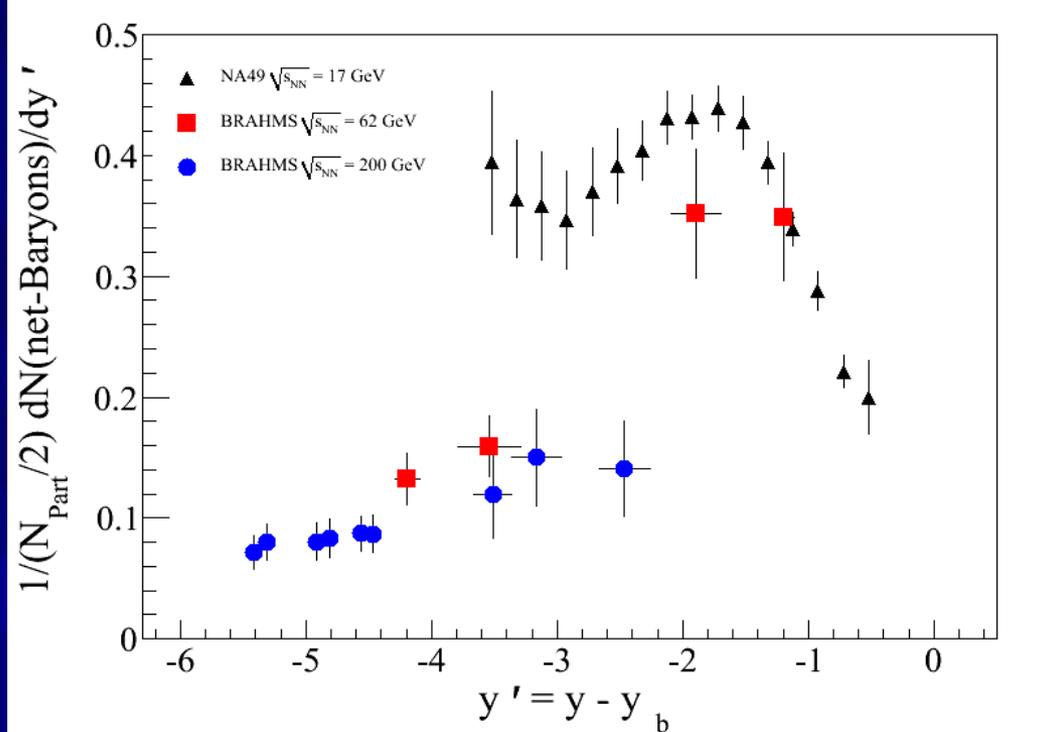
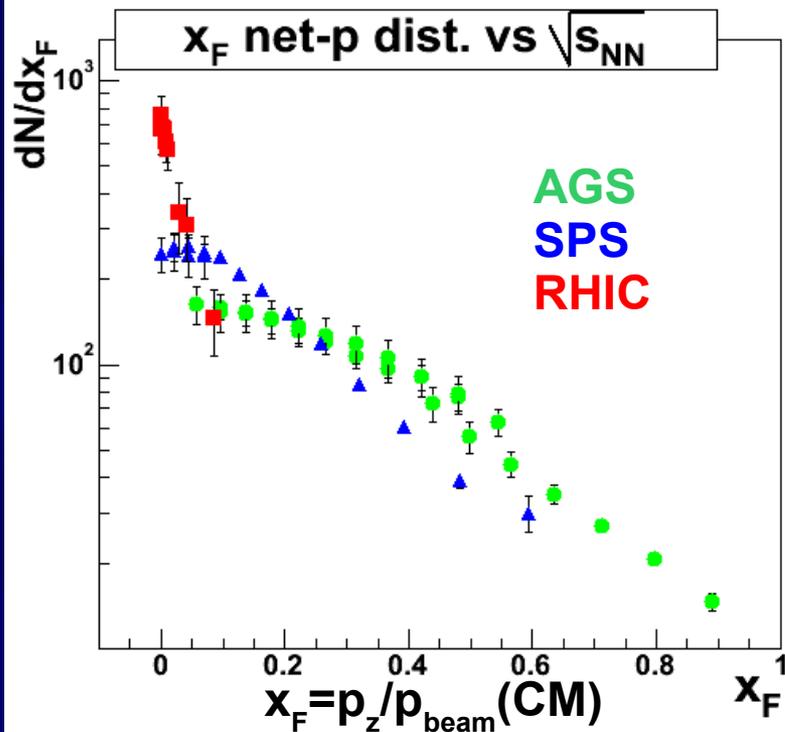
Stopping in $p+p$ collisions: Scaling of dN/dy



