

# Correlations of Quark-antiquarks in pA collisions

**Mauricio Martinez Guerrero**

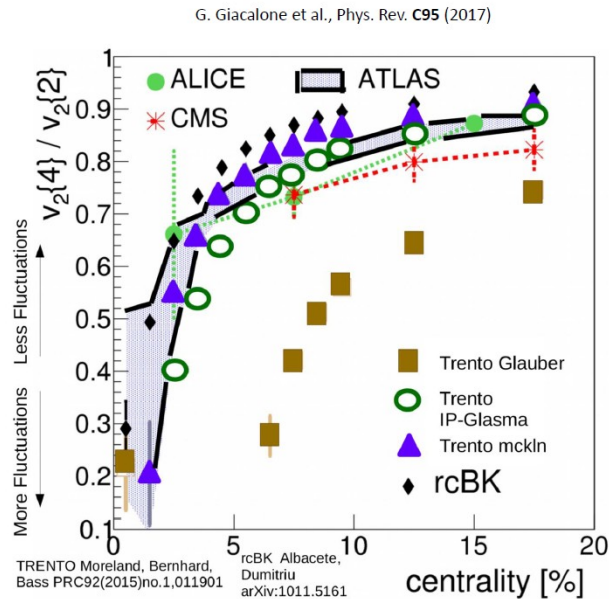
***2019 RHIC/AGS Annual User's Meeting***

**June 4-7, 2019**

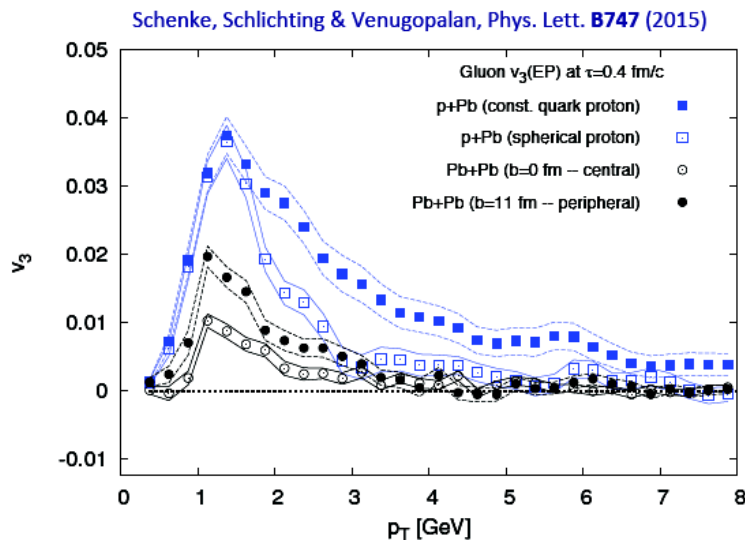
**BNL, Upton, NY, USA**

Collaborators: M. Sievert, D. Wertepny, J. Noronha-Hostler  
JHEP 1807 (2018) 03, JHEP 1902 (2018) 024, Forthcoming

# Role of sub-nucleonic fluctuations



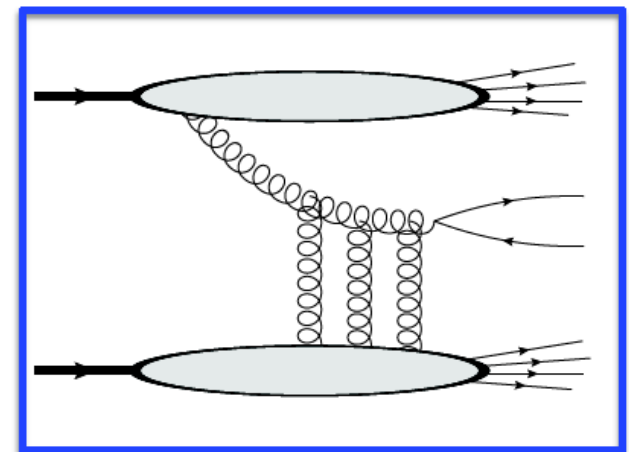
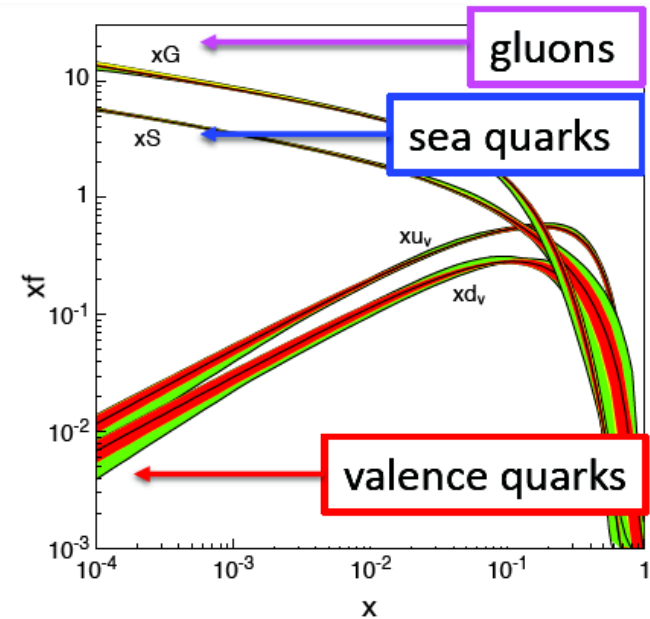
- Fluctuations in the initial state of heavy ion collisions contribute to measured anisotropic flow



- For especially sensitive observables, **sub-nucleonic fluctuations** significantly enhance the total flow and are necessary to describe heavy ion collisions.

# Including quarks in the initial state

- In high-energy collisions, the nuclei are dominated by **soft gluon radiation**
  - Contribute to sub-nucleonic fluctuations of the **energy density**
- **Other quantum numbers** like flavor and baryon number are carried only by **quarks**
  - The **net** production of these conserved charges is **nearly zero**
  - But there is a characteristic pattern of **fluctuations** due to **pair production**



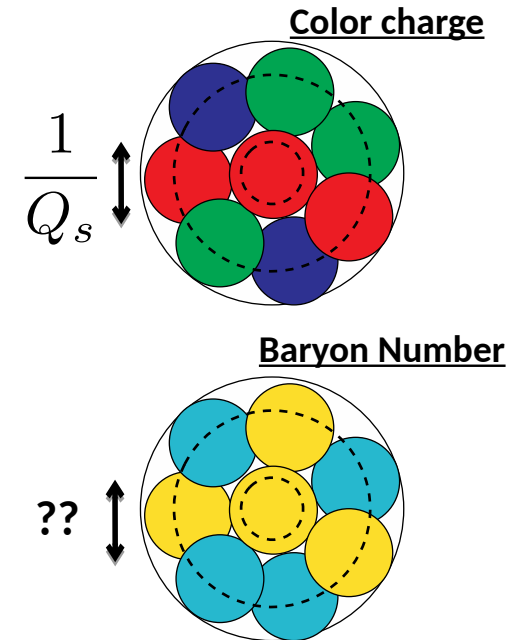
# Observable

- **Goal:** Calculate (anti)quark correlations in heavy-light ion collisions
  - Coordinate space profile for hydro
  - What is the typical size of a baryon number domain?

$$C^{q\bar{q}}(B_{1\perp}, Y_1; B_{2\perp}, Y_2) = \left\langle \frac{dn^q}{d^2B_1 dY_1} \frac{dn^{\bar{q}}}{d^2B_2 dY_2} \right\rangle - \left\langle \frac{dn^q}{d^2B_1 dY_1} \right\rangle \left\langle \frac{dn^{\bar{q}}}{d^2B_2 dY_2} \right\rangle$$

$$\left\langle \frac{dn^q}{d^2B_1 dY_1} \frac{dn^{\bar{q}}}{d^2B_2 dY_2} \right\rangle = \frac{1}{\sigma_{inel}} \frac{d\sigma^{q\bar{q}}}{d^2B_1 dY_1 d^2B_2 dY_2}$$

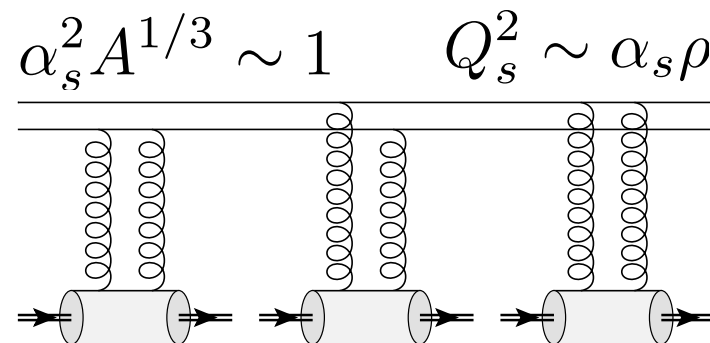
$$\left\langle \frac{dn^q}{d^2B_1 dY_1} \right\rangle = 0$$



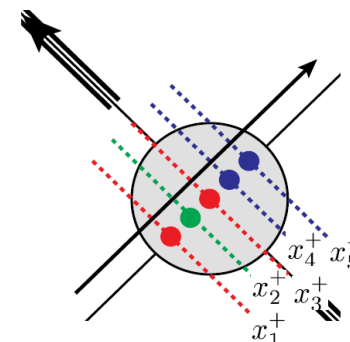
- Various mechanisms dominate at various length scales
  - Work to LO in each regime
  - Avoid complicated rescattering corrections

# Theoretical setup

- Dilute-Dense (pA) **resummation of QCD**
  - Dense target: classical gluon fields
  - High density sets hard momentum scale



- Light-cone “time”-ordered dynamics
  - Wave functions in light-front perturbation theory ( $A^+=0$  gauge)
  - Eikonal scattering via Wilson lines



