

# QCD phase diagram

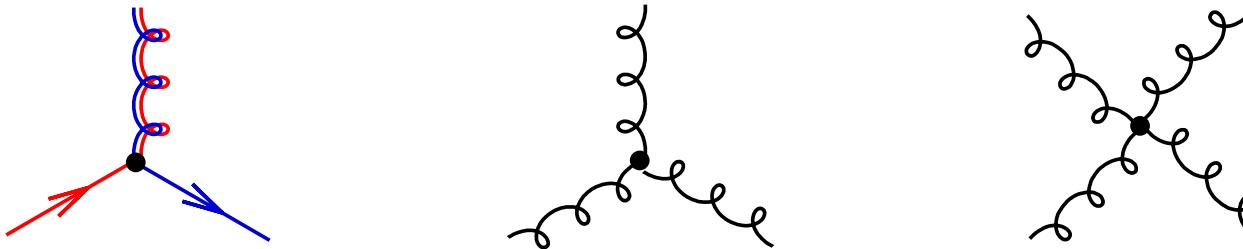
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*U. of Illinois at Chicago  
RBRC 1999-2004*

# QCD – asymptotically free field theory

- At short distances – can see fundamental constituents.
- QCD is a quantum field theory:

$$S = \int d^4x \left[ \sum_{f=1}^{N_f} \bar{q}_f (i\cancel{\partial} + g\cancel{A} - m_f) q_f - \frac{1}{2} \text{Tr } F_{\mu\nu} F^{\mu\nu} \right];$$



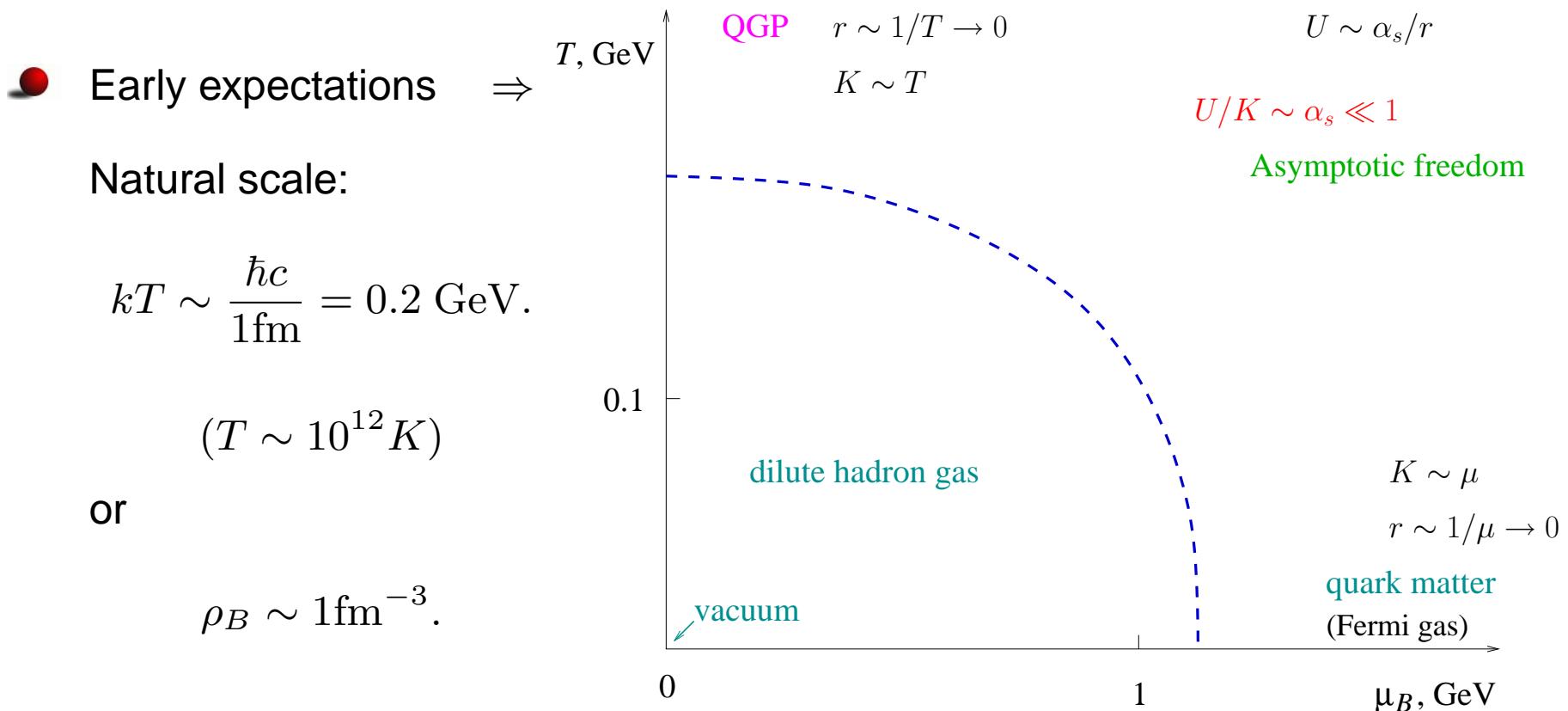
- Predictive power: i.e., for every physical quantity it gives a recipe to calculate it.
  - ... Whether we are ready to do the calculation is a different matter.
- Strongly interacting theory (confinement) — hadrons.  
QCD generates the mass as we know it.