- $p+p$ collisions (at low energy) exhibits Feynman scaling so that $dN/dx_F \sim \text{constant} \rightarrow dN/dy \sim A * \exp(-(y_{\text{beam}} - y))$
- This universal behavior is also observed at RHIC



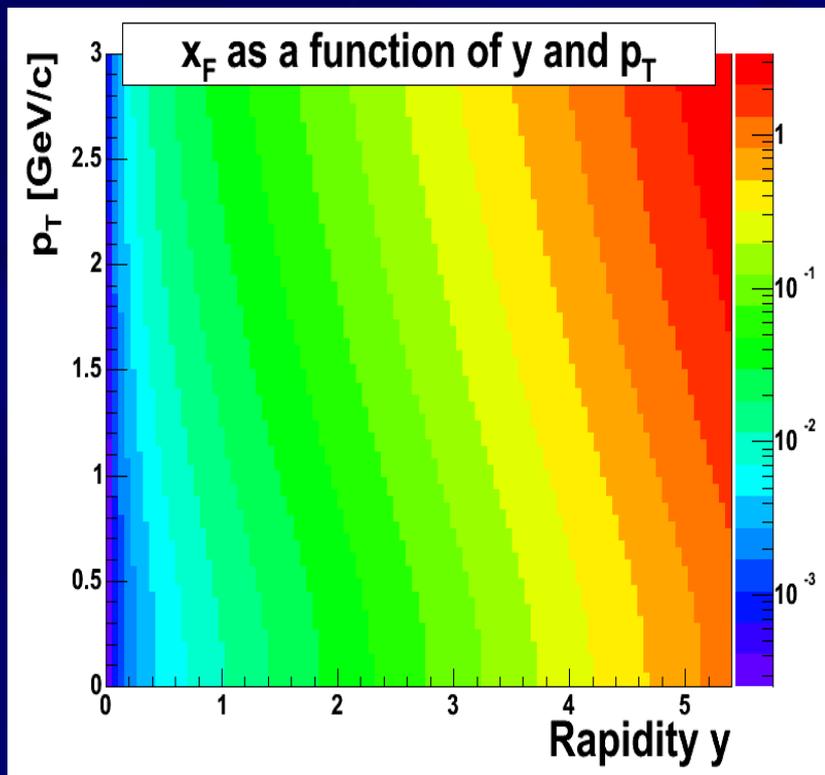
Stopping in A+A collisions: No obvious scaling of dN/dy



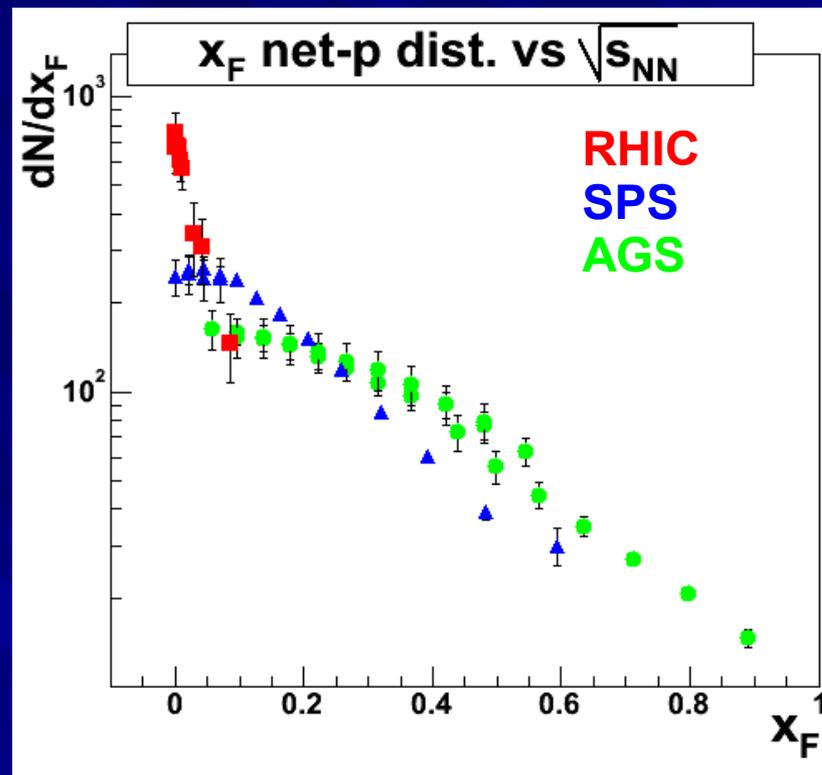
- In A+A collisions there is no Feynman scaling
- No obvious scaling in $y' = y_{beam} - y$ either
 - But when the target contribution is subtracted there is scaling!
- Quantify stopping by rapidity loss