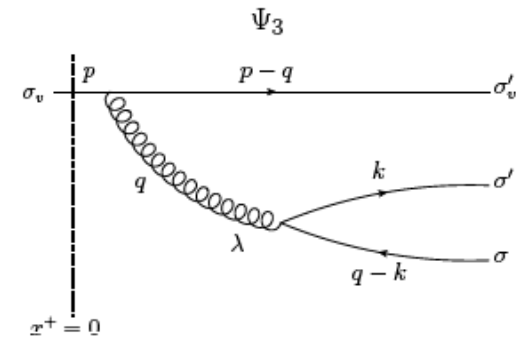
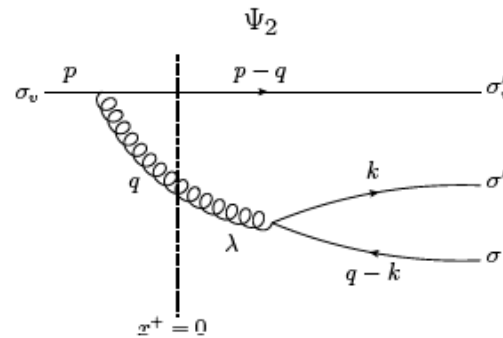
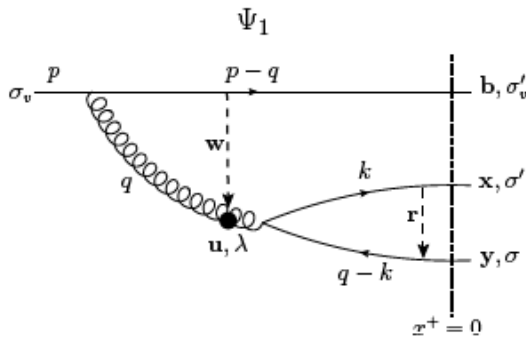
D. Wertepny, Ph. D. Thesis (2016) arXiv: 1608.08618

- “**Heavy-light**” (aA) paradigm incorporates projectile density **order by order in perturbation theory**
  - E.g.)  ${}^3\text{He}+\text{Au}$  or  $\text{Cu}+\text{Au}$
  - Moves toward the dense-dense limit

$$\alpha_s^2 A^{1/3} \sim 1$$

$$\alpha_s \ll \alpha_s^2 a^{1/3} \ll 1$$

# Ingredients I: wave functions



$$\Psi_1 + \Psi_2 + \Psi_3 = 0$$

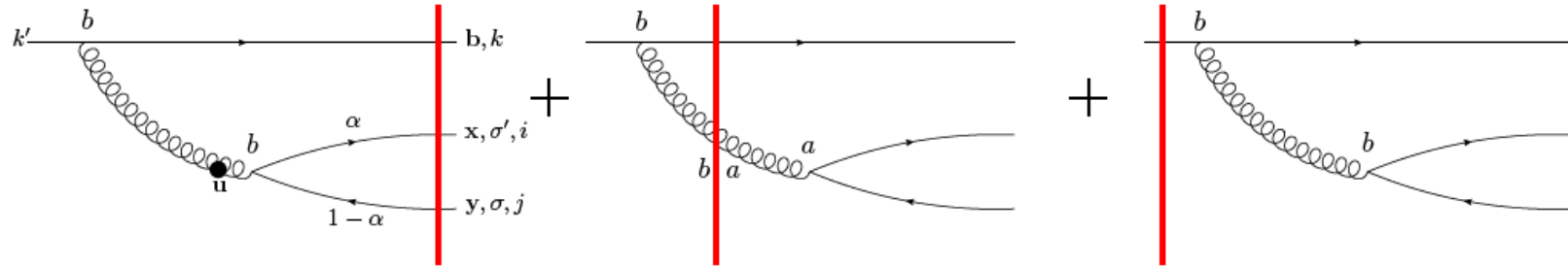
Blaizot, Gelis, & Venugopalan, Nucl. Phys. **A743** (2004)

Kovchegov & Tuchin, Phys. Rev. **D74** (2006)

- **“Time”-ordered wave functions** in coordinate space:

$$\text{E.g.) } \Psi_2(w_\perp, r_\perp, \alpha) = -\frac{2\alpha_s}{\pi} \sqrt{\alpha(1-\alpha)} \left\{ \delta_{\sigma, -\sigma'} \frac{m}{w_T} K_1(mr_T) \left[ (1-2\alpha) \frac{\vec{w}_\perp \cdot \vec{r}_\perp}{w_T r_T} - i\sigma' \frac{\vec{w}_\perp \times \vec{r}_\perp}{w_T r_T} \right] + i\sigma' \delta_{\sigma\sigma'} \frac{m}{w_T} K_0(mr_T) \left[ \frac{w_\perp^1}{w_T} - i\sigma' \frac{w_\perp^2}{w_T} \right] \right\}$$

# Ingredients II: amplitude



- The high-energy scattering **dresses** the WFs with **Wilson lines**:

$$V_x \equiv \mathcal{P} \exp \left[ ig \int dx^+ A^-(x^+, 0^-, \mathbf{x}) \right]$$

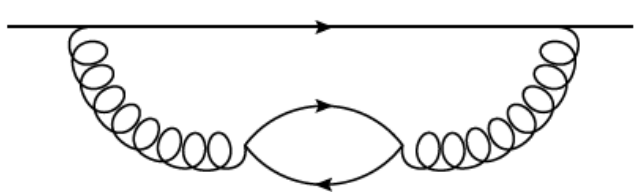
- Building block:** color and spin matrix at the amplitude level

$$(\tilde{\mathcal{A}}_{NA})_{(ij)(kk')(\sigma\sigma')}(\mathbf{x}, \mathbf{y}, \mathbf{b}, \mathbf{u}, \alpha) \equiv (V_b t^b)_{kk'} \left[ [W_1^b(\mathbf{x}, \mathbf{y}, \mathbf{b})]_{ij} [\tilde{\Psi}_1(\mathbf{u} - \mathbf{b}, \mathbf{x} - \mathbf{y}, \alpha)]_{\sigma', -\sigma} + [W_2^b(\mathbf{u}, \mathbf{b})]_{ij} [\tilde{\Psi}_2(\mathbf{u} - \mathbf{b}, \mathbf{x} - \mathbf{y}, \alpha)]_{\sigma', -\sigma} \right],$$

$$W_1^b(\mathbf{x}, \mathbf{y}, \mathbf{b}) \equiv V_x t^b V_y^\dagger - V_b t^b V_b^\dagger$$

$$W_2^b(\mathbf{u}, \mathbf{b}) \equiv V_u t^b V_u^\dagger - V_b t^b V_b^\dagger$$

# Single pair quark correlations



The diagram shows a horizontal line representing a quark. Below it, a gluon loop is formed by two wavy lines. A ghost loop is represented by two straight lines forming a loop between the two vertices of the gluon loop.

$$\langle |\tilde{\mathcal{A}}_{NA}|^2 \rangle = \frac{1}{2N_c} \sum_{i,j=1}^2 \left( \mathcal{U}_i \mathcal{U}_j - \mathcal{L}_i \mathcal{L}_j + \mathcal{T}_i \cdot \mathcal{T}_j \right) \underbrace{\langle \text{tr}_C [W_i^b W_j^{b\dagger}] \rangle}_{\Omega_{ij}}$$

- The **single-pair result** is simple and familiar:

E.g.) 
$$\Omega_{11} = 2N_c C_F - \frac{1}{2} N_c^2 \langle \hat{D}_2(\mathbf{B}_1, \mathbf{b}_1) \hat{D}_2(\mathbf{b}_1, \mathbf{B}_2) \rangle - \frac{1}{2} N_c^2 \langle \hat{D}_2(\mathbf{B}_2, \mathbf{b}_1) \hat{D}_2(\mathbf{b}_1, \mathbf{B}_1) \rangle + \frac{1}{2} \langle \hat{D}_2(\mathbf{B}_1, \mathbf{B}_2) \rangle + \frac{1}{2} \langle \hat{D}_2(\mathbf{B}_2, \mathbf{B}_1) \rangle$$

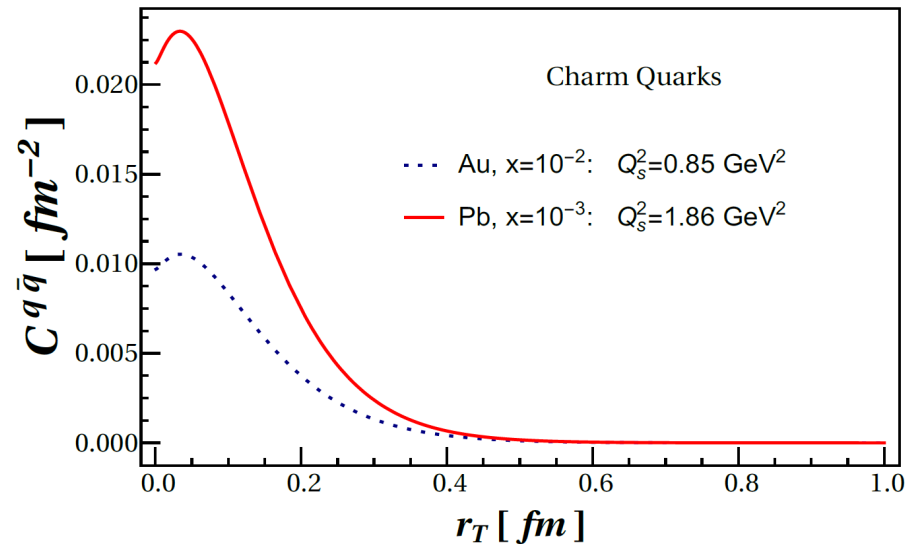
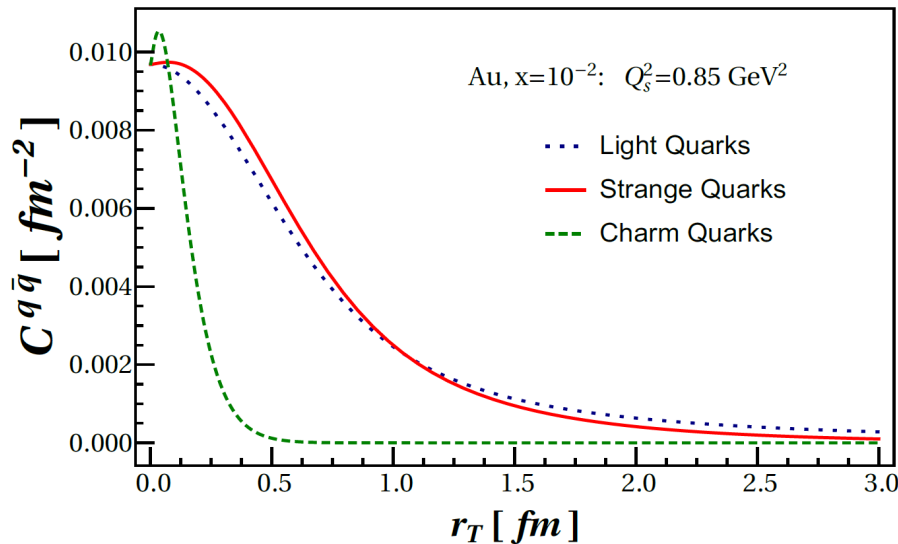
- Dipole** degrees of freedom: 
$$\hat{D}_2(\mathbf{x}, \mathbf{y}) \equiv \frac{1}{N_c} \text{tr}_C [V_{\mathbf{x}} V_{\mathbf{y}}^\dagger]$$

