

EIC theory overview

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Electron-Ion Collider (EIC)

A future (2029~) high-luminosity polarized ep , eA collider dedicated to the study of the nucleon and nucleus structure.

Center-of-mass energy
Luminosity

$$20 \lesssim \sqrt{s} \lesssim 140 \text{ GeV}$$

$$\sim 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$$

Gluons and the quark sea at high energies:
distributions, polarization, tomography

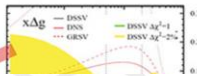
September 13 to November 19, 2010

Report from the INT program "Gluons and the quark sea at high energies: distributions, polarization, tomography"

2010 INT workshop

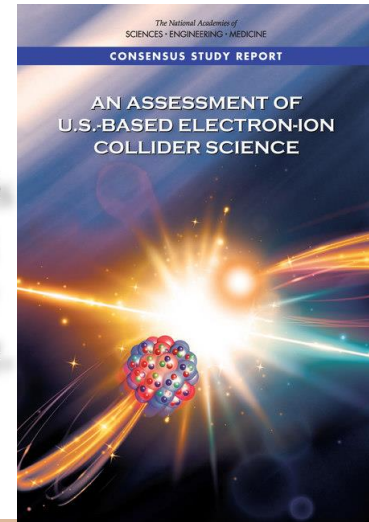
small x uncertainty from DSSV

$$\frac{dg_1}{d \log(Q^2)} \propto -\Delta g(x, Q^2)$$



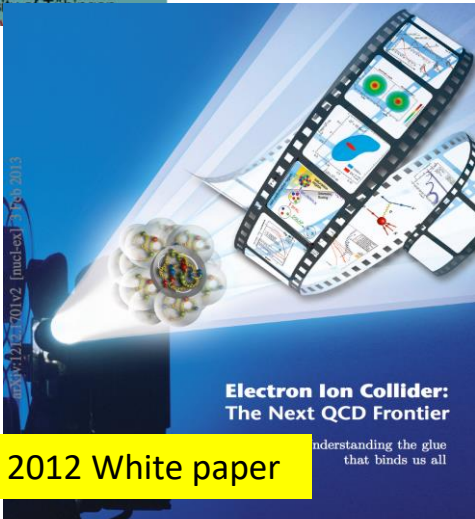
2018 NAS report

“The committee finds that the science that can be addressed by an EIC is compelling, fundamental and timely.”



REACHING FOR THE HORIZON

2015 NSAC Long Range Plan



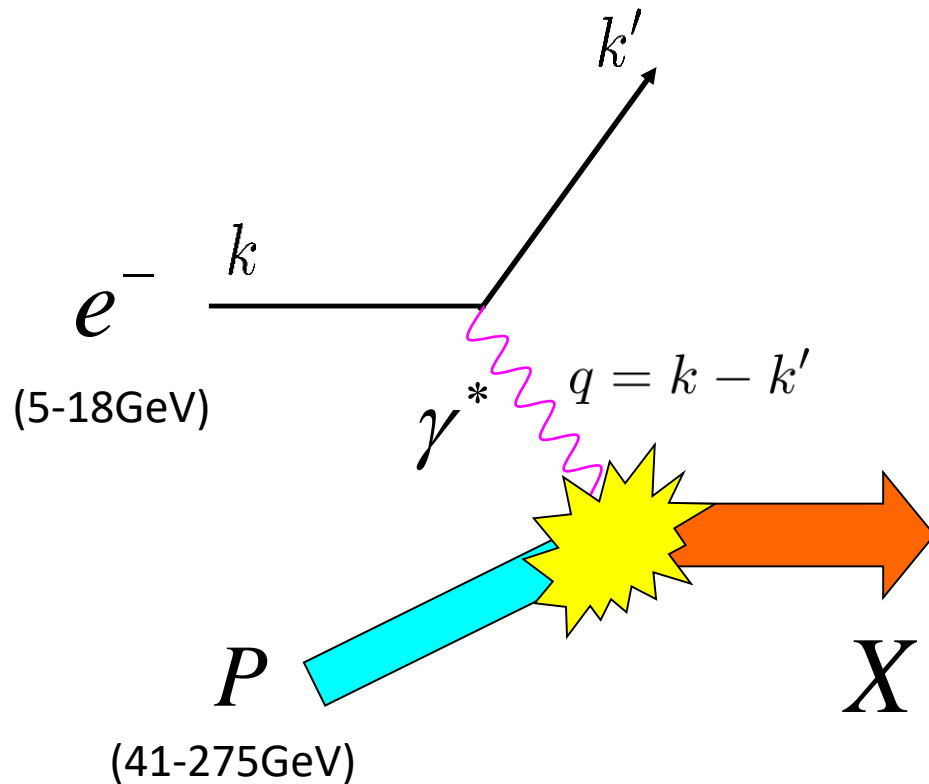
2012 White paper



2018 INT workshop

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Experiment at EIC: Deep Inelastic Scattering (DIS)



Two most important kinematic variables

$$Q^2 = -q^2 \quad \text{photon virtuality (resolution)}$$

$$x = \frac{Q^2}{2P \cdot q} \quad \text{Bjorken variable (inverse energy)}$$

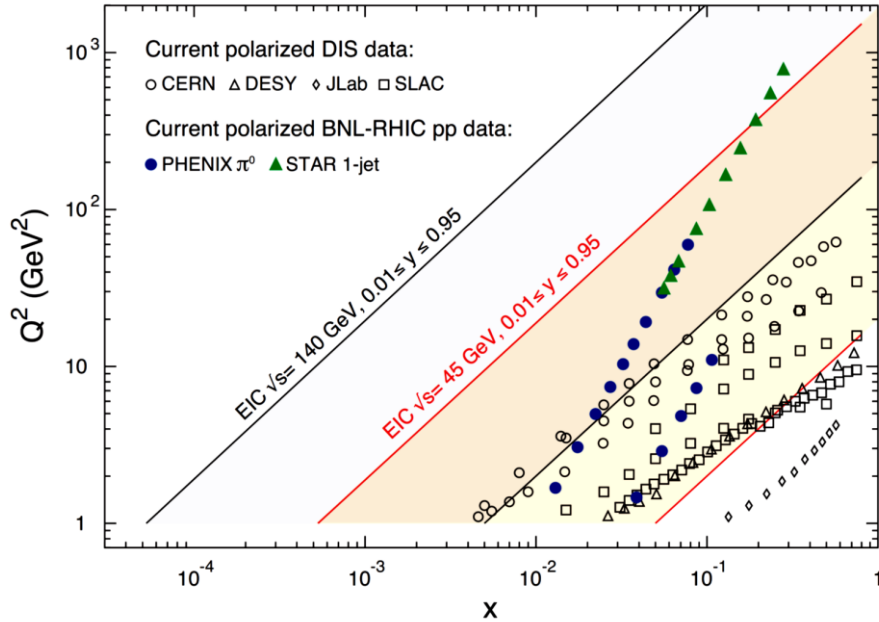
$$\approx \frac{E_{parton}}{E_{proton}}$$

Proton, deuteron, helium, gold...any nucleus of your choice!

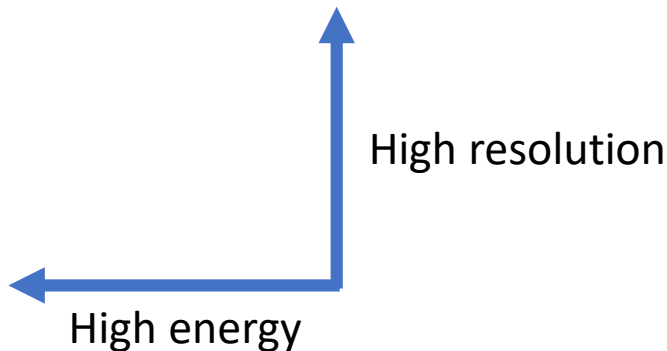
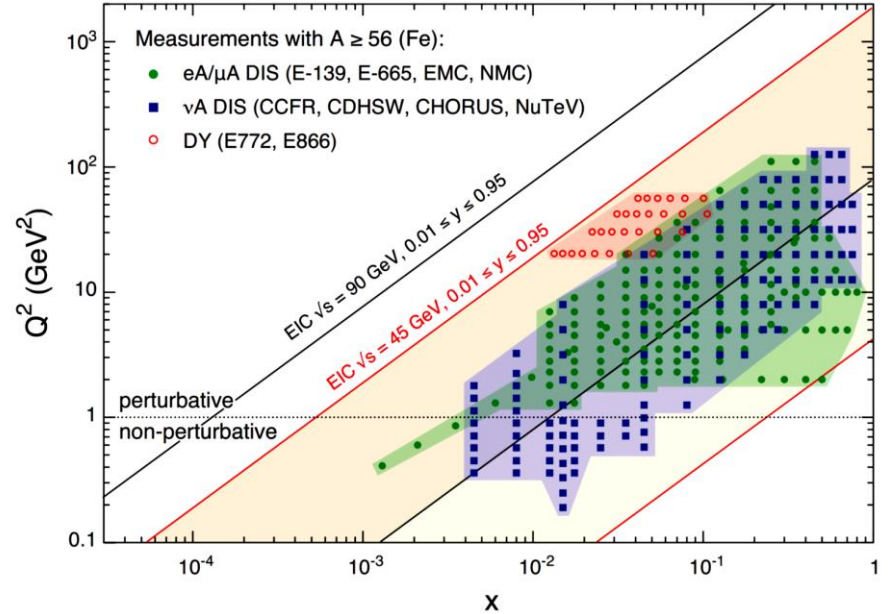
Electron, proton and light nuclei can be polarized.

EIC Kinematical coverage

Polarized DIS

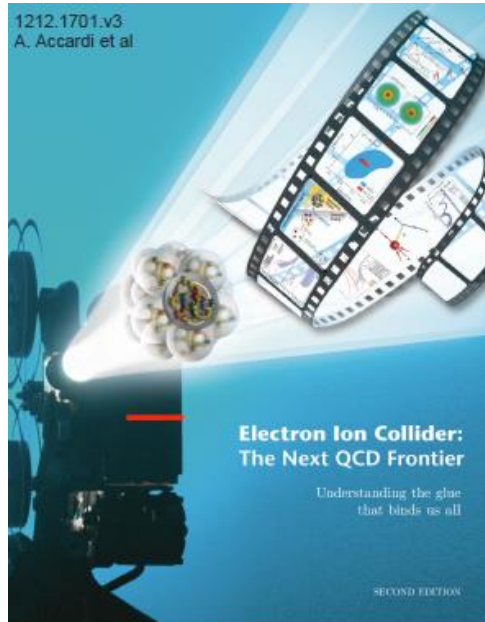


Nuclear DIS



Unprecedented coverage in kinematics.
Tremendous physics opportunities!