# QCD thermodynamics

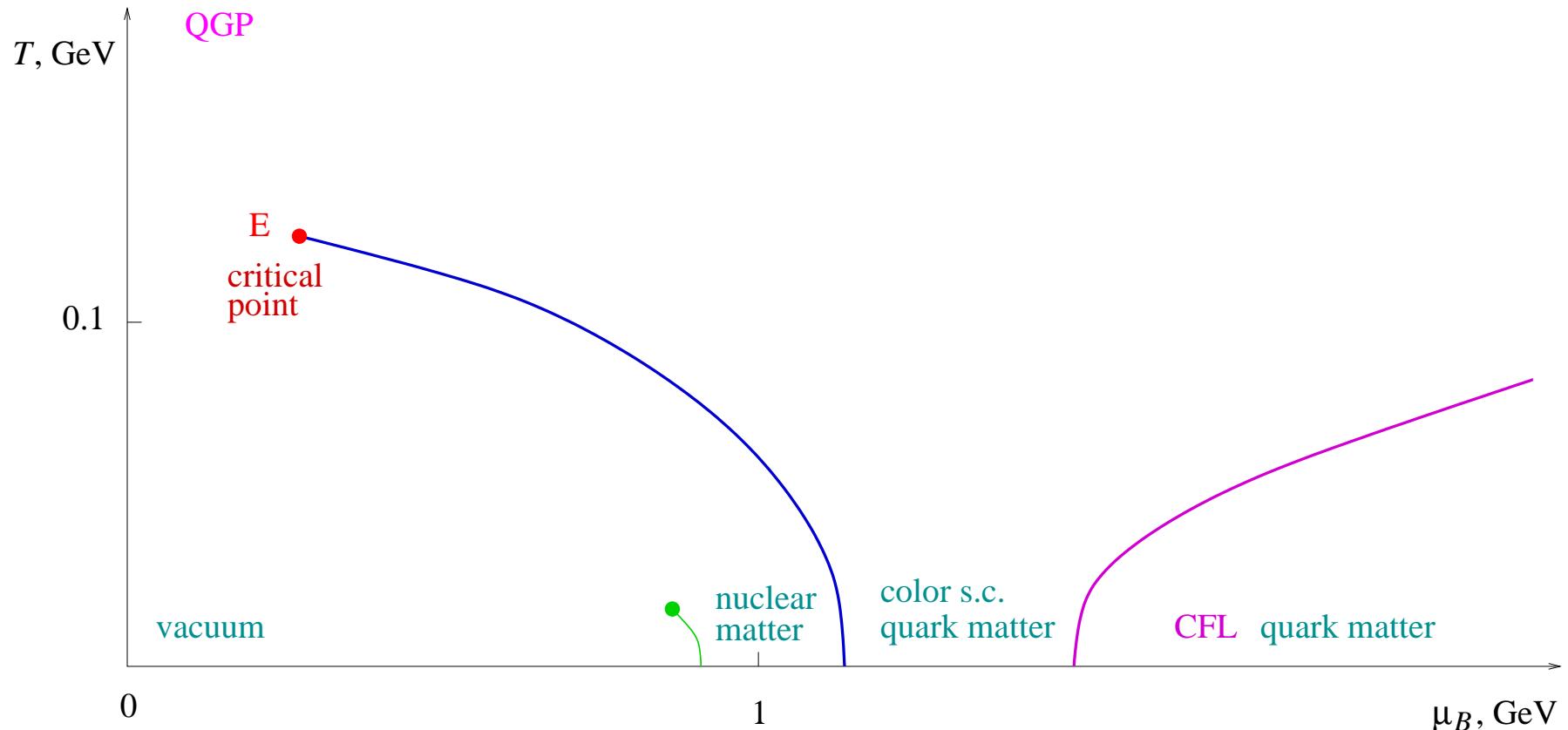
- Applications:
  - Neutron stars (large density, low  $T$ )
  - Heavy-ion collisions (large  $T$ , large density)
- QCD allows first principle calculations
- Questions: phases, phase diagram, as function of  $T$ ,  $\mu_B$ , ...

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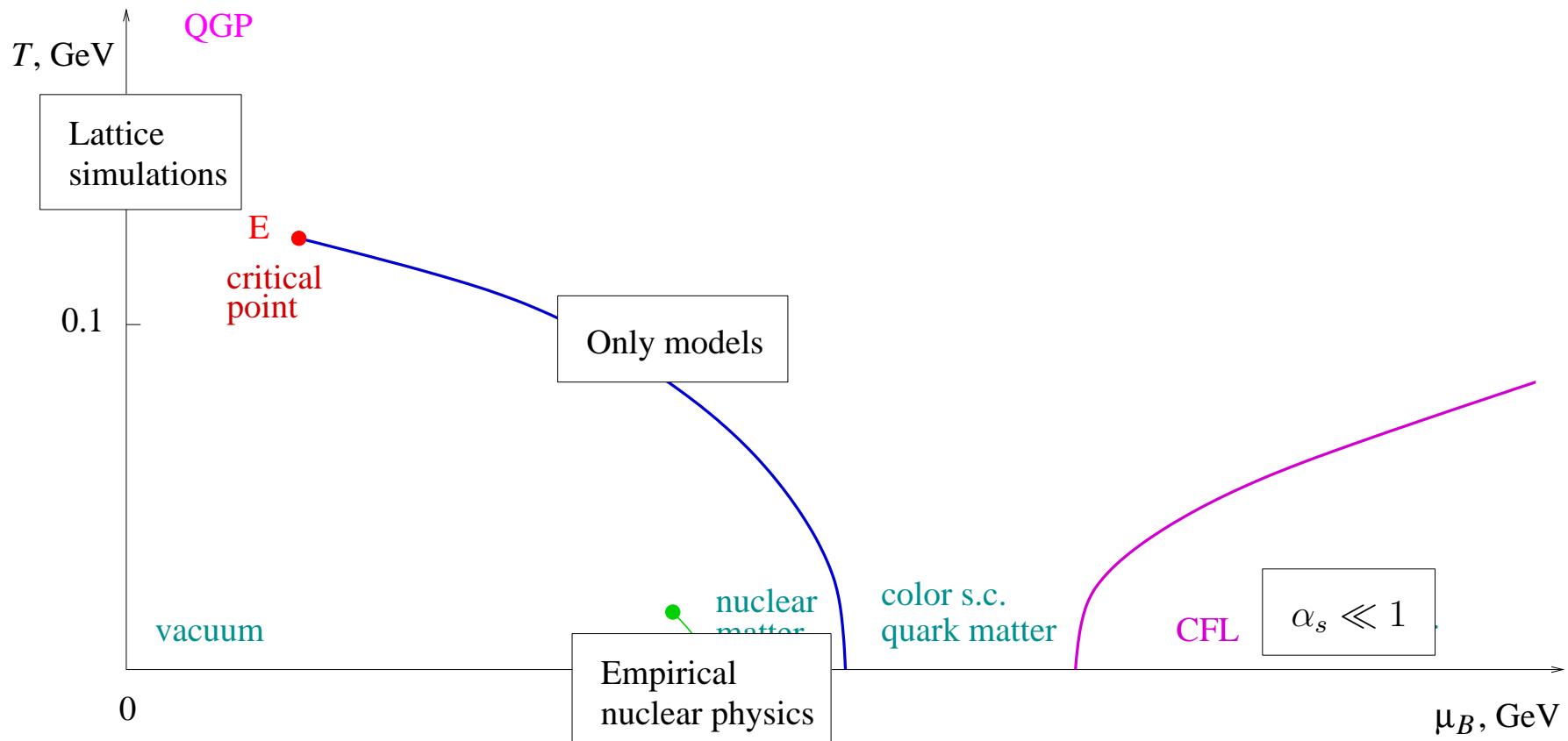


