Resolving Spectra Mixtures: XANES data analysis by LCF, PCA and MCR-ALS:

11

 $=H^{3}O$

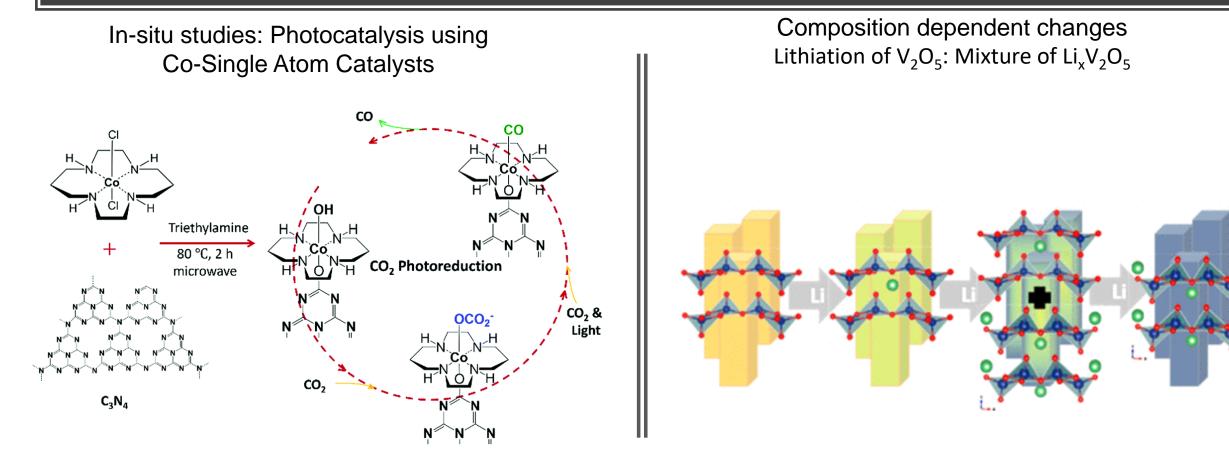
 OH^2

ns

Re

- Prahlad K. Routh, Ph.D.

Examples of Mixtures



How to deal with Spectral Mixtures?

The goal is to determine:

- Number of components in the mixture
- Concentrations of the components
- Spectra of the components: Pure Species
- Identity of Pure Species

Case-1: Mixtures of Known Samples

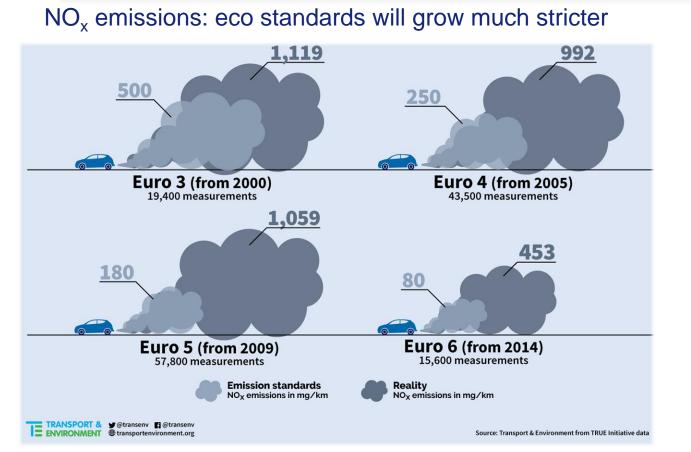
- Spectra of the components are known
- Concentration of the components are fitted

$$\boldsymbol{\mu}^{exp}(\boldsymbol{E}) = \sum_{i}^{w} \boldsymbol{w}_{i} \boldsymbol{\mu}_{i} (\boldsymbol{E})$$