Scientific goals of EIC



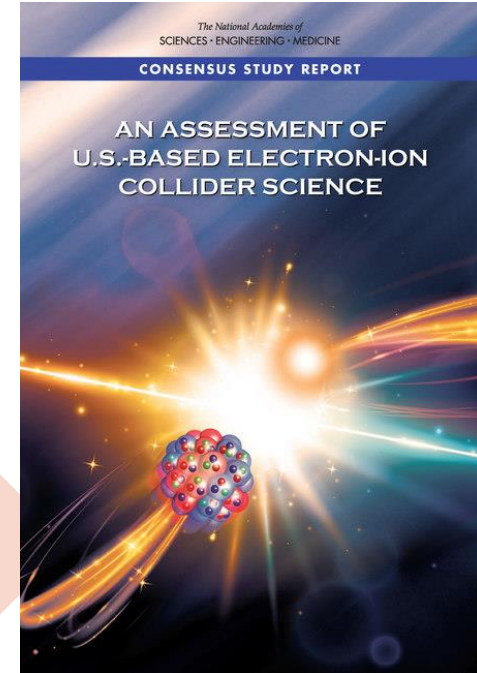
White paper
arXiv:1212.1701

Origin of
nucleon
mass

Origin of
nucleon
spin

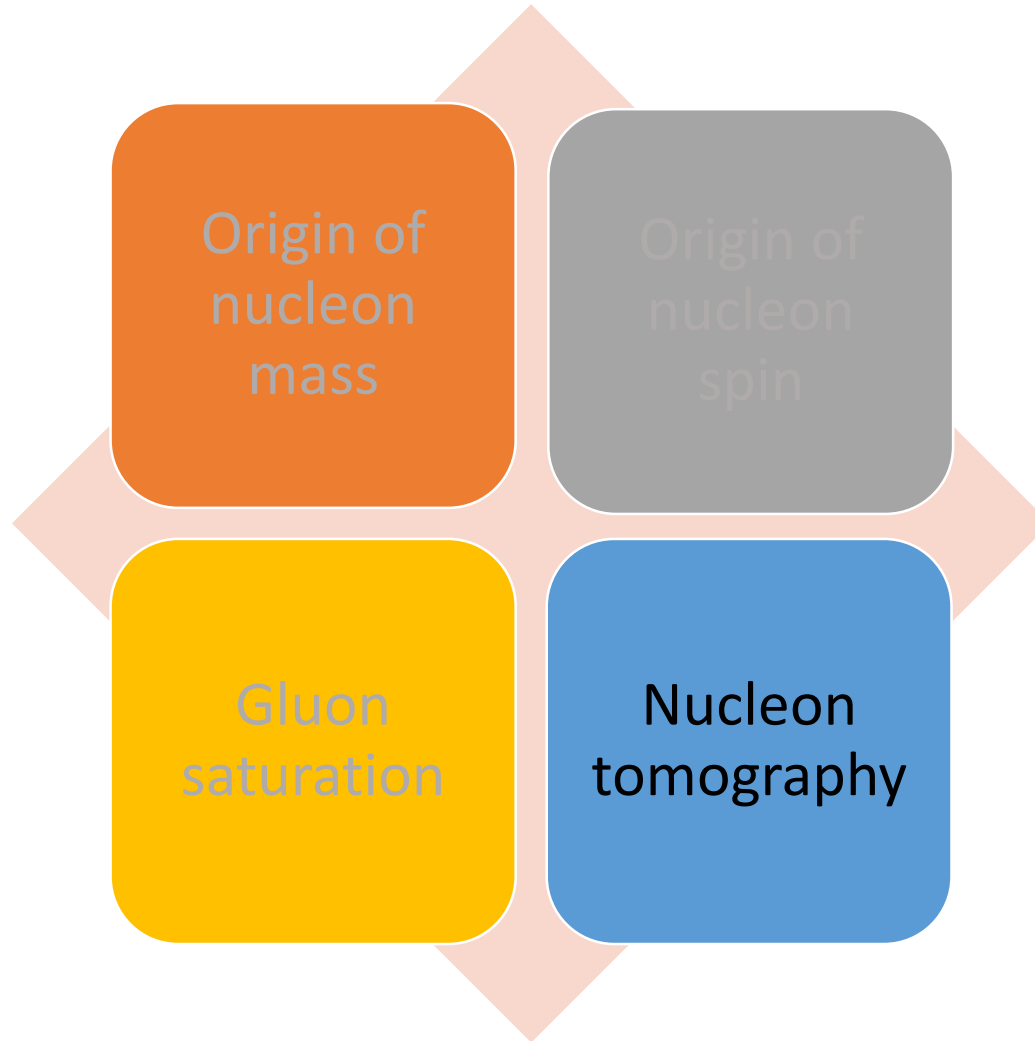
Gluon
saturation

Nucleon
tomography

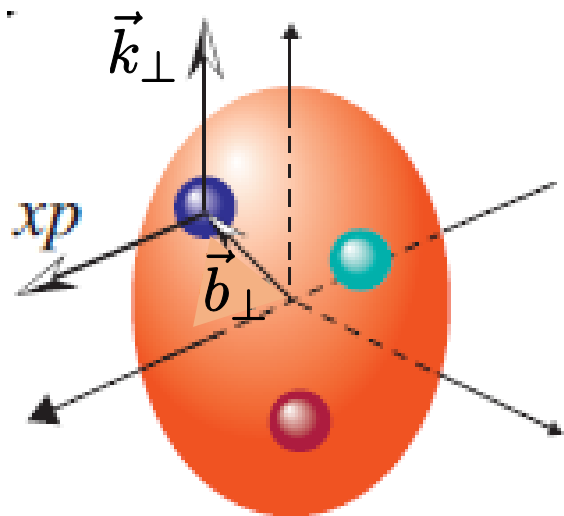


NAS report
July 2018

Scientific goals of EIC



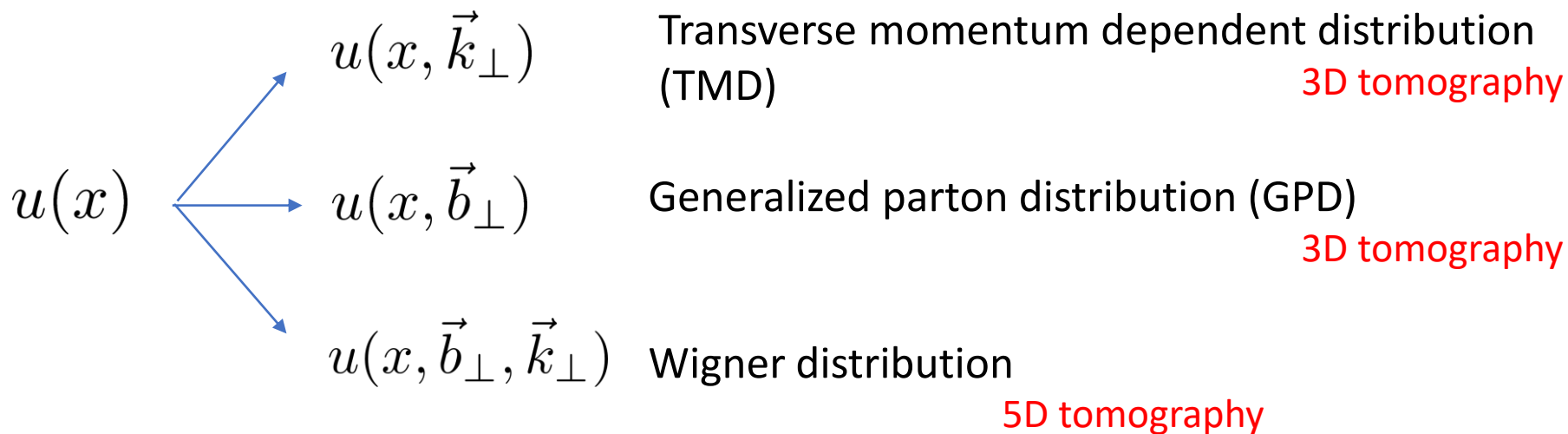
Multi-dimensional tomography



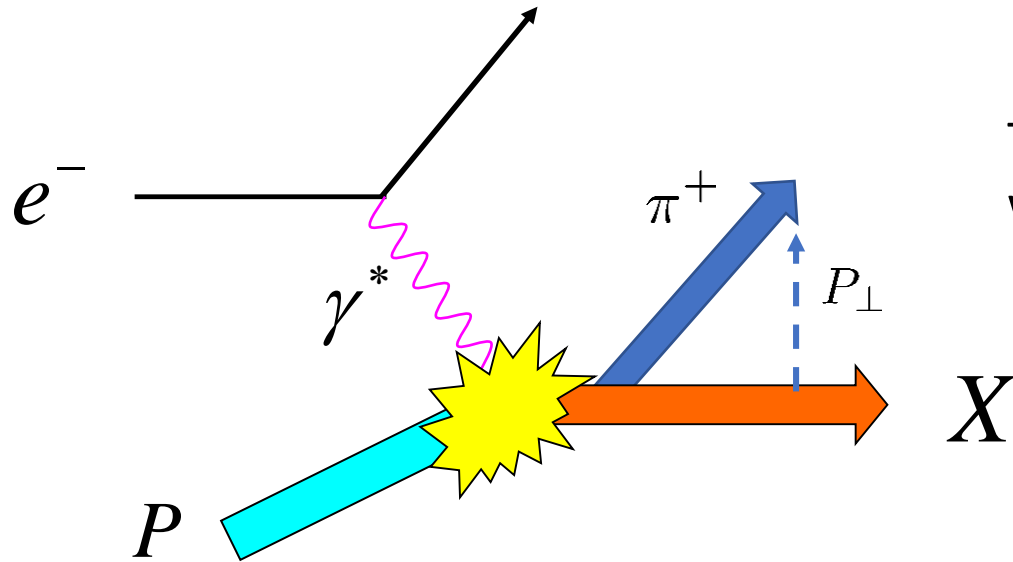
$$u(x) = \int \frac{dz^-}{4\pi} \langle P | \bar{u}(0) \gamma^+ u(z^-) | P \rangle$$

Ordinary parton distribution functions (PDF) can be viewed as the 1D tomographic image of the nucleon

The nucleon is much more complicated!
Partons also have transverse momentum \vec{k}_\perp
and are spread in impact parameter space \vec{b}_\perp



Semi-inclusive DIS



Tag one hadron species
with fixed transverse momentum P_\perp

When P_\perp is small, **TMD factorization**

Collins, Soper, Sterman;
Ji, Ma, Yuan,...

$$\frac{d\sigma}{dP_\perp} = H(\mu) \int d^2q_\perp d^2k_\perp \underbrace{f(x, k_\perp, \mu, \zeta)}_{\text{TMD PDF}} \underbrace{D(z, q_\perp, \mu, Q^2/\zeta)}_{\text{TMD FF}} \delta^{(2)}(zk_\perp + q_\perp - P_\perp) + \dots$$

Open up a new class of observables where perturbative QCD is applicable!