# Contemporary view



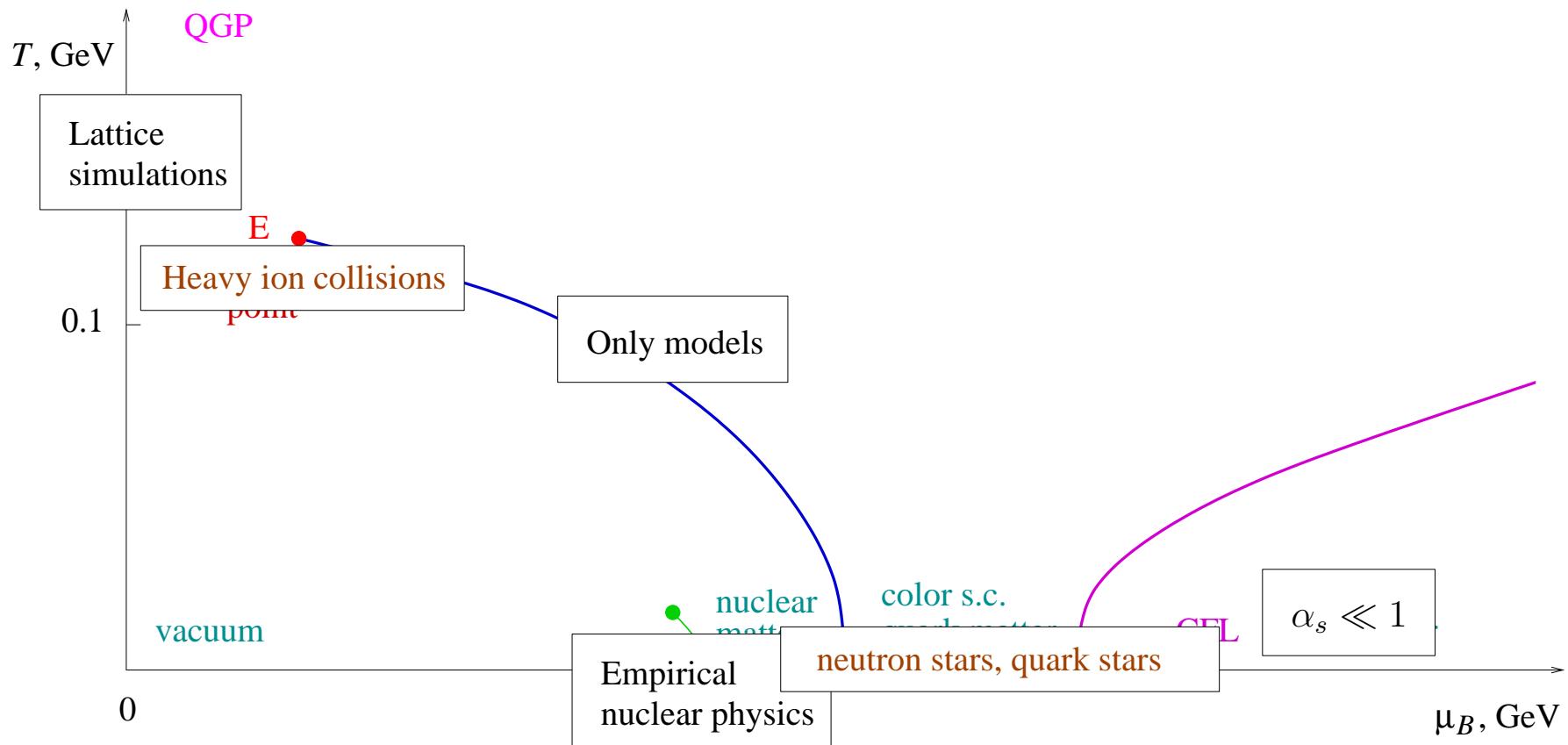
“Minimal” phase diagram

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“Minimal” phase diagram

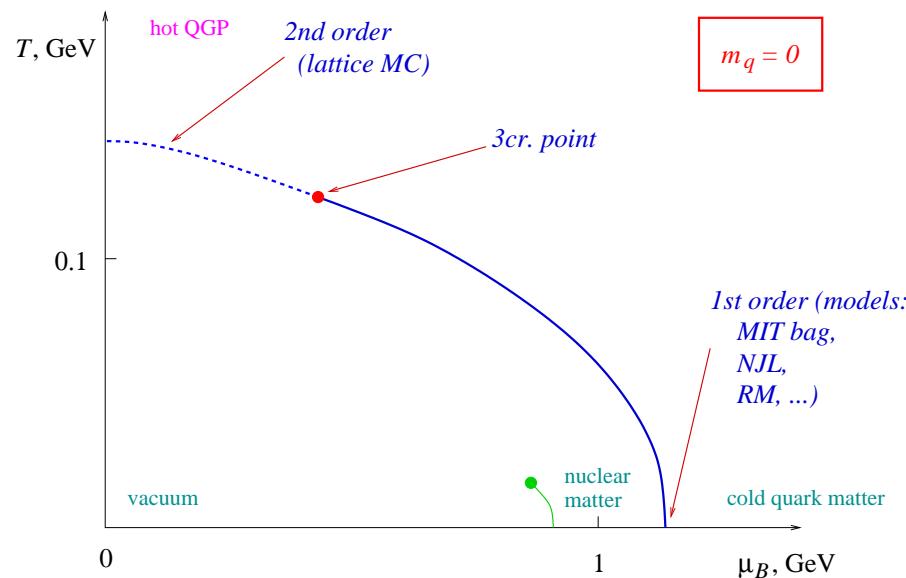
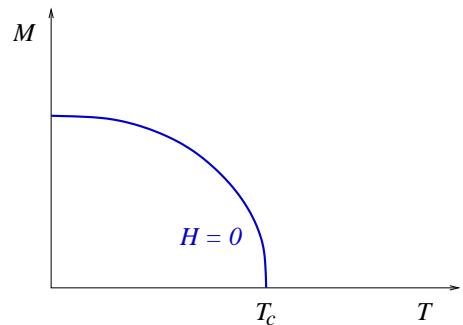
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“Minimal” phase diagram