Linear Combination Fitting

Case Study-: Cu-Zeolites

Cu-CHA zeolite: novel highly efficient SCR catalyst



 NH_3 -assisted Selective Catalytic Reduction (SCR) of NO_x

$4NO + 4NH_3 + O_2 \rightarrow 4N_2 + 6H_2O$

F. Giordanino, et al., *J. Phys. Chem. Lett.* 2014, 5, 1552
E. Borfecchia, et al., *Chem. Sci.* 2015, 6, 548
T.V.W. Janssens et al., *ACS Catal.*, 2015, 5, 2832
K.A. Lomachenko, et al., *J. Am. Chem. Soc.* 2016, 138, 12025
A. Martini, et al., *Chem. Sci.* 2017, 8, 6836
E. Borfecchia, et al., *Chem. Soc. Rev.* 2018, 47, 8097.
E. Borfecchia, et al., *React. Chem. Eng.* 2019, 4, 1067.
C. Negri, et al., *ChemCatChem* 2019, 11, 3828

in-situ XAS



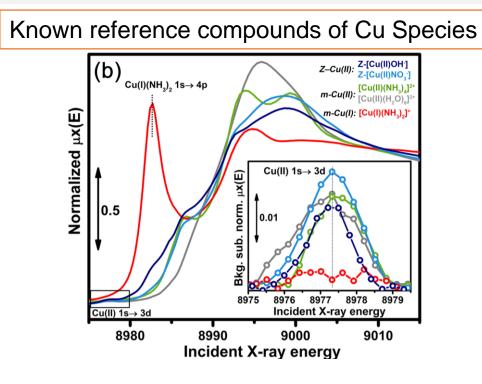


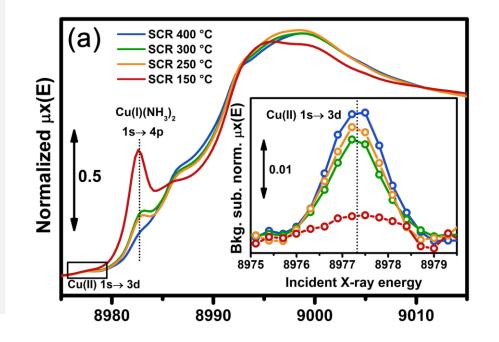
The Cu-CHA deNO_x Catalyst in Action: Temperature-Dependent NH₃-Assisted Selective Catalytic Reduction Monitored by Operando XAS and XES

Kirill A. Lomachenko,^{†,‡} Elisa Borfecchia,^{*,†} Chiara Negri,[†] Gloria Berlier,[†] Carlo Lamberti,^{†,‡} Pablo Beato,[§] Hanne Falsig,[§] and Silvia Bordiga[†]

Cu-type	Z-0	Çu(II)	m-C	m-Cu(l)	
(Dominant) Cu-species	Z-[Cu(II)OH ⁻]	Z-[Cu(II)NO₃⁻](*)	[Cu(II)(NH ₃) ₄] ²⁺	[Cu(II)(H ₂ O) ₆] ²⁺ (**)	[Cu(I)(NH₃)₂]⁺
Molecular geometry	1.8 2.05 2.02 2.82	2.65 2.02 2.44 2.03 2.82 2.03	2.00	2.37 2.02 2.02 2.02 2.02 2.02 2.02 2.02 2.0	1.92
XAS data collection conditions	50%O ₂ /He 400 °C	1000 ppm NO/10%O ₂ /He 200 °C	Solution phase Solution phase RT RT		Solution phase RT
Pertinent Cu-CHA <i>in situ</i> states	50%O ₂ /He 400 °C ca. 80% total Cu	1000 ppm NO/10%O ₂ /He 200 °C	1200 ppm NH₃/He 200 °C ca.75% total Cu	Hydrated, RT ca. 100% total Cu	1000 ppm NO/ 1200 ppm NH₃/He 200 °C ca. 100 % total Cu