TMD global analysis

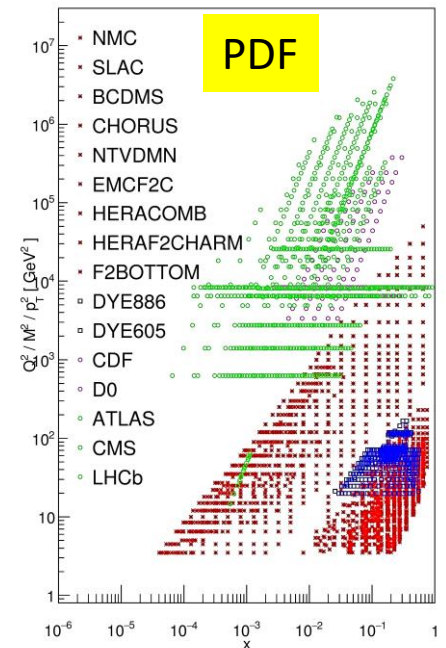
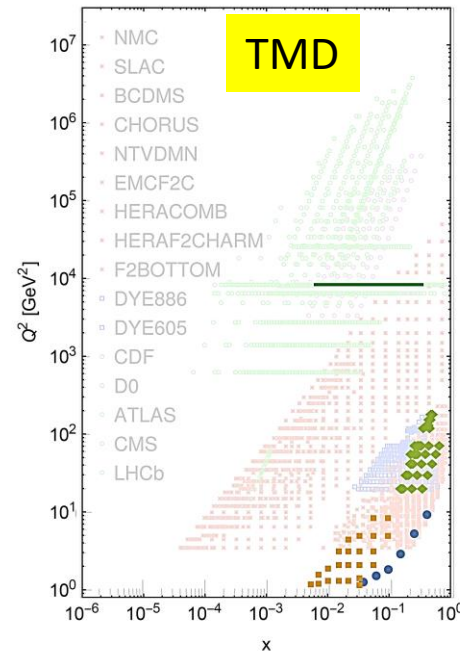
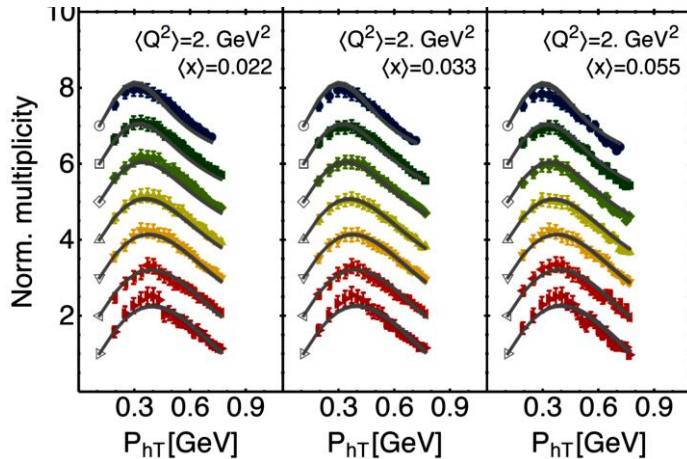
Global analysis of TMD based on ~ 8000 data points from SIDIS, Drell-Yan.

Bacchetta, Delcarro, Pisano, Radici, Signori (2017)

arTeMiDe state-of-the-art (NNLO+NNLL) implementation

Scimemi, Vladimirov (2017)

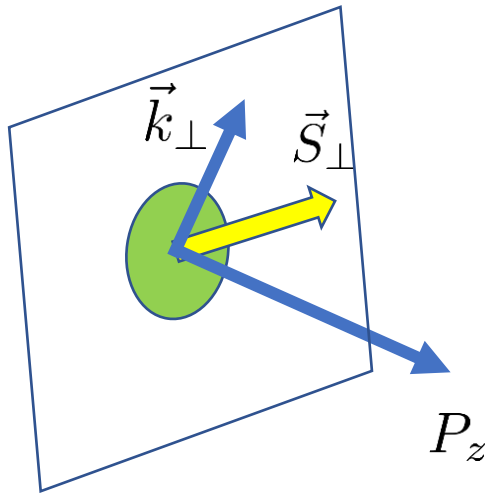
TMDlib public library Hautmann, Jung, Mulders,...



Still in its infancy. Fully blossoms in the EIC era!

Universality up to a sign

Sivers function for the transversely polarized nucleon



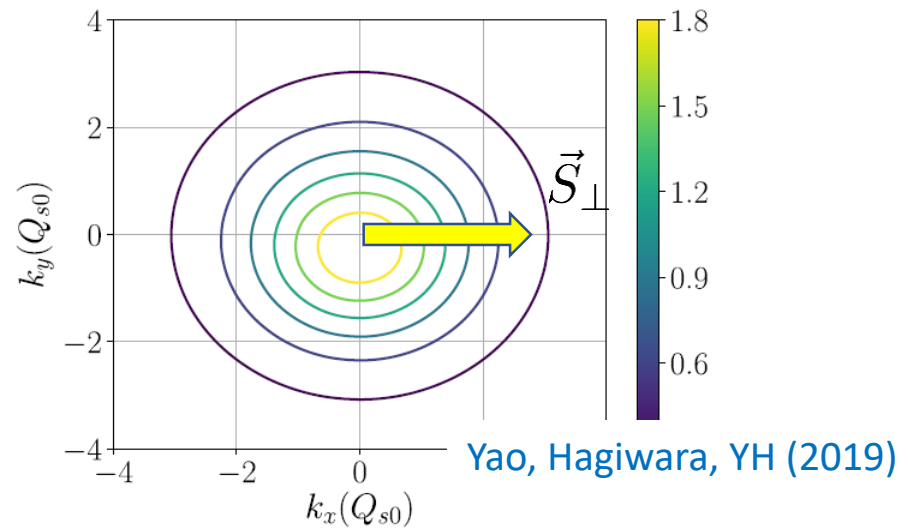
$$\sim \vec{k}_\perp \times \vec{S}_\perp f_{1T}^\perp(x, k_\perp)$$

Azimuthal anisotropy of parton distribution,
responsible for **single spin asymmetry**

The same function, but with **opposite signs**
in DIS and Drell-Yan. (Collins, 2002)

EIC can probe the **gluon** Sivers function
for the first time.

Zheng, Aschenauer, Lee, Xiao, Bao (2018)



Yao, Hagiwara, YH (2019)

Generalized parton distributions (GPD)

$$P^+ \int \frac{dy^-}{2\pi} e^{ixP^+y^-} \langle P' S' | \bar{\psi}(0) \gamma^\mu \psi(y^-) | PS \rangle$$

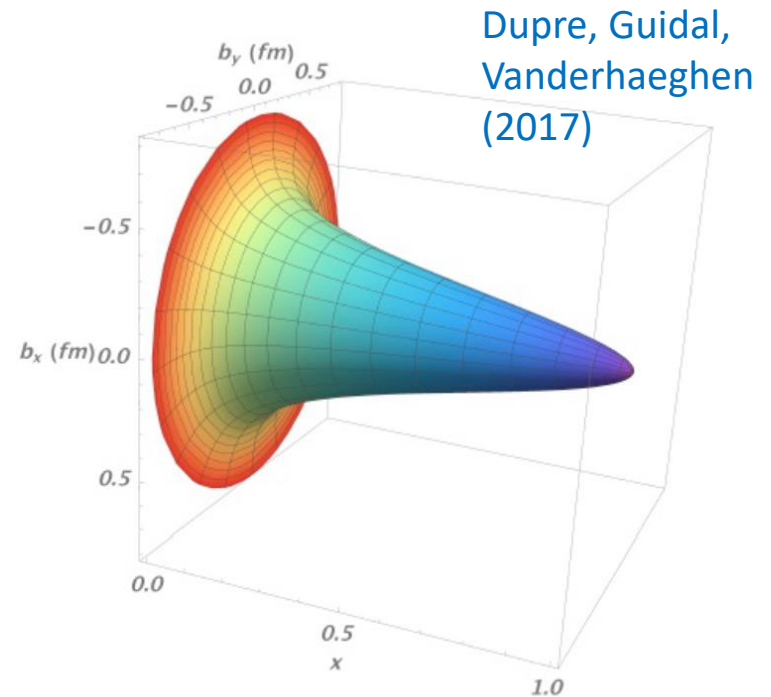
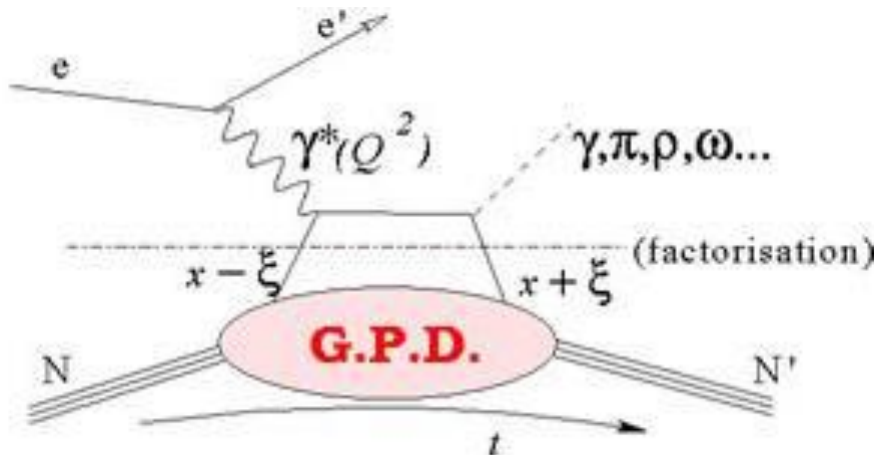
$$= H_q(x, \Delta) \bar{u}(P' S') \gamma^\mu u(PS) + E_q(x, \Delta) \bar{u}(P' S') \frac{i\sigma^{\mu\nu} \Delta_\nu}{2m} u(PS) \quad \Delta = P' - P$$



Fourier transform

Distribution of partons in **impact parameter** space b_\perp

Measurable in
Deeply Virtual Compton Scattering (DVCS)



Towards measuring GPD E at the EIC

Ji sum rule for proton spin $\frac{1}{2} = J_q + J_g$

$$J_q = \frac{1}{2} \int dx (H_q(x) + E_q(x))$$

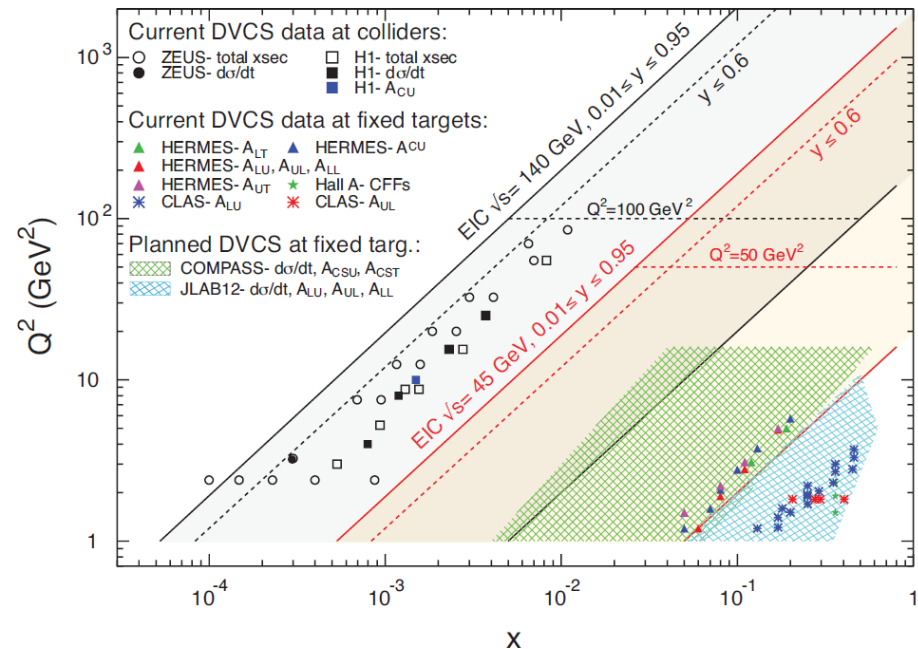
$$J_g = \frac{1}{4} \int dx (H_g(x) + E_g(x))$$

Currently very little is known about E_q ,
nothing about E_g from experiments.

At EIC, we can get a handle on E_q .

Aschenauer, Fazio, Kumericki, Muller (2013)

E_g is still challenging, but EIC is the only hope.