- Normalize by the inelastic cross-section (**1-gluon production**)

$$\sigma_{inel} = \frac{\alpha_s N_c}{\pi^2} (a \Delta Y) \int \frac{d^2 x_1 d^2 x_2}{(x_{21})_T^2} \left\langle 1 - \left| \hat{D}_2(\mathbf{x}_1, \mathbf{x}_2) \right|^2 \right\rangle$$

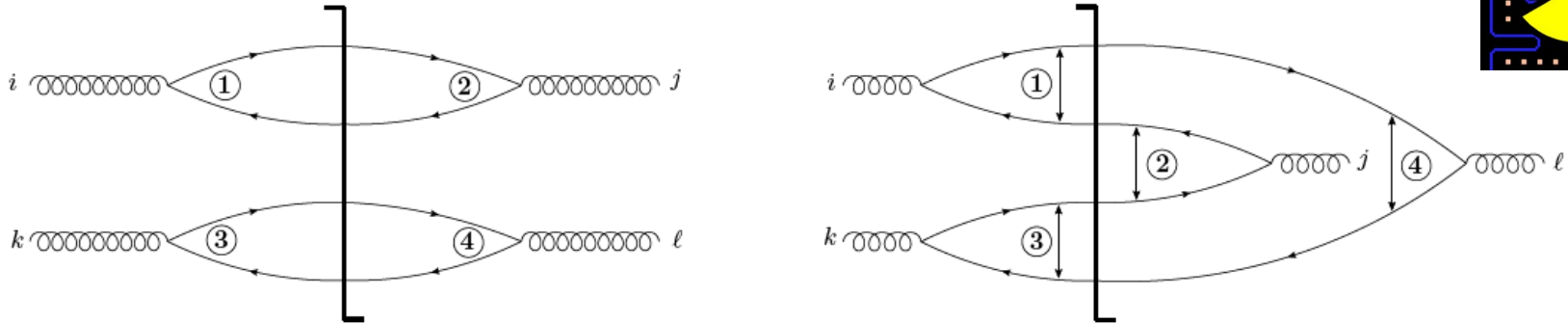
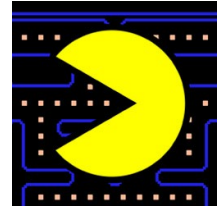


# Correlation function



- The **range of the correlation** is controlled by the **quark mass**, not the saturation scale
- But the **strength of the correlation** is controlled by  $Q_s$ 
  - Interaction mediated correlations: a **genuine pA / aA effect**
  - Arises from the **interference of gluon / pair scattering**

# Double pair production: Direct emissions vs. pacman diagrams

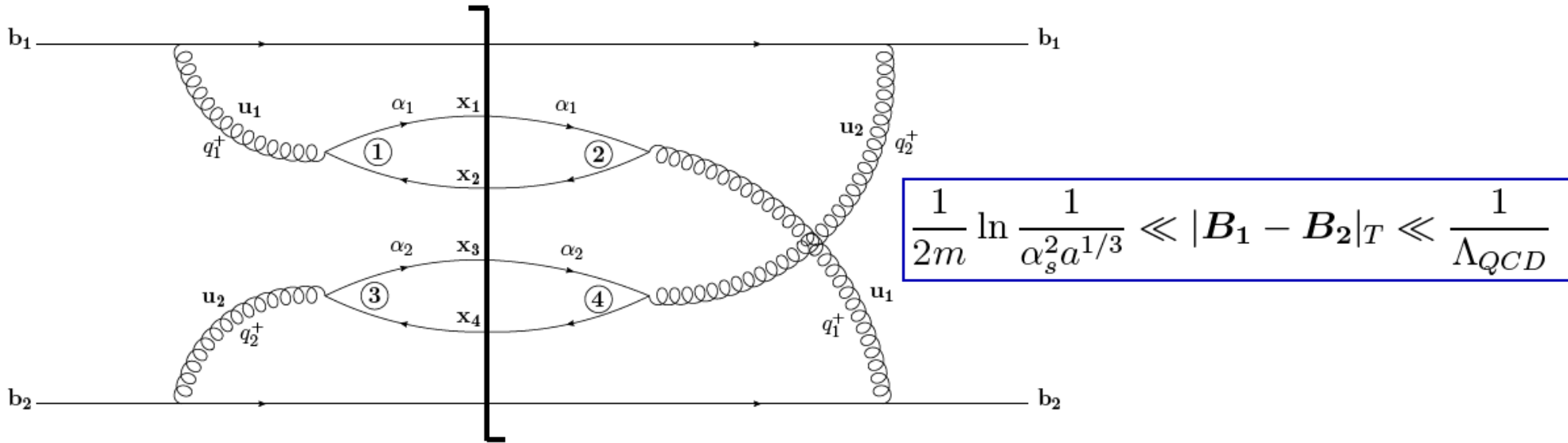


$$K_1^+ K_2^+ \frac{d\sigma_{double}}{d^2 B_1 dK_1^+ d^2 B_2 dK_2^+} = \int d^2 B d^2 b_1 d^2 b_2 T_a(\mathbf{b}_1 - \mathbf{B}) T_a(\mathbf{b}_2 - \mathbf{B}) \int \left( \prod_{i=1}^4 d^2 x_i \frac{dk_i^+}{4\pi k_i^+} \right) \times |\tilde{\mathcal{A}}_{NNA}(\mathbf{b}_1, \mathbf{b}_2; \{\mathbf{x}_i, k_i^+\}_{i=1}^4)|^2 \underbrace{Z(\mathbf{B}_1, K_1^+, \mathbf{B}_2, K_2^+, \{\mathbf{x}_i, k_i^+\}_{i=1}^4)}_{\text{Tagging delta functions}}.$$

Altinoluk et. al., (2017)  
MSW (2018)

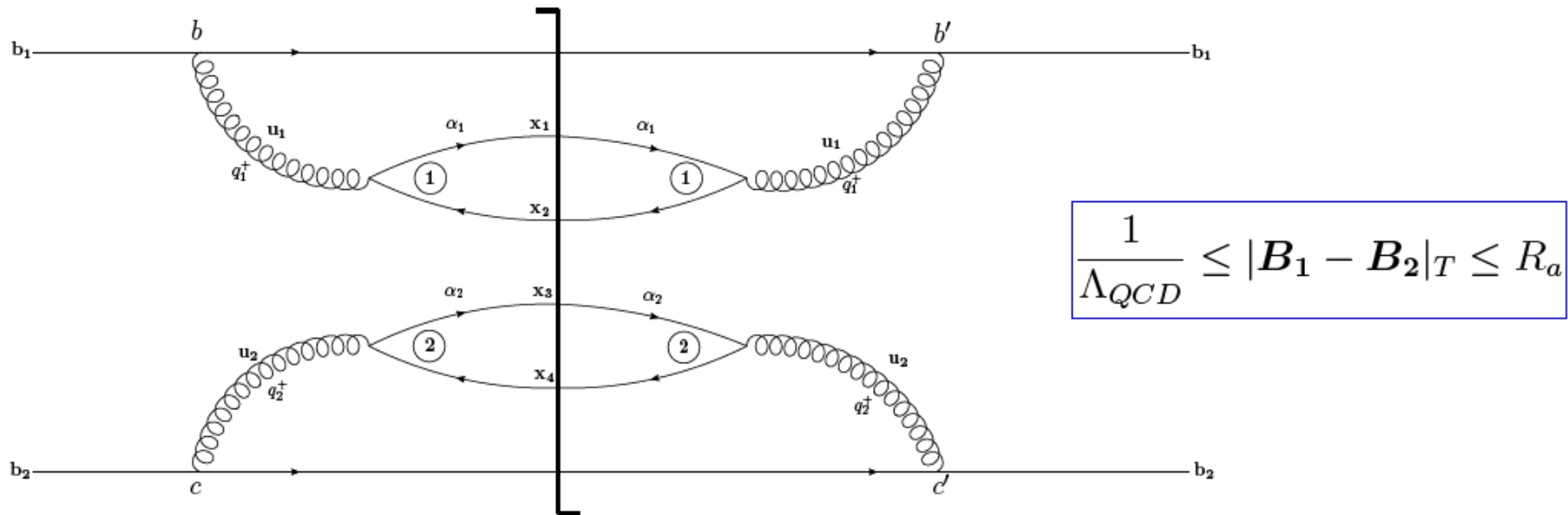
- In heavy-light power counting, **double-pair production is suppressed vs single-pair**, but it becomes important for **quark/quark correlations** and at **distances larger than  $1/m$** 
  - Opens up several **new channels** for correlations

# Double pair production: intermediate regime



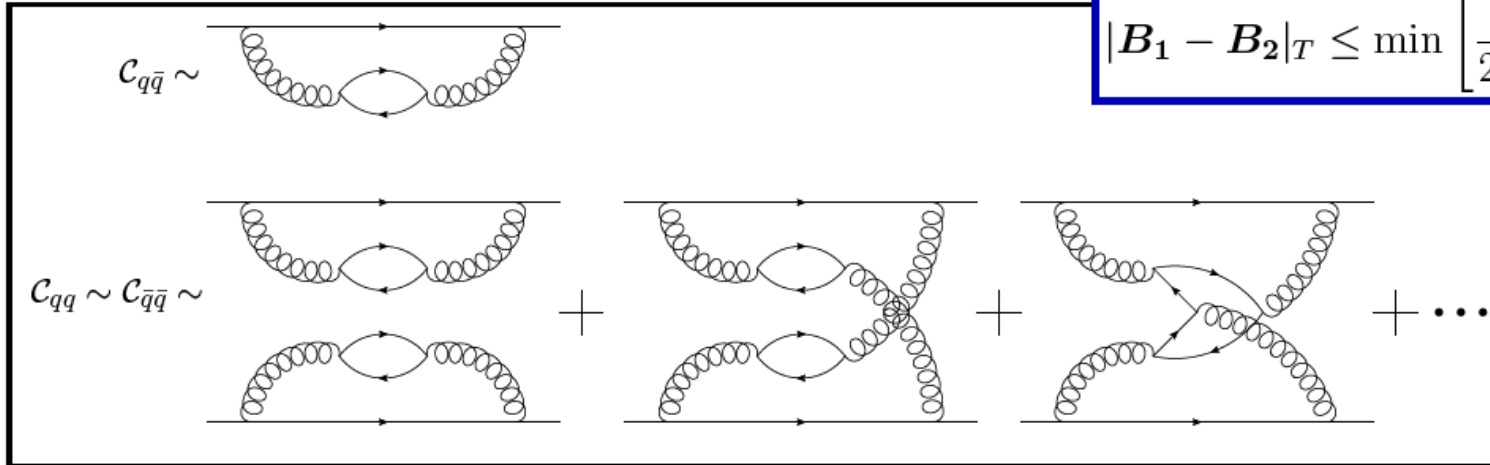
- For **heavy quarks**, there is an intermediate region which is dominated by **separated double-pair production**, but is still **perturbative**.
- Correlations arise from **perturbative mechanisms**:
  - Gluon entanglement
  - Scattering in correlated color fields