Cu-K-edge operando study of Cu species

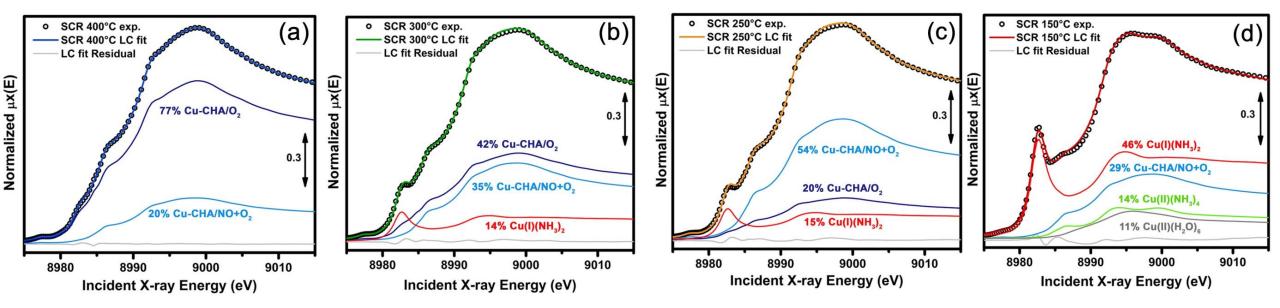




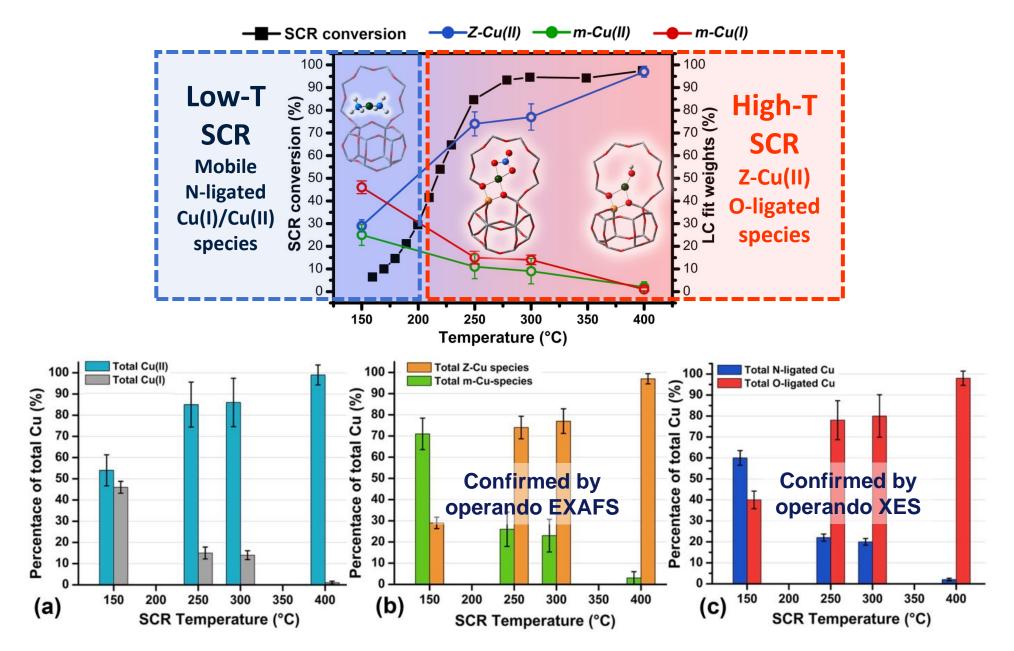
- 500 ppm NO 500 ppm NH₃
- 10% O₂
- 5% H₂O
- Si/AI: 15
- Cu/Al: 0.48

LCF Results

LCF



S	T (°C)	R-factor	Z-[Cu(II)OH ⁻]	Z-[Cu(II)NO ₃]	[Cu(II)(NH ₃) ₄] ²⁺	[Cu(II)(H ₂ O) ₆] ²⁺	[Cu(I)(NH ₃) ₂] ⁺
gh.	400	0.00001	77 ± 1	20 ± 2	1.0 ± 0.5	1 ± 1	1.0 ± 0.5
r co eigl	300	0.00005	42 ± 3	35 ± 3	6 ± 1	3 ± 1	14 ± 1
3	250	0.00006	20 ± 3	54 ± 3	7 ± 1	4 ± 1	15 ± 1
	150	0.00030	0.0 ± 0.5	29 ± 3	14 ± 3	11 ± 1	46 ± 3



LCF: Summary

Advantages:

- Works fine quite often
- No problem with the interpretation of the components
- Available in Athena

Main problem: choice of references

Often the references are not readily available at all...