D-term: the last global unknown

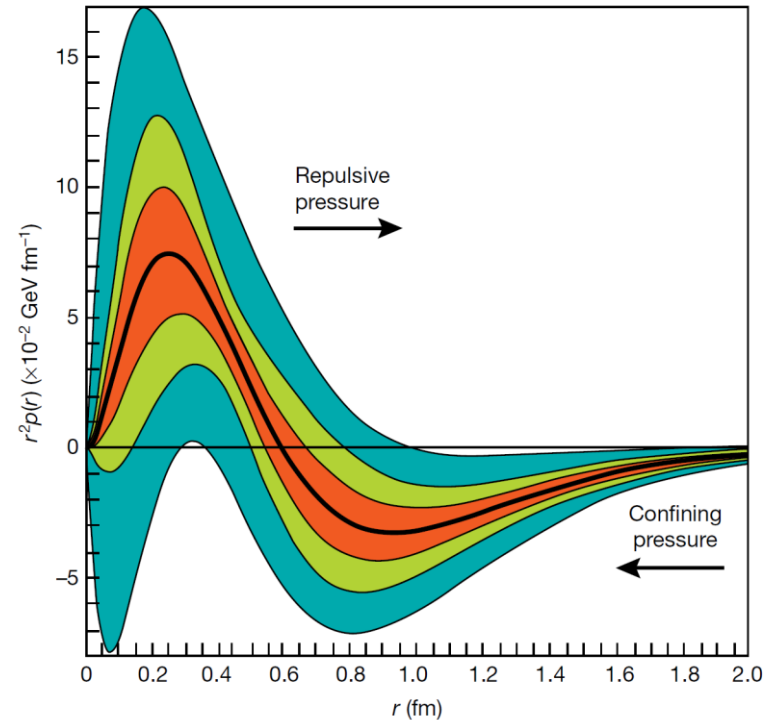
$$\langle P' | T^{ij} | P \rangle \sim (\Delta^i \Delta^k - \delta^{ik} \Delta^2) D(t)$$

$D(t=0)$ is a conserved charge of the nucleon, just like mass and spin!

Related to the radial 'pressure' inside a nucleon [Polyakov, Schweitzer,...](#)

$$T^{ij}(r) = \left(\frac{r^i r^j}{r^2} - \frac{1}{3} \delta^{ij} \right) s(r) + \delta^{ij} p(r)$$

Burkert, Elouadrhiri, Girod (Nature, 2018)

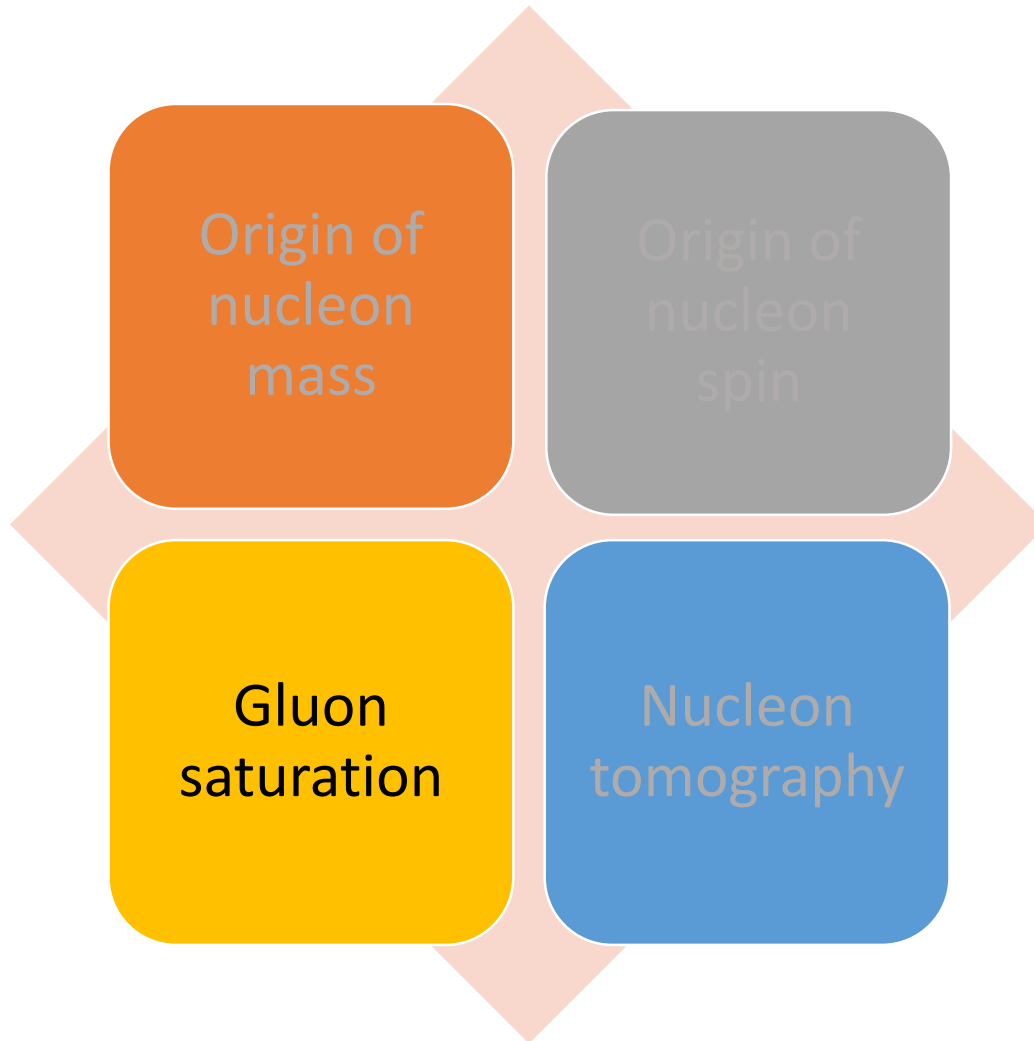


First extraction at Jlab, large model dependence.

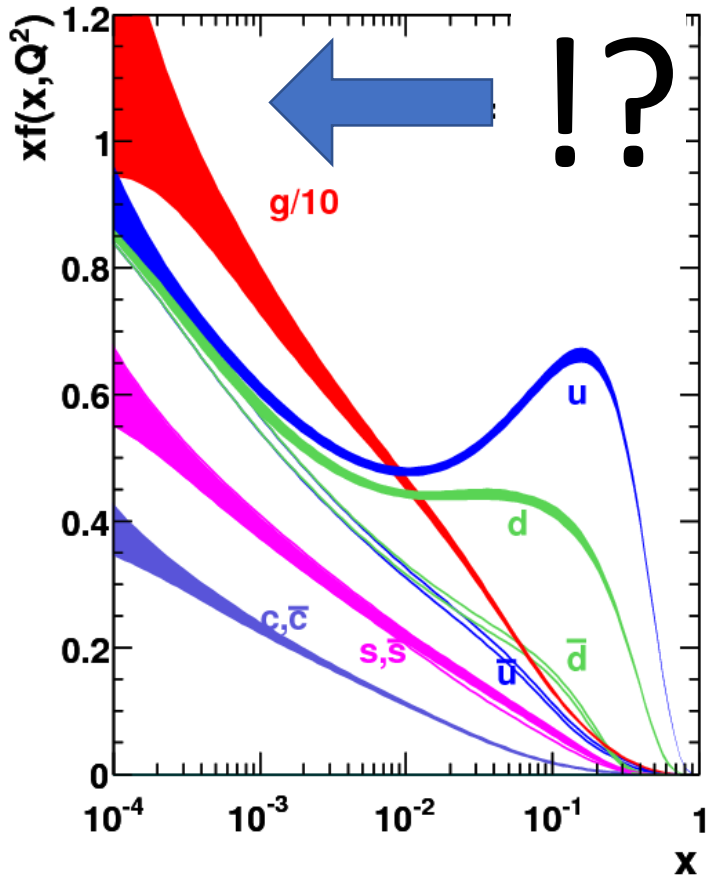
Need significant lever-arm in Q^2 to disentangle various moments of GPDs



Scientific goals of EIC

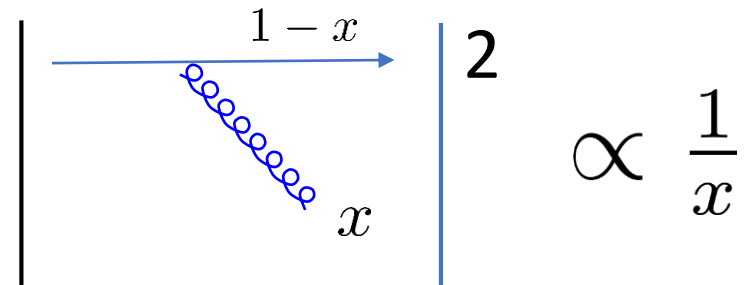


QCD at small-x



as predicted by BFKL
(Balitsky-Fadin-Kuraev-Lipatov)

Probability to emit a soft gluon diverges



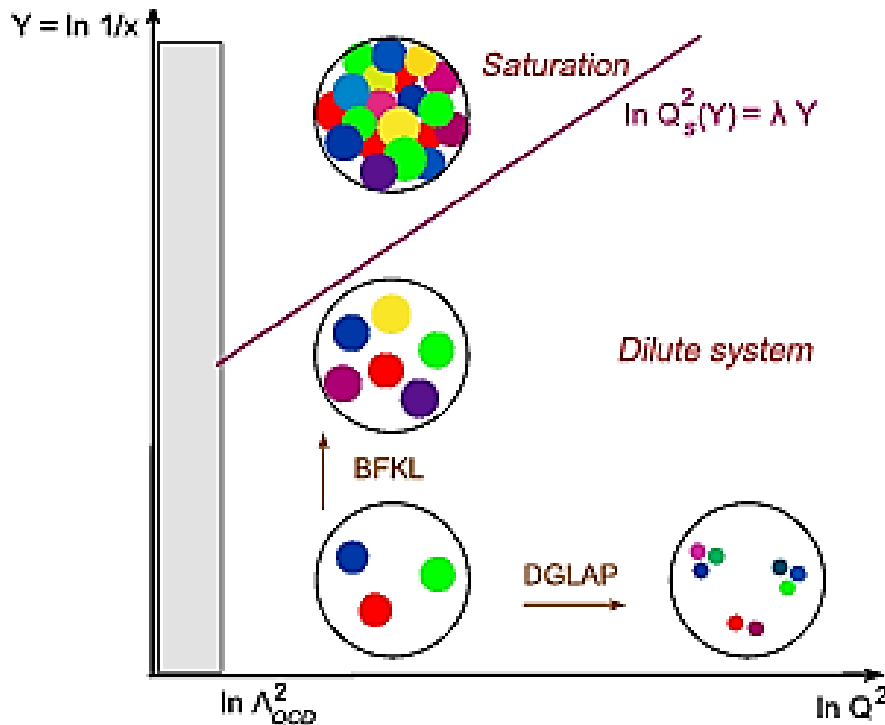
A myriad of small-x gluons
in a high energy hadron/nucleus!

$$\sum_n \frac{1}{n!} (\alpha_s \ln 1/x)^n \sim \left(\frac{1}{x}\right)^{\alpha_s}$$

Gluon saturation

The gluon number eventually saturates, forming the universal QCD matter at high energy called the **Color Glass Condensate**.