# Double pair production: geometrical

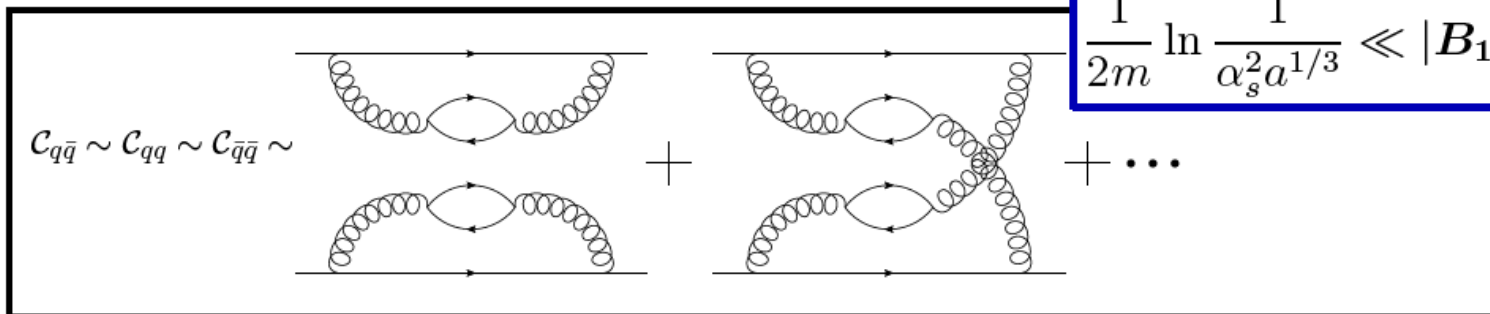


- Over **nonperturbative distances**, the two pairs are not connected by any perturbative degrees of freedom
  - Scatter in **uncorrelated color fields** from disjoint nucleons
  - Cross-section **factorizes**, but **geometrical correlations** remain

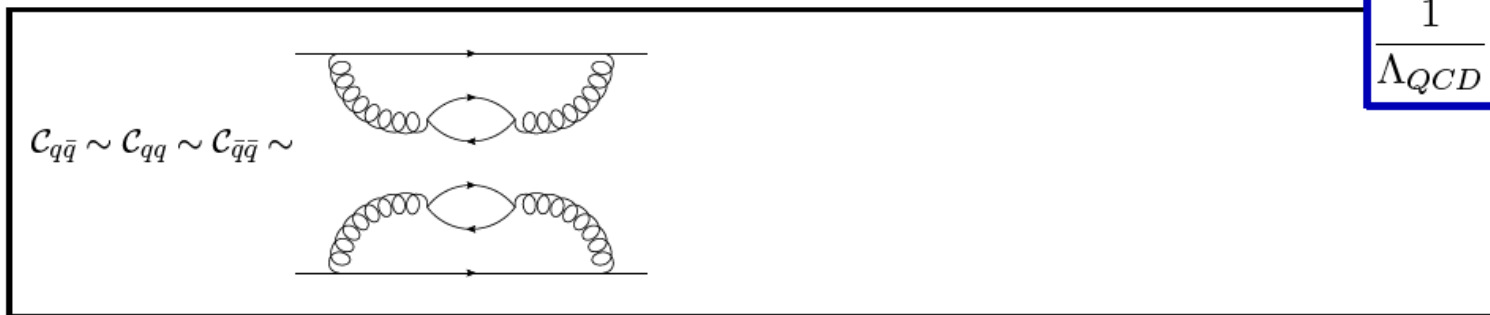
# Summary I



$$|B_1 - B_2|_T \leq \min \left[ \frac{1}{2m} \ln \frac{1}{\alpha_s^2 a^{1/3}}, \frac{1}{\Lambda_{QCD}} \right]$$

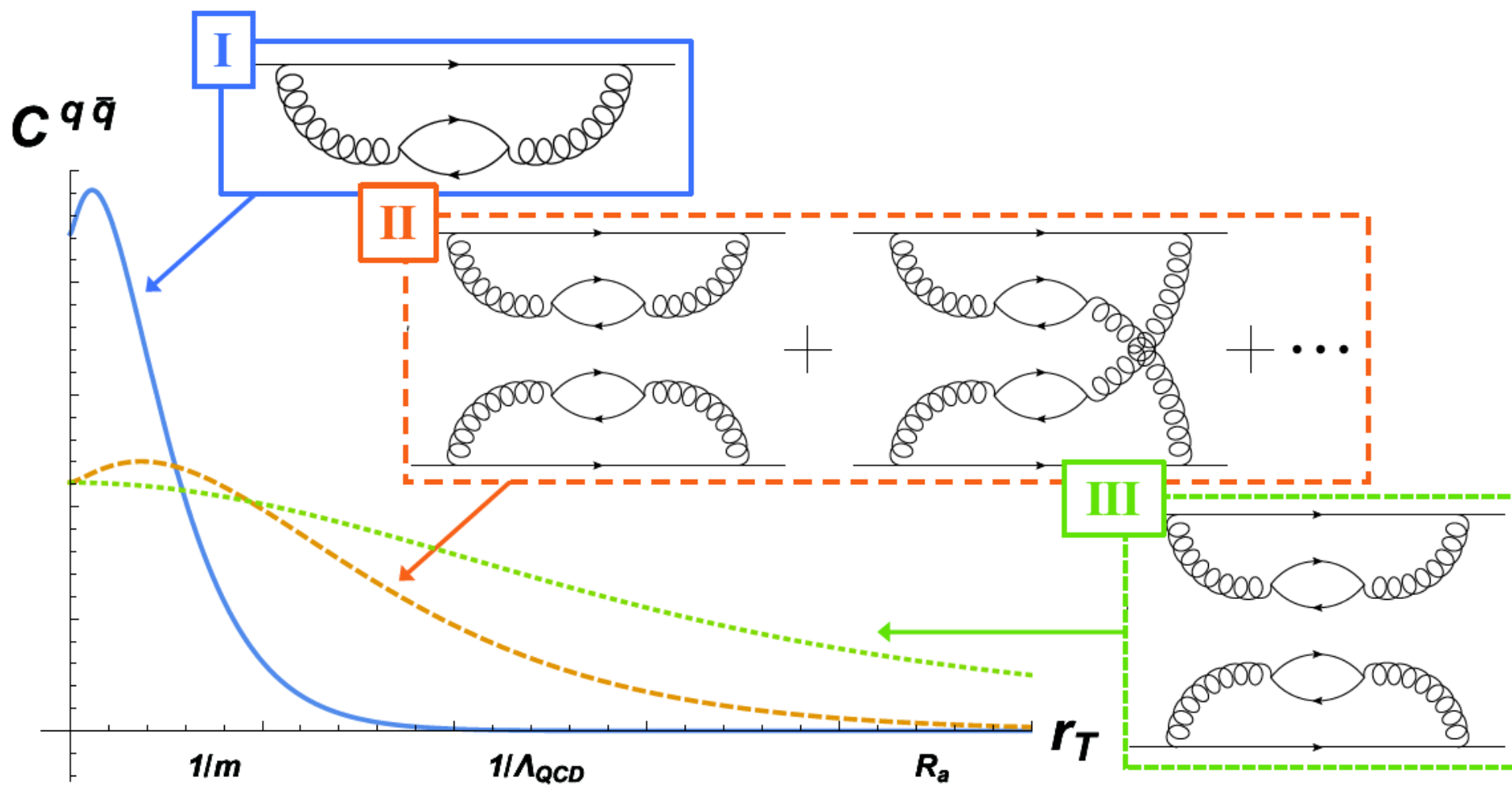


$$\frac{1}{2m} \ln \frac{1}{\alpha_s^2 a^{1/3}} \ll |B_1 - B_2|_T \ll \frac{1}{\Lambda_{QCD}}$$