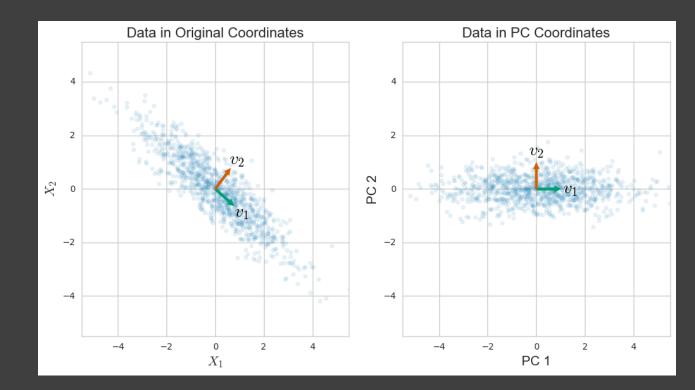
Case-2: Number of Species is not known

- Number of pure components is not known
- Spectra of most of the pure components are not readily available

Apply PCA + MCR-ALS

Principal Component Analysis (PCA): A dimensionality reduction technique

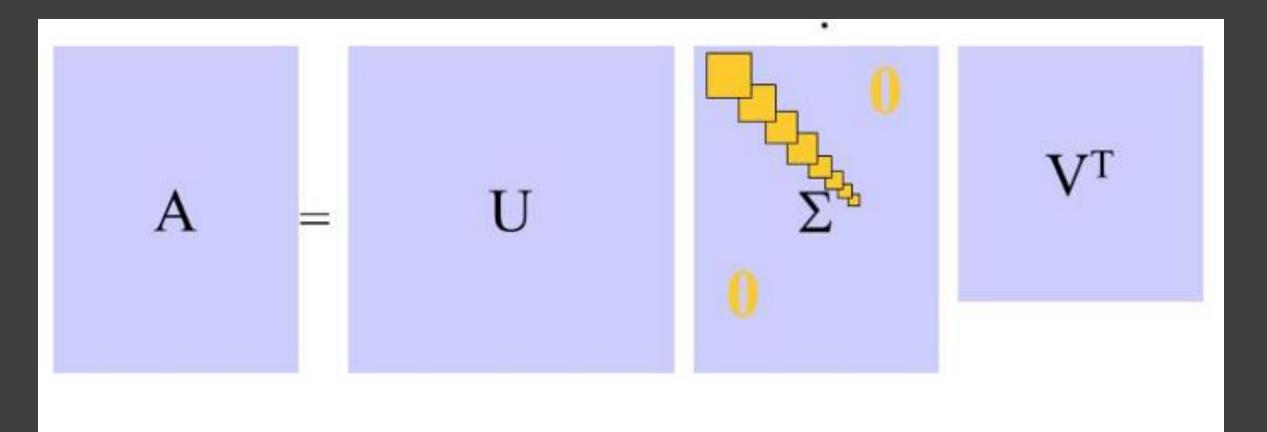
- Coined in 1901 by Pearson
- Main Attraction
 - Reduce the number of variables to a manageable number
 - Retaining most of the information
 - doesn't need any information outside of spectral data



Excellent tool for Discovery and Exploratory Analysis

Goal: to determine the minimum number of pure components in the mixture, that adequately reproduce the whole dataset

