

# Spin dynamics for high energy protons

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# Lagrange

born at via Lagrange within Torino, 1736

worked in Torino, Berlin, and Paris, 1813

# Hamilton

born in Dublin at 12pm, August 3, 1805

worked all his life near Dublin until 1865

events: [www.hamilton.tcd.ie](http://www.hamilton.tcd.ie)

# Summary

- New spin frontier from RHIC  $pp$  collider
- Partonic spin structure of the nucleon
- Scaled proton proton helicity amplitudes
- Rôle in understanding analyzing powers
- Longitudinal and transverse asymmetries
- Spin dependence studies for polarimetry
- Conclusions

# Introduction

Polarized proton beams facilitate a study of the spin dependent amplitudes of  $pp$  elastic scattering, particularly

$$\phi_+(s, 0) \propto \sigma_{\text{tot}} (i + \rho)$$

$$\phi_-(s, 0) \propto \Delta\sigma_L (i + \rho_-)$$

$$\phi_2(s, 0) \propto \Delta\sigma_T (i + \rho_2)$$

$$\phi_5(s, t) \propto \sqrt{-t}$$

with the definitions,  $\phi_{\pm} = (\phi_1 \pm \phi_3)/2$  where  $\phi_+$  here refers to the dominant spin averaged proton proton amplitude.

Proton carbon elastic scattering has been successfully used by the E950 Collaboration as a polarimeter for RHIC. Polarized neutron studies could use forward deuteron carbon elastic scattering or helium-3 carbon elastic scattering for polarimetry. Understanding the hadronic spin dependence would increase the effectiveness of each polarimeter.

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# Scaled amplitudes

Introduce ratios of amplitudes relative to the dominant imaginary proton proton amplitude  $\text{Im } \phi_+$

$$R_2 + i I_2 = \frac{\phi_2}{2 \text{Im } \phi_+}$$

$$R_- + i I_- = \frac{\phi_-}{\text{Im } \phi_+}$$

$$R_5 + i I_5 = \left( \frac{m}{\sqrt{-t}} \right) \frac{\phi_5}{\text{Im } \phi_+}$$

as such ratios are expected to have a variation in  $t$  that is less pronounced near the forward direction of scattering.

To first order in small quantities  $\rho$ ,  $R_5$ ,  $I_5$ , and Coulomb phase  $\delta$ , the maximum of the pC asymmetry  $A_N$  occurs at  $t$  value

$$\frac{t_{\max}}{t_c} = \sqrt{3} - \rho - \delta - \frac{8}{\mu - 1} R_5 + \dots$$

where  $t_c = 8 \pi \alpha / \sigma_{\text{tot}}$  near interference. The maximum of  $A_N$  to first order is

$$\frac{4 m A_{\max}}{\sqrt{-3} \sqrt{3} t_c} = (\mu - 1) \left[ 1 + \frac{\sqrt{3}}{2} (\rho + \delta) \right] - 2\sqrt{3} R_5 - 2 I_5 + \dots$$

Similar expressions appear for the pp asymmetry  $A_N$  but with additional terms  $R_2$ ,  $I_2$ ,  $R_-$ ,  $I_-$ , reflecting the more elaborate pp spin dependence.

- A positive value of  $\rho$ , about 0.10 over the RHIC energy range, would enhance the single spin asymmetry maximum
- A positive real or imaginary part of the single helicity flip amplitude would reduce the maximum of the asymmetry
- It would be helpful to know more about the augmented helicity flip amplitudes,  $R_5$  and  $I_5$ , and generally  $R_2$ ,  $I_2$ ,  $R_-$ ,  $I_-$  in the case of pp elastic scattering.

The spin dependent amplitudes of proton proton collisions are, in fact, accessible from asymmetry measurements undertaken in the interference region with both initial protons spin polarized.

# Spin asymmetries

$A_N, A_{NN}, A_{SS}, A_{LL}, A_{SL}$  have singular terms in  $t$  arising from CN interference. The scaled  $pp$  differential cross section

$$\mathcal{I}_0 \equiv \left( \frac{t}{e^{2Bt} \sigma_{\text{tot}}} \right) \frac{d\sigma}{dt}$$

with a logarithmic slope parameter  $2B$  has a singular expansion in powers of  $t$

$$\mathcal{I}_0 = \frac{4\pi \alpha^2}{\sigma_{\text{tot}} t} + \alpha a_0 + \frac{\sigma_{\text{tot}}}{8\pi} b_0 t + \dots$$

where it is assumed here that coefficients like  $a_0, b_0$  are essentially  $t$ -independent.