dN/dxF



■ $X_F = p/PCM$





How to measure the net-baryon dN/dy after the collision

- Need good rapidity coverage
 - BRAHMS, (STAR FTPC), NA49
- Need good p_T coverage
 - 1st problem: extrapolate spectra to regions with no coverage
 - Solution: Require good fit description and consistent $\langle p_T \rangle$
- Need good particle identification for protons, Λ s and neutrons
 - 2nd problem: Neutrons are hard to measure
 - Solution: Use results from AGS: E941
 - 3rd problem: BRAHMS can measure protons, but not Λ s. STAR can measure forward Λ s only.
 - Solution 1: NA49 can measure both protons and Λ s.
 - Solution 2: The Λ s almost cancel in the conversion to net-B!

In the following I will use BRAHMS as an example



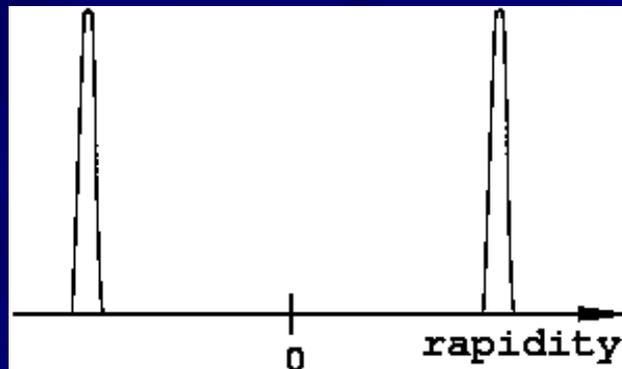
How to measure stopping

Use rapidity variable → distributions are boost invariant

Physical space

$$y = \frac{1}{2} \log \left(\frac{E + p_z}{E - p_z} \right)$$

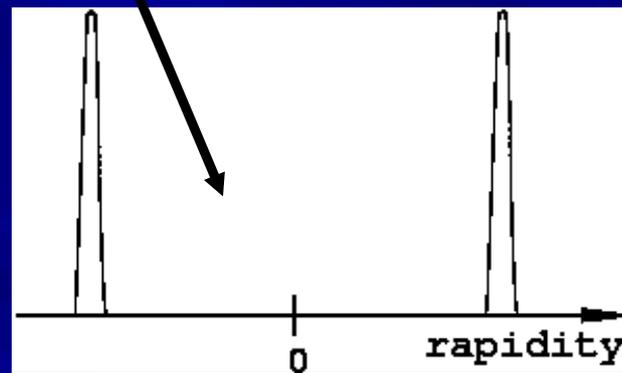