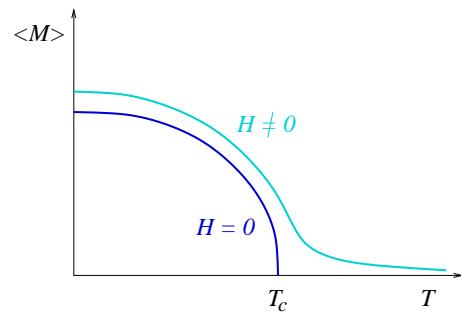
# Role of chiral symmetry and $m_q \neq 0$

Ferromagnet

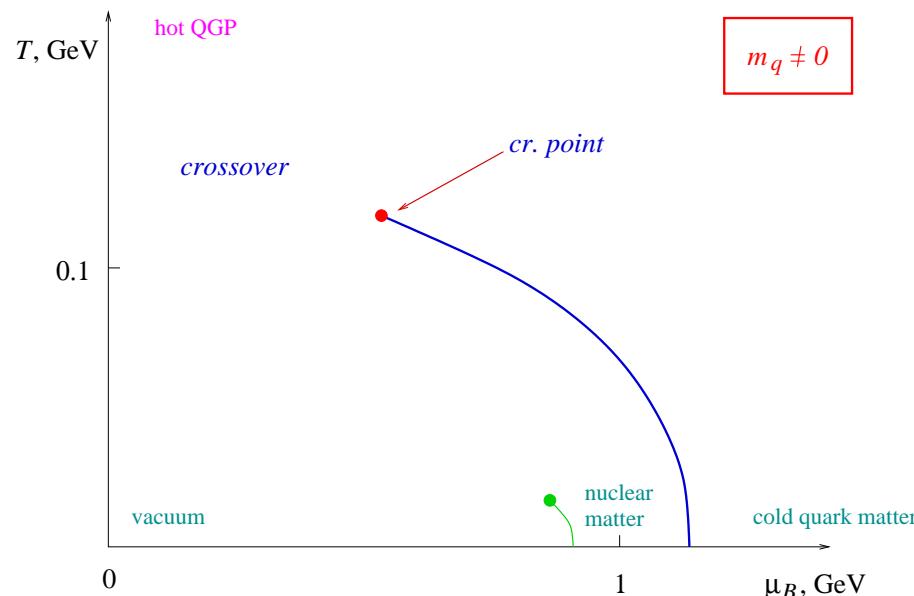


# Role of chiral symmetry and $m_q \neq 0$

Ferromagnet at  $H \neq 0$ :



no phase transition, but crossover

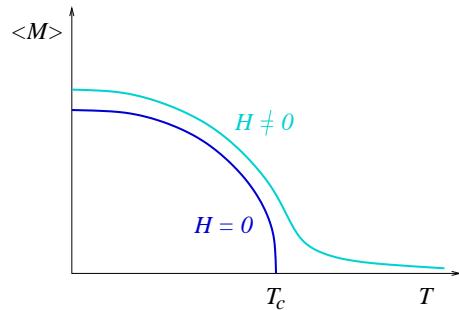


- Why all phases (can be) connected? Because  $\nexists$  order parameters:  
no chiral symmetry ( $m_q \neq 0$ );