Solution: singular value decomposition (SVD) algorithm



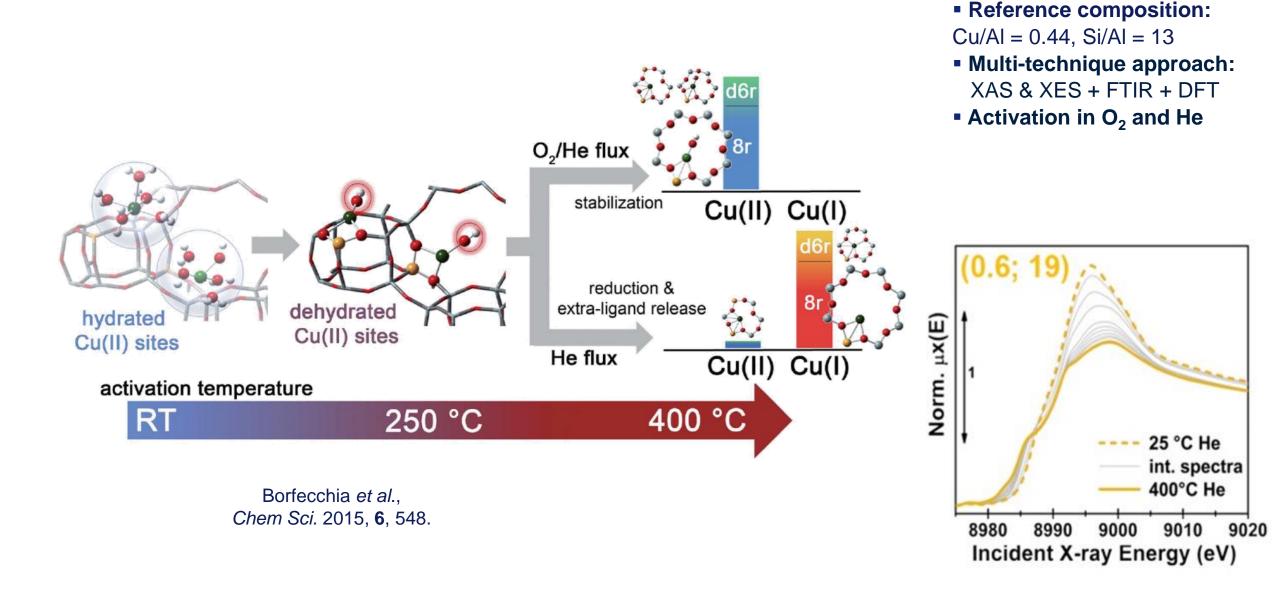
m x n

n x n

m x m

m x n

Continuing with Cu-CHA: self-reduction

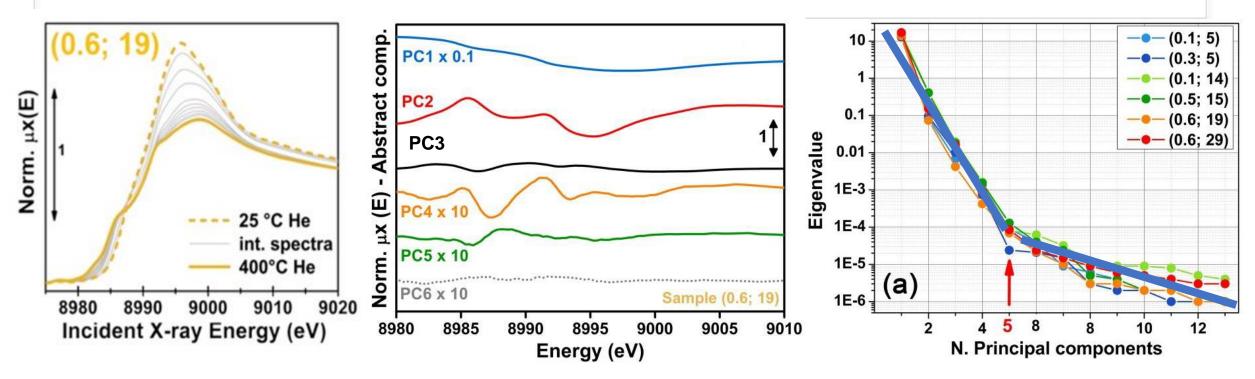


Determining the number of components

Spectra

Principal components

Scree plot



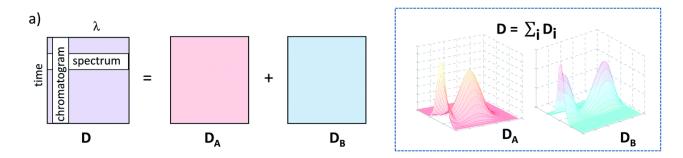
Starting from PC6, the variance described by the components is very low

 5 ± 1 components is a reasonable choice

Goal: Recovering Spectra of Pure Species $\mu^{\exp}\left(\frac{\mathrm{Cu}}{\mathrm{A1}};\frac{\mathrm{Si}}{\mathrm{A1}},T,E\right) = \sum_{i=1}^{N_{\mathrm{pure}}} w_i^{\mathrm{pure}}\left(\frac{\mathrm{Cu}}{\mathrm{A1}};\frac{\mathrm{Si}}{\mathrm{A1}},T\right) \times \mu_i^{\mathrm{pure}}\left(E\right)$ **UNKNOWN**