“Velocity” space



BEFORE COLLISION

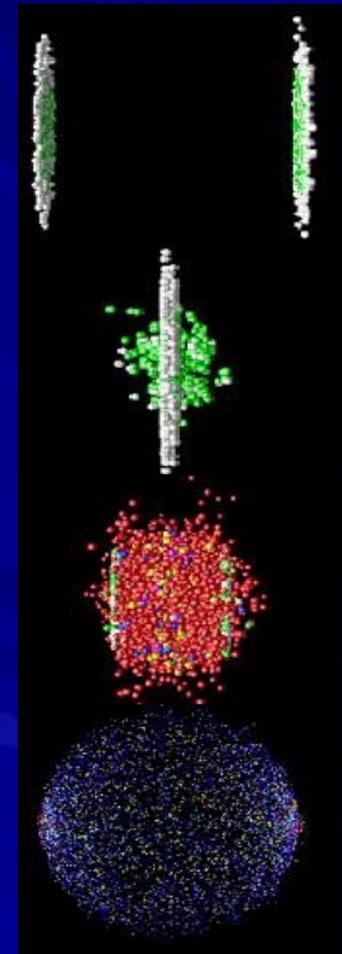


Full stopping



Full transparency

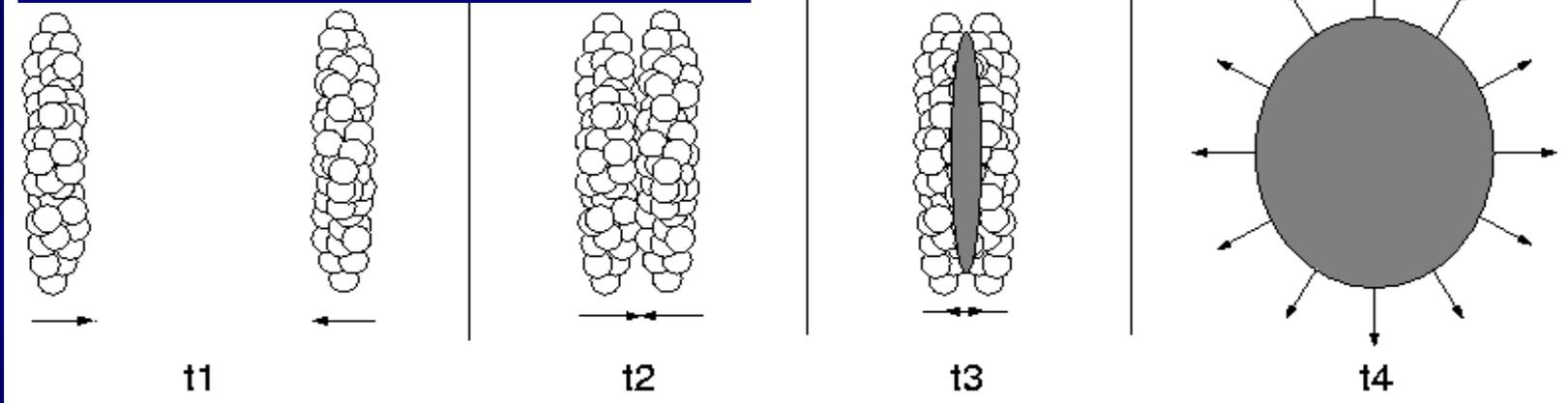
AFTER COLLISION
2 extreme final states



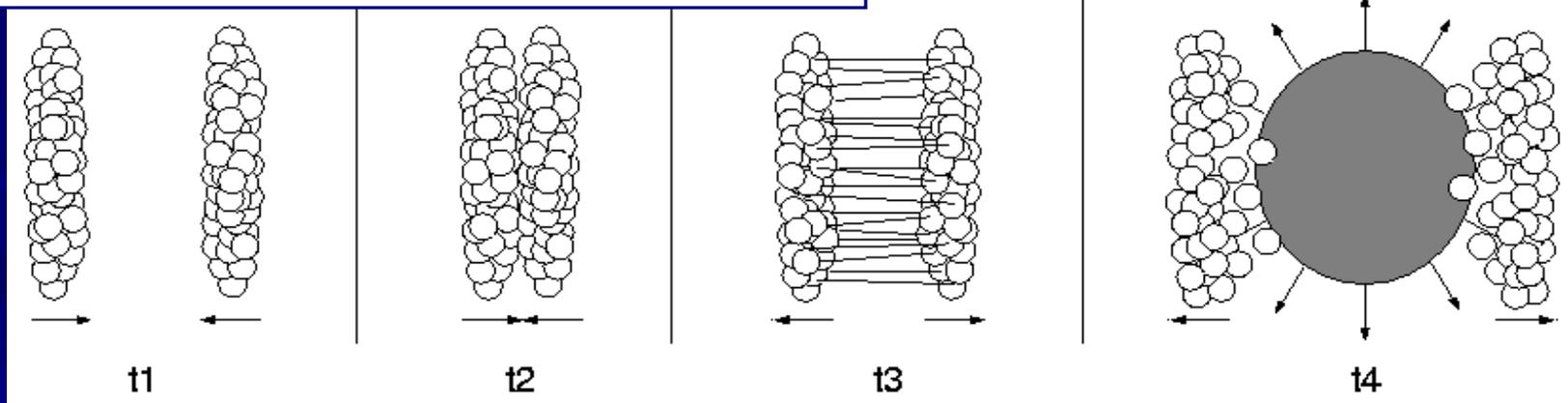


Two physics pictures

Stopping - excited nucleons



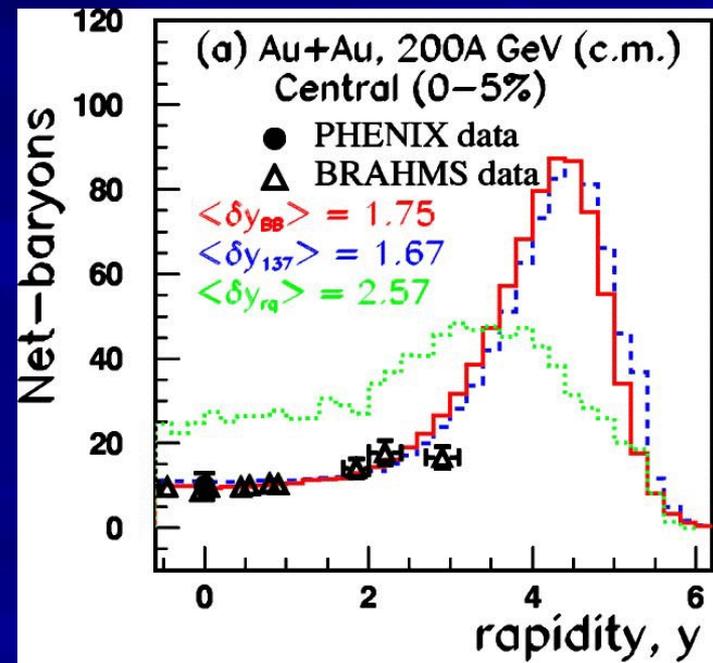
Transparency - excited color field





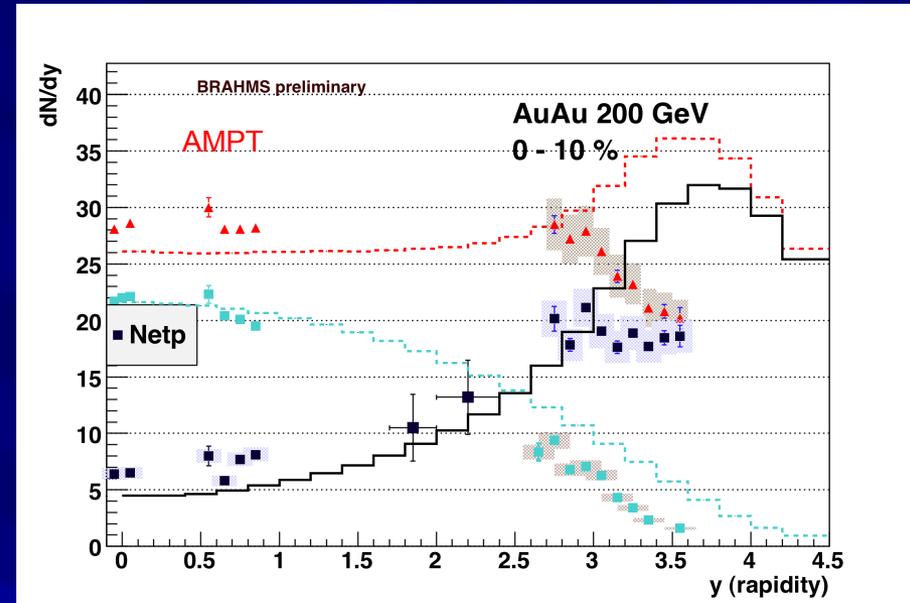
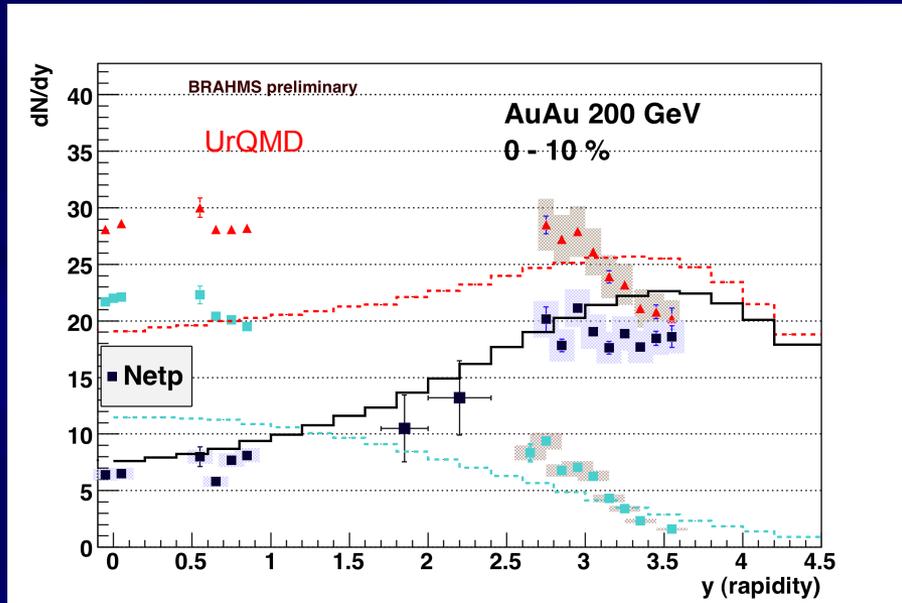
This is also important for models