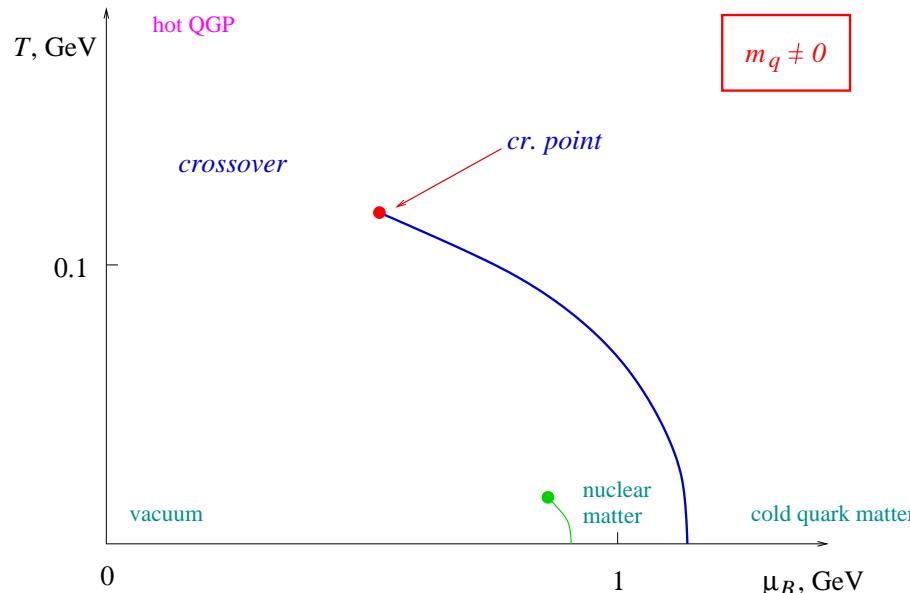
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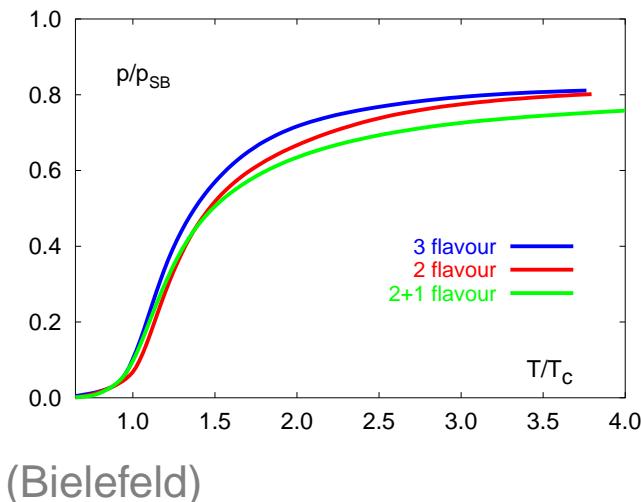
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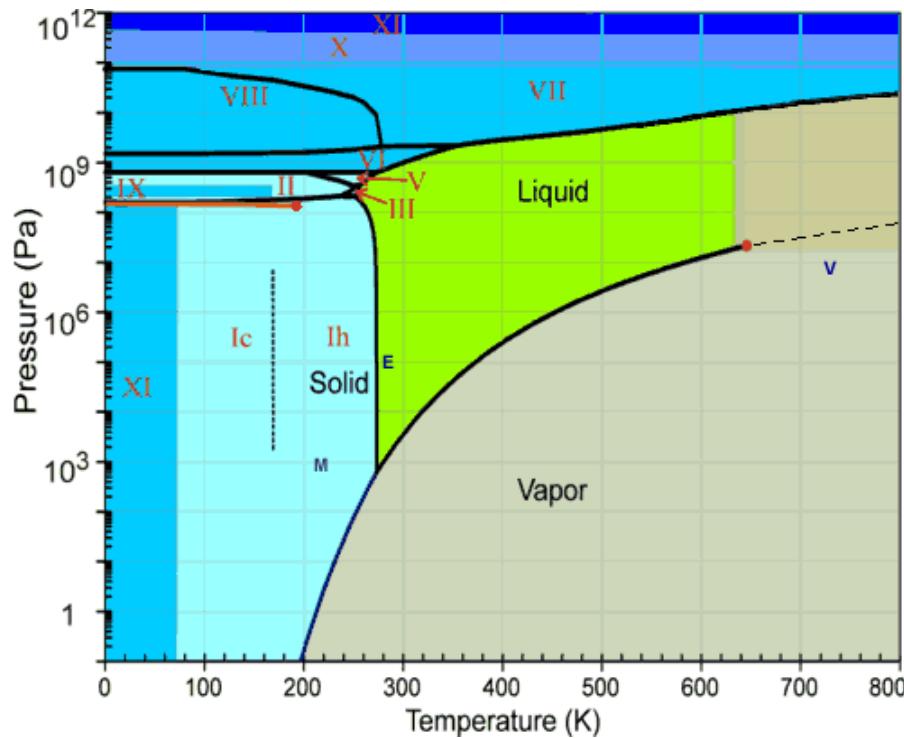
- Why all phases (can be) connected? Because  $\nexists$  order parameters:  
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...
- No phase boundary does not mean same physics:  
(compare water-vapor, gas-plasma)



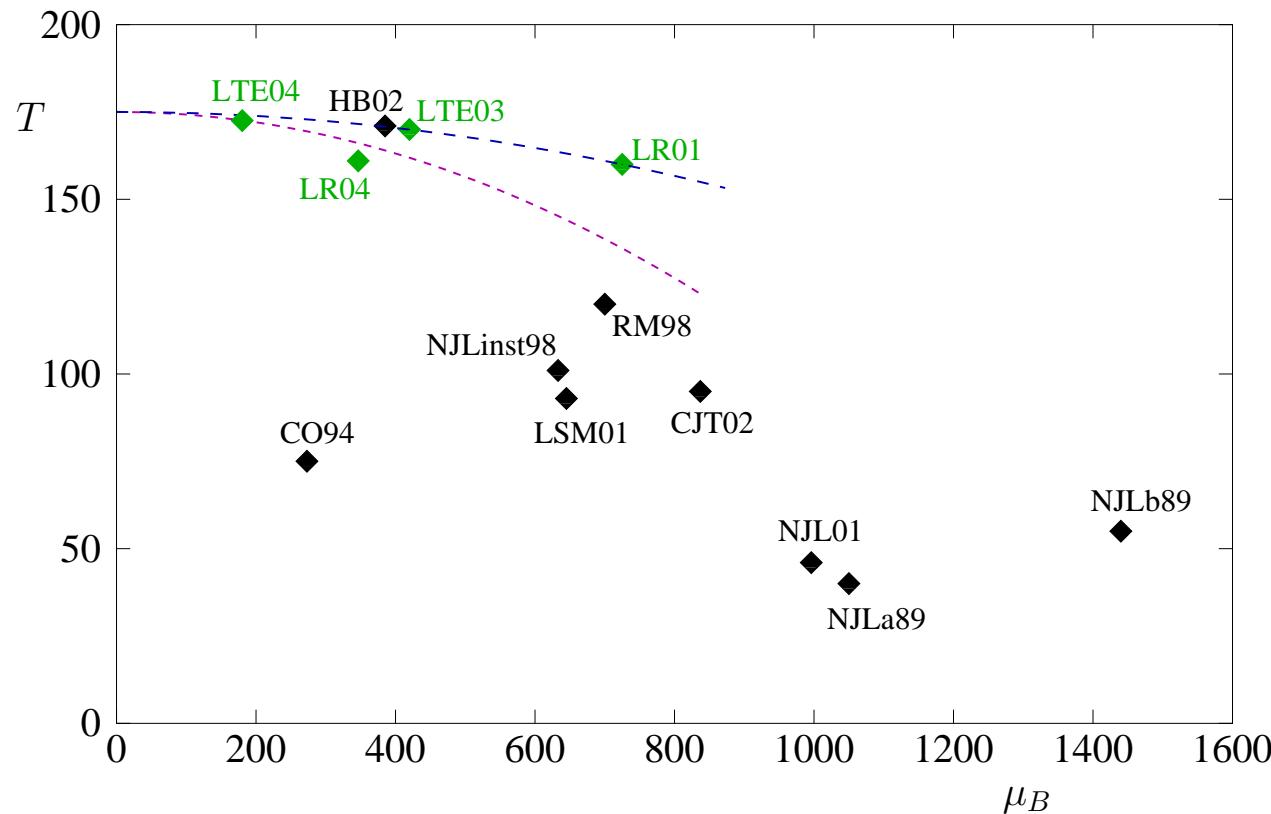
# Critical point in known liquids

Critical point  $\exists$  in many liquids (critical opalescence).