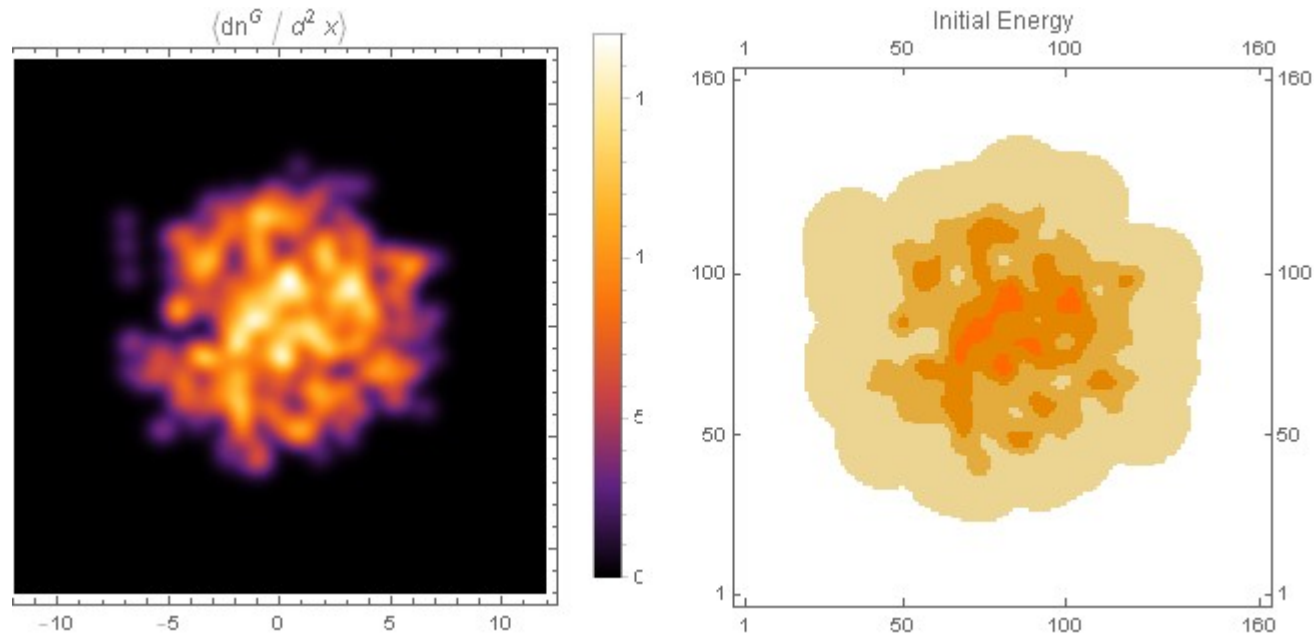


$$\frac{1}{\Lambda_{QCD}} \leq |B_1 - B_2|_T \leq R_a$$

# Summary II



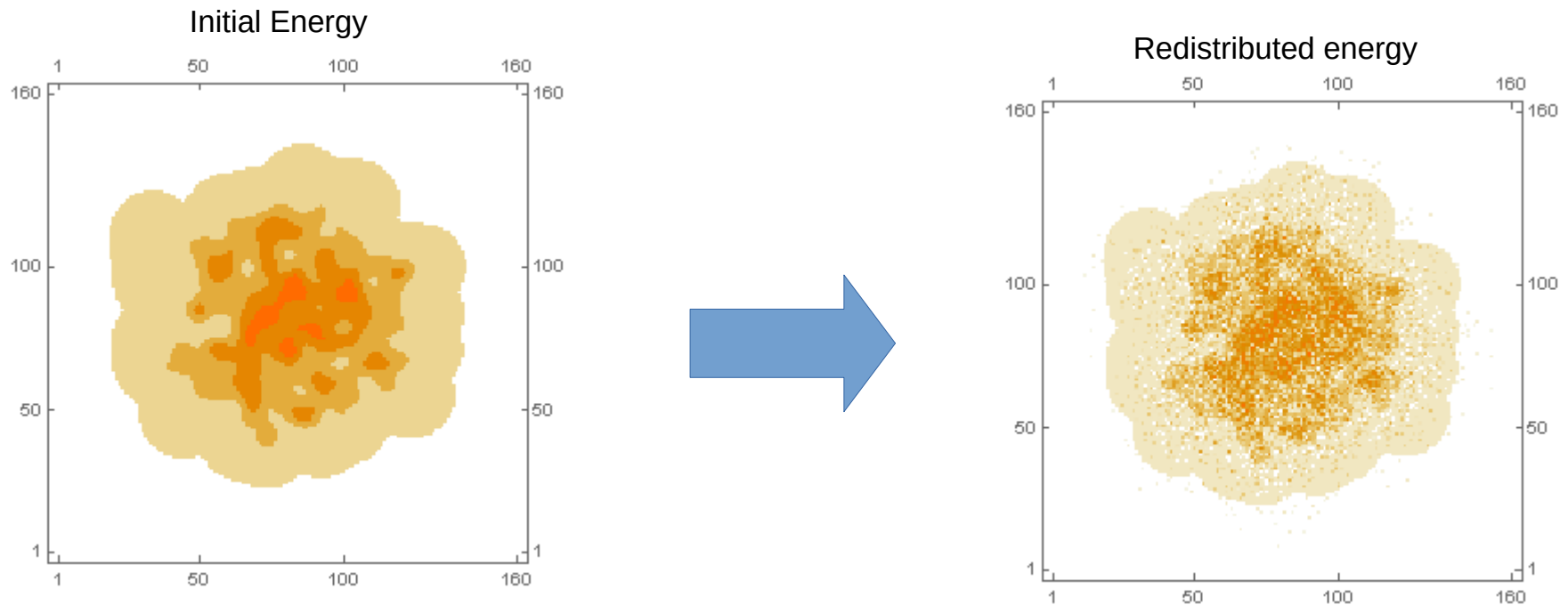
# Towards initial conditions for conserved charges



## Step 1

- MC Glauber is used to generate the initial energy distribution of the collision.
- Since this is dominated by gluons we can use this to find the gluon density at a given point.

# Redistributing energy $g \rightarrow q\bar{q}$

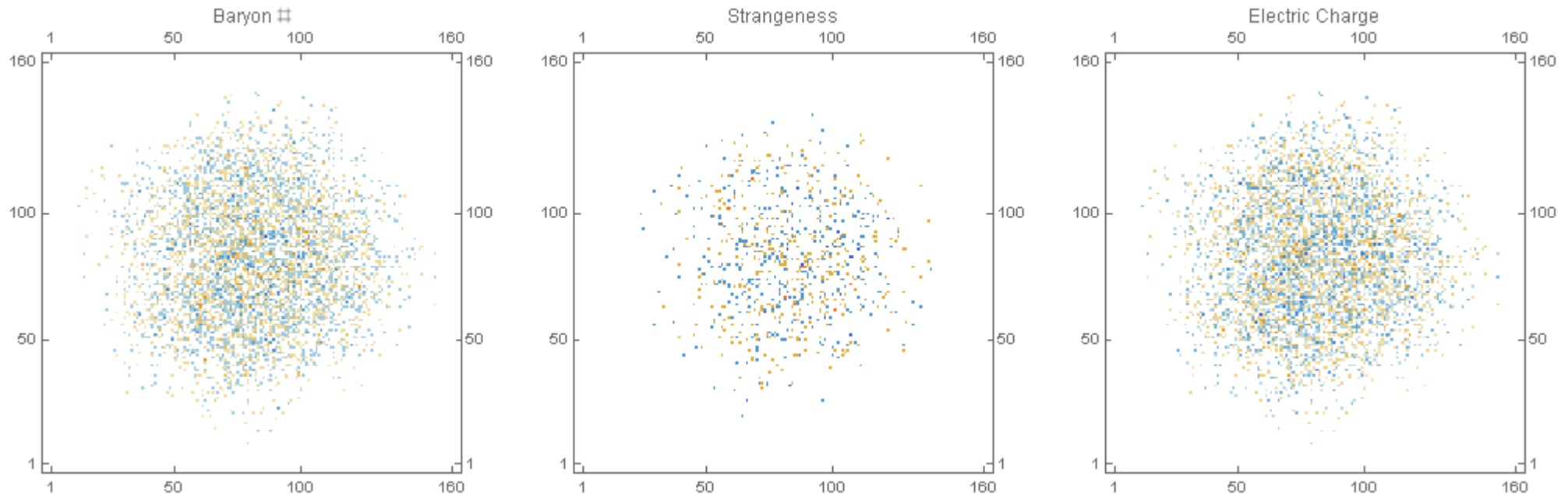


## Step 2

- Once we know the number of gluons produced we can find the number of quark – antiquark pairs produced at a given point in the transverse plane



# Conserved charge distributions

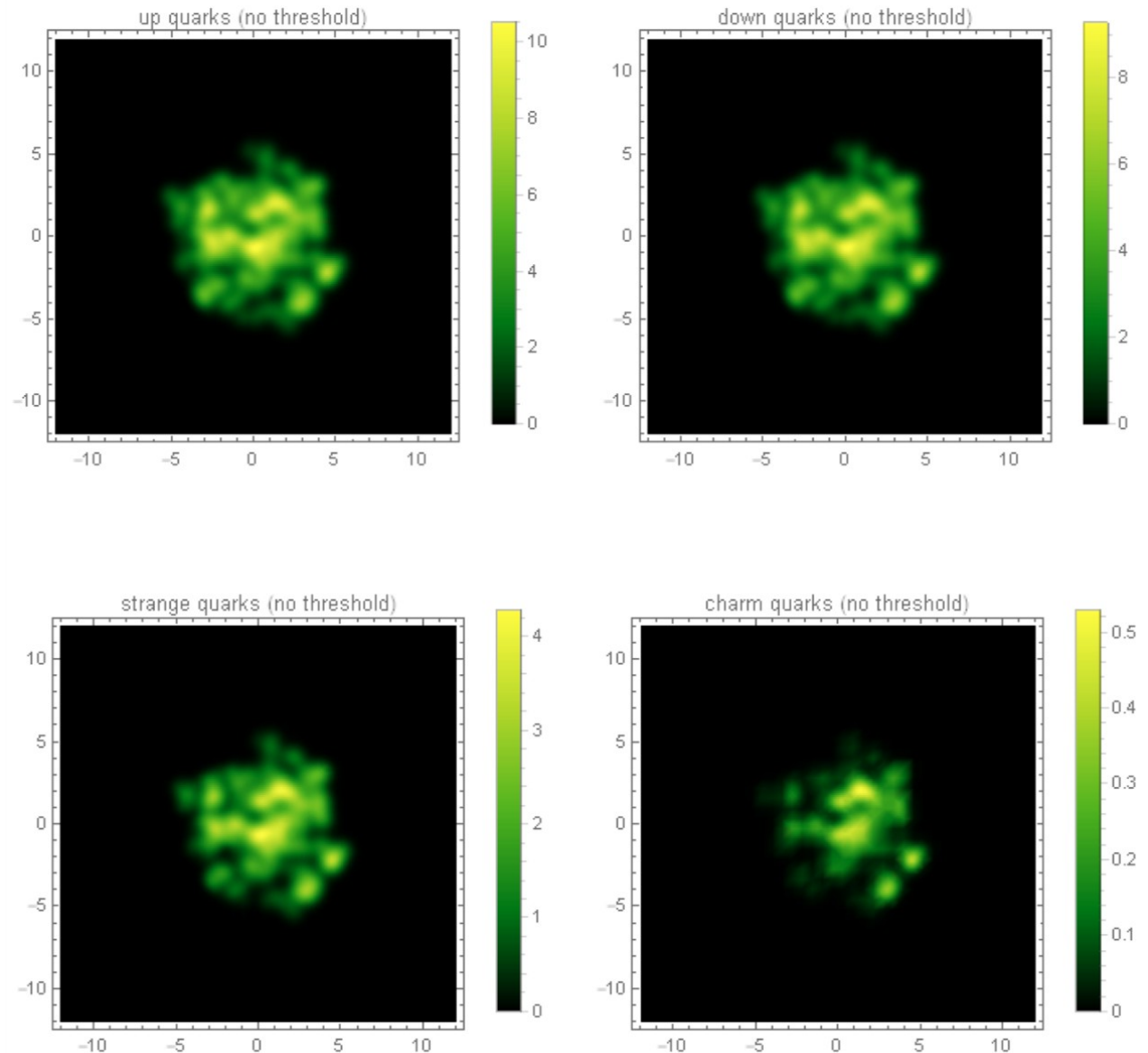


- We can also take a look to fluctuations of baryon number distributions, strangeness and electric charge in a given event in pA collisions