- Some examples where comparison to net-p is done with the calculation normalized to the number of initial protons which is $\sim N_{\text{part}}/2.5 \neq N_{\text{part}}/2$
 - But I believe it is better to use net-B even there are systematic uncertainties
- Crosscheck normalization:
 - The plot on the right has wrong normalization of data:
 - $dN/dy(y=0) \sim 14$ and not 10!
 - It seems that by accident the two corrections from previous page has both been applied
 - [V. T. Pop et al, PRC 70, 064906 (2004)]





Model Comparisons shown at QM09



- Both models are “incoherent”. Several binary collisions with reduced cross section after the first one.



Can energy conservation explain Landau

Assume:
$$\frac{dN}{dy} = \frac{N_{total}}{\sqrt{y} \pi \sigma} e^{-y^2/2\sigma^2}$$

And that $\langle m_T \rangle$ does not depend on rapidity.

Integrate $\langle m_T \rangle \text{Cosh}(y) dN/dy$ and set equal to total energy:

$$E_{total} = N_{total} \langle m_T \rangle e^{\sigma^2/2} = N_{part/2} \sqrt{s}$$

So that:
$$\sigma^2 = 2 \ln \frac{N_{part/2} \sqrt{s}}{N_{total} \langle m_T \rangle}$$

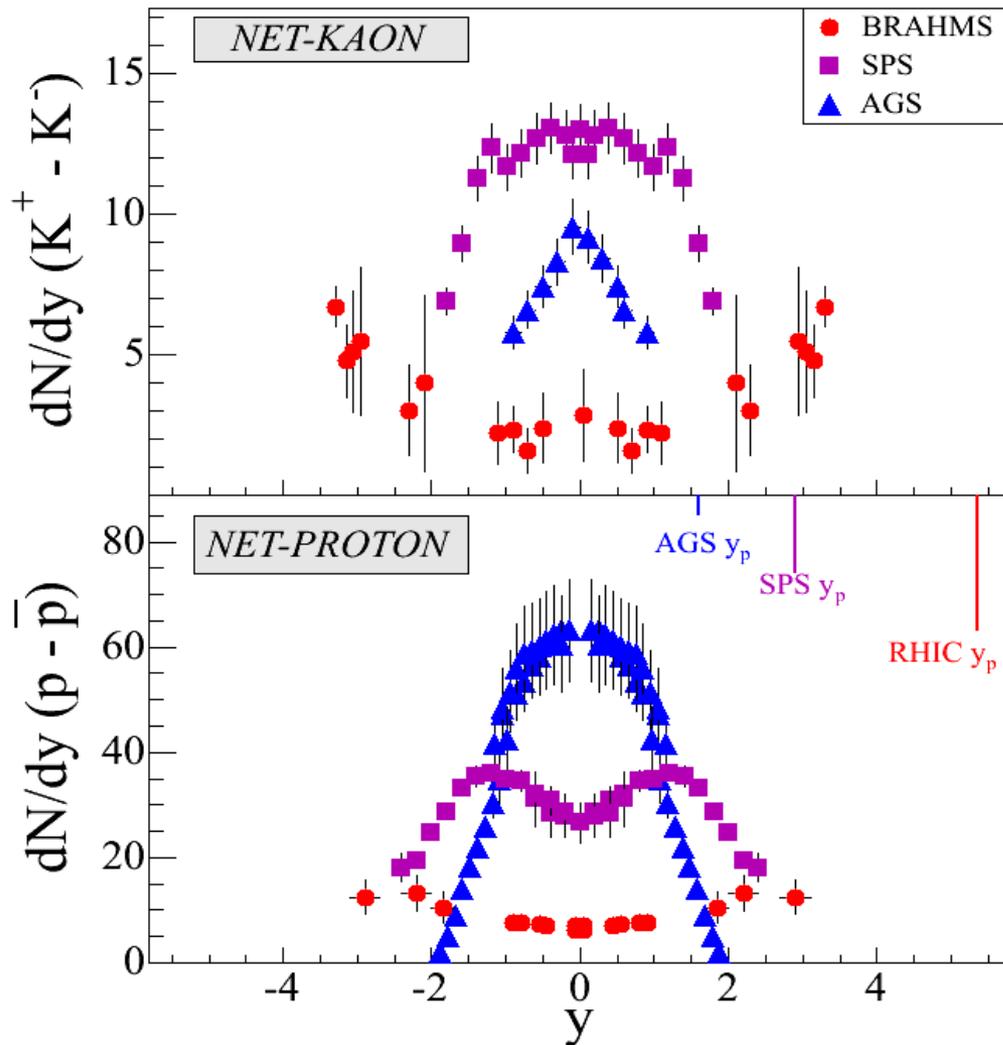
Landau/experimental fits to data predicts:
$$\frac{N_{total}}{N_{part/2}} = A s^{1/4}$$