Gribov, Levin, Ryskin (1980); Mueller, Qiu (1986); McLerran, Venugopalan (1993)



Gluons overlap when

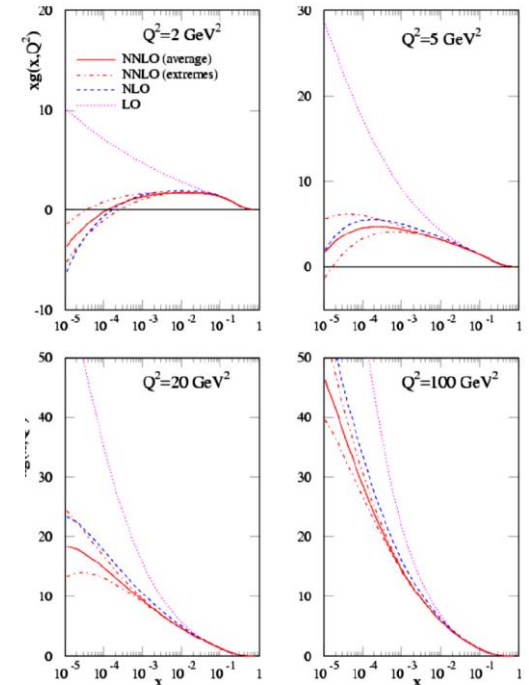
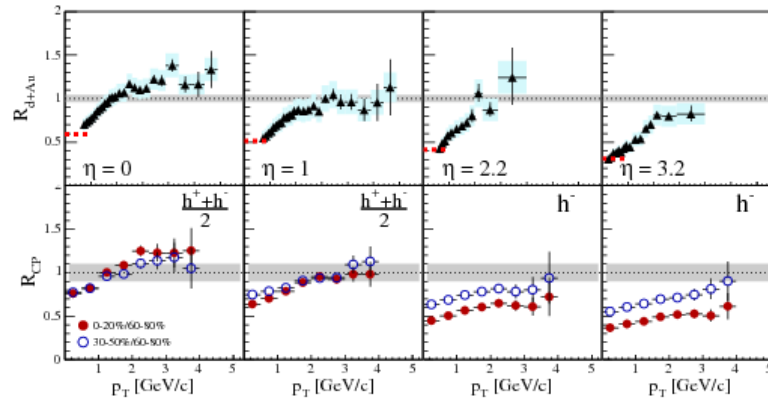
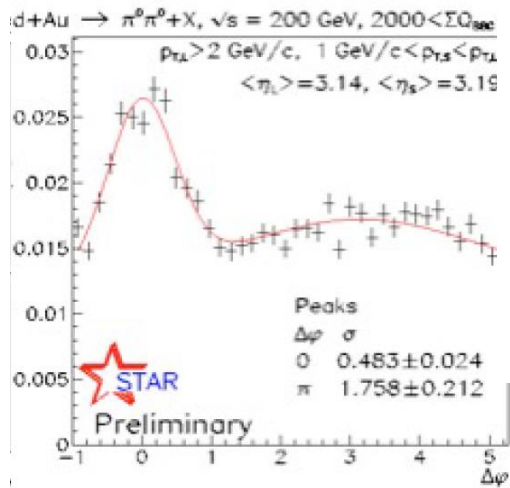
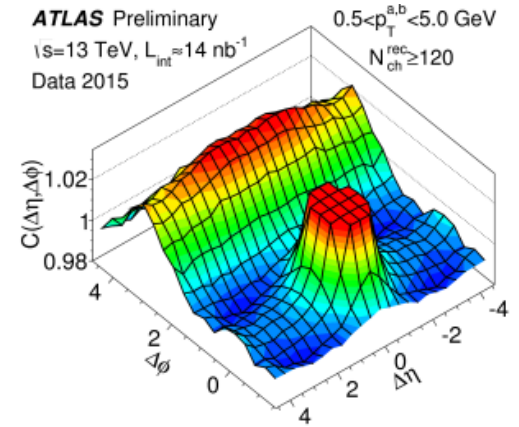
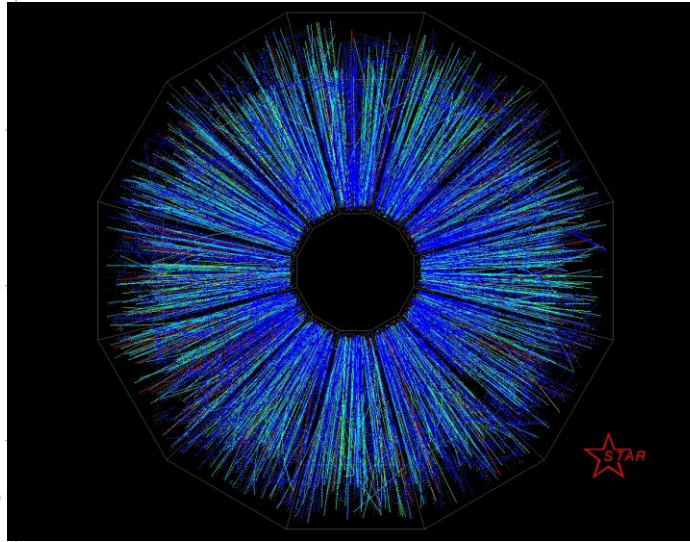
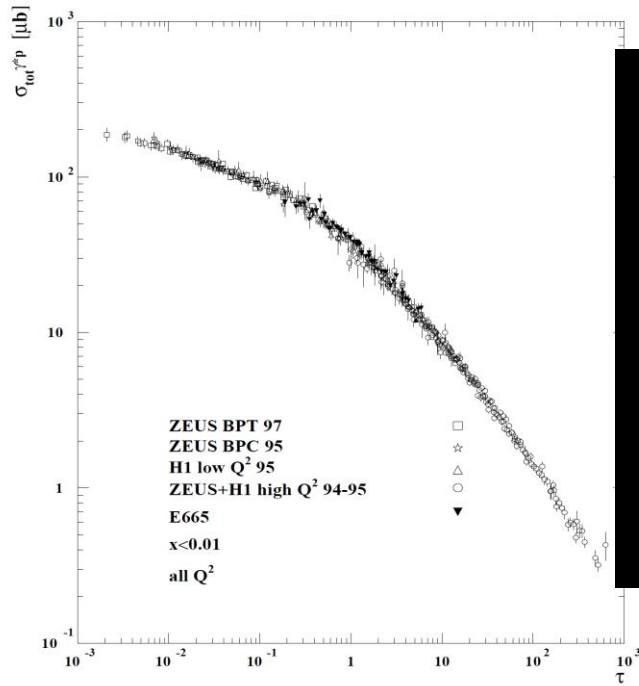
$$\frac{\alpha_s}{Q^2} x G(x, Q^2) = \pi R_p^2$$

The saturation momentum

$$Q = Q_s(x) \gg \Lambda_{QCD}$$

High density, but weakly coupled many-body problem

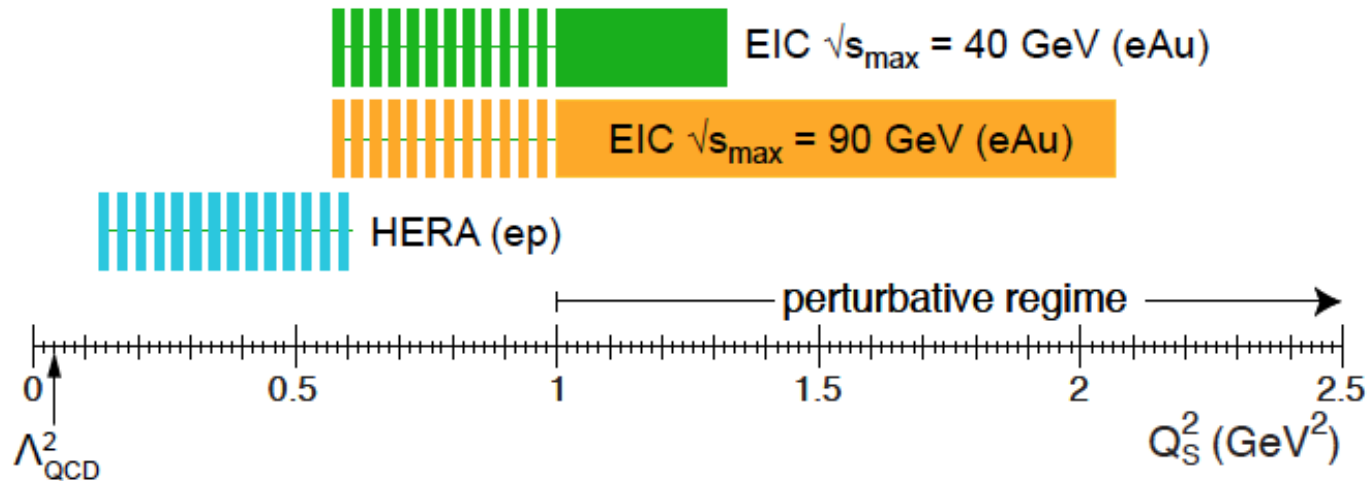
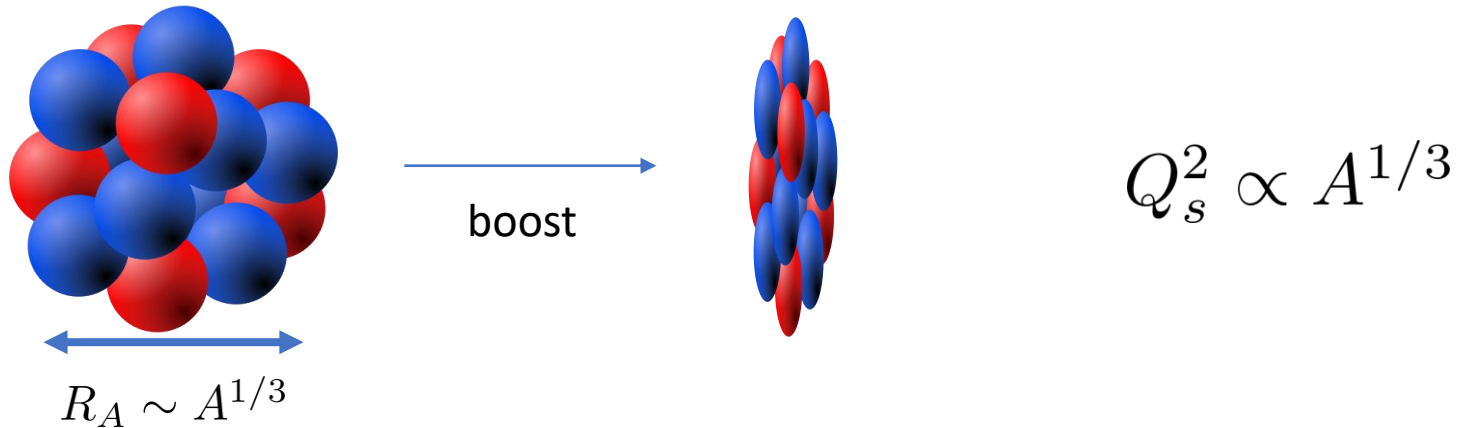
Has saturation been observed at HERA, RHIC, LHC?



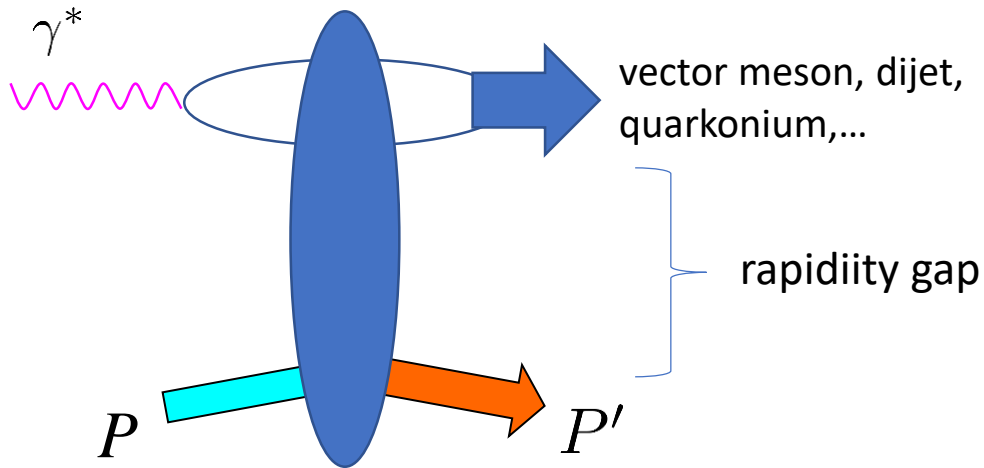
eA collision at EIC : ideal place to study saturation

No initial state interactions (advantage over LHC, RHIC)

Nuclear enhancement of the saturation momentum (advantage over HERA)



Golden channel for saturation: Diffraction



Cross sections proportional to the **square** of the gluon distribution

→ More sensitive to saturation

'Day 1 prediction'

[Kowalski, Lappi, Marquet, Venugopalan \(2008\)](#)

$$\left. \frac{\sigma_{diff}}{\sigma_{tot}} \right|_{eA} \approx 20\% > \left. \frac{\sigma_{diff}}{\sigma_{tot}} \right|_{ep}$$

Nucleus stays intact in every 1 out of 5 events!