# Quark pair density distribution in pA collisions: preliminary results

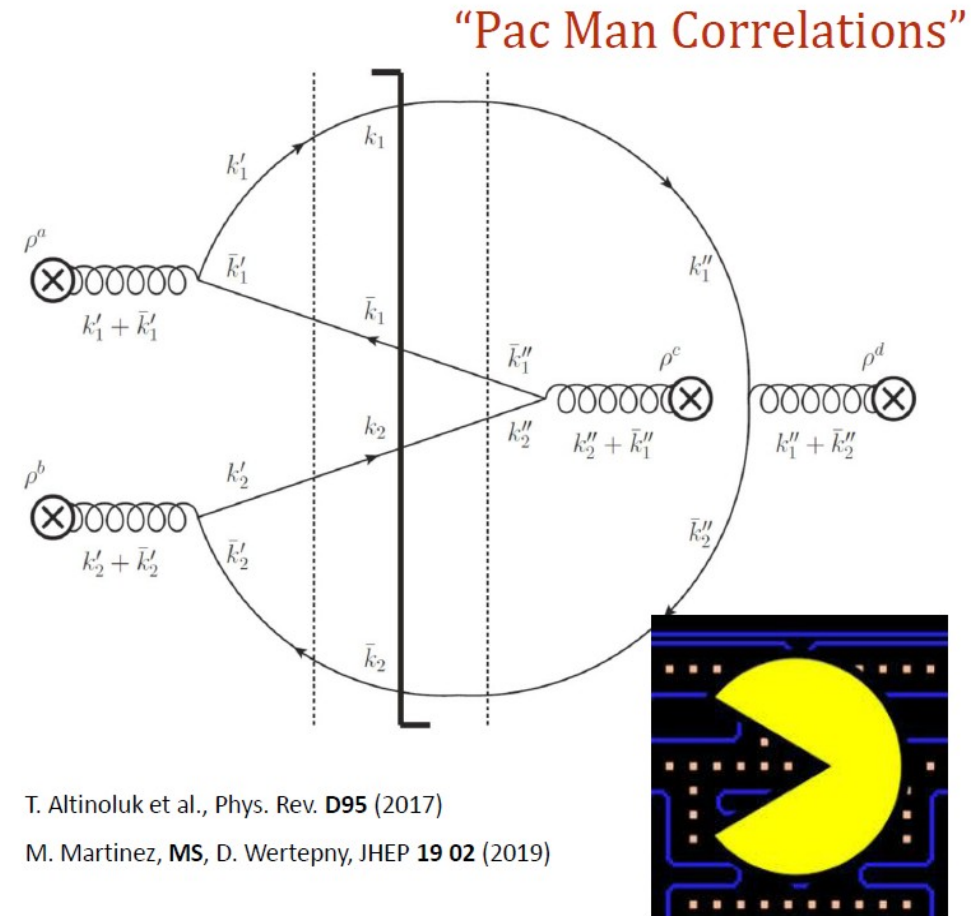
Mean  $q\bar{q}$  density distribution for different flavors.

- Shape of the distribution changes depending on the mass of the pair.
- Different eccentricities which are flavor-dependent



# More about double pair correlations

- **Double  $c\bar{c}$  production** introduces a first sensitivity to **quark Fermi statistics**
  - Antisymmetric wave functions
  - Reduces correlations among quarks
  - Not a **“ridge,”** but a **“trough”**
- New classes of “non-flow” quantum correlations are possible
  - Cleanest identification of quark channels in the **heavy sector**



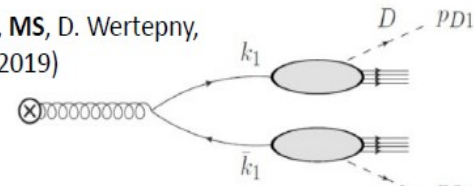
# One calculation to rule them all



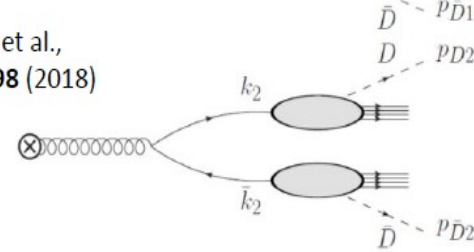
- One  $(c\bar{c})(c\bar{c})$  calculation can be **simultaneously constrained** in both the  $D$  and  $J/\psi$  sectors

- $c\bar{c} \rightarrow D\bar{D}$  by fragmentation
- $c\bar{c} \rightarrow J/\psi$  by NRQCD / ICEM

M. Martinez, MS, D. Wertepny,  
JHEP **19 02** (2019)

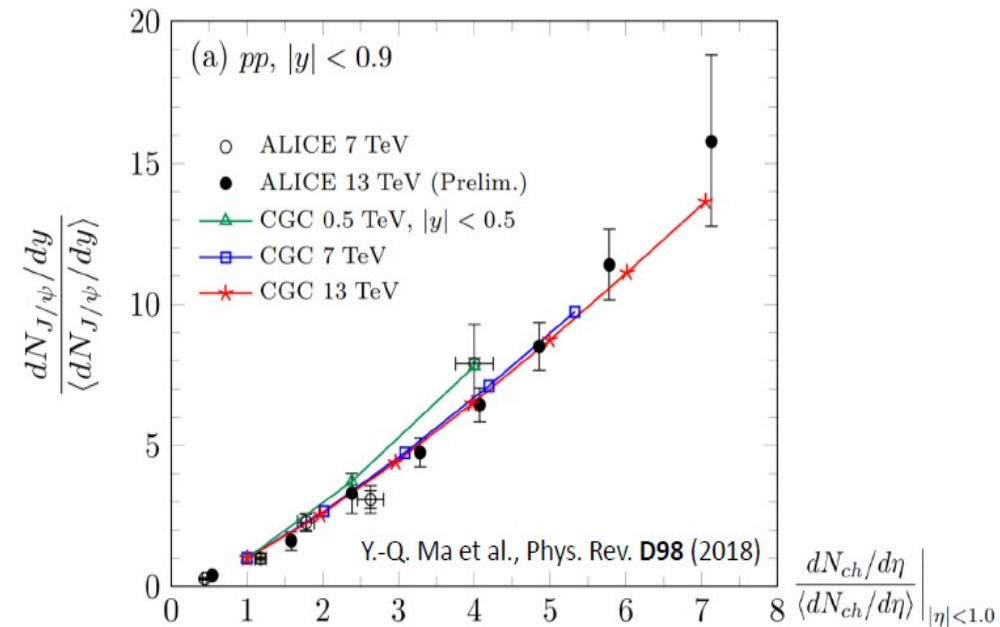


R. Boussarie et al.,  
Phys. Rev. **D98** (2018)



- Like in **pQCD for pp**, we can honestly **test the partonic** mechanisms

- $(D\bar{D}) (D\bar{D})$
- $(D\bar{D}) h$
- $(D\bar{D}) (J/\psi)$
- $(J/\psi) h$
- $(J/\psi) (J/\psi)$
- Bottom sector?

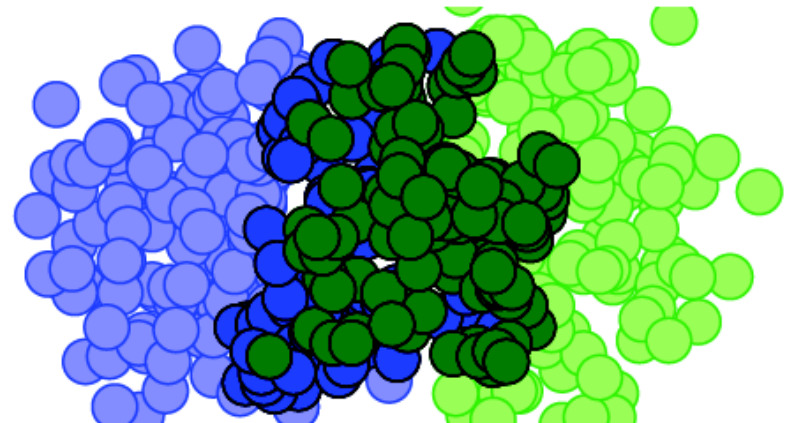
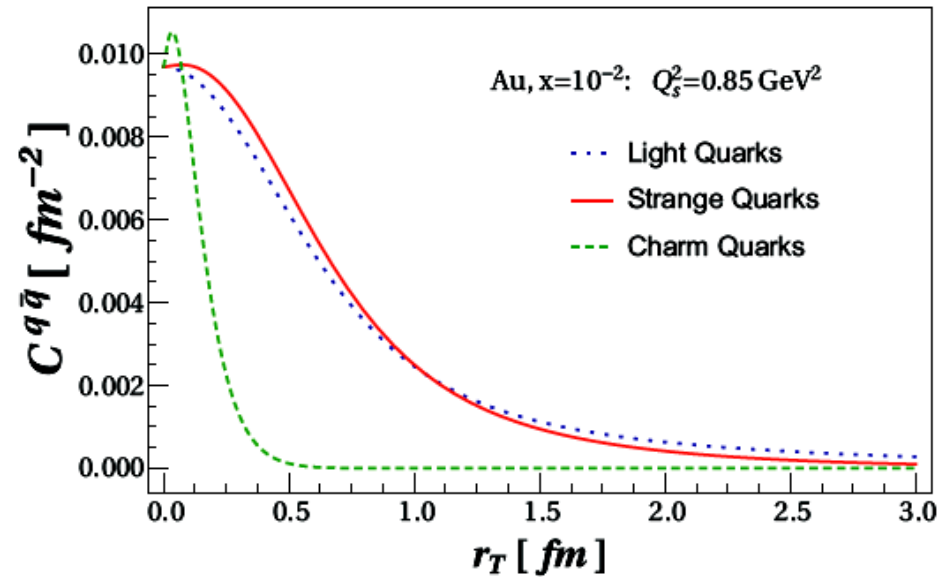


# Conclusions

- We have computed in detail the **spatial correlations among quarks and antiquarks** in the initial stages of heavy-ion collisions
  - **Explicit results** for single-pair production
  - **Operator-level results** for double-pair production
- **Ultimate goal:** perform event-by-event sampling of all 3 regions to initialize various conserved charges.

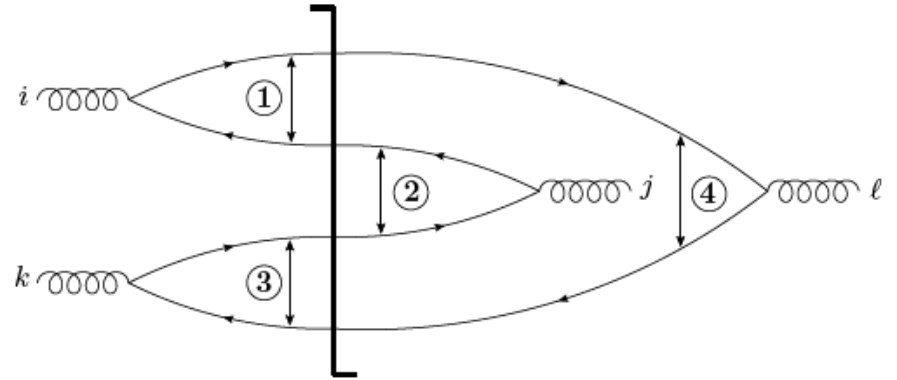
# Outlook

- There are many places we can **improve on the approximations** for the single-pair result
- In addition to the correlations, we can also calculate the **local fluctuations**
- This is an ideal **testbed for the Monte Carlo sampling** and proof of principle.