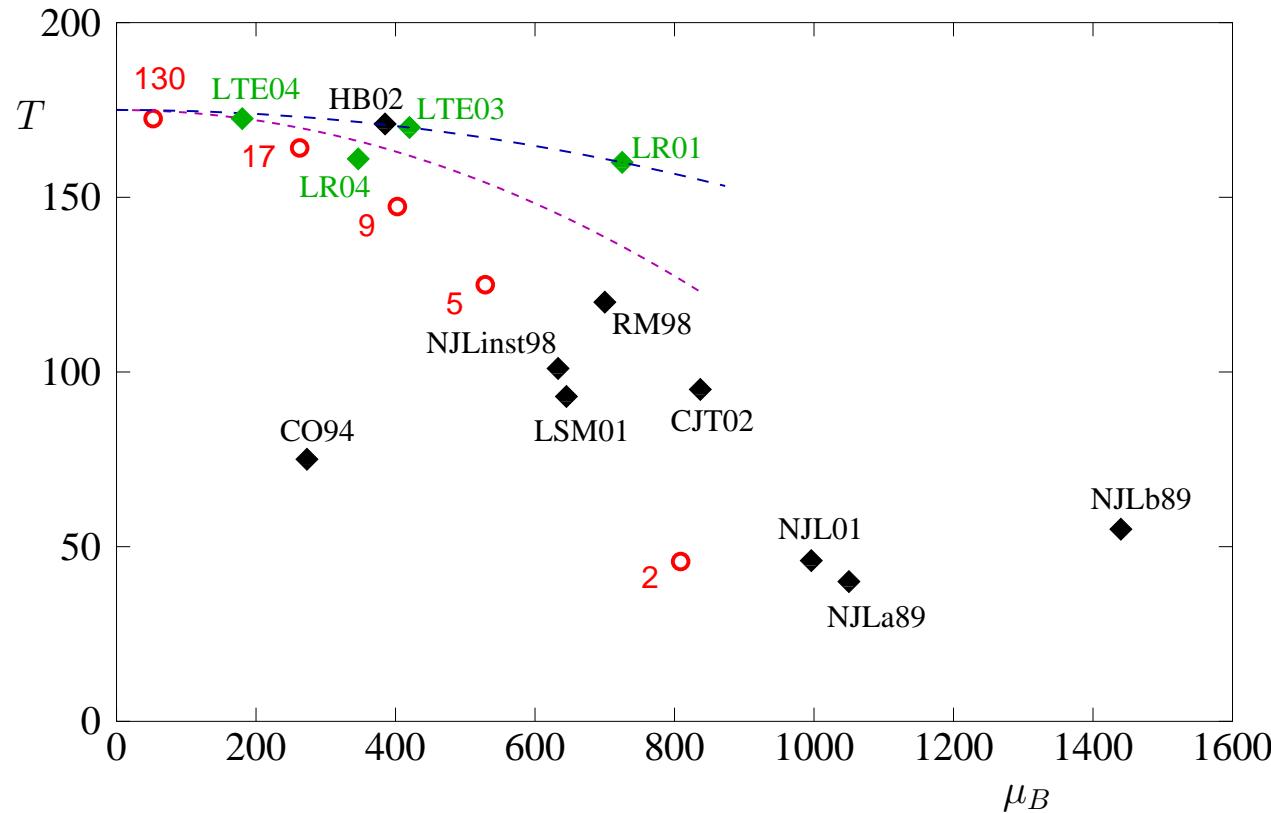
Water:



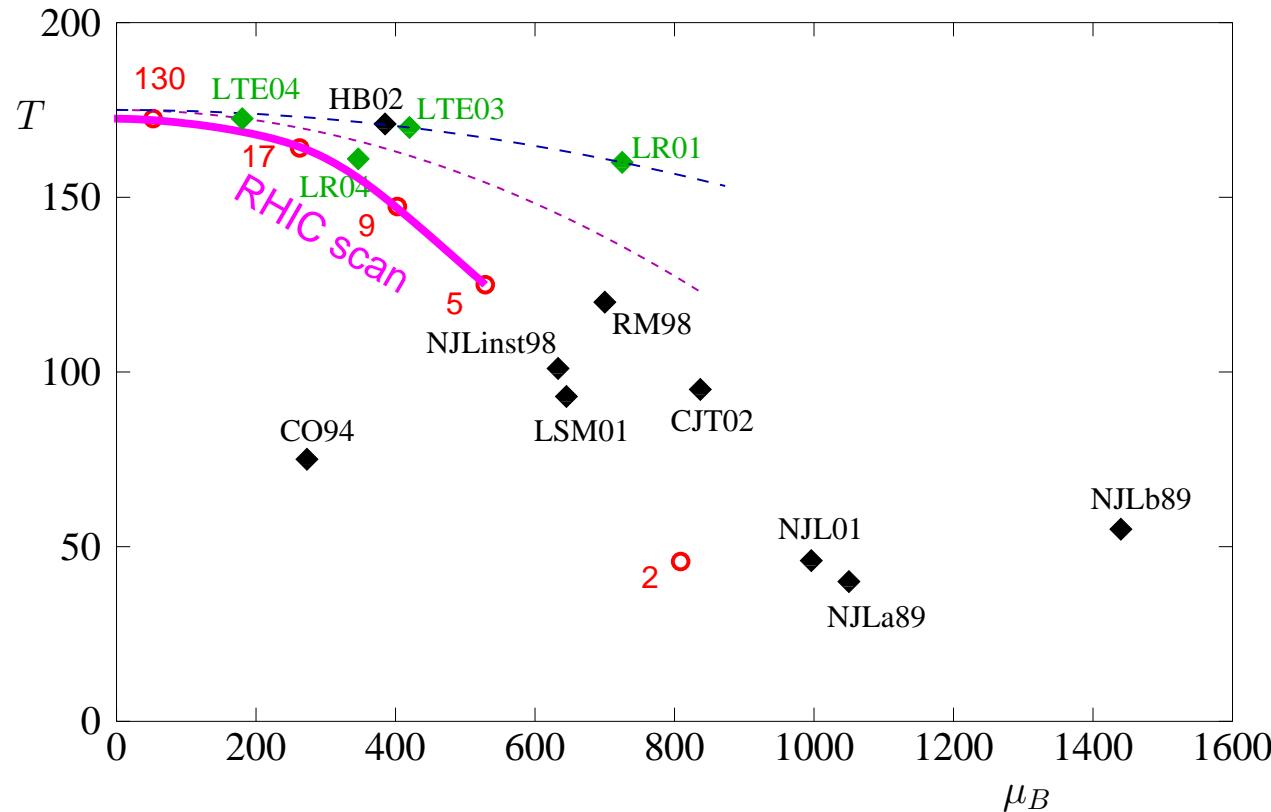
# Locating the QCD critical point



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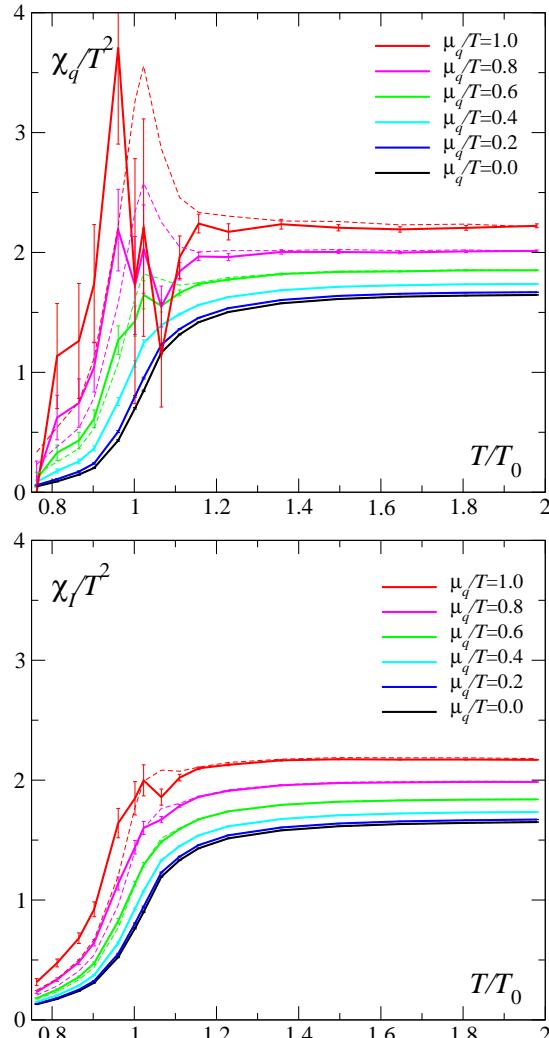


Experiments can scan the phase diagram by changing  $\sqrt{s}$ : RHIC.

Signatures: event-by-event fluctuations.

Susceptibilities diverge  $\Rightarrow$  fluctuations grow towards the critical point.

# Critical point on the lattice

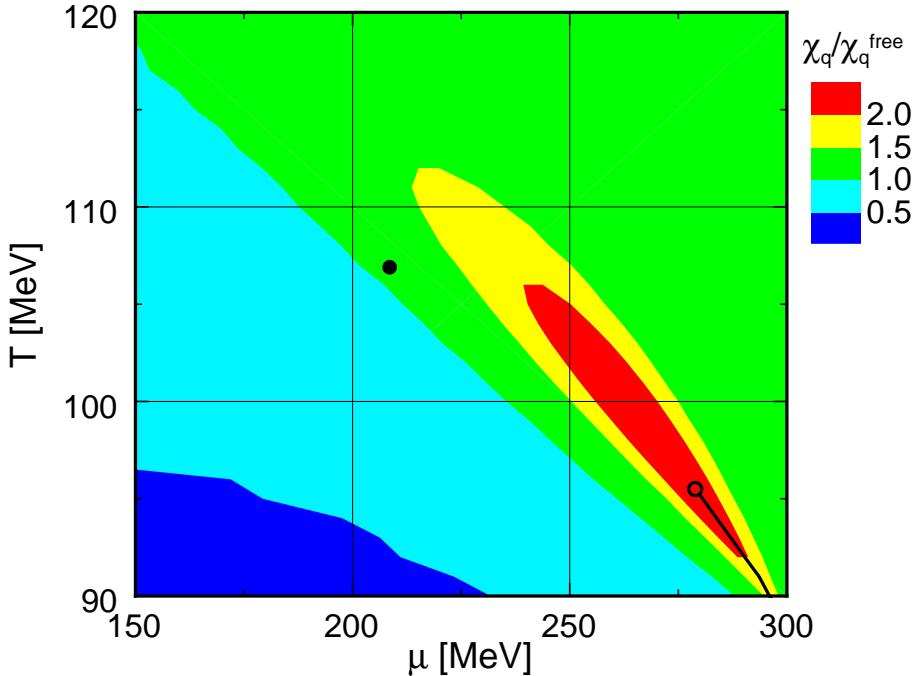


Allton, *et al.*: peak in  $\chi_B$ , but not in  $\chi_I$

Several approaches:

- Reweighting: Fodor-Katz
  - 2001:  $\mu_B \sim 725$  MeV
  - 2004:  $\mu_B \sim 360$  MeV (smaller  $m_q$  and  $V$ )
- Taylor expansion: Bielefeld-Swansea (to  $\mu^6$ )
  - 2003:  $\mu_B \sim 420$  MeV
  - 2005:  $300 \text{ MeV} \lesssim \mu_B \lesssim 500 \text{ MeV}$
- Taylor expansion: Gavai-Gupta (to  $\mu^8$ )
  - $\mu_B \sim 180$  MeV (more precisely  $> 180$  MeV)
- Imaginary  $\mu$ : Philipsen-deForcrand, Lombardo, *et al*
  - Sensitive to  $m_s$ , perhaps  $\mu_B \gg 300$  MeV
- Fixed density: deForcrand, Kratochvila
  - ? ( $N_f = 4$ , small volumes)

# Shape and size of singular region



(from Hatta, Ikeda)

Important for experimental scan:  
We only need to hit the ‘petal’.  
Maximum  $\xi$  is anyway limited by finite  
 $\tau$  to  $\xi \sim 2-3$  fm, hence  $\chi/\chi_0 \sim 4-9$ .