So that:
$$\sigma^2 = \ln \frac{\sqrt{s}}{A \langle m_T \rangle^2} = \ln \frac{2 m_p}{A \langle m_T \rangle^2} + \ln \frac{\sqrt{s}}{2 m_p}$$

But the first term is not small.....



Net-kaons

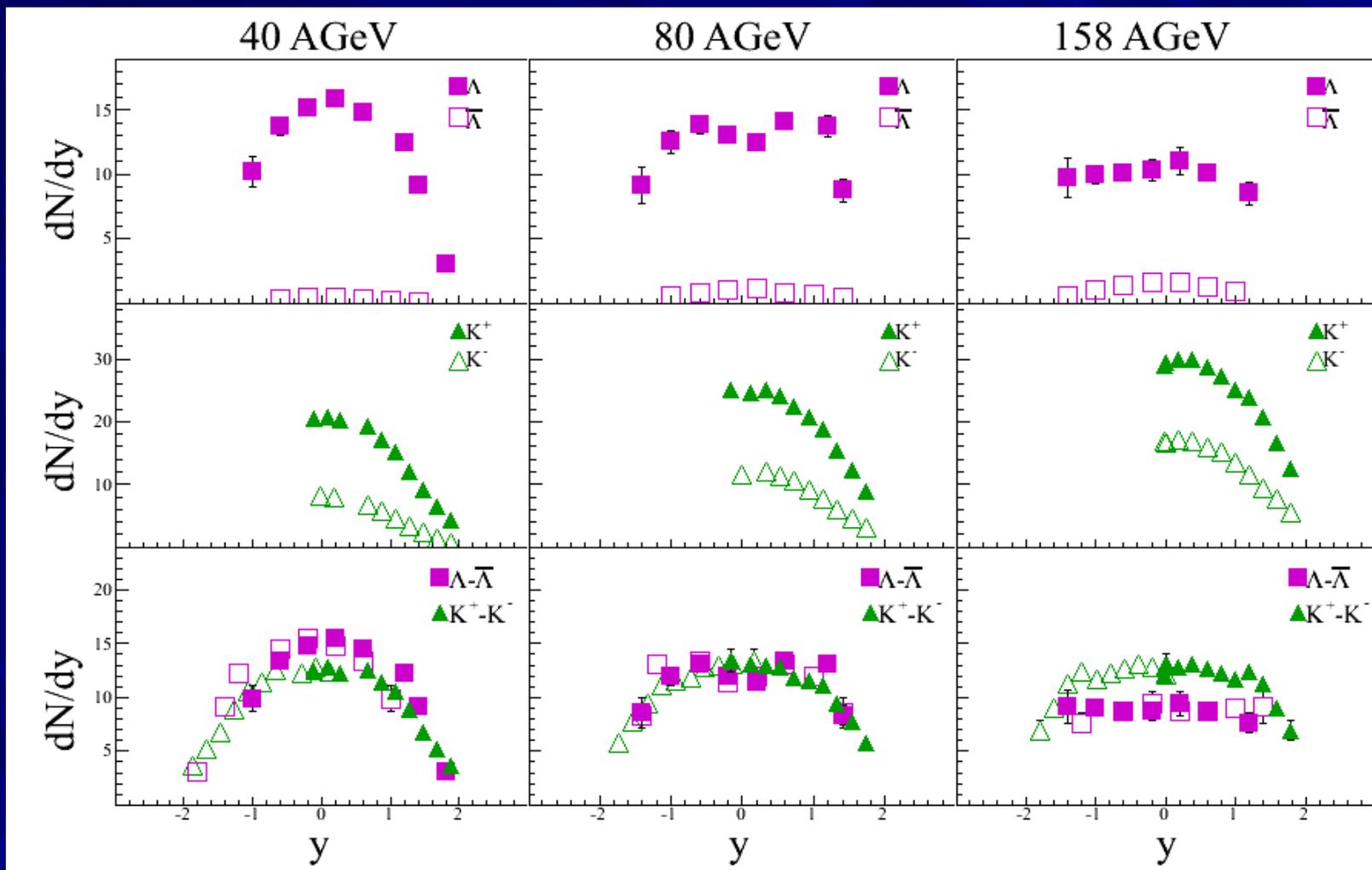


Net-Kaons follows the net-protons.