Recently extended to NLL+NLO for dijet, vector meson...

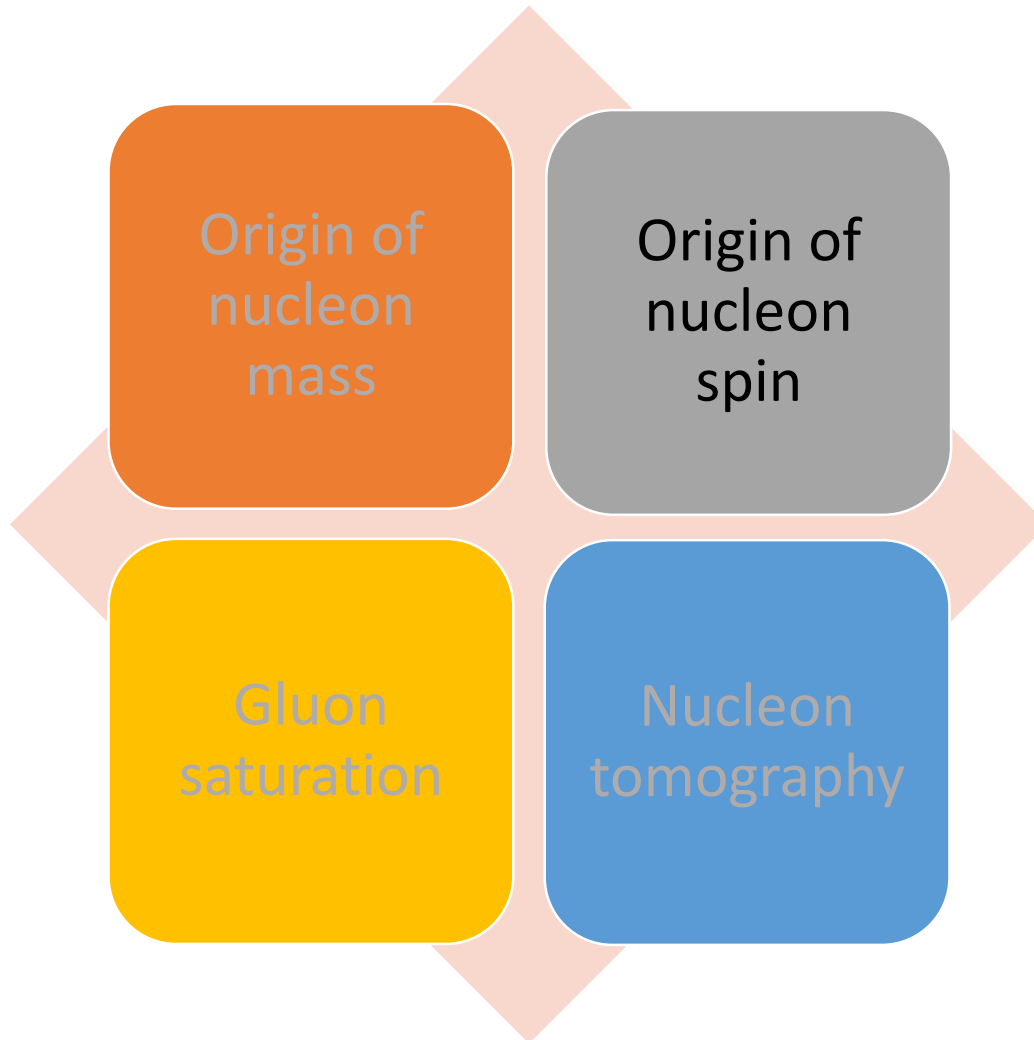
[Boussarie, Grabovsky, Szymanowski, Wallon \(2016,2019\)](#)

Can access also the Wigner distribution

[YH, Xiao, Yuan \(2016\)](#)

[Mantysaari, Mueller, Schenke 1902.05087](#)

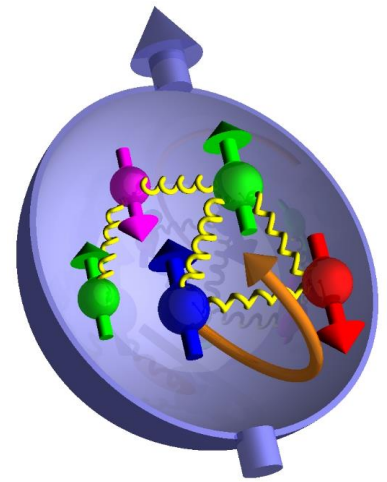
Scientific goals of EIC



Proton spin decomposition

The proton has spin $\frac{1}{2}$.

The proton is not an elementary particle.



➔ Jaffe-Manohar sum rule

$$\frac{1}{2} = \frac{1}{2} \Delta\Sigma + \Delta G + L^q + L^g$$

Quarks' helicity Gluons' helicity Orbital angular Momentum (OAM)

$$\Delta\Sigma = 1 \text{ in the quark model}$$

Proton spin crisis

In 1987, EMC (European Muon Collaboration) announced a very small value of the quark helicity contribution

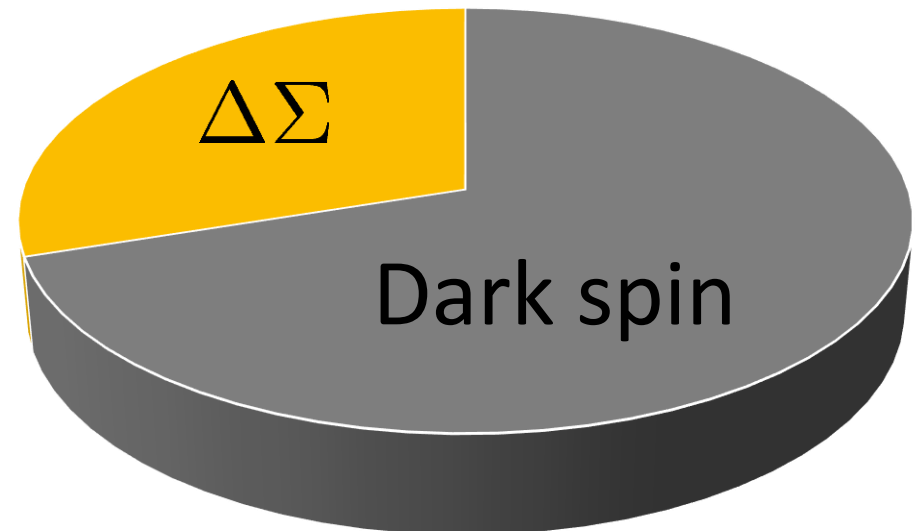
$$\Delta\Sigma = 0.12 \pm 0.09 \pm 0.14 \text{ !?}$$

Recent values from NLO global analysis

$$\Delta\Sigma = 0.25 \sim 0.3$$

$$\int_{0.05}^1 dx \Delta G(x, Q^2) \approx 0.2 \pm_{0.07}^{0.06}$$

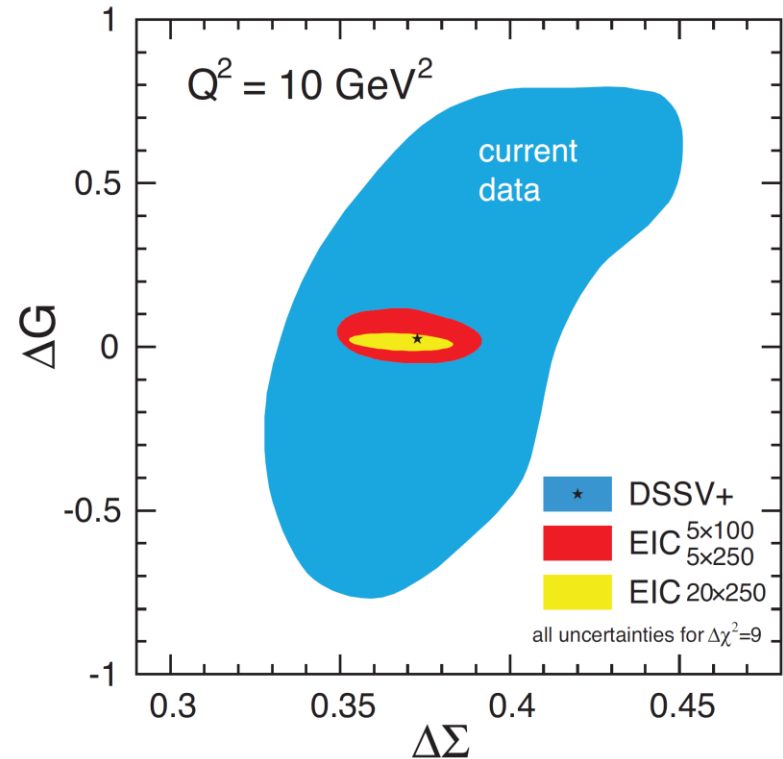
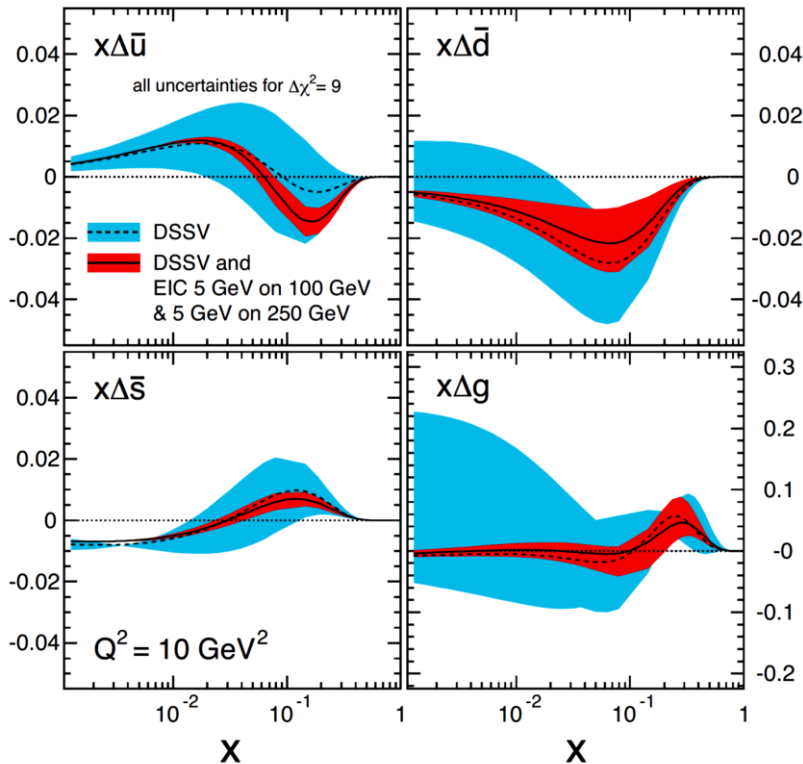
DeFlorian, Sassot, Stratmann, Vogelsang (2014)



Warning: Huge uncertainties from the small-x region

Helicity measurements at EIC

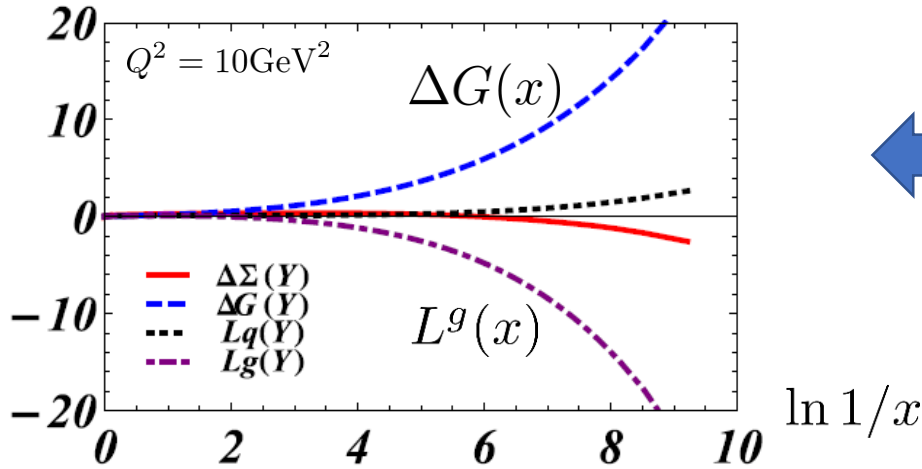
After one-year of data taking at EIC...