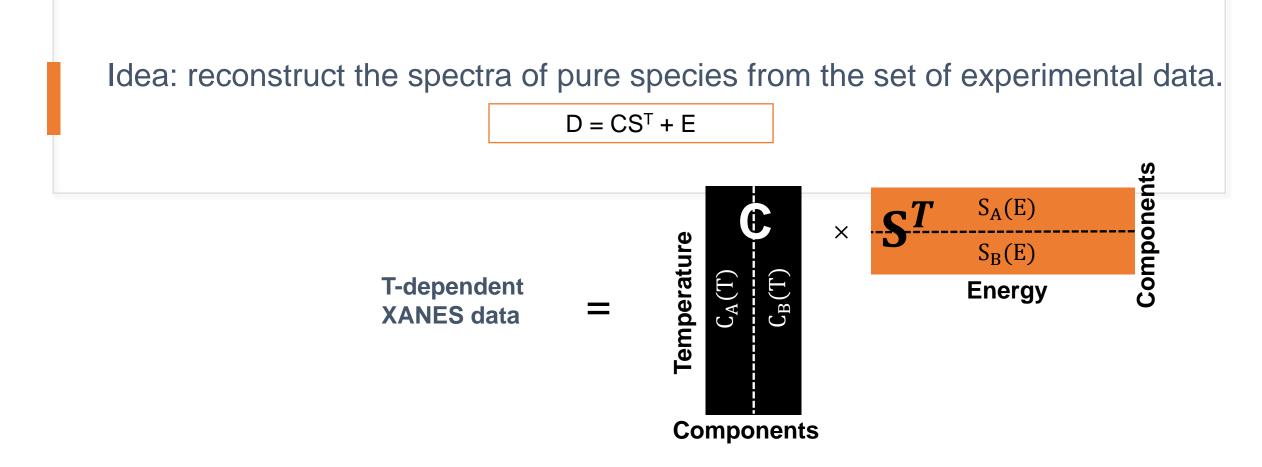
Goal: Recovering Spectra of Pure Species

Solution: Multivariate Curve Resolution-Alternate Least Square



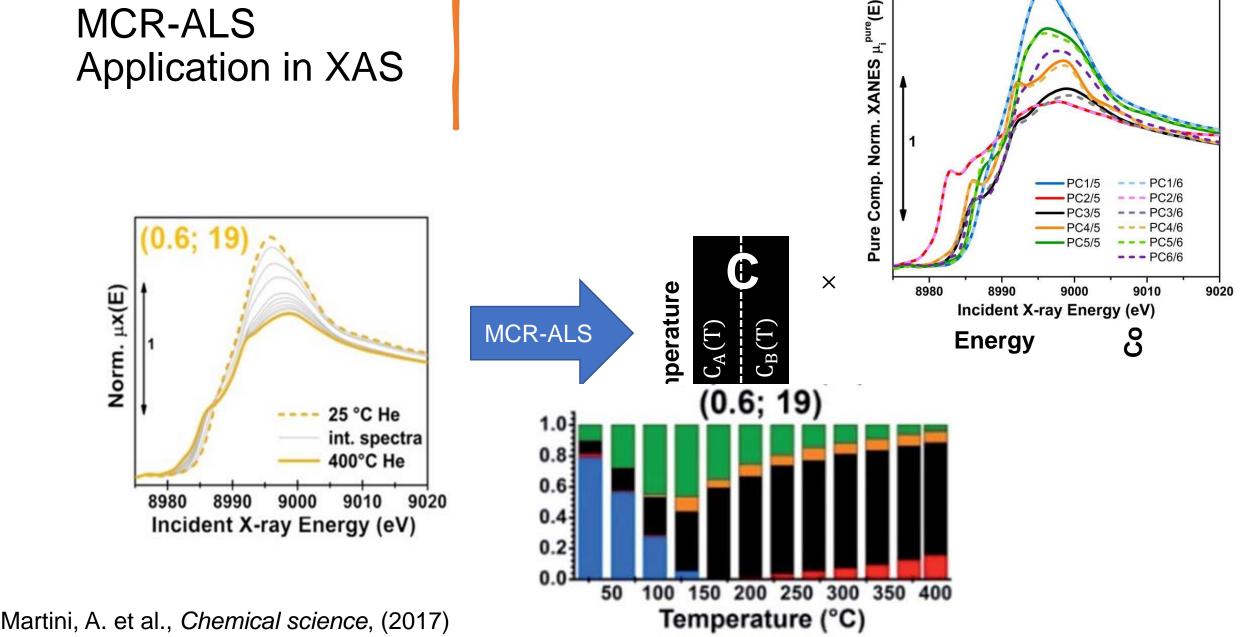
Multivariate Curve Resolution (MCR). Solving the mixture analysis problem

de Juan et al, Anal. Methods, 2014, 6, 4964-4976 J. Jaumot et al, Chemometrics Intell. Lab. Syst., 2005, 76, 101-110