For initial protons both polarized along axis,  $N$  (normal to the scattering plane), or  $L$  (longitudinal), the  $t$  expansion is

$$A_{NN} \mathcal{I}_0 = \alpha a_{NN} + \frac{\sigma_{\text{tot}}}{8\pi} b_{NN} t + \dots$$

$$A_{LL} \mathcal{I}_0 = \alpha a_{NN} + \frac{\sigma_{\text{tot}}}{8\pi} b_{LL} t + \dots$$

Spin observables with both initial protons polarized along perpendicular axes  $S$ ,  $L$  have a similar power series expansion in  $t$

$$-A_{SL} \mathcal{I}_1 = \alpha a_{SL} + \frac{\sigma_{\text{tot}}}{8\pi} b_{SL} t + \dots$$

In identical  $pp$  scattering,  $A_{LS} = A_{SL}$  and near the forward direction one could check the expected equality  $A_{NN} \approx A_{SS}$ .

Like  $A_{SL}$ , the spin asymmetry with one of the initial protons polarized has a  $\sqrt{-t}$  factor and so in

$$-A_N \mathcal{I}_1 = \alpha a_N \frac{\sigma_{\text{tot}}}{8\pi} + b_N t + \dots$$

it is convenient to define another scaled unpolarized differential cross section

$$\mathcal{I}_1 \equiv \frac{m\sqrt{-t}}{e^{2Bt}\sigma_{\text{tot}}} \cdot \frac{d\sigma}{dt}$$

The eight expressions for the measurable coefficients,  $a_j$ ,  $b_j$ , of the asymmetry expansions are sufficient to determine

$$R_j, I_j, \quad j = +, -, 2, 5$$

or at least bounds on these amplitudes.

Table 1: The expansion coefficients  $a_j$

Observable	$a_j$
$\mathcal{I}_0$	$\rho$
$A_{NN}\mathcal{I}_0$	$R_2$
$A_{LL}\mathcal{I}_0$	$R_-$
$-A_{SL}\mathcal{I}_1$	$\kappa(R_2 + R_-)/2$
$-A_N\mathcal{I}_1$	$I_5 - \kappa(1 + I_2)/2$

Recall that for  $A_N$ , the occurrence of the single helicity flip value  $I_5$  in the coefficient  $a_N$  presented a difficulty for polarimeter normalization as does, incidentally, a non-zero value of  $I_2$ .

Only the single helicity flip amplitude represents a problem for proton carbon elastic scattering with just two helicity amplitudes or for deuteron carbon elastic scattering with four helicity amplitudes.

Table 2: The expansion coefficients  $b_j$

Observable	$b_j$
$\mathcal{I}_0$	$(1 + \rho^2 + R_-^2 + I_-^2)/2 + R_2^2 + I_2^2$
$A_{NN}\mathcal{I}_0$	$R_2(\rho + R_-) + I_2(1 + I_-)$
$A_{LL}\mathcal{I}_0$	$\rho R_- + I_- + R_2^2 + I_2^2$
$-A_{SL}\mathcal{I}_1$	$R_5(R_2 + R_-) + I_5(I_2 + I_-)$
$-A_N\mathcal{I}_1$	$I_5(\rho + R_2) - R_5(1 + I_2)$

# Analyzing power

- The analyzing power for polarized protons has a maximum in the Coulomb interference momentum transfer region.
- Spin effects change the value of the maximum expected on theoretical grounds in the absence of such effects.
- Many spin dependent terms can be obtained from double spin asymmetry measurements near forward angles.
- A study of the energy dependence of individual terms via interpolation, or

through the use of analyticity relations, would assist the understanding of their contribution to other processes such as deuterium or helion carbon elastic scattering

- The dipole magnetic moment of the deuteron  $\mu_d = 0.8574$  is less than the proton's  $\mu_p = 2.7928$  changing the maximum in the pC analyzing power to a small minimum in the dC analyzing power near the interference region.
- Isolating helicity dependent terms could elicit their energy and momentum transfer dependence and facilitate the understanding of proton spin structure.

# Conclusions

- Understanding hadronic spin dependence assists polarimetry
- Change in maximum analyzing power at interference
- Implications for polarized deuteron and helion beams
- Causality test via analyticity of spin dependent amplitudes
- Measurement of double spin asymmetries near forward direction

# Colours

pink mgnt prpl

navy

azur cyan teal