Suggest that there is (at least) a central and a fragmentation source.

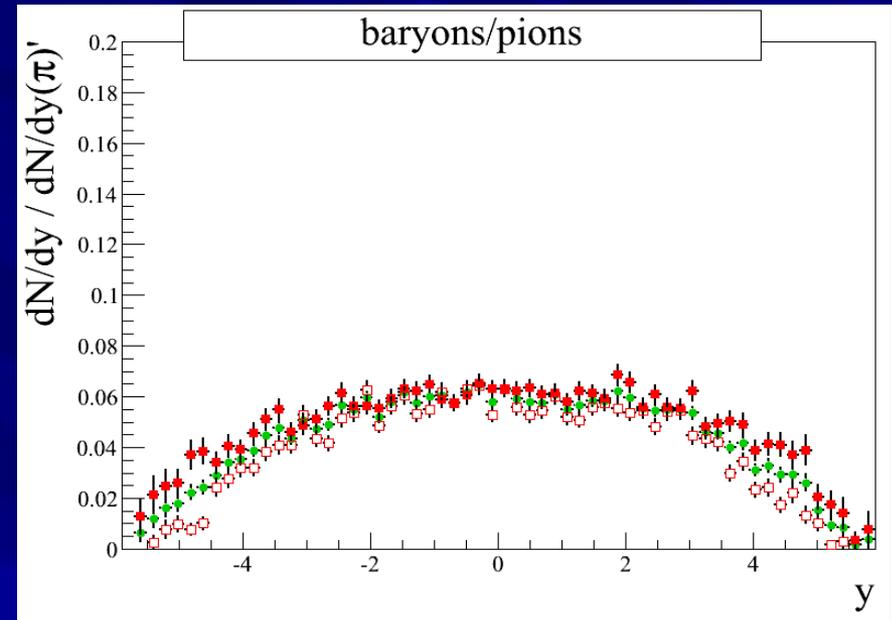
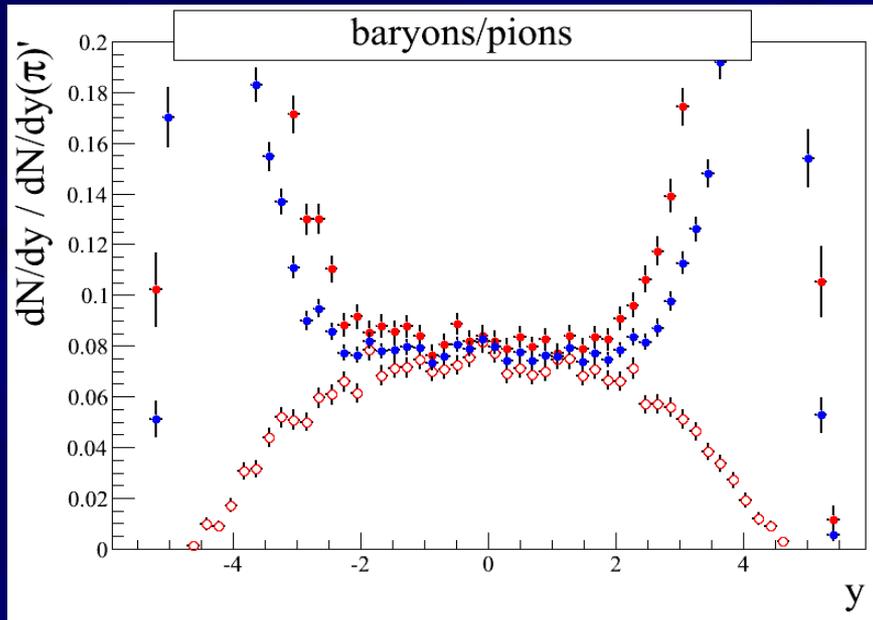


Net-Lambdas vs Net-Kaons at SPS





PYTHIA ratios vs y at 200 GeV



- Similar behavior for baryons, but different for kaons