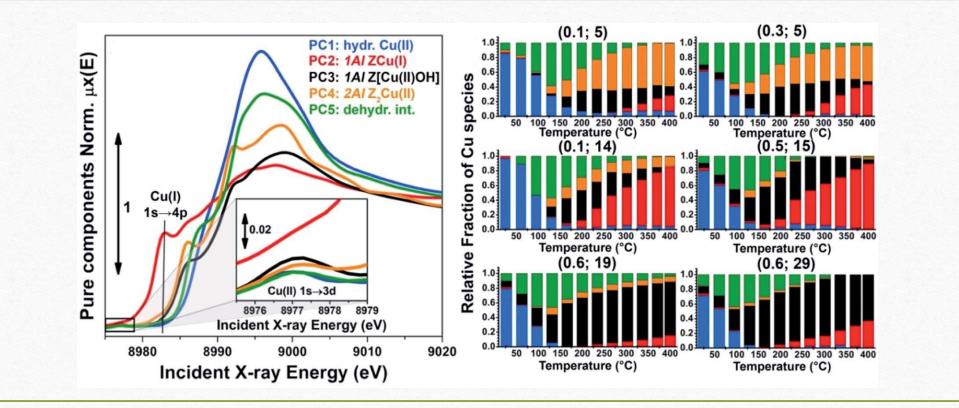


- Number of pure components is determined independently by PCA
- Spectra and concentrations of pure components are deduced iteratively using constraints for C and S matrices

MCR-ALS Application in XAS



MCR ALS analysis of XANES allows to monitor the evolution of Cu speciation



MCR-ALS: Additional Constraints

- Concentration Non-Negativity
- Spectra Non-Negativity
- Closure to 1 for Concentrations



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pyMCR: A Python Library for Multivariate Curve Resolution Analysis with Alternating Regression (MCR-AR)

https://github.com/usnistgov/pyMCR

https://mcrals.wordpress.com/

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MCR-ALS

Advantages:

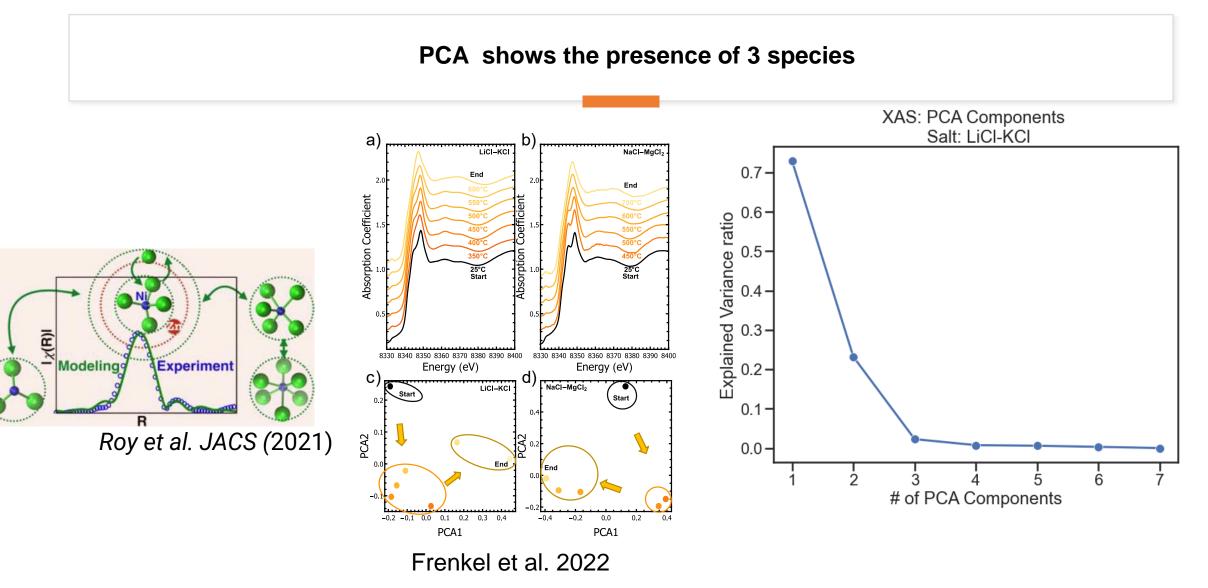
- No need for reference spectra
- Less "subjective" than LCA