# Outlook II

- We have the **formal results** for the double-pair calculation, but they're **long and unwieldy**



- Analytic tools are likely to be of limited value; need **numerics**
- ...But directly applicable to **many measured correlations**
  - **Double-quarkonia** correlations
  - **4-particle open heavy / light flavor** correlations
  - Same sign / opposite sign **charge correlations**, etc.

**Backup slides**

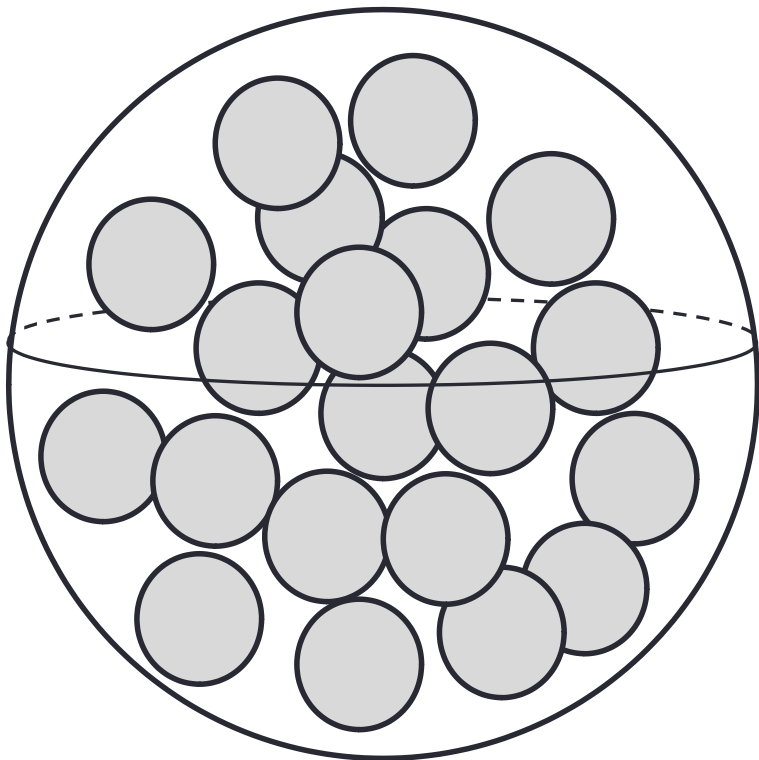


# Model for the nucleus at high energies

- Heavy ions can be thought of as a bag of nucleons.
- Volume scales with the number of nucleons:  $r \sim A_T^{\frac{1}{3}}$

$$\int d^3r \rho(\vec{r}) = A_T$$

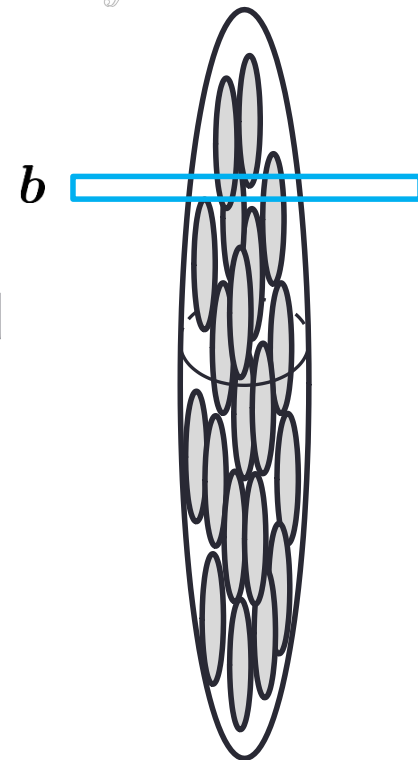
$$T(b) = \int dz \rho(\vec{r}) \sim A_T^{\frac{1}{3}}$$



Lorentz Contracted  
(per nucleon):

RHIC:  $\gamma \sim 200$

LHC:  $\gamma \sim 5000$



# Interacting with a single nucleon

- Quark/gluon interacts with a nucleon
- Exchanges 2 gluons
- Introduces the saturation scale (classical)

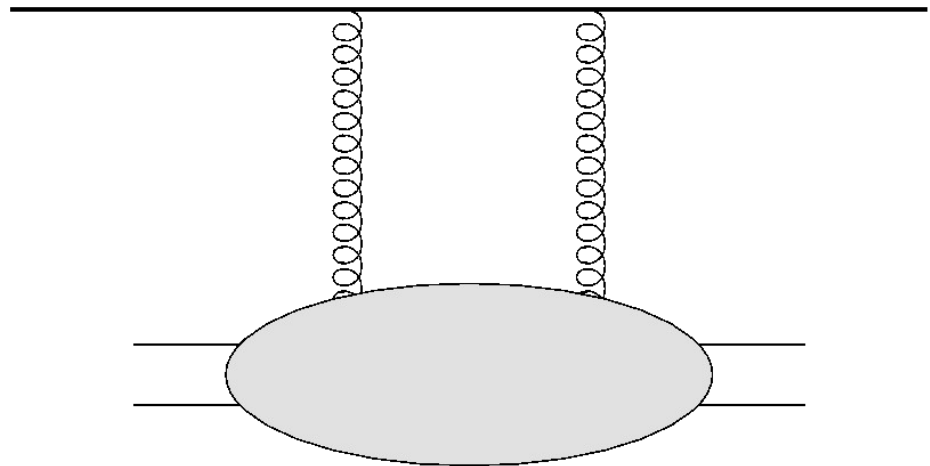
$$Q_{s0}^2 = 4\pi\alpha_s^2 T(\mathbf{b})$$

- On the order of

$$Q_{sT}^2 \sim \alpha_s^2 A_T^{\frac{1}{3}}$$

- In heavy ions

$$\alpha_s^2 A_T^{\frac{1}{3}} \sim 1$$



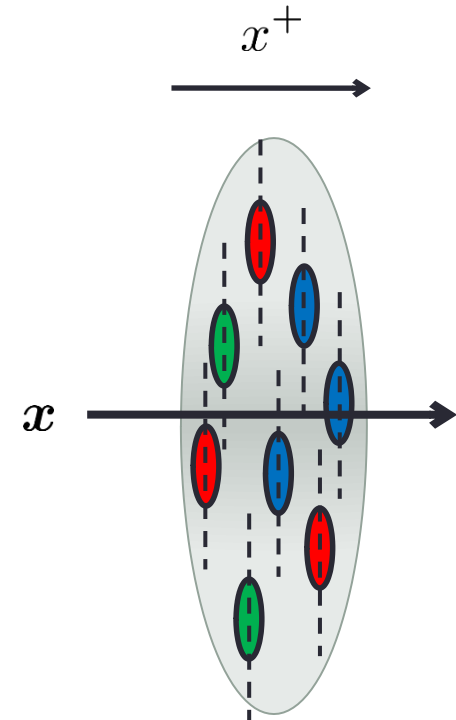
# Interacting with many nucleons

- Quarks and gluons pass through the shock wave
- Interaction is nearly instantaneous
- Doesn't change transverse position
- Interacts with fields from many nucleons
- Gains a factor per nucleon

$$Q_{sT}^2 \sim \alpha_s^2 A_T^{\frac{1}{3}}$$

- For a heavy ion we can consider all the scatterings if

$$\alpha_s^2 A_T^{\frac{1}{3}} \sim 1$$



$$Q_{sT}^2 \sim \alpha_s^2 A_T^{\frac{1}{3}}$$

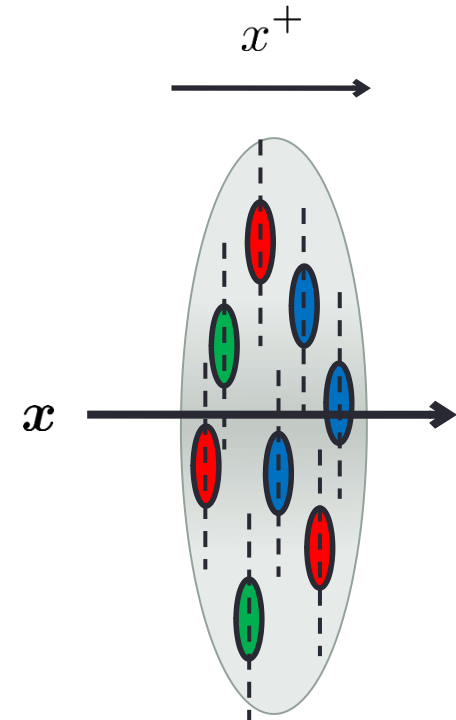
# The interaction is a Wilson line

- These can be represented as Wilson lines in the light-cone gauge,  $A^+ = 0$ .
- Path ordered exponentials
- Quarks:

$$V_{\mathbf{x}} = \text{P exp} \left\{ i g \int dx^+ t^a A_a^-(x^+, x^- = 0, \mathbf{x}) \right\}$$

- Gluons:

$$U_{\mathbf{x}} = \text{P exp} \left\{ i g \int dx^+ T^a A_a^-(x^+, x^- = 0, \mathbf{x}) \right\}$$



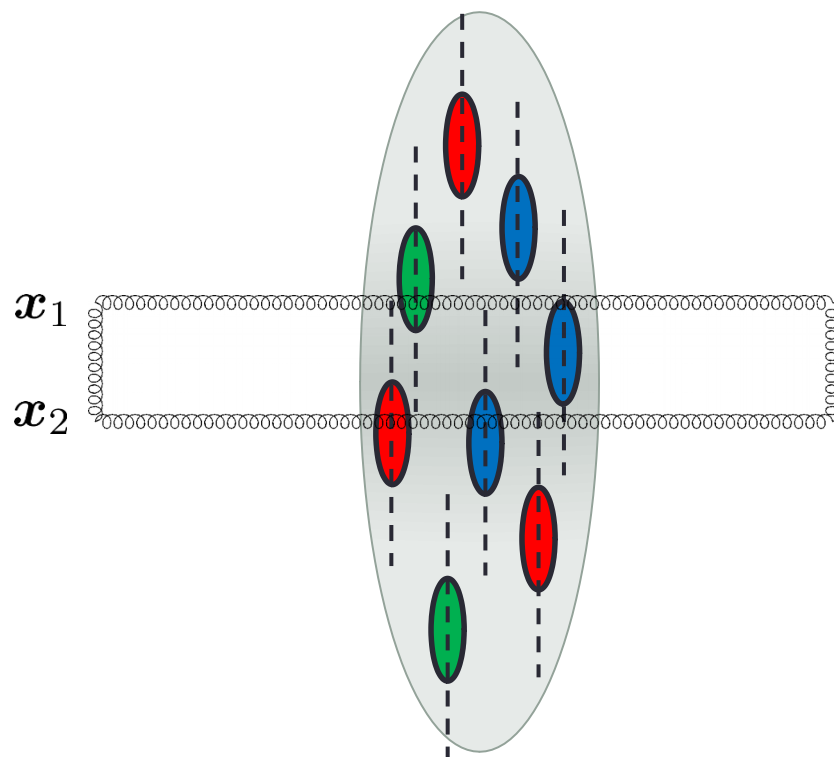
$$Q_{sT}^2 \sim \alpha_s^2 A_T^{\frac{1}{3}}$$