Wider coverage in x and Q^2 ... finally solve the spin puzzle?

No!

Don't forget Orbital Angular Momentum. It's there!

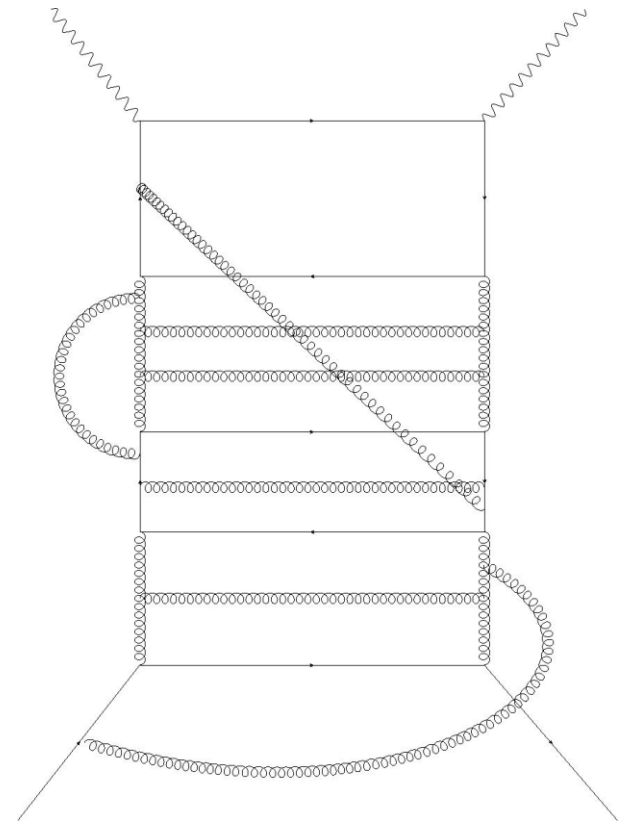


Significant cancellation at small-x
from one-loop DGLAP
YH, Yang (2018)

All-loop resummation of small-x double logarithms
($\alpha_s \ln^2 1/x$)ⁿ gives

$$L_g(x) \approx -2\Delta G(x)$$

Boussarie, YH, Yuan (2019)



Measuring OAM at EIC

Ji, Yuan, Zhao (2016)

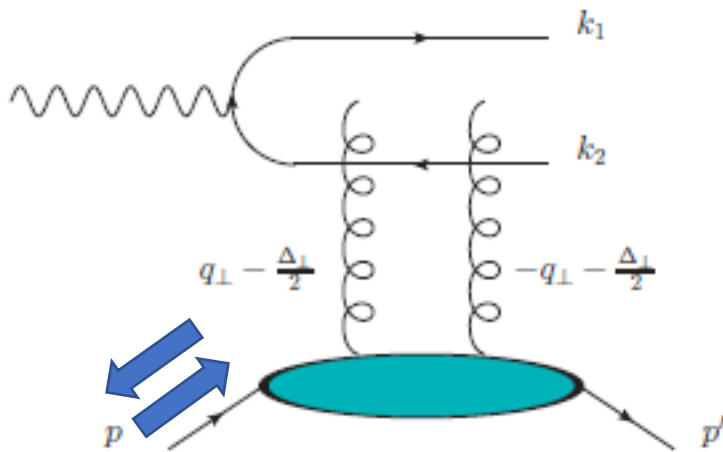
YH, Nakagawa, Xiao, Yuan, Zhao (2016)

Bhattacharya, Metz, Zhou (2017)

Exploit the connection between OAM and the **Wigner distribution**

$$L^{q,g} = \int dx \int d^2b_{\perp} d^2k_{\perp} (\vec{b}_{\perp} \times \vec{k}_{\perp})_z W^{q,g}(x, \vec{b}_{\perp}, \vec{k}_{\perp})$$

Longitudinal single spin asymmetry in diffractive dijet production



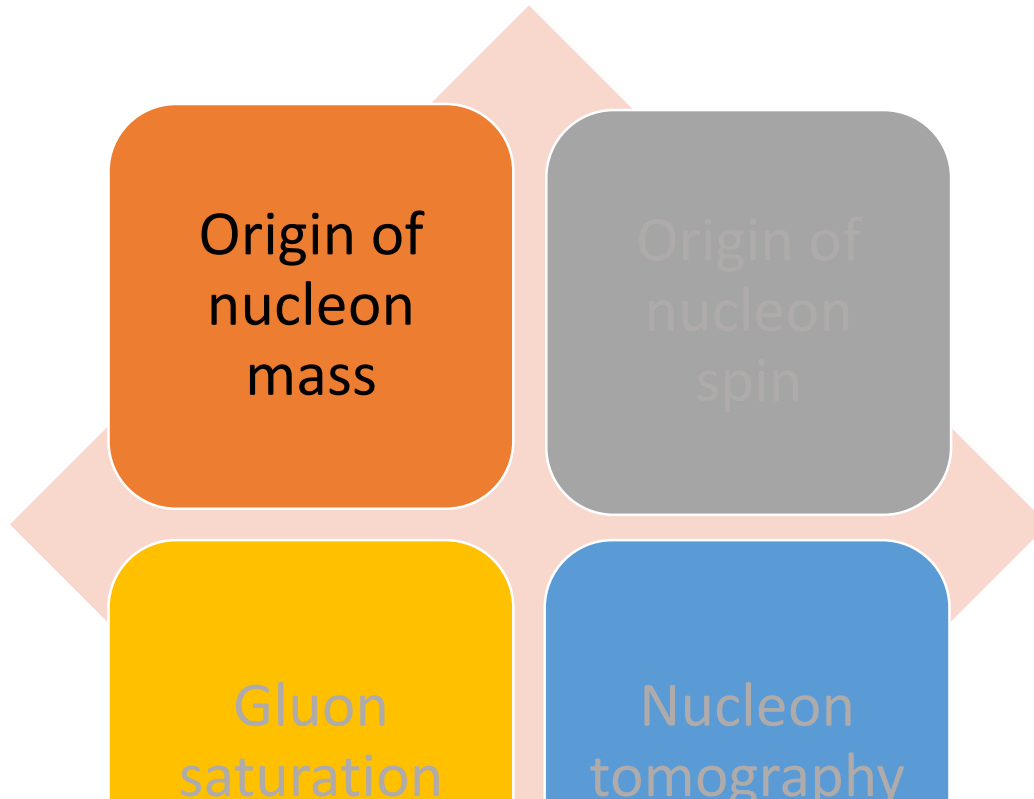
$$\sigma^{\rightarrow} - \sigma^{\leftarrow} \propto \sin(\phi_P - \phi_{\Delta})$$

proton recoil momentum

dijet relative momentum

Need more work, more new ideas!

Scientific goals of EIC



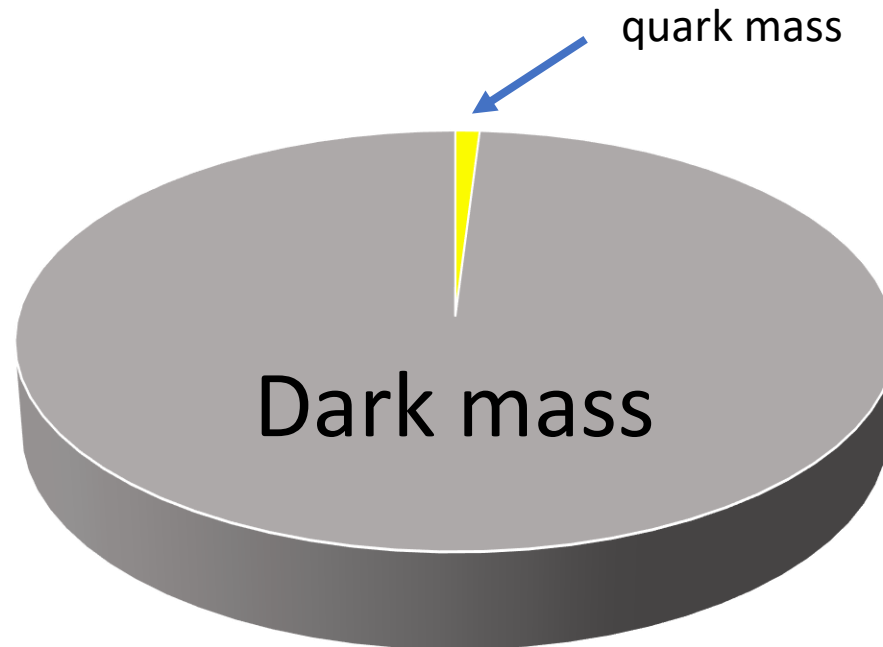
Finding 1: An EIC can uniquely address three profound questions about nucleons—protons—and how they are assembled to form the nuclei of atoms:

- How does the mass of the nucleon arise?
- How does the spin of the nucleon arise?
- What are the emergent properties of dense systems of gluons?

NAS report
(2018/07)

Proton mass crisis

u,d quark masses add up to $\sim 10\text{MeV}$, only 1 % of the proton mass!



Higgs mechanism explains quark masses, but not hadron masses!

The trace anomaly

QCD Lagrangian approximately scale (conformal) invariant.

Why is the proton mass nonvanishing in the first place?

Conformal symmetry is explicitly broken by the **trace anomaly**.