- Wide in  $\mu_B$ , slim in  $T$ . (Note scale:  $\mu_B : T \sim 15 : 1$ .)
- $\chi/\chi_0 > 2.5$  in the interval  $\Delta\mu_B \sim 150$  MeV;
- $\chi/\chi_0 > 4$  —  $\Delta\mu_B = ?$
- Lattice?

# Magnitude of the effect

Scaling and universality of critical phenomena:  $\chi \sim \xi^{\text{power}}$  (power  $\approx 2$ ).

How big can  $\xi$  grow?

Limited by:

- Finite size of the system  $\xi < 6 \text{ fm}$ .
- Finite time:  $\tau \sim 10 \text{ fm}$ .

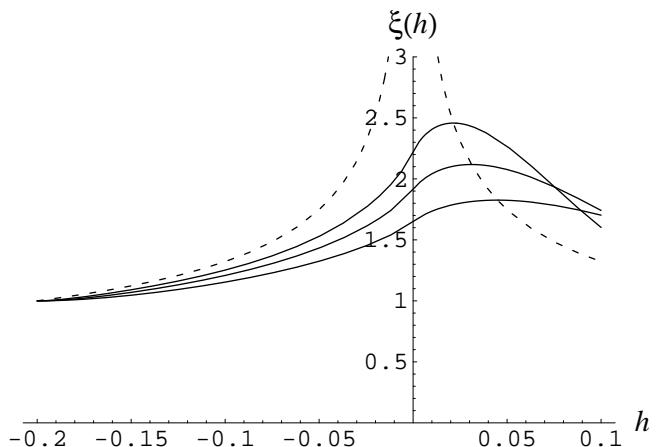
$$\xi \sim \tau^{1/z}$$

$z > 1$  – dynamical critical exponent.

Dynamic universality class of liquid-gas phase transition, i.e.,  $z \approx 3$ :

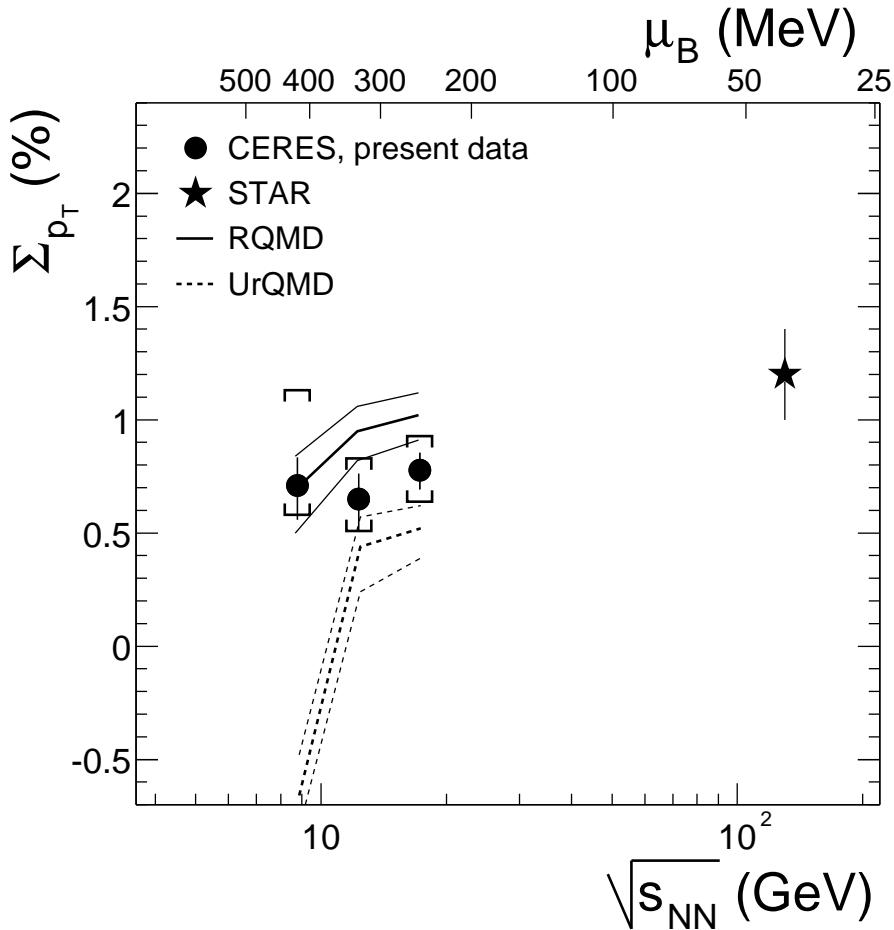
- Critical mode – diffusive:  $\omega \sim iDq^2$ ,
- $D = \frac{\lambda_B}{\chi_B} \sim \xi^{-1} \rightarrow 0$        $2 + 1 = 3$ .

(Son, MS, PRD70:056001,2004)



(Berdnikov, Rajagopal,  
PRD61:105017,2000)

# Data (example): $p_T$ fluctuations (CERES)



Near the critical point (for CERES acceptance) one expects:

$$\sim 2\% \times \left( \frac{G}{300 \text{ MeV}} \right)^2 \left( \frac{\xi_\sigma}{3 \text{ fm}} \right)^2$$

$$(\xi_\sigma = 1/m_\sigma)$$

Signal one is looking for:  
*non-monotonic* dependence on  $\sqrt{s}$ .

Also: low transverse momenta (thermal, soft)),  $p_T < 3T \sim 500 \text{ MeV}$  – where critical point correlations are (cf. CERES data –  $p_T < 1.5 \text{ GeV}$ ).

# Current status and summary notes

- Phase diagram of QCD at nonzero baryon density is under active theoretical investigation: much progress in lattice calculations.  
Still a lot to be done to narrow down the prediction for the critical point.
- Heavy ion collision experiments can discover the critical point by observing non-monotonous signatures.
- Needed:
  - Accelerator with variable  $\sqrt{s}$  to scan phase diagram
  - Detector with sufficient acceptance and p.id. at  $p_T \lesssim 500$  MeV to
    - measure fluctuations (of mean  $p_T$ , ratios, etc.);
    - measure  $\mu_B$ ,  $T$  of freezeout.
- RHIC is the ideal machine to do this