Difficulties:

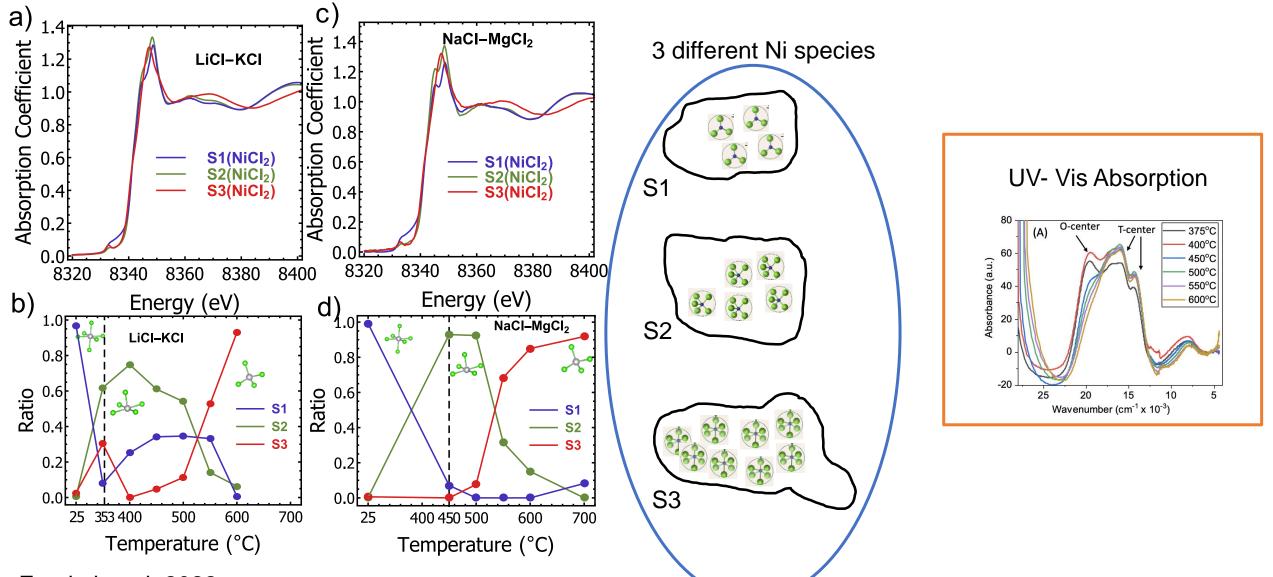
- Results might depend on initial guess
- Interpretation of "pure spectra" can be challenging
- Very sensitive to data quality and alignment of the spectra

Case Study-2: Molten Salt

Dimensionality reduction and Scree Plot



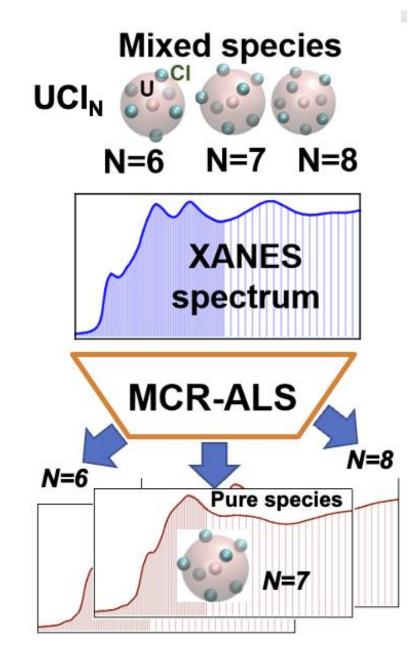
Mixture of Ni-complexes



Frenkel et al. 2022

- If the standards are known:
 - Use LCF to obtain fractions
- If the standards and number of species is NOT known
 - Use PCA to learn the number of species.
 - MCR-ALS for extraction of pure species.

Summary



After the break: XANES modeling using FEFF by F. Vila



Thank you for your attention!