QCD energy-momentum tensor

$$T^{\mu\nu} = -F^{\mu\lambda}F^\nu{}_\lambda + \frac{\eta^{\mu\nu}}{4}F^2 + i\bar{q}\gamma^{(\mu}D^{\nu)}q$$

$$T^\mu{}_\mu = \frac{\beta(g)}{2g}F^2 + m(1 + \gamma_m(g))\bar{q}q$$

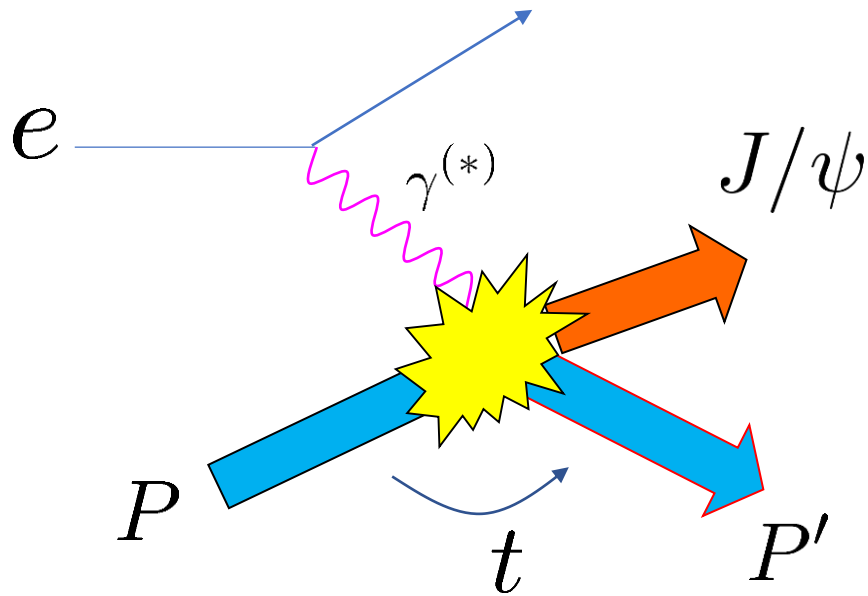
$$\langle P|T^\mu{}_\mu|P\rangle = 2M^2$$

Photo-production of J/ψ near threshold

Kharzeev, Satz, Syamtomov, Zinovjev (1998)

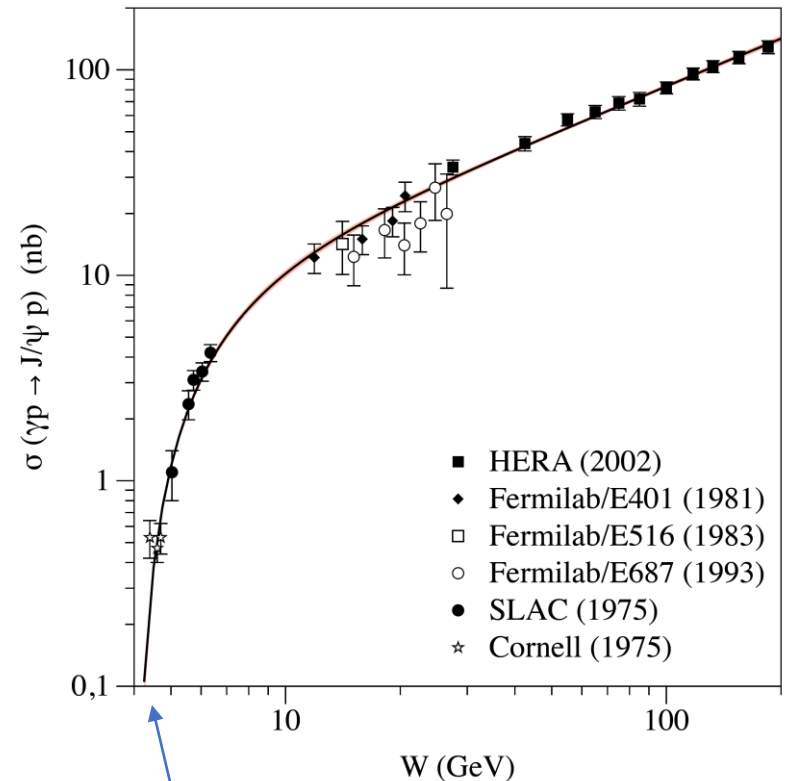
Brodsky, Chudakov, Hoyer, Laget (2000)

Sensitive to the matrix element $\langle P' | F^{\mu\nu} F_{\mu\nu} | P \rangle$



Straightforward to measure.
Ongoing experiments at Jlab.

Difficult to compute from first principles
(need nonperturbative approaches)



$W_{th} \approx 4.04 \text{ GeV}$

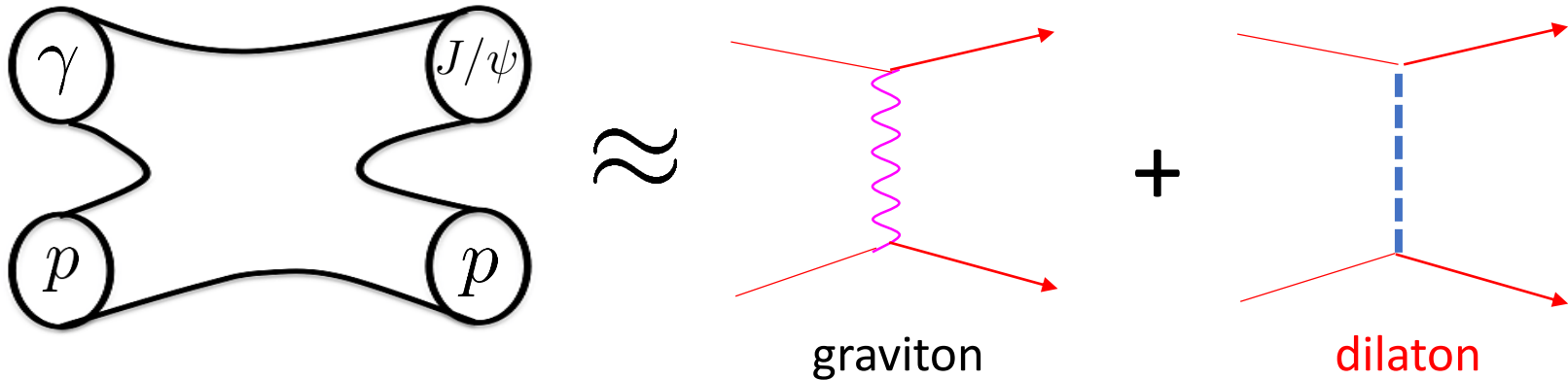
Holographic approach

YH, Yang (2018),

YH, Rajan, Yang, 1906.00894 ← NEW!!

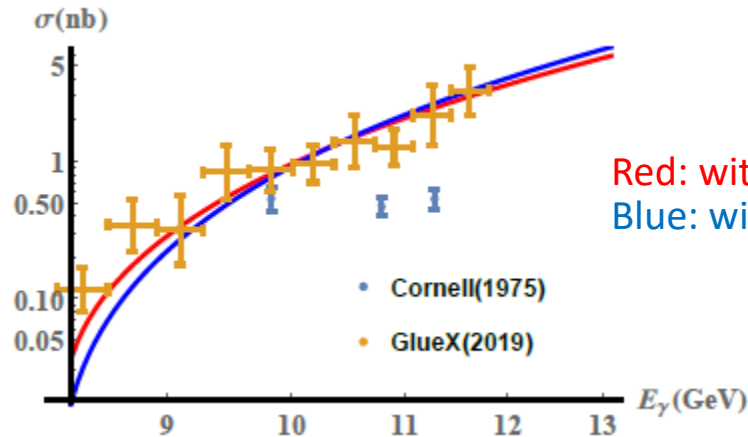
Scattering of hadrons \approx scattering of strings in anti-de Sitter

The operator $F^{\mu\nu}F_{\mu\nu}$ is dual to a massless string called **dilaton**



Data from the GlueX collaboration

1905.10811 ← NEW!!

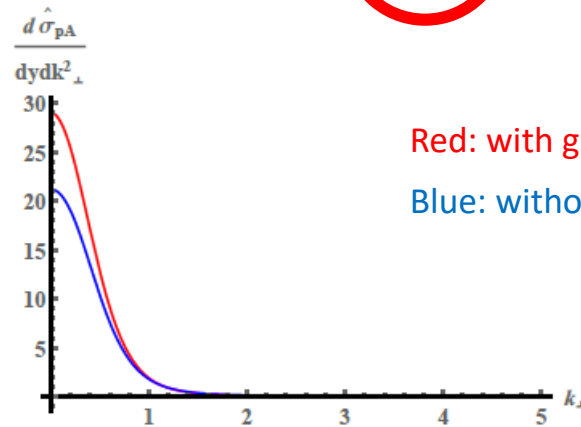
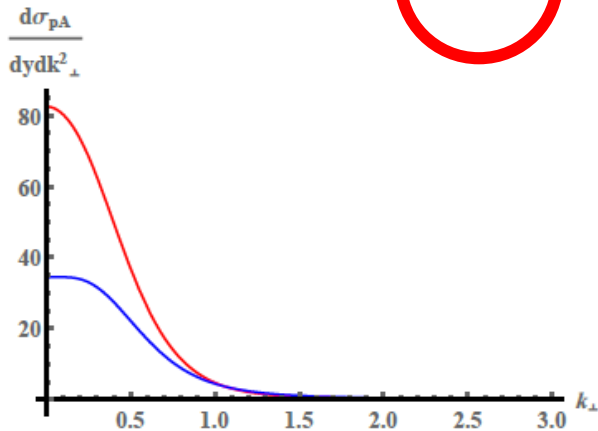
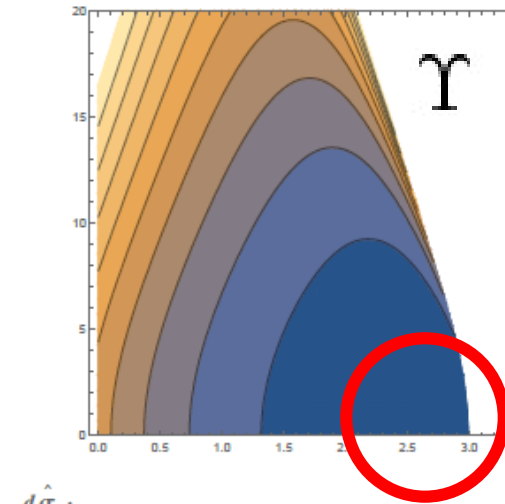
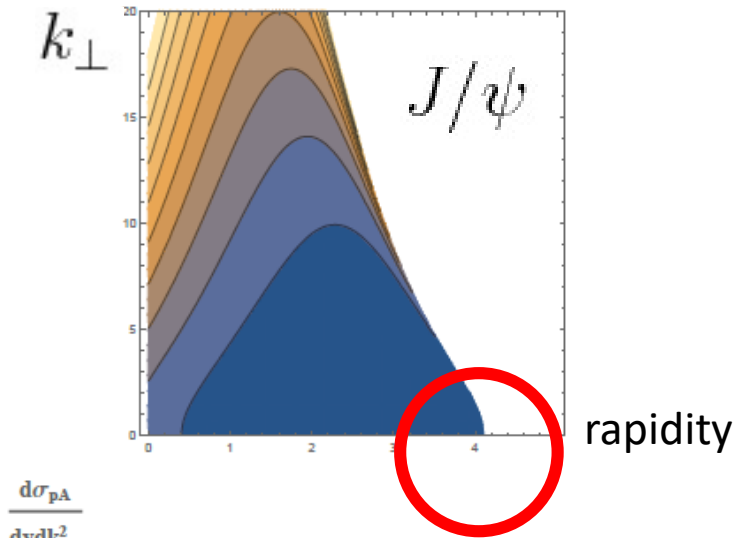


Red: with gluon condensate
Blue: without gluon condensate

We can do it at RHIC, too!

Near threshold production in ultra-peripheral pA collisions (UPC)

YH, Rajan, Yang,
1906.00894



Red: with gluon condensate
Blue: without gluon condensate

...and in future, at the EIC

Conclusion

- The science of EIC is one of the key future directions of nuclear physics in the US and around the world.
- EIC will significantly advance our knowledge of the nucleons/nuclei, the fundamental building blocks of the universe.
- Topics not covered include:
 - jets, lattice, EMC, short-range correlation, transverse spin, SSA, nPDF, etc. etc.



EIC user group
833 members, 177 institutions
(as of Nov.2018)

Let's join the groundswell.
Exciting times ahead!