# Gluon dipole

- Lets look at the simple case of a gluon dipole
- Gluon dipole passing through the target can be represented with Wilson lines.
- The survival probability for the gluon dipole is:

$$S_G(\mathbf{x}_1, \mathbf{x}_2) \equiv \frac{1}{N_c^2 - 1} \langle \text{Tr}[U_{\mathbf{x}_1} U_{\mathbf{x}_2}^\dagger] \rangle$$

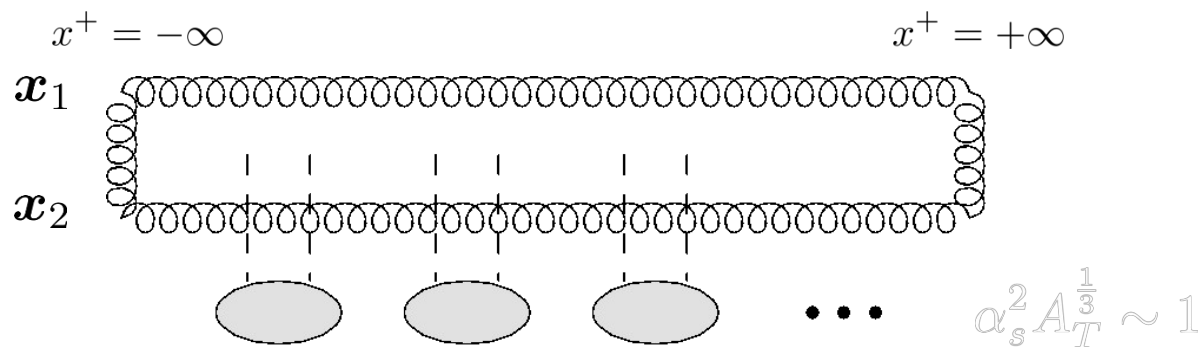
- Angle brackets represent averaging over all possible charge configurations.



# Gluon dipole – survival probability

- The gluon dipole interacts with many nucleons in the target, exchanging two gluons each time (McLerran Venugopalan (MV) model).

$$S_G(\mathbf{x}_1, \mathbf{x}_2) \equiv \frac{1}{N_c^2 - 1} \langle \text{Tr}[U_{\mathbf{x}_1} U_{\mathbf{x}_2}^\dagger] \rangle$$



$$S_G(\mathbf{x}_1, \mathbf{x}_2) = \exp \left[ -\frac{1}{4} |\mathbf{x}_1 - \mathbf{x}_2|^2 Q_{sT}^2 \left( \frac{\mathbf{x}_1 + \mathbf{x}_2}{2} \right) \ln \left( \frac{1}{|\mathbf{x}_1 - \mathbf{x}_2| \Lambda} \right) \right]$$

- $\Lambda$  is an IR cutoff:

$$\Lambda \sim \Lambda_{QCD} \approx 250 \text{ MeV}$$

# Heavy-light ion paradigm

- Take into account all nucleons in one of the ions (heavy) and only a few in the other (light).

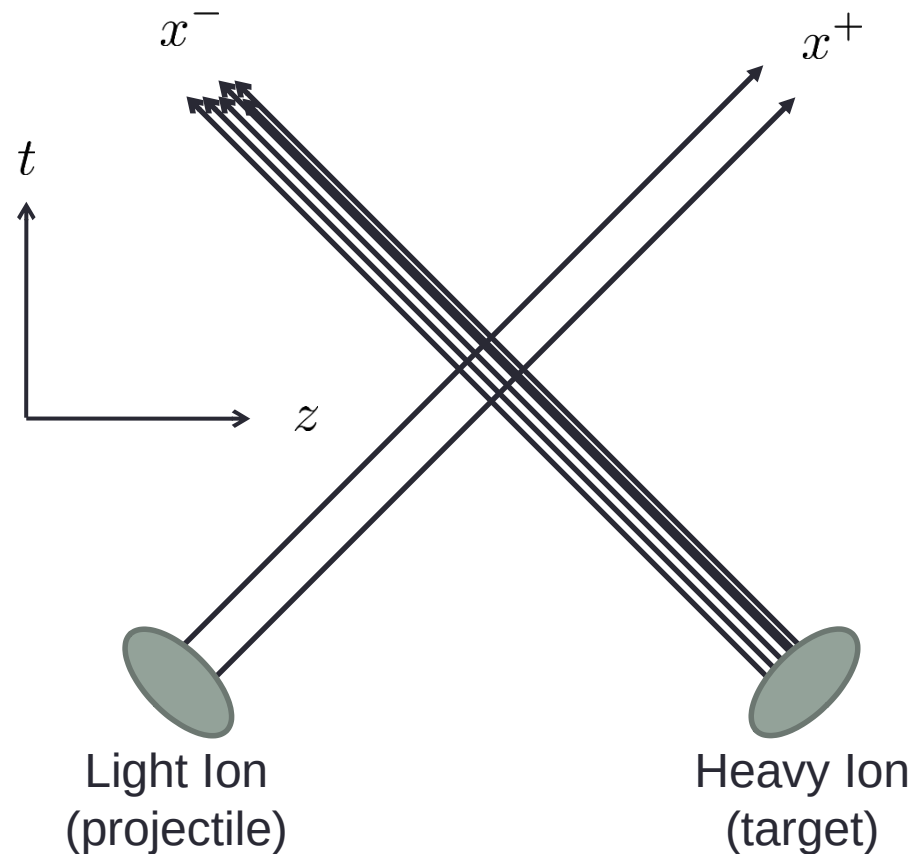
$$1 \ll A_P^{\frac{1}{3}} \ll A_T^{\frac{1}{3}}$$

- Target power counting:

$$\alpha_s^2 A_T^{\frac{1}{3}} \sim 1$$

- Projectile power counting:

$$\alpha_s \ll \alpha_s^2 A_P^{\frac{1}{3}} \lesssim 1$$



# Definitions

- **Multiplicities:** inclusive probability densities

$$\left\langle \frac{dn^i}{d\omega_1} \right\rangle = \frac{1}{\sigma_{inel}} \frac{d\sigma^i}{d\omega_1} \quad \left\langle \frac{dn^i}{d\omega_1} \frac{dn^j}{d\omega_2} \right\rangle = \frac{1}{\sigma_{inel}} \frac{d\sigma^{ij}}{d\omega_1 d\omega_2} + \delta^{ij} \delta(\omega_1 - \omega_2) \frac{1}{\sigma_{inel}} \frac{d\sigma^i}{d\omega_1}$$

- Quarks and antiquarks:

$$\left\langle k_1^+ \frac{dn^q}{d^2 B_1 dk_1^+} k_2^+ \frac{dn^q}{d^2 B_2 dk_2^+} \right\rangle_{ev} = \frac{1}{\sigma_{inel}} \left[ k_1^+ k_2^+ \frac{d\sigma^{qq}}{d^2 B_1 dk_1^+ d^2 B_2 dk_2^+} + \delta^{(2)}(\mathbf{B}_1 - \mathbf{B}_2) k_2^+ \delta(k_1^+ - k_2^+) k_1^+ \frac{d\sigma^q}{d^2 B_1 dk_1^+} \right]$$

$$\left\langle k_1^+ \frac{dn^q}{d^2 B_1 dk_1^+} k_2^+ \frac{dn^{\bar{q}}}{d^2 B_2 dk_2^+} \right\rangle_{ev} = \frac{1}{\sigma_{inel}} \left[ k_1^+ k_2^+ \frac{d\sigma^{q\bar{q}}}{d^2 B_1 dk_1^+ d^2 B_2 dk_2^+} \right]$$

- **Correlation function** (various definitions!):

$$C_{ij}(\mathbf{B}_1, k_1^+; \mathbf{B}_2, k_2^+) \equiv \left\langle k_1^+ \frac{dn^i}{d^2 B_1 dk_1^+} k_2^+ \frac{dn^j}{d^2 B_2 dk_2^+} \right\rangle_{ev} - \left\langle k_1^+ \frac{dn^i}{d^2 B_1 dk_1^+} \right\rangle_{ev} \left\langle k_2^+ \frac{dn^j}{d^2 B_2 dk_2^+} \right\rangle_{ev}$$

- “Parton-level” **baryon number:**  $\mathcal{B} \equiv \frac{1}{3} \sum_f (n^{qf} - n^{\bar{q}f})$



# MV model quick review

- Target averages in **classical random color fields** (MV model)

$$\langle \mathcal{A}_a^-(x^+, x^-, \mathbf{x}) \mathcal{A}_b^-(y^+, x^-, \mathbf{y}) \rangle = \delta_{ab} \delta(x^+ - y^+) \gamma(\mathbf{x} - \mathbf{y})$$

- Take the **large-Nc limit** to simplify the color algebra

$$\langle \hat{D}_2(\mathbf{x}, \mathbf{y}) \hat{D}_2(\mathbf{u}, \mathbf{v}) \rangle \approx \langle \hat{D}_2(\mathbf{x}, \mathbf{y}) \rangle \langle \hat{D}_2(\mathbf{u}, \mathbf{v}) \rangle$$

$$\langle \hat{D}_2(\mathbf{B}_1, \mathbf{B}_2) \rangle = \langle \hat{D}_2(\mathbf{B}_2, \mathbf{B}_1) \rangle = e^{-\frac{1}{4} |\mathbf{B}_1 - \mathbf{B}_2|_T^2 Q_s^2}$$

- Neglect the **weak spatial dependence** of the saturation scale

$$\langle k_T^2 \rangle \sim Q_s^2(b_T) \propto \rho_{2D}(b_T)$$

- Work in the **quasi-classical approximation** (no small-x evolution)